

M U N I
E C O N

Portfolio Theory

Important Assumptions of Mean-Variance Analysis

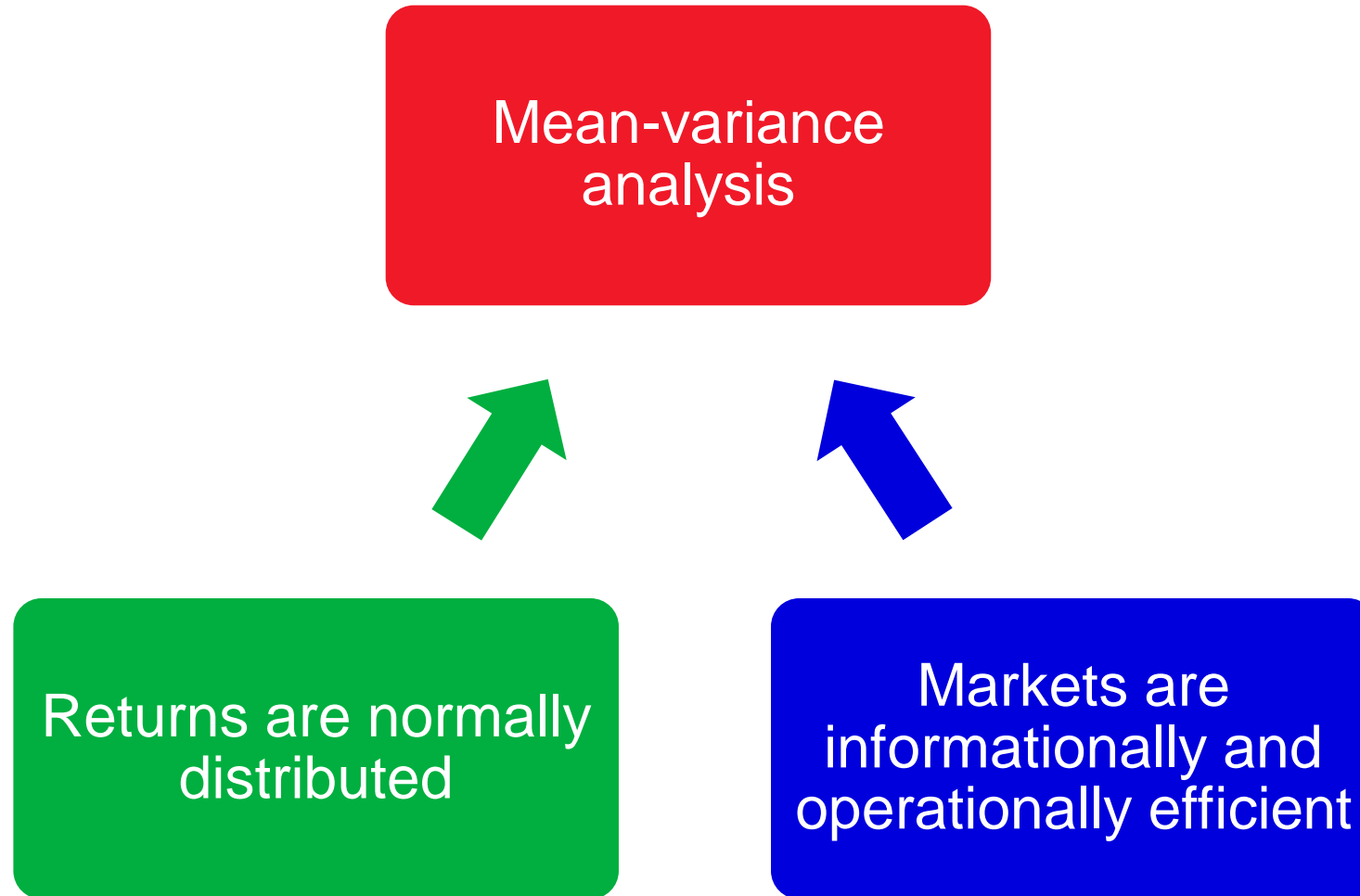
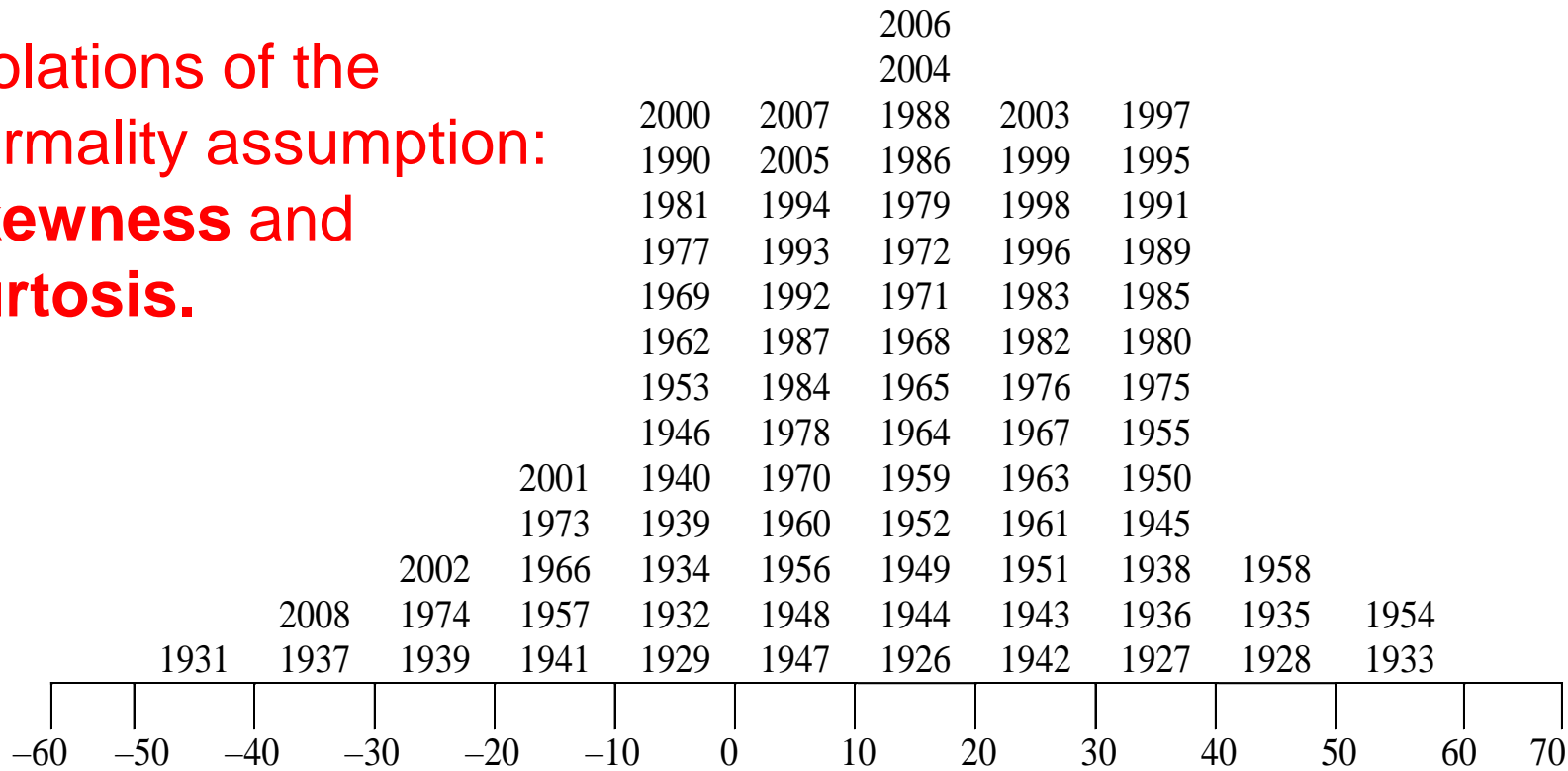


EXHIBIT 5-9 Histogram of U.S. Large Company Stock Returns, 1926-2008

Violations of the normality assumption: skewness and kurtosis.



