

# Static and dynamic games, preventing the entry and predation

Industrial organization – lecture 2

# Cournot model

Pepall et al. (2014, pp. 222-228)

2 firms with

- the same marginal cost  $c_1 = c_2 = c$
- zero fixed cost  $F_1 = F_2 = 0$

Inverse demand function:  $p = A - (q_1 + q_2)$

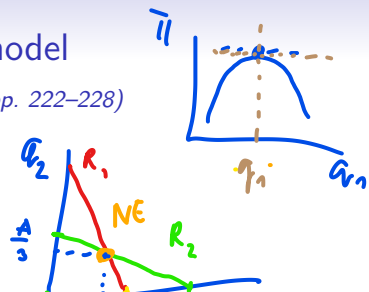
→ What is the Cournot equilibrium?  
What is the profit?

$$\begin{aligned} \Pi_1 &= p \cdot q_1 - c \cdot q_1 \\ \Pi_2 &= (A - q_1 - q_2) \cdot q_2 - c \cdot q_2 \\ \Pi_1 &= Aq_1 - q_1^2 - q_1q_2 - cq_1 \\ \Pi_1' &= A - 2q_1 - q_2 - c = 0 \end{aligned}$$

$$\begin{aligned} R_1: q_1 &= \frac{A - q_2 - c}{2} \\ R_2: q_2 &= \frac{A - q_1 - c}{2} \end{aligned}$$

$$\begin{aligned} q_2 &= \frac{A - c - \frac{A - q_1 - c}{2}}{2} = \frac{A + q_1 - c}{4} \\ \frac{d}{dq_1} q_2 &= \frac{1}{4} \\ q_1 &= \frac{A - c}{3} \quad q_2 = \frac{A - c}{3} \end{aligned}$$

$$\begin{aligned} \Pi &= (p - c) \cdot q_1 = \left( A - \frac{A - c}{3} - \frac{A - c}{3} - c \right) \cdot \frac{A - c}{3} \\ &= \left( \frac{A}{3} - \frac{c}{3} \right) \cdot \frac{A - c}{3} = \frac{(A - c)^2}{9} \end{aligned}$$



$$\frac{4A}{4} - \frac{2A}{4} - \frac{1A}{4}$$

# Stackelberg model

Pepall et al. (2014, pp. 265-268)

$$\bar{\pi}_2 = \frac{(A-c)^2}{16}$$

2 firms:

- firm 1 is the leader
- firm 2 is the follower

Both firms have

- the same marginal cost  $c_1 = c_2 = c$
- zero fixed cost  $F_1 = F_2 = 0$

Inverse demand function:  $p = A - (q_1 + q_2)$

What is the Stackelberg equilibrium?

What is the profit?

What is the reason for the dominance of the leader?

$$\begin{aligned} \pi_1 &= p \cdot q_1 - c \cdot q_1 \\ \pi_2 &= (A - q_1 - q_2) \cdot q_2 - c \cdot q_2 \\ \pi_1 &= (A - q_1 - \frac{A - q_1 - c}{2}) \cdot q_1 - c \cdot q_1 \\ \pi_1 &= \frac{Aq_1 - q_1^2 - \frac{Aq_1}{2} + \frac{q_1^2}{2} + \frac{c}{2}q_1 - cq_1}{2} \\ \pi_1 &= \frac{Aq_1}{2} - \frac{q_1^2}{2} - \frac{c}{2} \cdot q_1 \end{aligned}$$

leader knows:  $q_2 = \frac{A - q_1 - c}{2}$

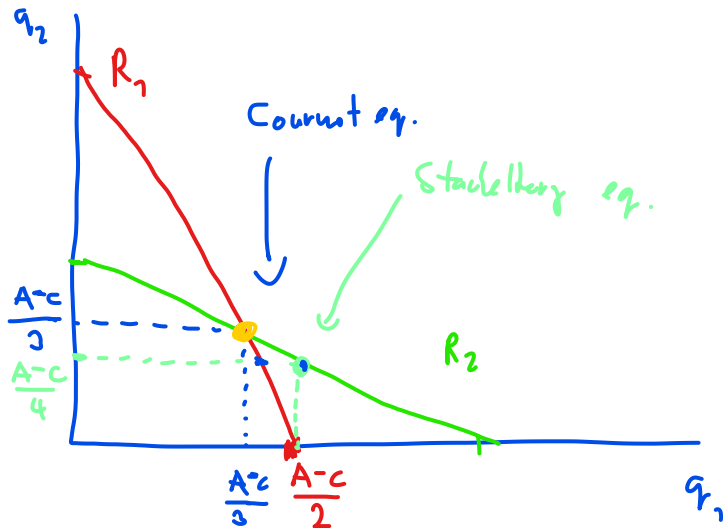
$$\pi_1' = \frac{A}{2} - q_1 - \frac{c}{2} = 0$$

$$q_1 = \frac{A - c}{2}$$

$$q_2 = \frac{A - c - \frac{A - c}{2}}{2} = \frac{A - c}{4}$$

$$\pi_1 = (p - c) \cdot q_1 = \left( A - \frac{A - c}{2} - \frac{A - c}{4} - c \right) \cdot \frac{A - c}{2} = \left( \frac{A}{4} - \frac{c}{4} \right) \cdot \frac{A - c}{2} = \frac{(A - c)^2}{8} = \frac{A - c}{4}$$

