

INTERMEDIATE

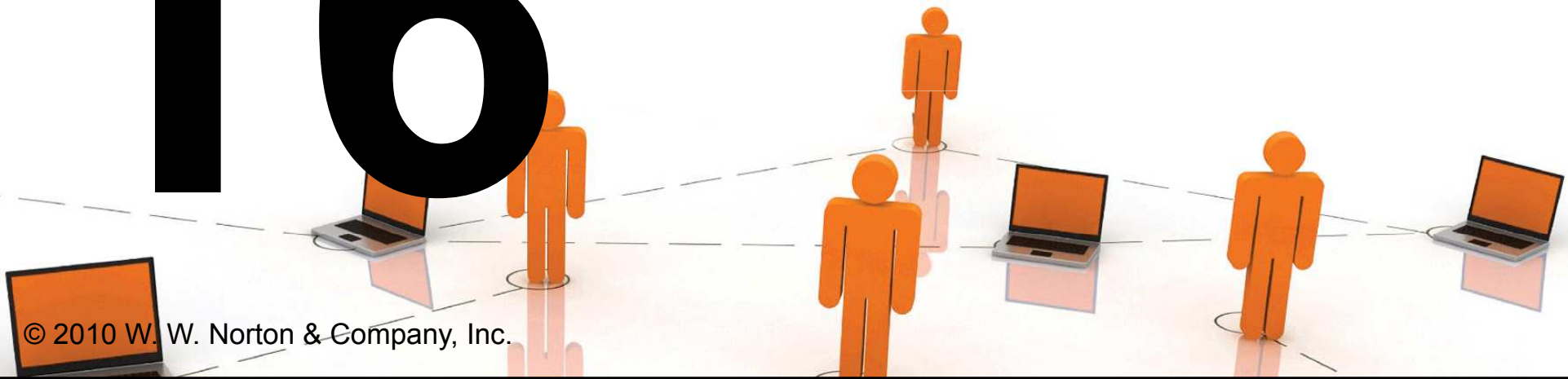
8TH EDITION

# MICROECONOMICS

HAL R. VARIAN

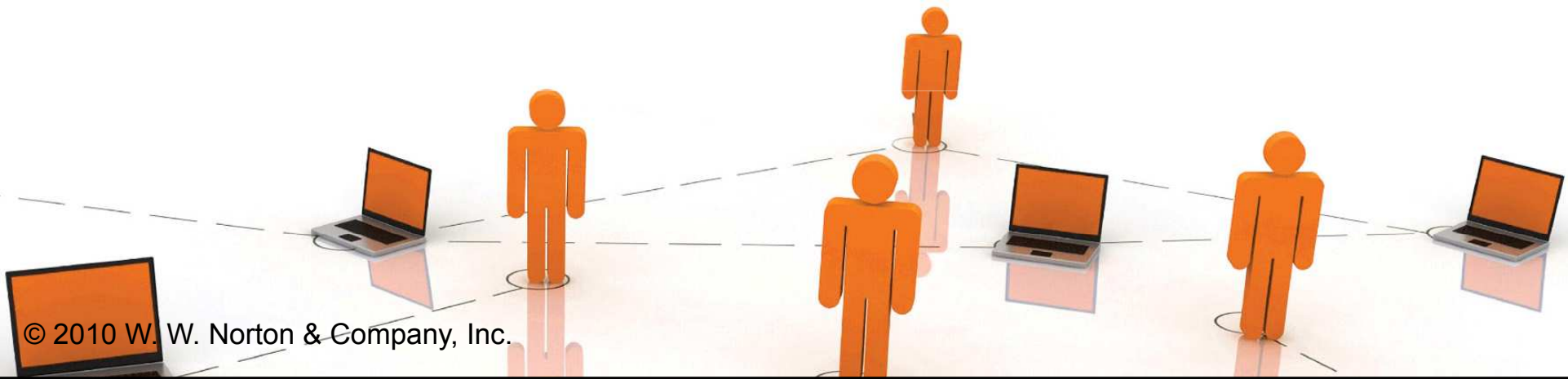
16

Equilibrium

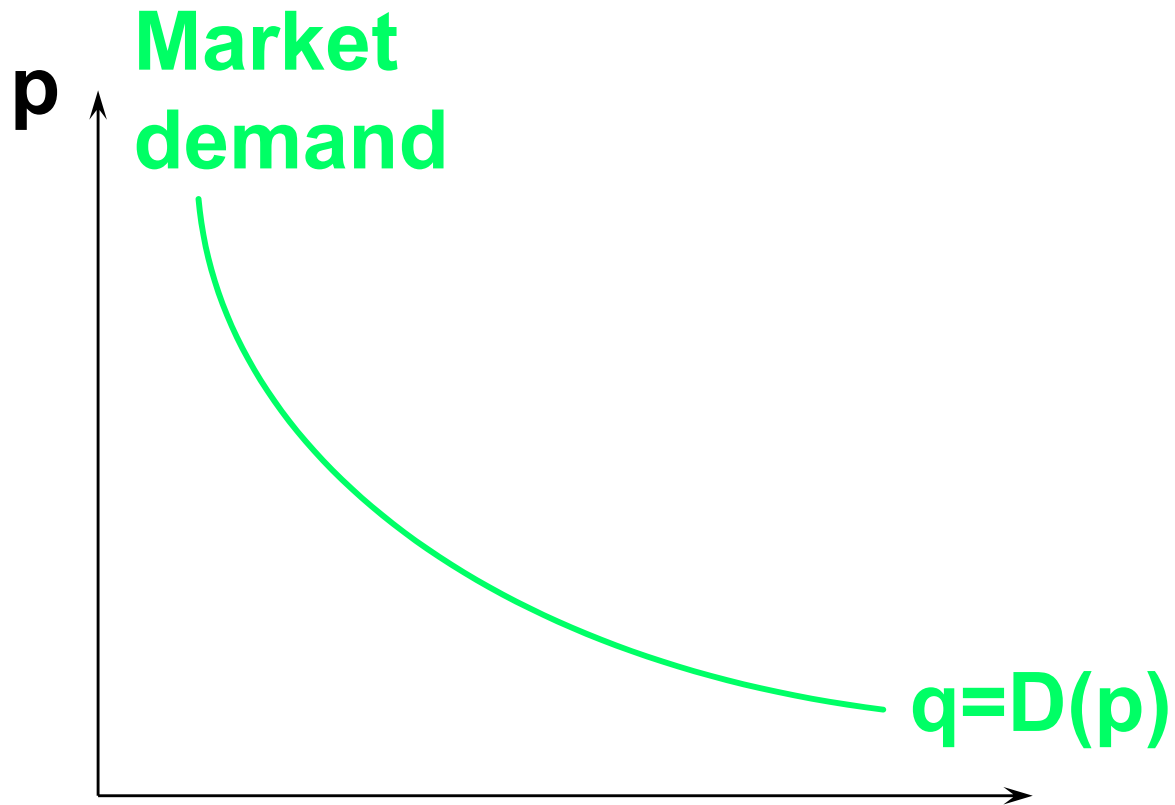