Utility Theory

Expected
return

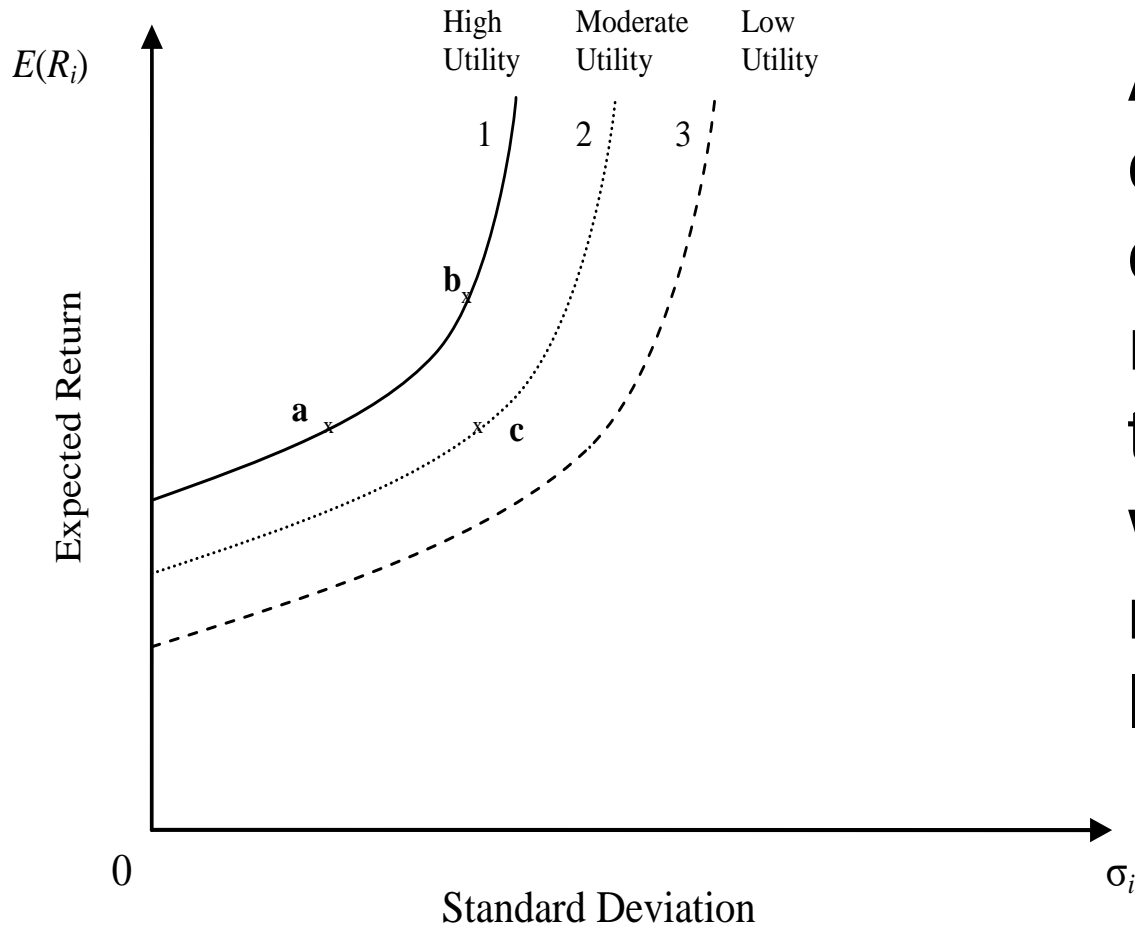
Variance or
risk

$$U = E(r) - \frac{1}{2} A \sigma^2$$

Utility of an
investment

Measure of
risk
tolerance or
risk aversion

Indifference Curves



An indifference curve plots the combination of risk-return pairs that an investor would accept to maintain a given level of utility.

Portfolio Expected Return and Risk Assuming a Risk-Free Asset

Assume a portfolio of two assets, a risk-free asset and a risky asset. Expected return and risk for that portfolio can be determined using the following formulas:

$$E(R_P) = w_1 R_f + (1 - w_1) E(R_i)$$

$$\sigma_P^2 = w_1^2 \sigma_f^2 + (1 - w_1)^2 \sigma_i^2 + 2w_1(1 - w_1)\rho_{fi}\sigma_f\sigma_i$$

$$= (1 - w_1)^2 \sigma_i^2$$

$$\sigma_P = \sqrt{(1 - w_1)^2 \sigma_i^2} = (1 - w_1)\sigma_i$$

The Capital Allocation Line (CAL)

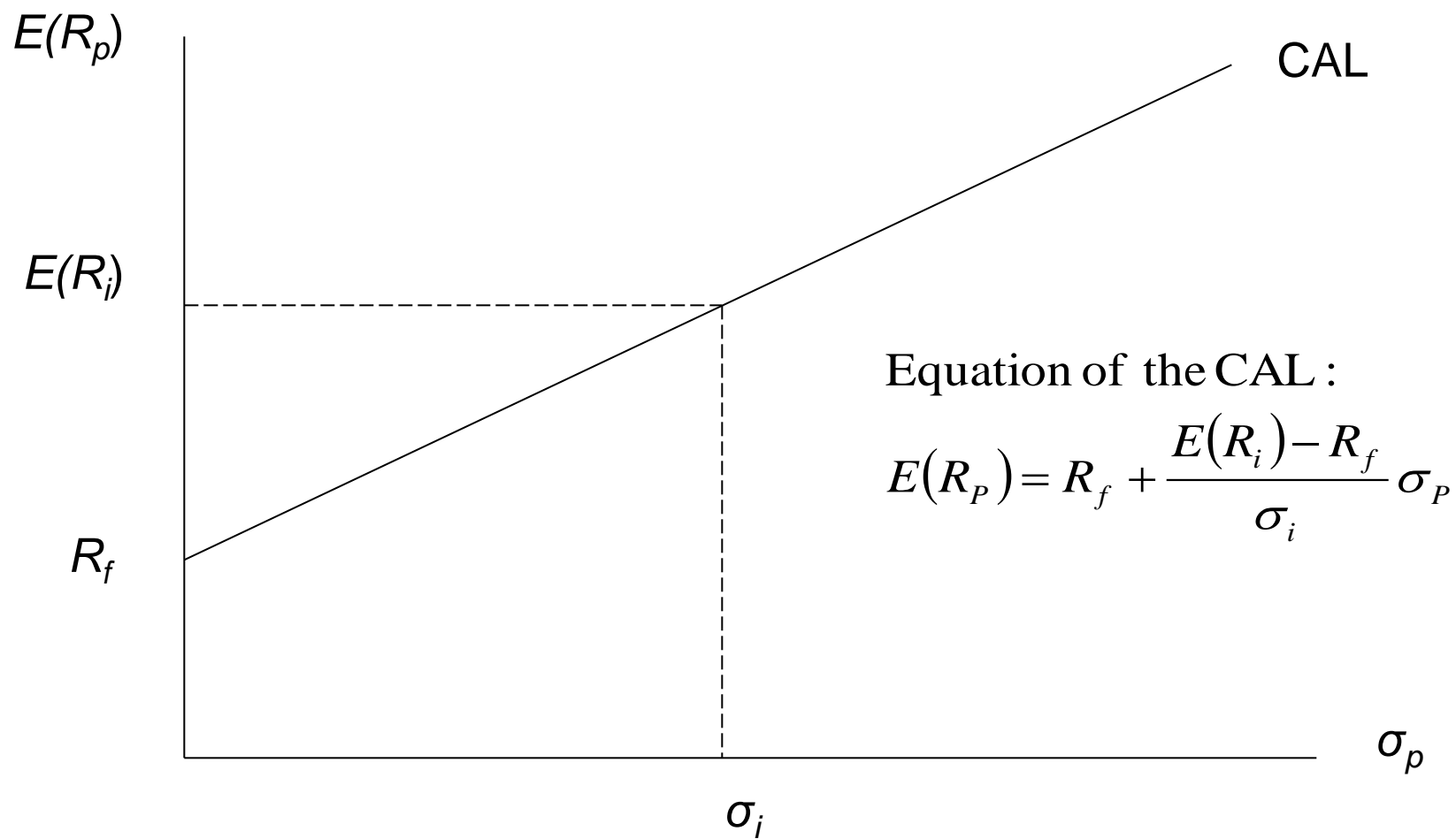
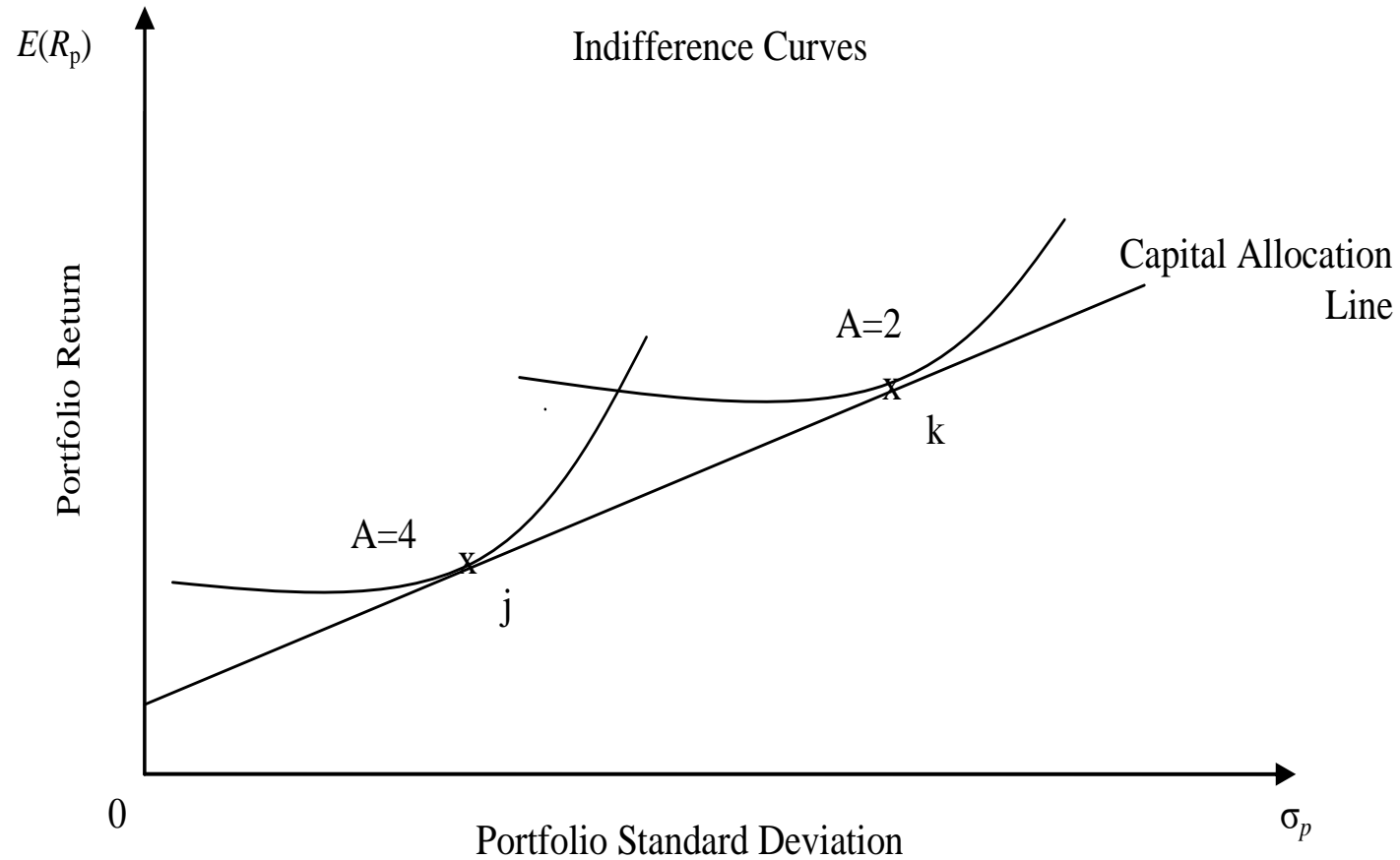
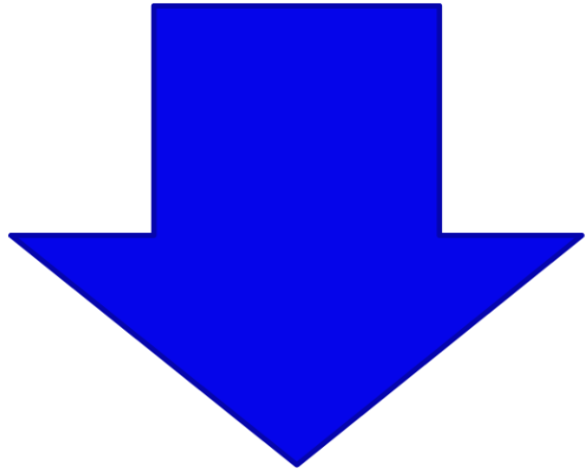