## Stackelberg model – graph



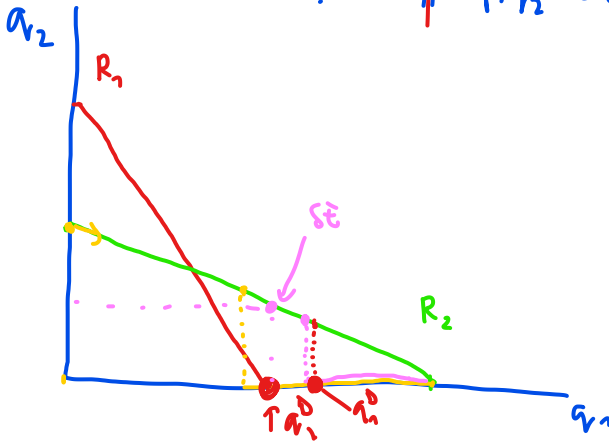
# Limit output and limit price models

*Pepall et al. (2014, pp. 289–291)*

Stackelberg + the follower has one-time sunk entry costs  $F$ .

What quantity  $q_1^d$  would deter entry?

$$\pi = p \cdot q_2 - c \cdot q_2 - F$$



# Limit output and limit price models

*Pepall et al. (2014, pp. 289–291)*

When does the leader choose the quantity  $q_L^d$ ?

# Capacity expansion as a credible entry-detering commitment

*Pepall et al. (2014, pp. 291–299)*

Dixit, A. (1980). The role of investment in entry-deterrence. *The economic journal*, 90(357), 95–106.

A dynamic two-stage game between two firms:

1. The incumbent chooses the capacity level  $\overline{K}_1$  at a cost  $r\overline{K}_1$ .
2. Cournot game:

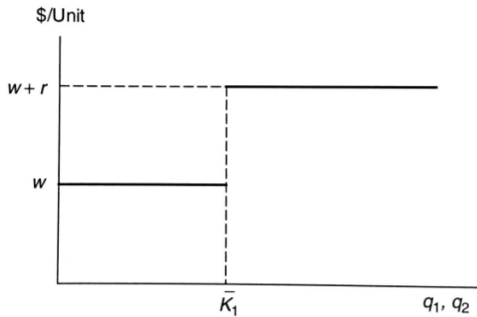
The incumbent's costs are

$$c_1(q_1) = \begin{cases} wq_1 + r\overline{K}_1 + F_1 & \text{for } q_1 \leq \overline{K}_1 \\ (w + r)q_1 + F_1 & \text{for } q_1 > \overline{K}_1 \end{cases}$$

The entrant's costs are

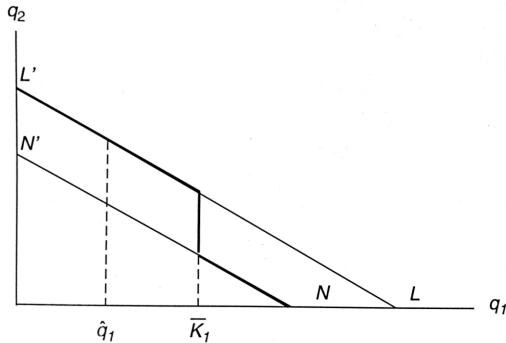
$$c_2(q_2) = (w + r)q_2 + F_2$$

# The effect of previously acquired capacity

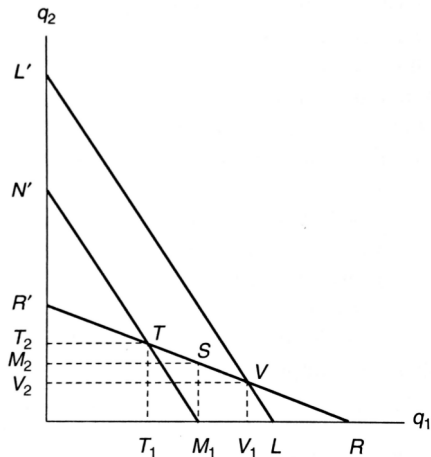




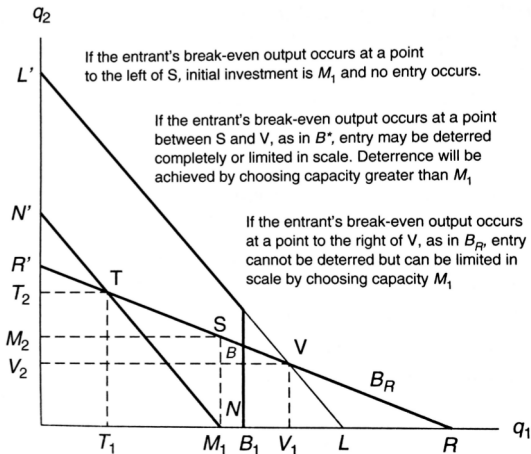
## The incumbent's best response in stage 2



# The rational bounds on the incumbent's choice of $\overline{K}_1$



# Possible locations of the entrant's break-even point



# Evidence on predatory capacity expansion

*Pepall et al. (2014, pp. 304–309)*

- Alcoa case – increased capacity 8x between 1912 and 1934
- Weiman and Levin (1994) – preemptive investment in SBT
- Safeway in Edmonton in 1960s and 1970s
- DuPont production of titanium dioxide
- Excess capacity expansion in Texas hotels