# Market Equilibrium

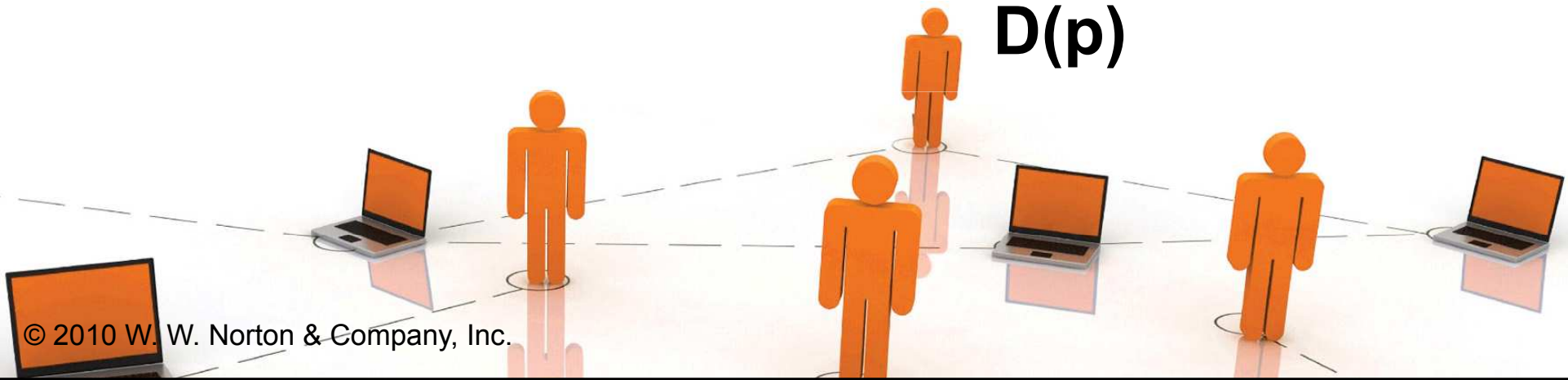
- ◆ **A market is in equilibrium when total quantity demanded by buyers equals total quantity supplied by sellers.**