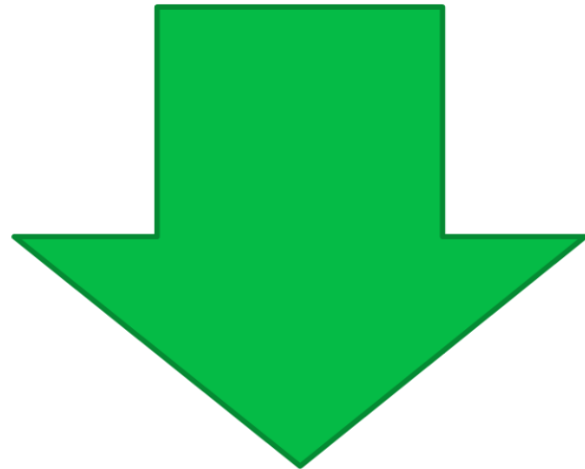
EXHIBIT 5-15 Portfolio Selection for Two Investors with Various Levels of Risk Aversion



Correlation and Portfolio Risk



Correlation
between assets
in the portfolio



Portfolio risk

EXHIBIT 5-16 Relationship between Risk and Return

Weight in Asset 1	Portfolio Return	Portfolio Risk with Correlation of			
		1.0	0.5	0.2	-1.0
0%	15.0	25.0	25.0	25.0	25.0
10%	14.2	23.7	23.1	22.8	21.3
20%	13.4	22.4	21.3	20.6	17.6
30%	12.6	21.1	19.6	18.6	13.9
40%	11.8	19.8	17.9	16.6	10.2
50%	11.0	18.5	16.3	14.9	6.5
60%	10.2	17.2	15.0	13.4	2.8
70%	9.4	15.9	13.8	12.3	0.9
80%	8.6	14.6	12.9	11.7	4.6
90%	7.8	13.3	12.2	11.6	8.3
100%	7.0	12.0	12.0	12.0	12.0

