

Market	Security	r_i	risk	correlation _{A,B}
I	A	0.22	0.3	0.15
	B	0.31	0.32	
II	A	0.26	0.29	-0.06
	B	0.34	0.33	
III	A	0.18	0.2	0.09
	B	0.41	0.38	

Market	rp
I	0.261589
II	0.295149
III	0.224674

Market I.

Covar_M

0.09	0.0144
0.0144	0.1024

0.09	0.0144
0.0144	0.1024

System of Matrix

0.18	0.0288	1
0.0288	0.2048	1
1	1	0

VRS

0
0
1

Inversion M

3.056235	-3.05623	0.537897
-3.05623	3.056235	0.462103
0.537897	0.462103	-0.11013

wi

w1	0.537897
w2	0.462103
lambda	-0.11013

Proof

1	0	0
0	1	0
0	0	1

Proof

1

Market II.

Covar_M

0.0841	-0.00574
-0.00574	0.1089

9.340571	-5.02427
-5.02427	0.289334

System of Matrix

0.1682	-0.01148	1
-0.01148	0.2178	1
1	1	0

VRS

0
0
1

Inversion M

2.445179	-2.44518	0.56064
-2.44518	2.445179	0.43936
0.56064	0.43936	-0.08925

wi

w1	0.56064
w2	0.43936
lambda	-0.08925

Proof

1	0	0
0	1	0
0	0	1

Proof

1

Market III.

Covar_M

0.04	0.00684
0.00684	0.1444

0.314318	0
0	0

System of Matrix

0.08	0.01368	1
0.01368	0.2888	1
1	1	0

VRS

0
0
1

Inversion M

2.928772	-2.92877	0.805764
-2.92877	2.928772	0.194236
0.805764	0.194236	-0.06712

wi

w1	0.805764
w2	0.194236
lambda	-0.06712

Proof 1

Proof

1	0	0
0	1	0
0	0	1

sigmap

0.234659	1.114761	0.897053
0.211251	1.397146	0.715745
0.183192	1.226445	0.815365

0.18	0.0288	1
0.0288	0.2048	1
1	1	0

3.056235	-3.05623	0.537897
-3.05623	3.056235	0.462103
0.537897	0.462103	-0.11013

Rp	0.261589	VarP	0.055065
		SigmaP	0.234659

18.68114	-10.0485	1
-10.0485	0.578667	1
1	1	0

0.025409	-0.02541	0.270021
-0.02541	0.025409	0.729979
0.270021	0.729979	2.290906

Rp	0.295149	VarP	0.044627
		SigmaP	0.211251

0.628635	0	1
0	0	1
1	1	0

1.590747	-1.59075	0
-1.59075	1.590747	1
0	1	0

Rp	0.224674	VarP	0.033559
		SigmaP	0.183192

	Company 1	Company 2	Company 3	Correlation	
μ	0.8	0.3	0.6	$\sigma_{1.2}$	-0.1
σ	1.2	0.8	1.1	$\sigma_{1.3}$	-0.5
				$\sigma_{2.3}$	0.3

Χωραρ_M

1.44	-0.096	-0.66
-0.096	0.64	0.264
-0.66	0.264	1.21

2.88	-0.192	-1.32	1
-0.192	1.28	0.528	1
-1.32	0.528	2.42	1
1	1	1	0

Inversion M

0.222691	-0.25436	0.031669	0.351616
-0.25436	0.668746	-0.41439	0.313964
0.031669	-0.41439	0.382718	0.33442
0.351616	0.313964	0.33442	-0.51094

2.88	-0.192	-1.32	1
-0.192	1.28	0.528	1
-1.32	0.528	2.42	1
1	1	1	0
0.8	0.3	0.6	0

Inversion M

0.076093	0.050729	-0.12682	-0.34729
0.050729	0.033819	-0.08455	1.768474
-0.12682	-0.08455	0.21137	-0.42118
-0.34729	1.768474	-0.42118	-3.84297
1.213095	-2.5246	1.311509	5.783435