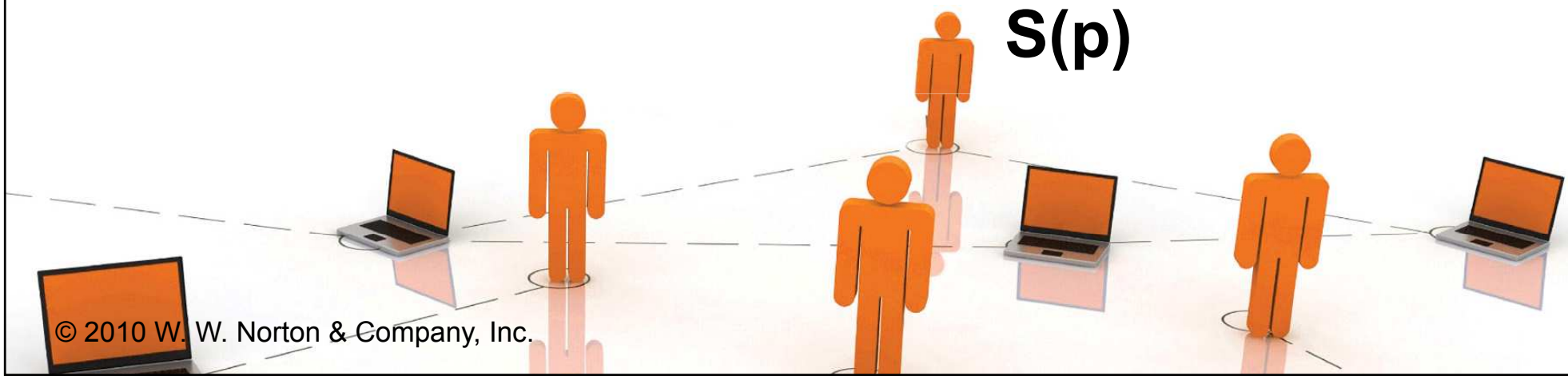
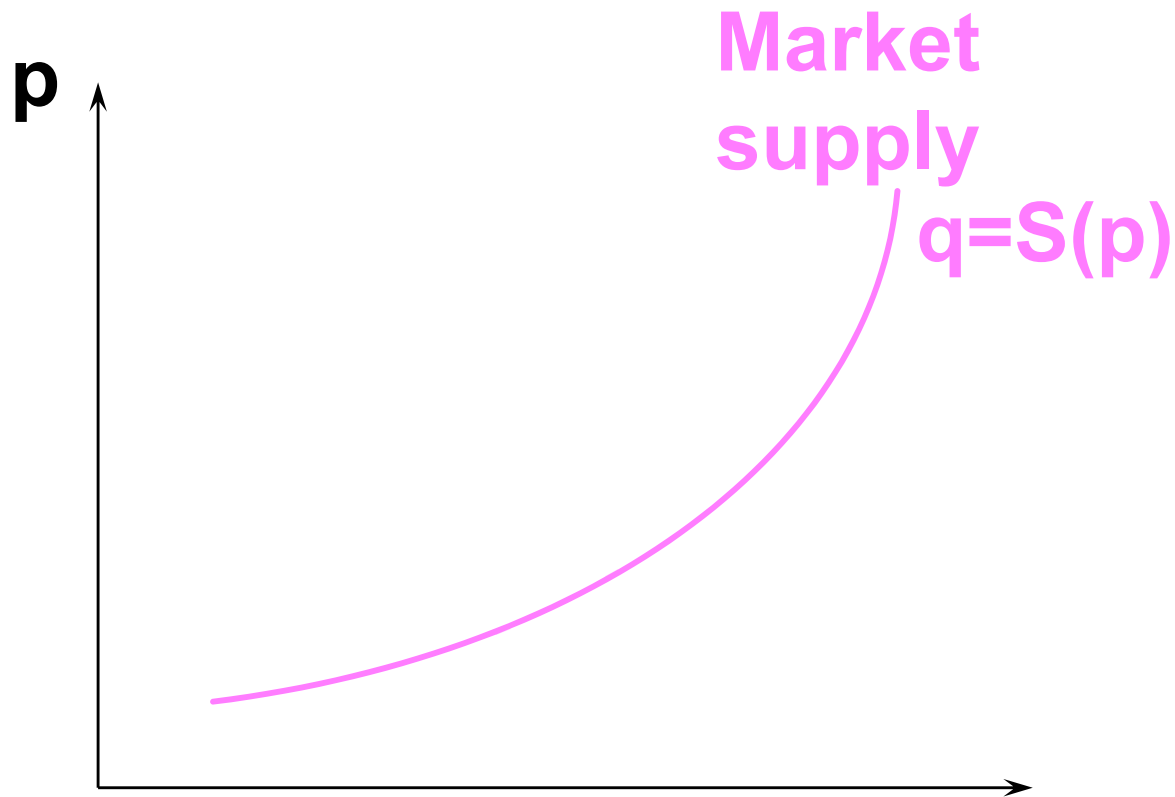
# Market Equilibrium