EXHIBIT 5-17 Relationship between Risk and Return

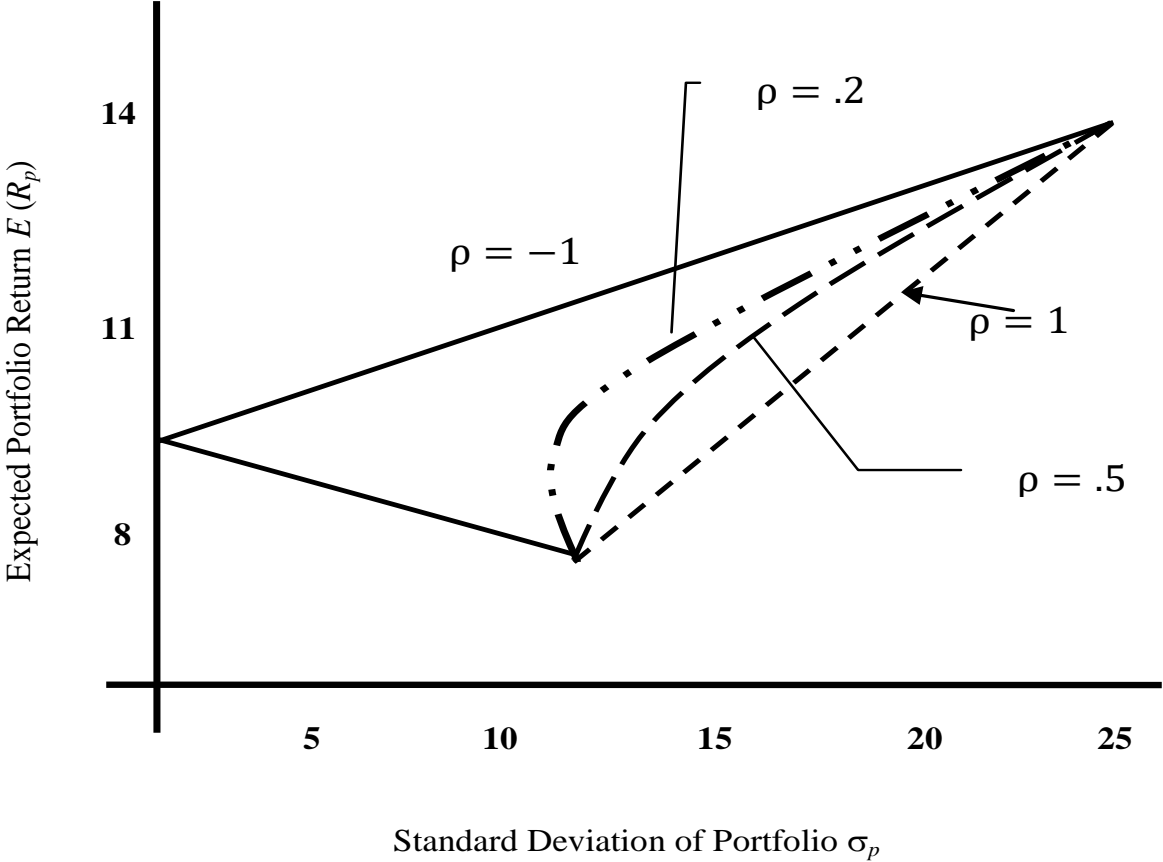


EXHIBIT 5-22 Minimum-Variance Frontier

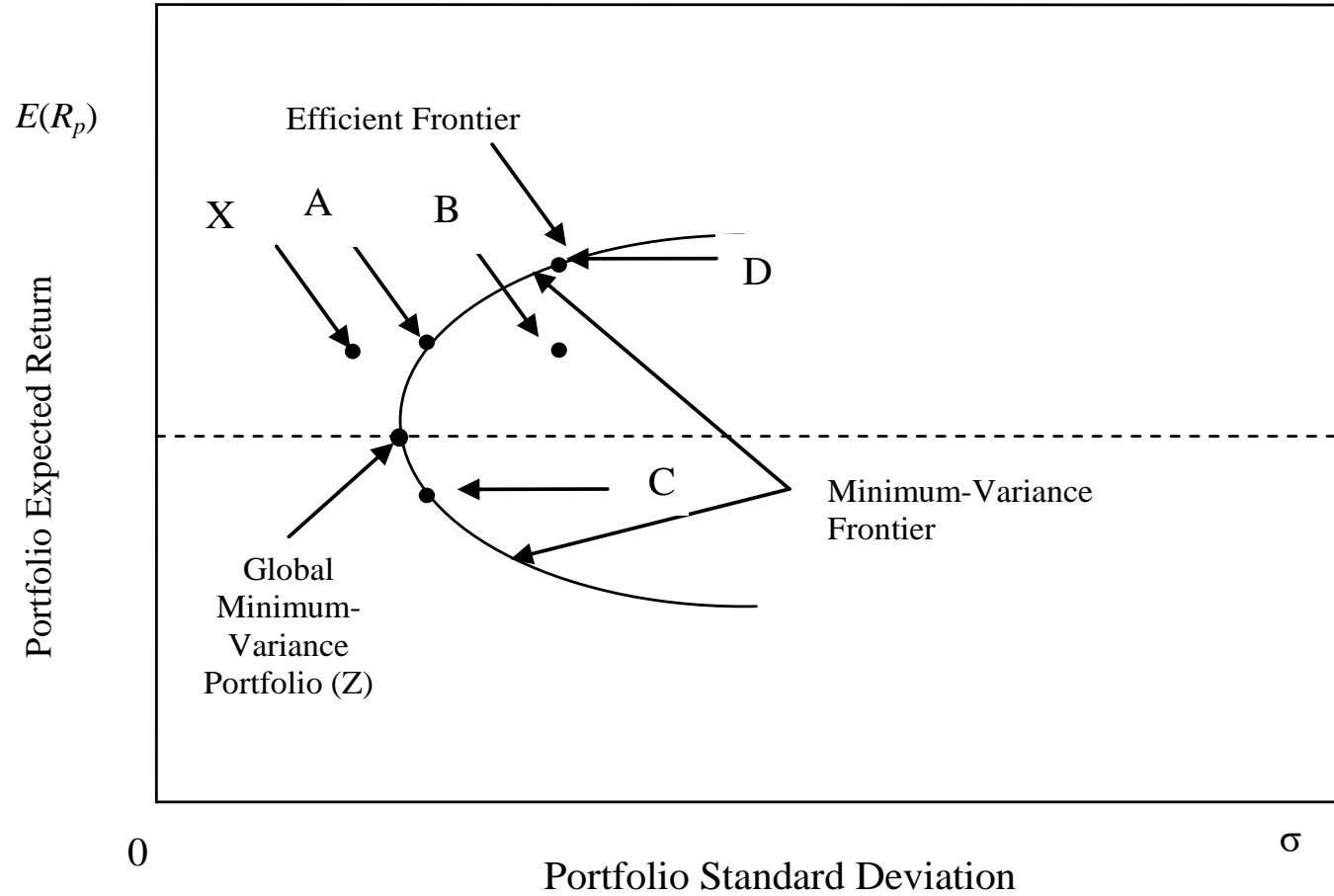
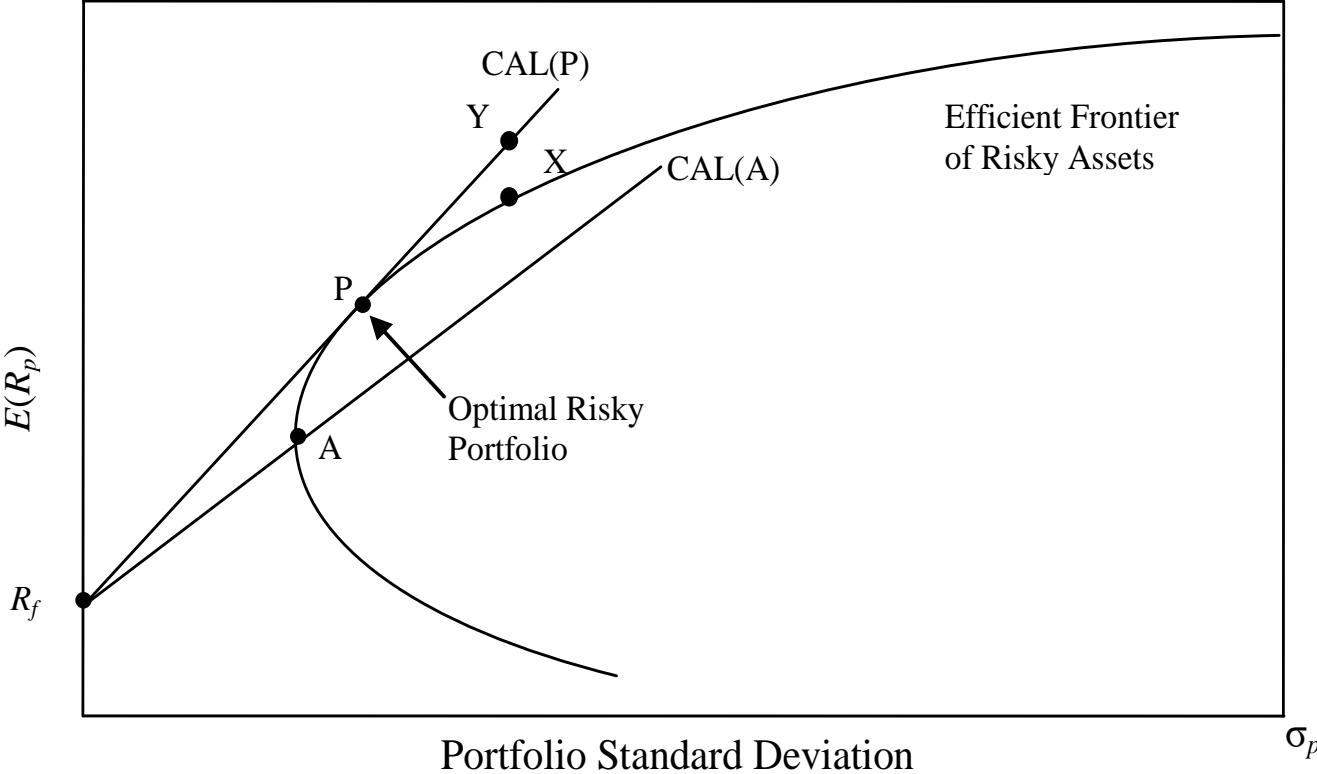


EXHIBIT 5-23 Capital Allocation Line and Optimal Risky Portfolio



CAL(P) is the optimal capital allocation line and portfolio P is the optimal risky portfolio.