				0.351616	0.313964	0.33442
	VRS			0.178032	-0.0106	-0.07761
		0		-0.0106	0.063087	0.027719
		0		-0.07761	0.027719	0.135323
		0				
		1				
	wi	Rp	0.576134	var-p	0.255469	
w1	0.351616			sigma-p	0.505439	
w2	0.313964					
w3	0.33442					
lambda	-0.51094					
proof	1					

		VRS		1.472353	-2.01843	1.546079
0.8		0				
0.3		0		3.121665	0.285297	-1.50241
0.6		0		0.285297	2.607402	-0.82385
0		1		-1.50241	-0.82385	2.892335
0		1.5				

		wi	Rp	1.5	var-p	4.539477
1.213095	w1	1.472353			sigma-p	2.130605
-2.5246	w2	-2.01843				
1.311509	w3	1.546079				
5.783435	lambda1	4.832182				
-10.0384	lambda2	-9.27409				
	proof	1				

0.178032	-0.0106	-0.07761
-0.0106	0.063087	0.027719
-0.07761	0.027719	0.135323

	Sec ₁	Sec ₂	Sec ₃	Sec ₄	Sec ₅	Sec ₆	Sec ₇	r _i (%)
Sec ₁	80.5	82.7	85.3	85.1	123.9	22	3.5	1.9
Sec ₂	82.7	184.7	131.5	69.4	49.5	58	-9.9	6.1
Sec ₃	85.3	131.5	374.2	384.5	366.5	103.8	343.5	2.9
Sec ₄	85.1	69.4	384.5	684.8	599.1	51.6	502.7	4
Sec ₅	123.9	49.5	366.5	599.1	871.4	-21.2	520.4	5.7
Sec ₆	22	58	103.8	51.6	-21.2	89.7	74.4	3.4
Sec ₇	3.5	-9.9	343.5	502.7	520.4	74.4	574.6	4.9

161	165.4	170.6	170.2	247.8	44	7	1
165.4	369.4	263	138.8	99	116	-19.8	1
170.6	263	748.4	769	733	207.6	687	1
170.2	138.8	769	1369.6	1198.2	103.2	1005.4	1
247.8	99	733	1198.2	1742.8	-42.4	1040.8	1
44	116	207.6	103.2	-42.4	179.4	148.8	1
7	-19.8	687	1005.4	1040.8	148.8	1149.2	1
1	1	1	1	1	1	1	0

InvM

0.077542	-0.00619	0.008788	-0.00971	-0.03769	-0.07775	0.045002	2.1372
-0.00619	0.007803	-0.00362	0.000167	0.001056	-0.00048	0.001254	0.044435
0.008788	-0.00362	0.007544	-0.00229	-0.00426	-0.00879	0.002623	-0.29067
-0.00971	0.000167	-0.00229	0.004278	0.004072	0.01066	-0.00718	-0.23027
-0.03769	0.001056	-0.00426	0.004072	0.02058	0.040175	-0.02394	-0.77333
-0.07775	-0.00048	-0.00879	0.01066	0.040175	0.086382	-0.0502	-1.1224
0.045002	0.001254	0.002623	-0.00718	-0.02394	-0.0502	0.032436	1.235036
2.1372	0.044435	-0.29067	-0.23027	-0.77333	-1.1224	1.235036	-30.2875

2nd opt - E(rp)=5%

161	165.4	170.6	170.2	247.8	44	7	1
165.4	369.4	263	138.8	99	116	-19.8	1
170.6	263	748.4	769	733	207.6	687	1
170.2	138.8	769	1369.6	1198.2	103.2	1005.4	1
247.8	99	733	1198.2	1742.8	-42.4	1040.8	1
44	116	207.6	103.2	-42.4	179.4	148.8	1
7	-19.8	687	1005.4	1040.8	148.8	1149.2	1
1	1	1	1	1	1	1	0
1.9	6.1	2.9	4	5.7	3.4	4.9	0