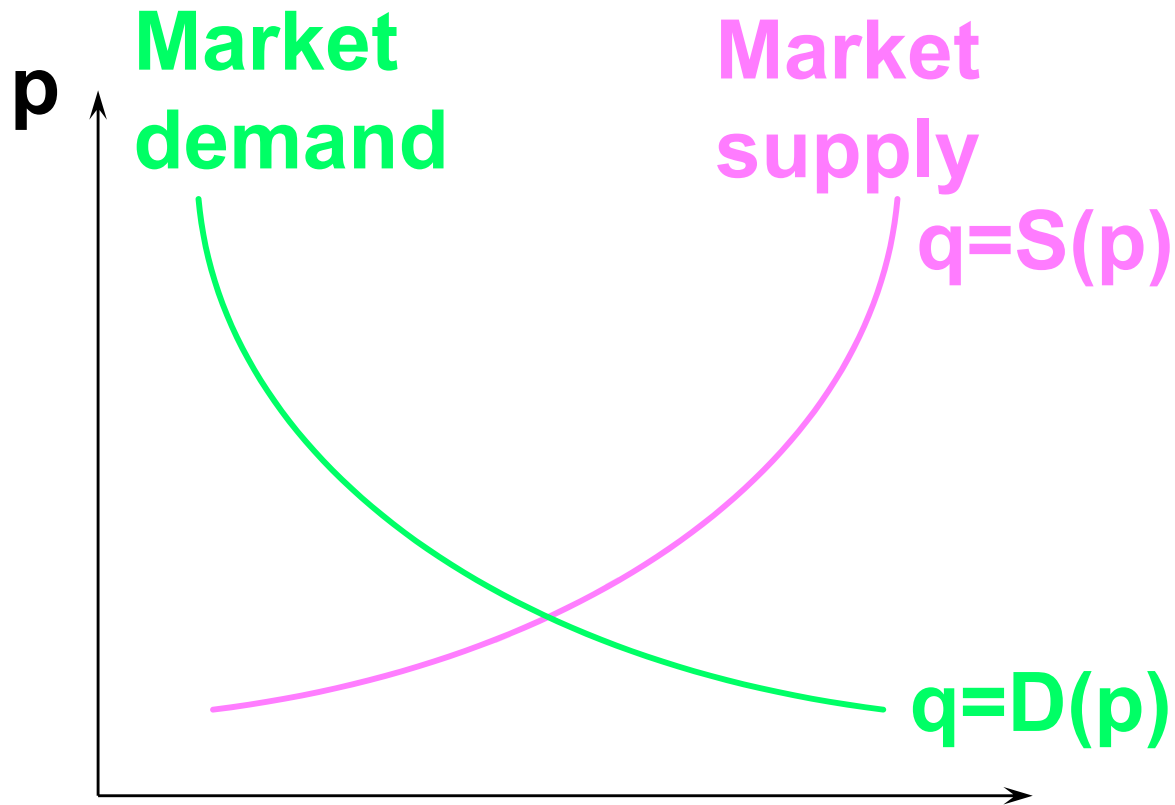
**$D(p)$**



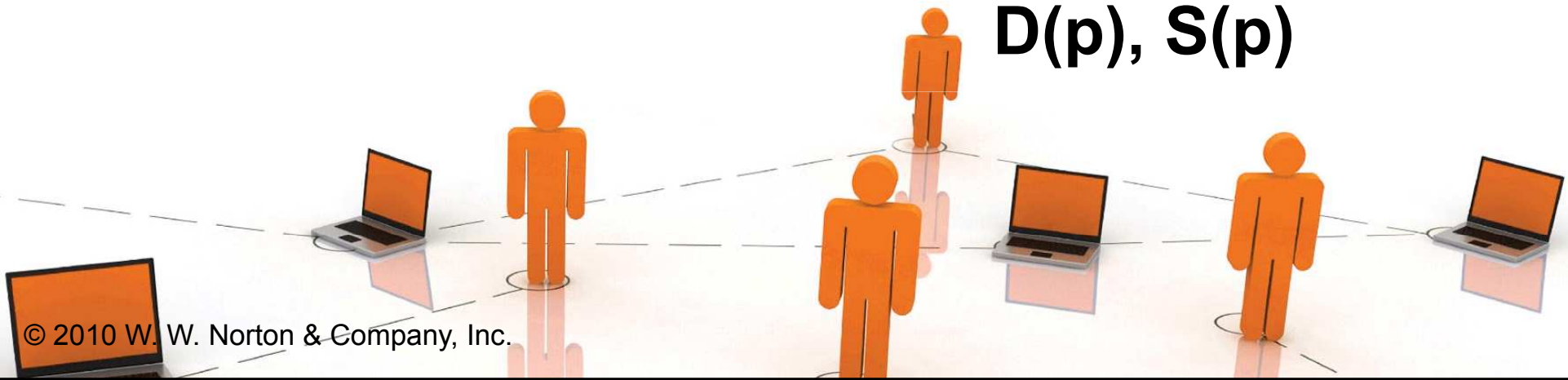