The Two-Fund Separation Theorem

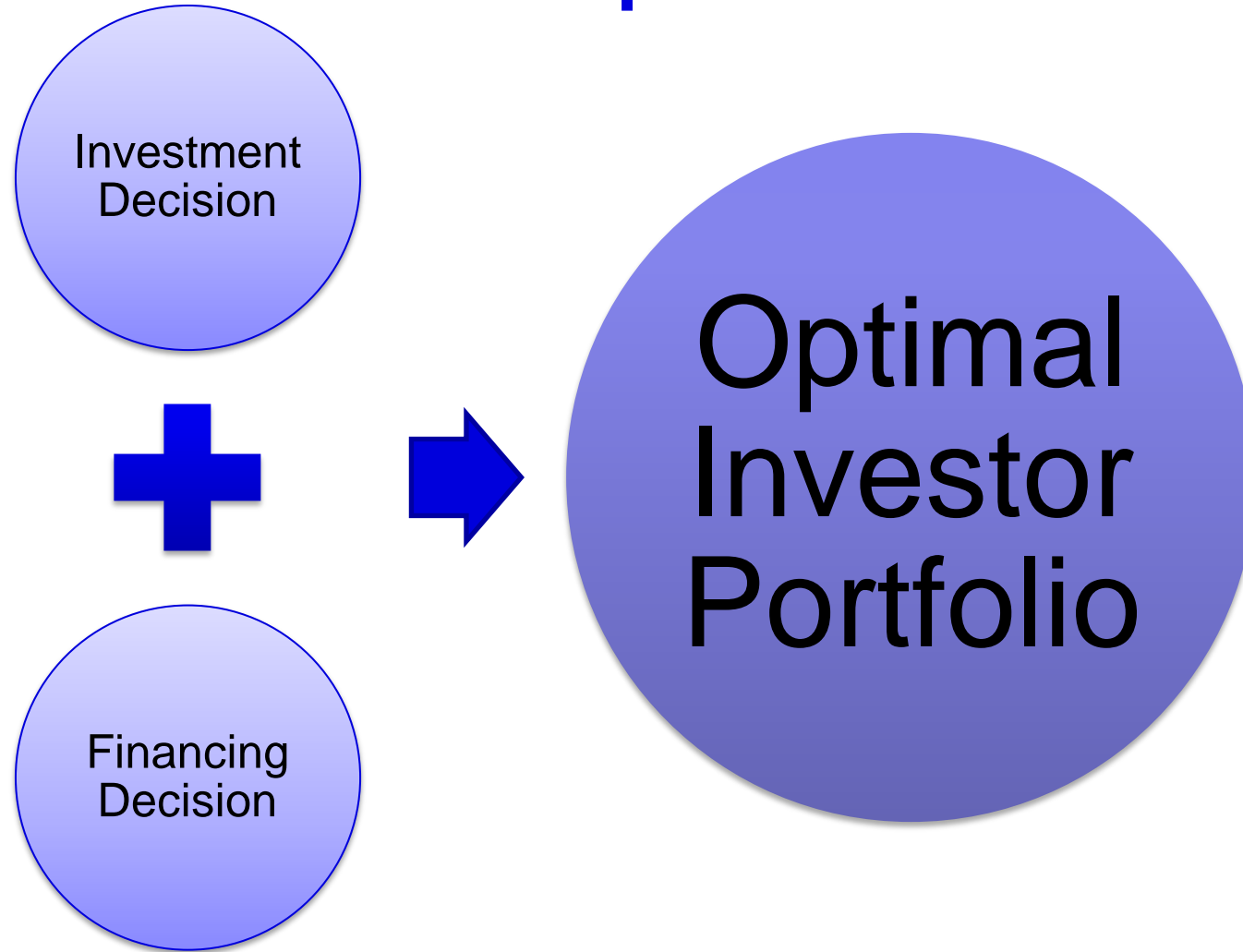
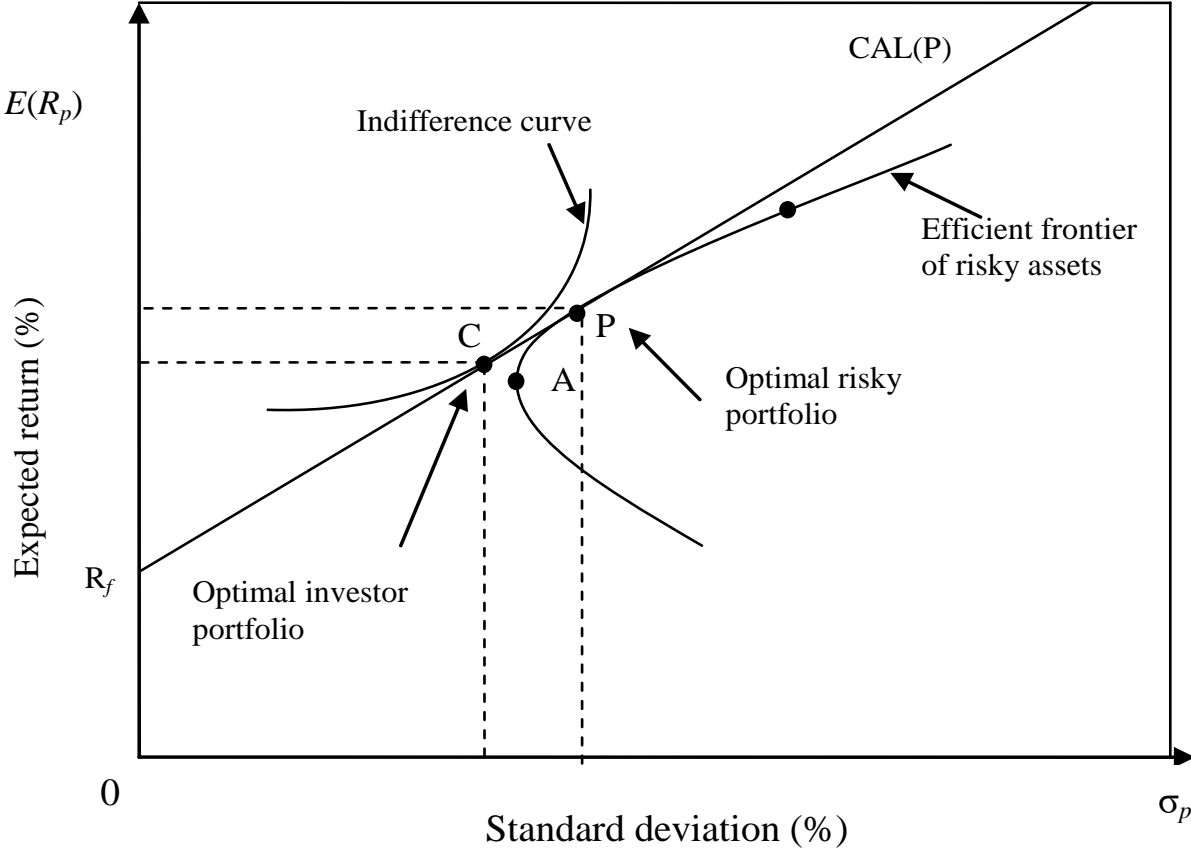


EXHIBIT 5-25 Optimal Investor Portfolio



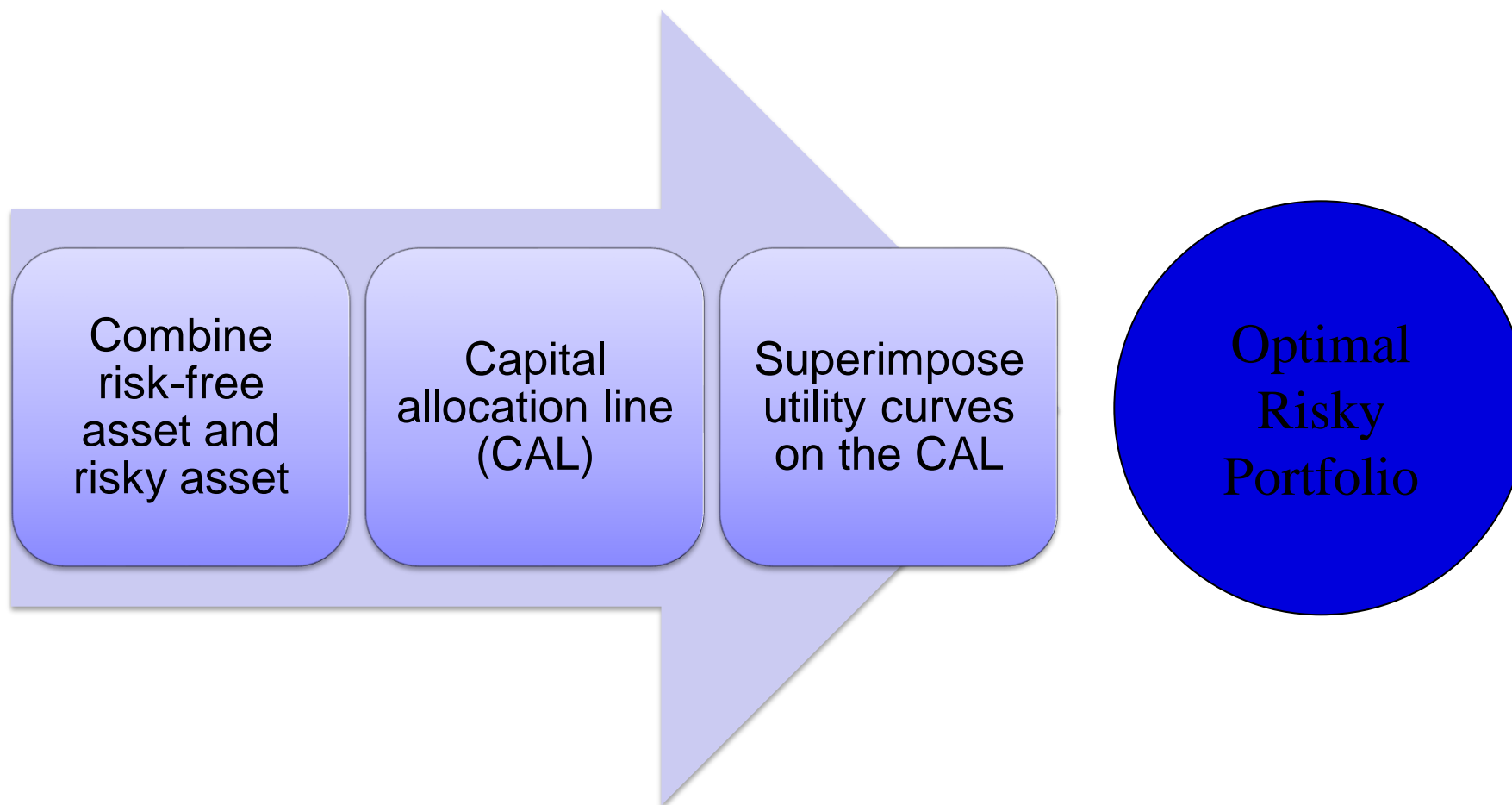
Given the investor's indifference curve, portfolio C on $CAL(P)$ is the optimal portfolio.