InvMatrix

0.016039	0.007661	-0.00407	-0.00315	-0.00914	-0.02351	0.016171	2.286871
0.007661	0.004685	-0.00072	-0.00131	-0.00537	-0.01269	0.007746	0.010736
-0.00407	-0.00072	0.004856	-0.00092	0.001708	0.002544	-0.0034	-0.25938
-0.00315	-0.00131	-0.00092	0.003579	0.001028	0.004877	-0.00411	-0.24623
-0.00914	-0.00537	0.001708	0.001028	0.00733	0.015	-0.01055	-0.8428
-0.02351	-0.01269	0.002544	0.004877	0.015	0.038551	-0.02477	-1.2544
0.016171	0.007746	-0.0034	-0.00411	-0.01055	-0.02477	0.01892	1.305199

2.286871	0.010736	-0.25938	-0.24623	-0.8428	-1.2544	1.305199	-30.6517
-0.37867	0.085259	-0.07916	0.040381	0.175762	0.333946	-0.17751	0.921531

			2.1372	0.044435	-0.29067
			367.6936	7.853678	-52.9898
			7.853678	0.36468	-1.69843
			-52.9898	-1.69843	31.61554
			-41.881	-0.71011	25.73579
VRS			-204.776	-1.70094	82.38249
	0		-52.7736	-2.89267	33.86451
	0		9.238319	-0.5433	-123.312
	0				
	0				
	0				
	0				
	0				
	1				

wi	Rp	0.39525	VarP	15.14374
2.1372			SigmaP	3.891496
0.044435				
-0.29067				
-0.23027				
-0.77333				
-1.1224				
1.235036				
-30.2875				

proof 1

	VRS				
1.9	0				
6.1	0	0.3935	0.43703	-0.65518	-0.04433
2.9	0				
4	0	12.46483	14.22203	-21.9915	-1.48441
5.7	0	14.22203	35.27677	-37.6528	-1.34447
3.4	0	-21.9915	-37.6528	160.6291	11.167
4.9	0	-1.48441	-1.34447	11.167	1.345623
0	1	1.755887	0.779106	-8.64797	-0.95644
0	5	3.595548	10.52776	-28.2459	-0.95001
		0.57518	-1.80691	-93.9892	-9.30635
	wi				
-0.37867	0.3935	Rp	5	VarP	39.86213
0.085259	0.43703			SigmaP	6.313646
-0.07916	-0.65518				
0.040381	-0.04433				
0.175762	0.036015				
0.333946	0.415334				
-0.17751	0.417629				

0.921531

-26.0441

-2.33151

-10.736

proof

1

-0.23027 -0.77333 -1.1224 1.235036

-41.881 -204.776 -52.7736 9.238319
-0.71011 -1.70094 -2.89267 -0.5433
25.73579 82.38249 33.86451 -123.312
36.31192 106.6853 13.33649 -142.966
106.6853 521.1259 -18.4013 -497.027
13.33649 -18.4013 113.0031 -103.134
-142.966 -497.027 -103.134 876.446

0.036015 0.415334 0.417629

1.755887 3.595548 0.57518
0.779106 10.52776 -1.80691
-8.64797 -28.2459 -93.9892
-0.95644 -0.95001 -9.30635
1.130259 -0.31711 7.827232
-0.31711 15.47344 12.90509
7.827232 12.90509 100.2183

Risky portfolio	A	B	C	D
\bar{r}_p	6.20%	4%	7.50%	8.40%
σ_p	14.50%	9.70%	17%	20%

rf

0.035

	1	2	3	4	5
r_f	0.2	0.4	0.5	0.6	0.8
Portfolio	0.8	0.6	0.5	0.4	0.2

Rp

A	0.0566	0.0512	0.0485	0.0458	0.0404
B	0.039	0.038	0.0375	0.037	0.036
C	0.067	0.059	0.055	0.051	0.043
D	0.0742	0.0644	0.0595	0.0546	0.0448

SigmaP

A	0.116	0.087	0.0725	0.058	0.029
B	0.0776	0.0582	0.0485	0.0388	0.0194
C	0.136	0.102	0.085	0.068	0.034
D	0.16	0.12	0.1	0.08	0.04