# Market Equilibrium



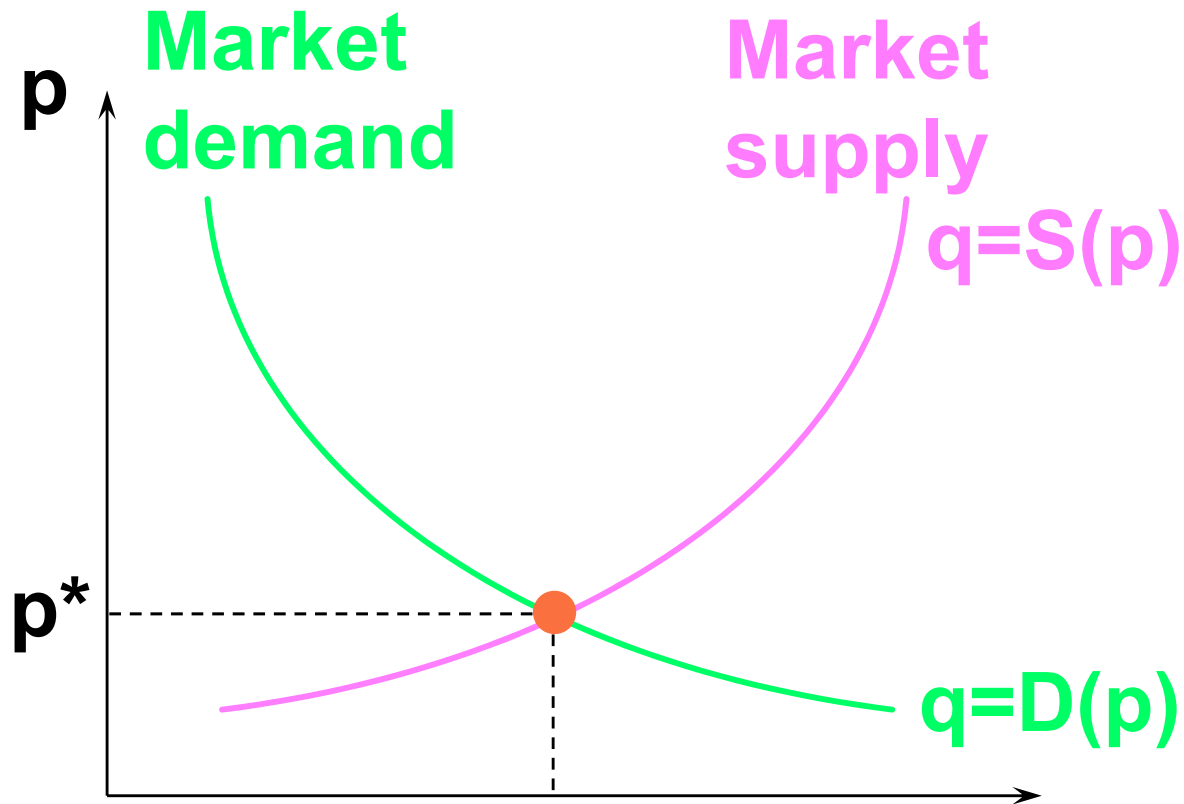
# Market Equilibrium



$D(p), S(p)$



# Market Equilibrium