EXHIBIT 6-1 Portfolio Risk and Return

Portfolio	Weight in Asset 1	Weight in Asset 2	Portfolio Return	Portfolio Standard Deviation
X	25.0%	75.0%	6.25%	9.01%
Y	50.0	50.0	7.50	11.18
Z	75.0	25.0	8.75	15.21
Return	10.0%	5.0%		
Standard deviation	20.0%	10.0%		
Correlation between Assets 1 and 2		0.0		

$$\sigma_X = \sqrt{(.25^2)(.20^2) + (.75^2)(.10)^2 + (.25)(0)(.20)(.10) + (.75)(0)(.10)(.20)} \approx 9.01\%$$

Portfolio of Risk-Free and Risky Assets



Portfolio Beta

Portfolio beta is the weighted sum of the betas of the component securities:

$$\beta_p = \sum_{i=1}^N w_i \beta_i = (0.40 \times 1.50) + (0.60 \times 1.20) = 1.32$$

The portfolio's expected return given by the CAPM is:

$$E(R_p) = R_f + \beta_p [E(R_m) - R_f]$$

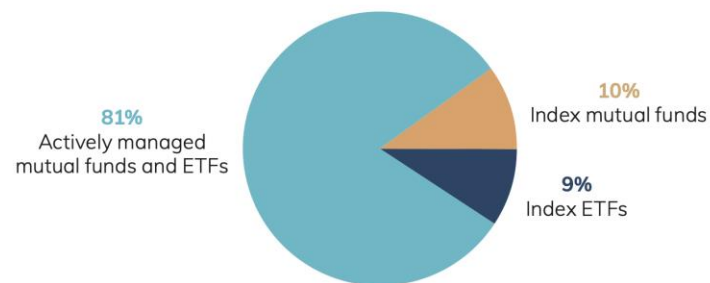
$$E(R_p) = 3\% + 1.32 [9\% - 3\%] = 10.92\%$$

Comparison of funds performance

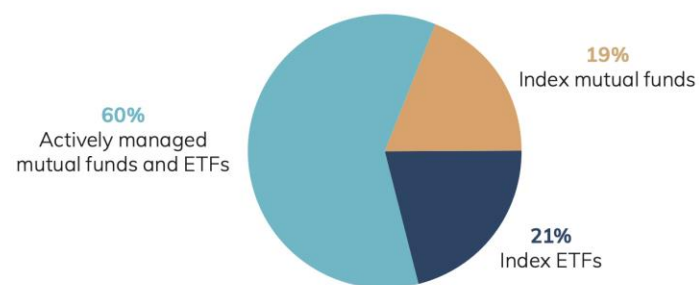
Active vs. Passive Investing

Index Funds Have Grown as a Share of the Fund Market

Percentage of total net assets, year-end



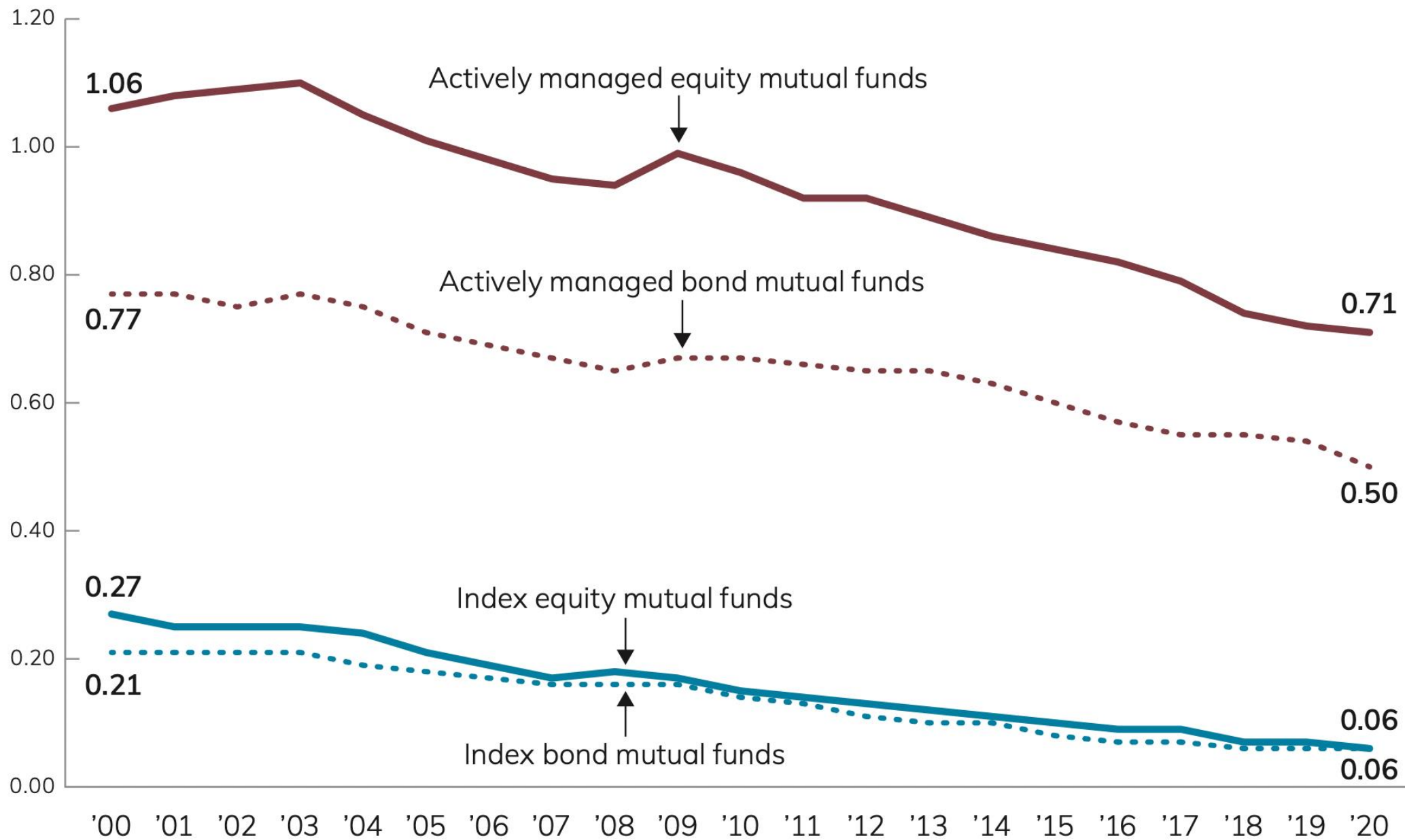
2010 total net assets: \$9.9 trillion



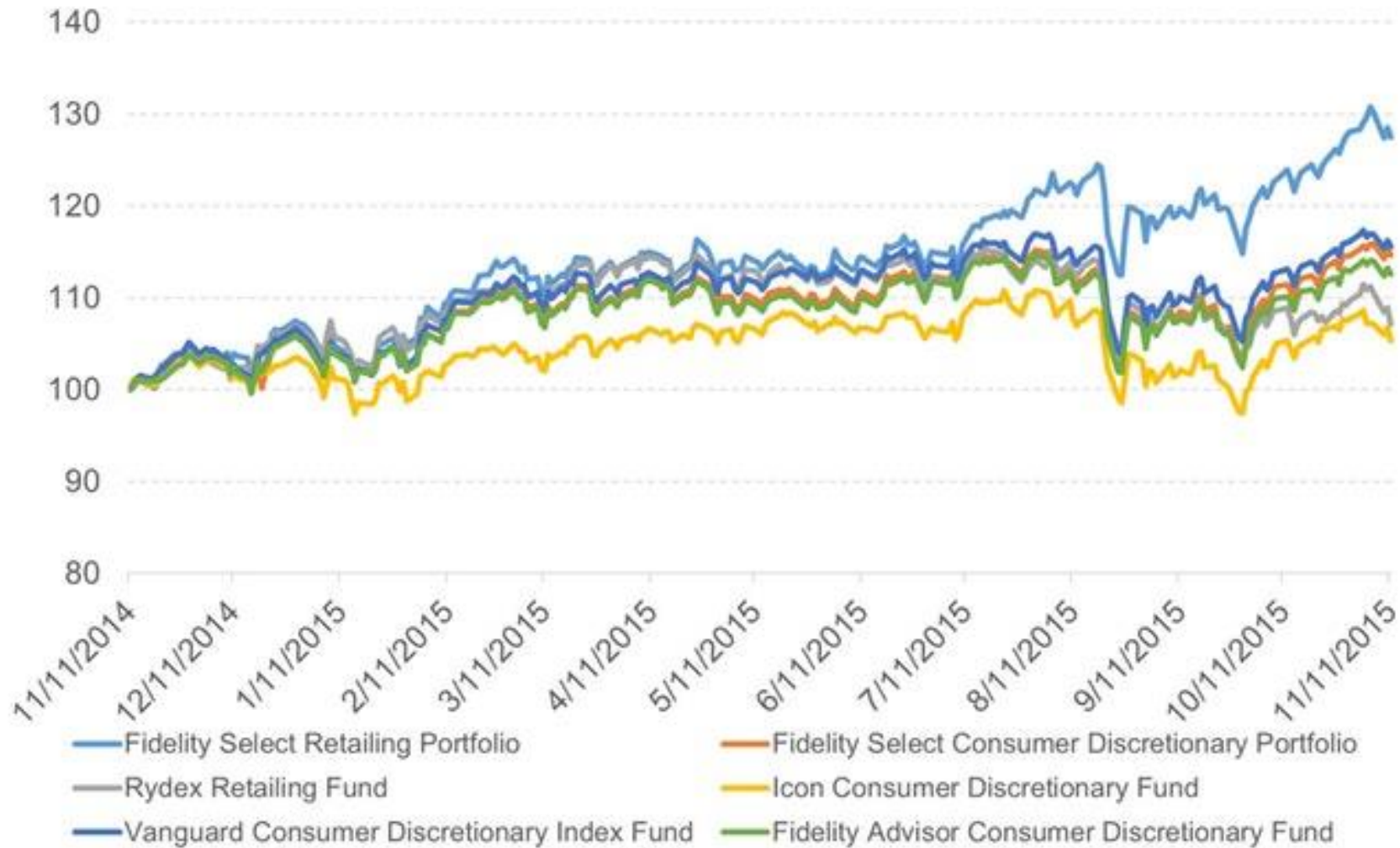
2020 total net assets: \$24.9 trillion

Expense Ratios of Actively Managed and Index Mutual Funds Have Fallen

Percent



Performance Comparison of Consumer Discretionary Mutual Funds



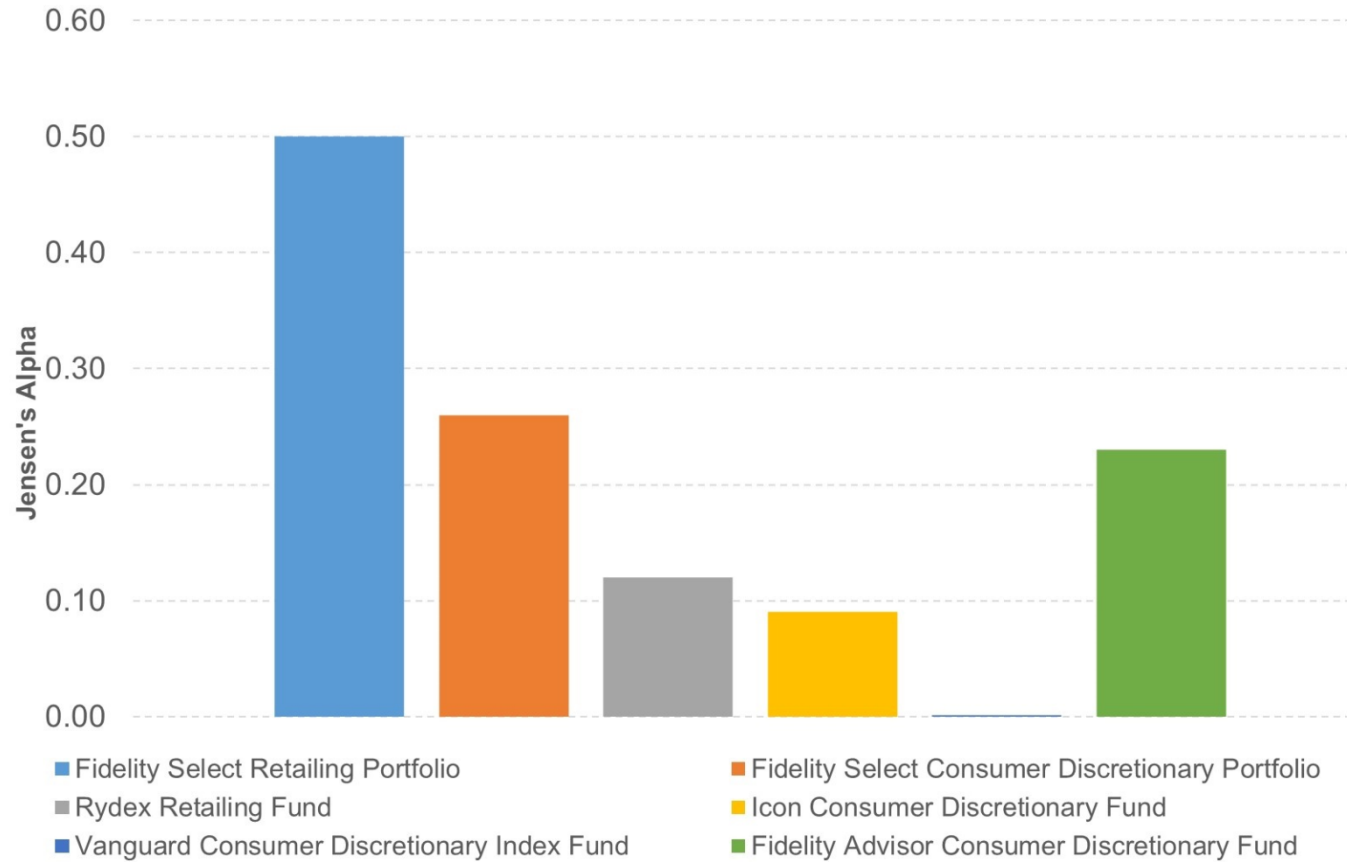
Jensen's alpha

Jensen's alpha helps an investor determine how much extra return a fund has earned above the expected return while considering the non-diversifiable risk of the market. The expected return is calculated using the CAPM (capital asset pricing model). A positive Jensen's alpha indicates that the managers of the fund, through careful stock selection, have been able to extract higher returns than the market (which in our case is the underlying indexes).

Jensen's alpha is calculated as follows:

Jensen's alpha = (portfolio return – expected return CAPM)

Jensen's Alpha of Consumer Discretionary Mutual Funds



The Sharpe ratio

Investors often use the Sharpe ratio to gauge the performance of investment portfolios. The Sharpe ratio measures the units of excess return earned by a portfolio over the risk-free rate for every unit of risk taken. The risk is the standard deviation of the portfolio returns. The equation for the Sharpe ratio is as follows:

Sharpe ratio = (average return of portfolio – risk-free rate of return)/standard deviation of portfolio returns

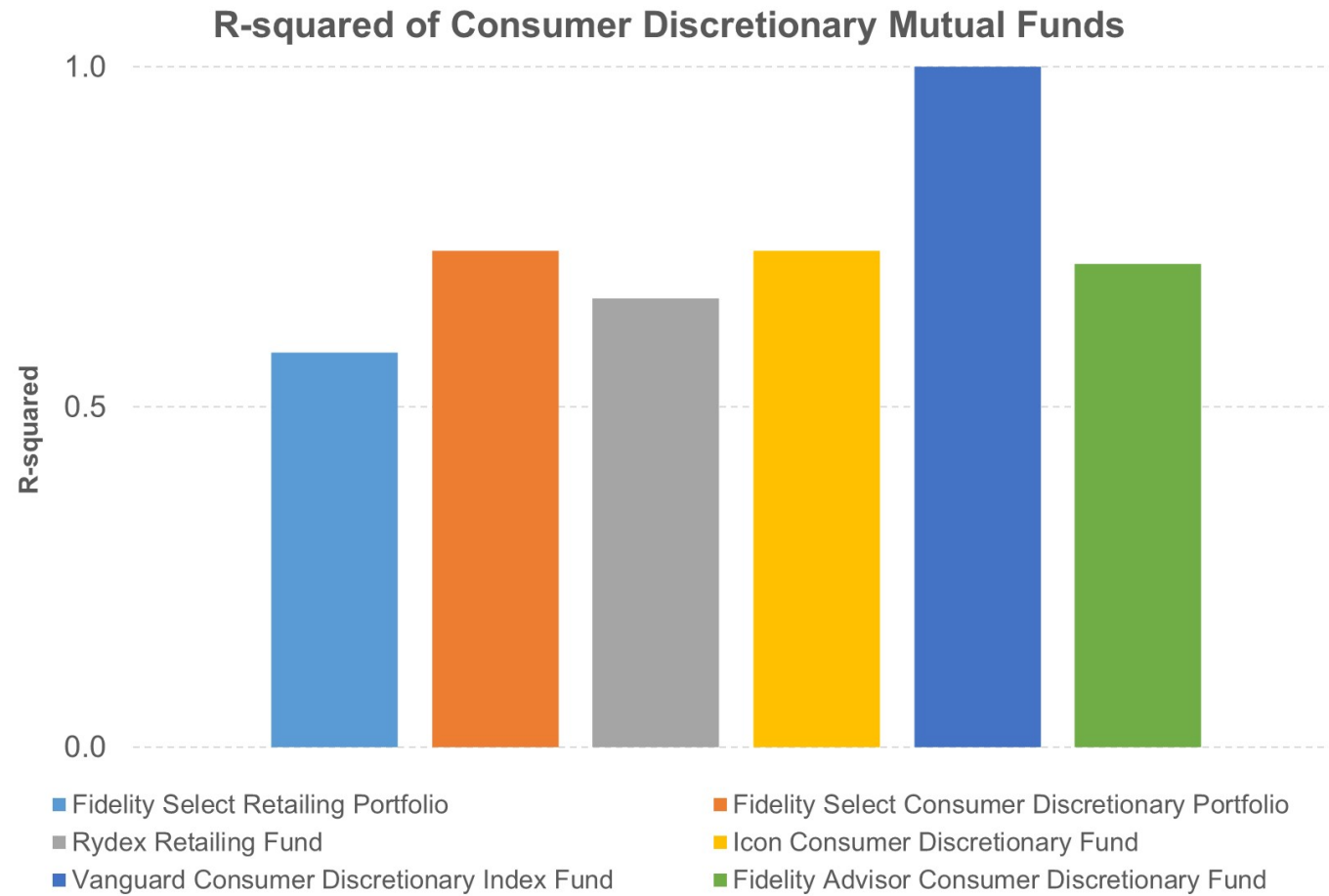
Sharpe Ratio of Consumer Discretionary Mutual Funds



R-squared value

The R-squared value is a statistical measure that compares the movement of a fund against that of its benchmark index. The R-squared value ranges from 0 to 1. A value closer to 1 indicates that the fund's performance follows the movement of the underlying index, whereas a fund with a low R-squared value does not closely follow the performance of the underlying index.