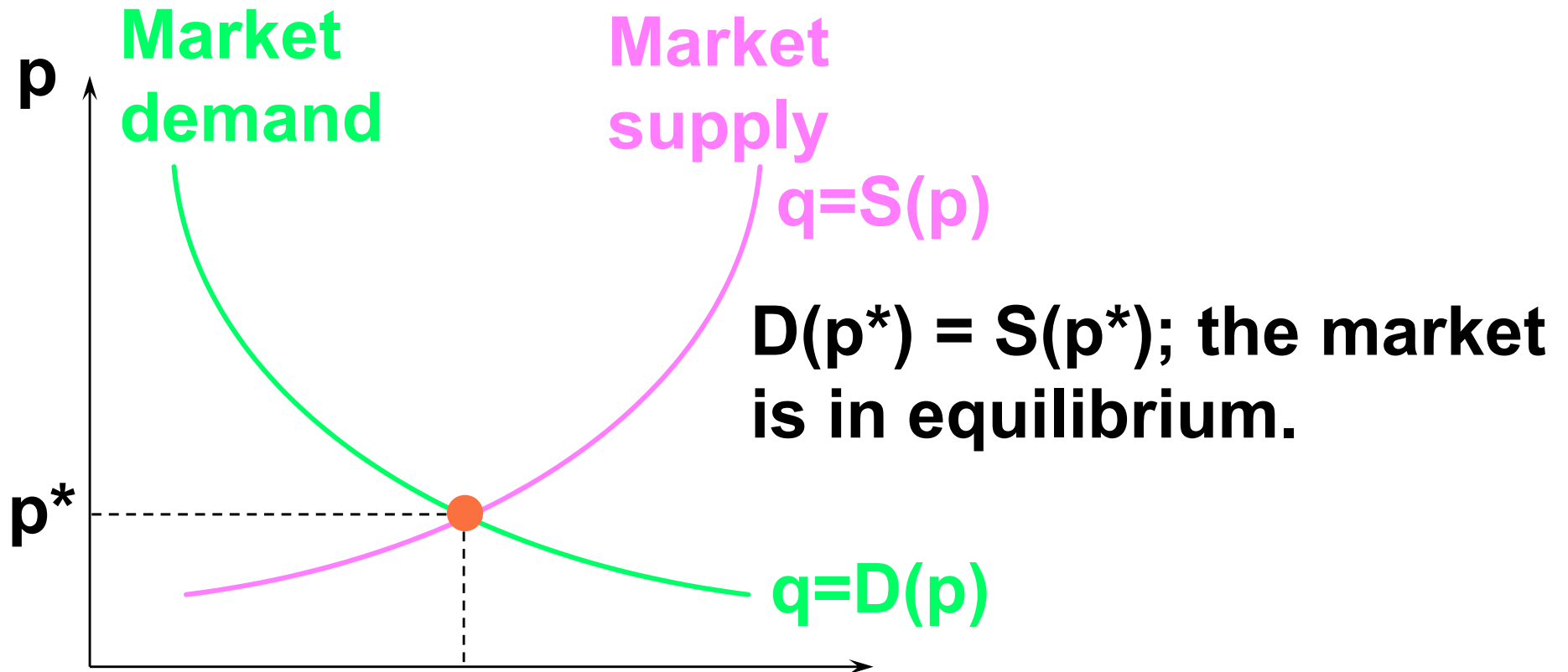


$q^*$

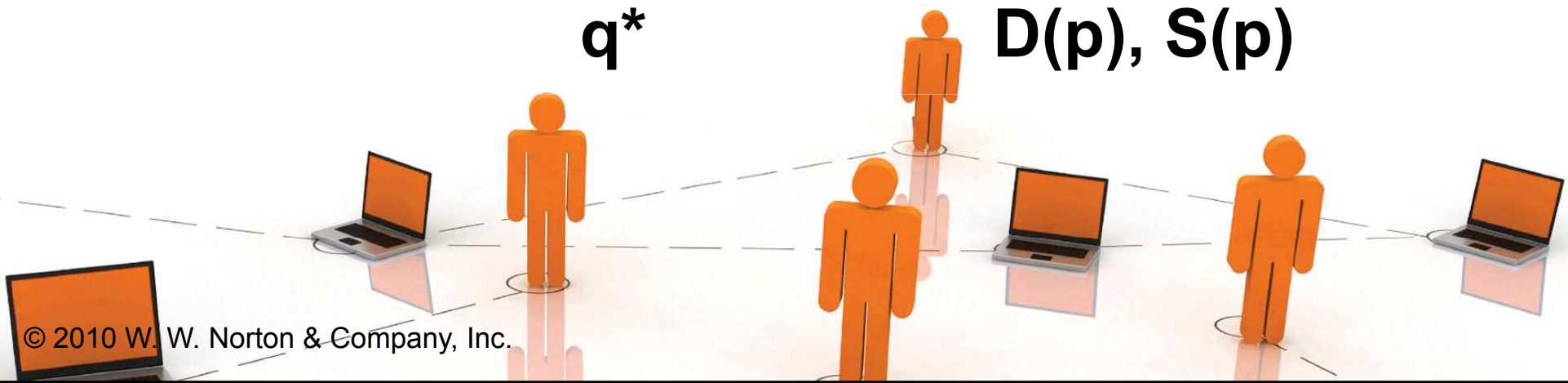
$D(p), S(p)$