R-squared value

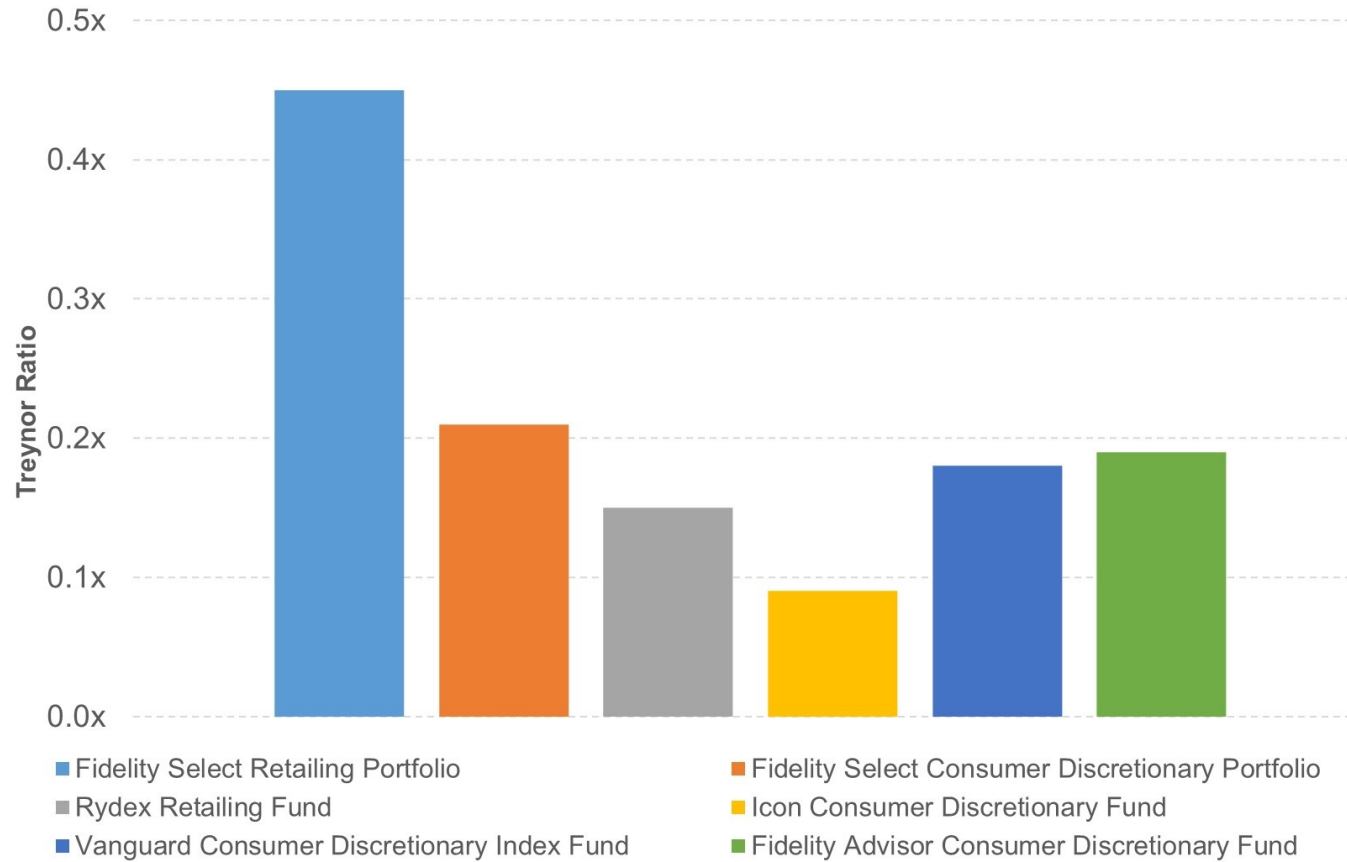


The Treynor ratio

The Treynor ratio calculates how much an investment has earned above the risk-free market rate for every unit of risk assumed. Although it is similar to the Sharpe ratio, its measure of risk is different. Whereas the Sharpe ratio considers the total risk of the investment, the Treynor ratio only considers the systematic risk, assuming that the non-systematic risk is fully diversified in developing the portfolio. Risk in the Treynor ratio, represented by beta, is the systematic risk or non-diversifiable risk. The equation for the Treynor ratio is as follows:

Treynor ratio = (average return of portfolio – risk-free rate of

Treynor Ratio of Consumer Discretionary Mutual Funds

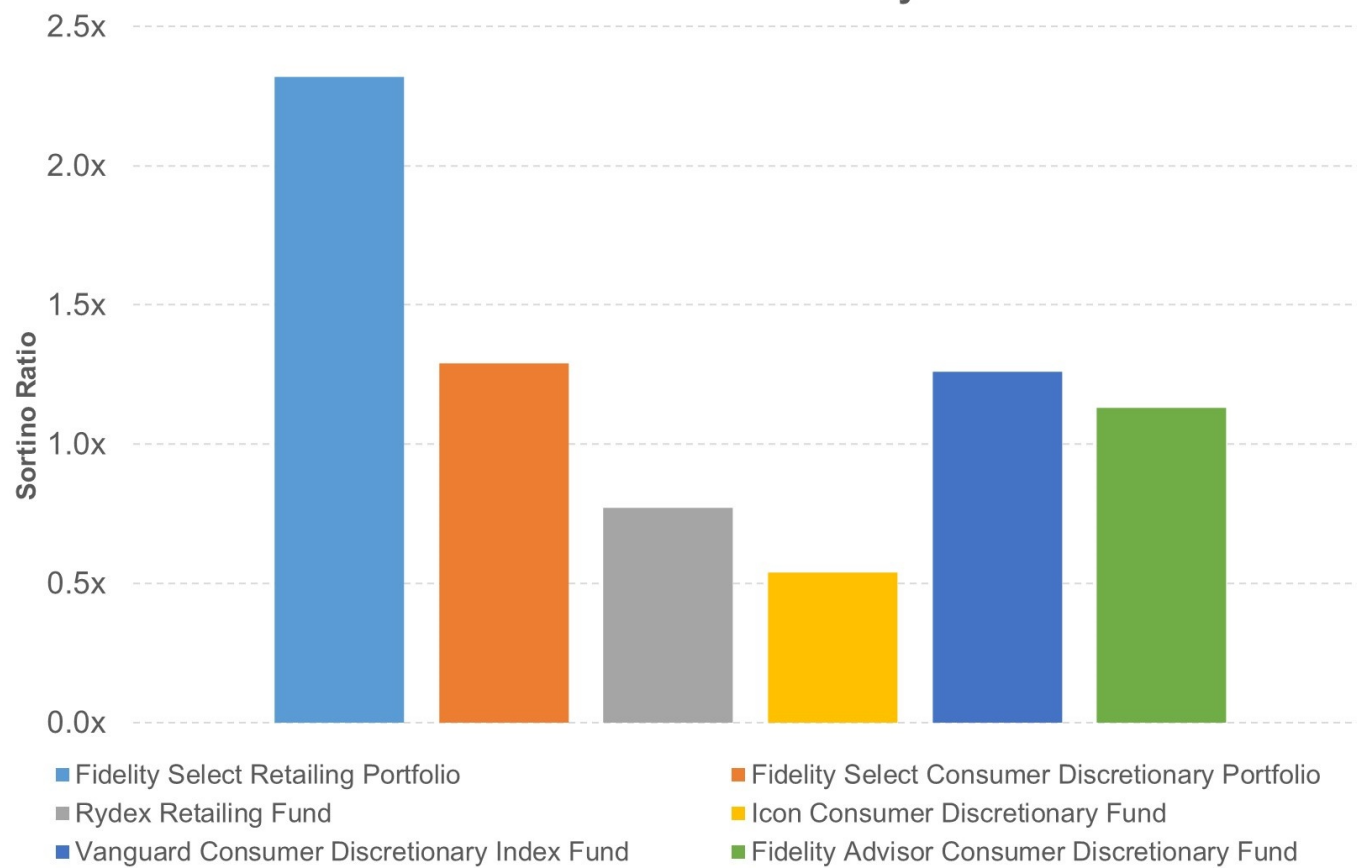


The Sortino ratio

The Sharpe ratio can sometimes be unfavorable for stocks that have high upside volatility. To prevent this, we can use the Sortino ratio. Although the calculation of the Sortino ratio is similar to that of the Sharpe ratio, the Sortino ratio's denominator is the downside deviation of the portfolio. The equation for the Sortino ratio is as follows:

Sortino ratio = (average return of portfolio – risk-free rate of return)/downside deviation of portfolio returns

Sortino Ratio of Consumer Discretionary Mutual Funds



The information ratio

The information ratio can be used to evaluate the performance of an actively managed fund. It can determine how consistently the manager of the fund has generated excess returns for its investors. In simple terms, it is the ratio of the active return generated by the manager over the index return, divided by the active risk taken. The risk taken is measured by the standard deviation of the difference between the returns of the portfolio and the index, which is referred to as the tracking error. The equation is as follows:

$$\text{Information ratio} = (\text{portfolio return} - \text{benchmark return}) / \text{tracking error}$$

Information Ratio of Consumer Discretionary Mutual Funds