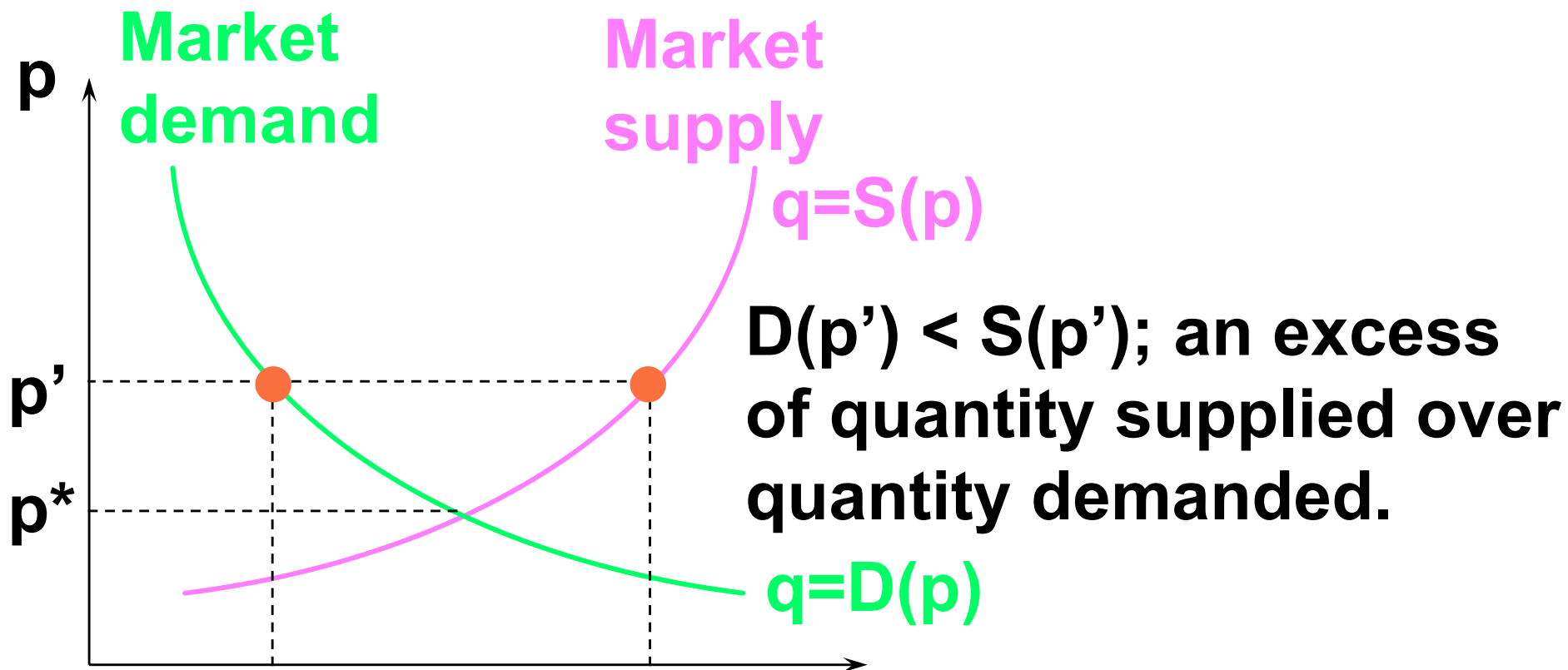
# Market Equilibrium



$q^*$   **$D(p), S(p)$**



# Market Equilibrium



$D(p')$

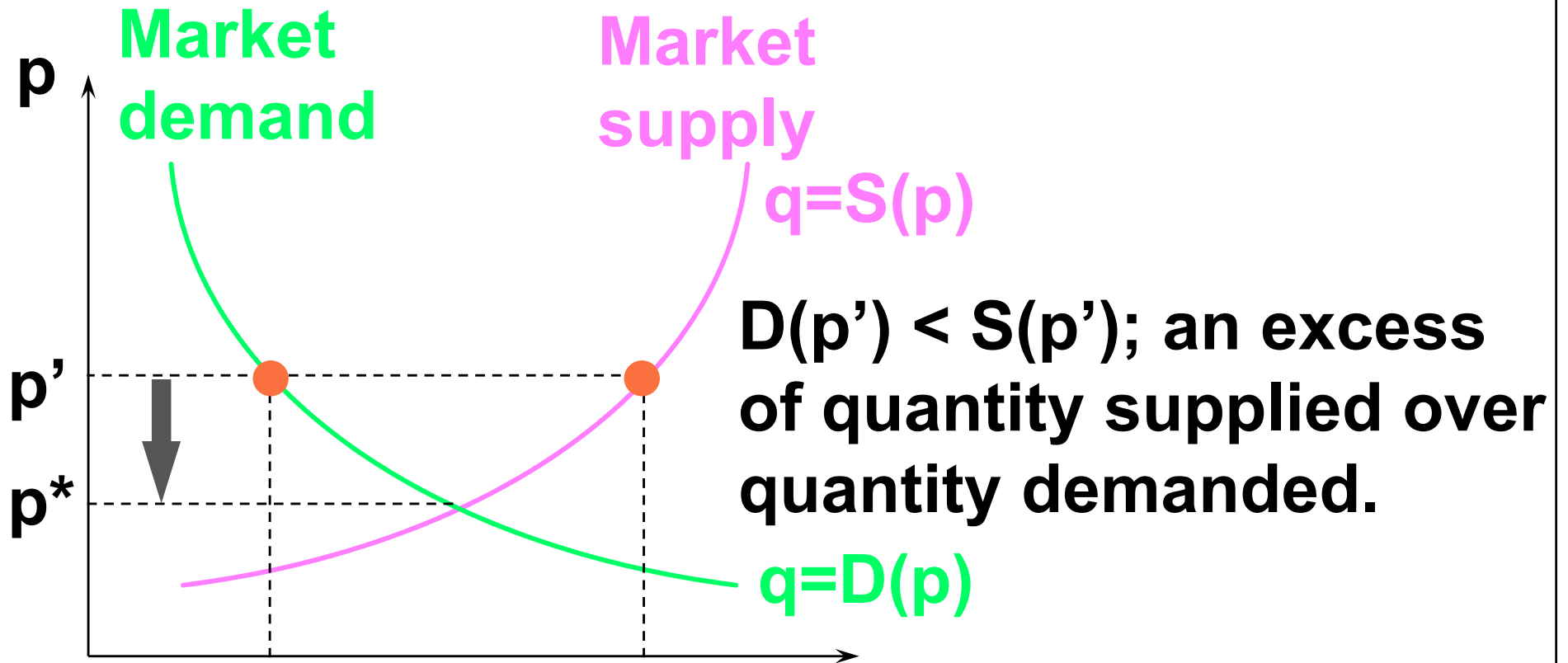
$S(p')$

$D(p), S(p)$





# Market Equilibrium



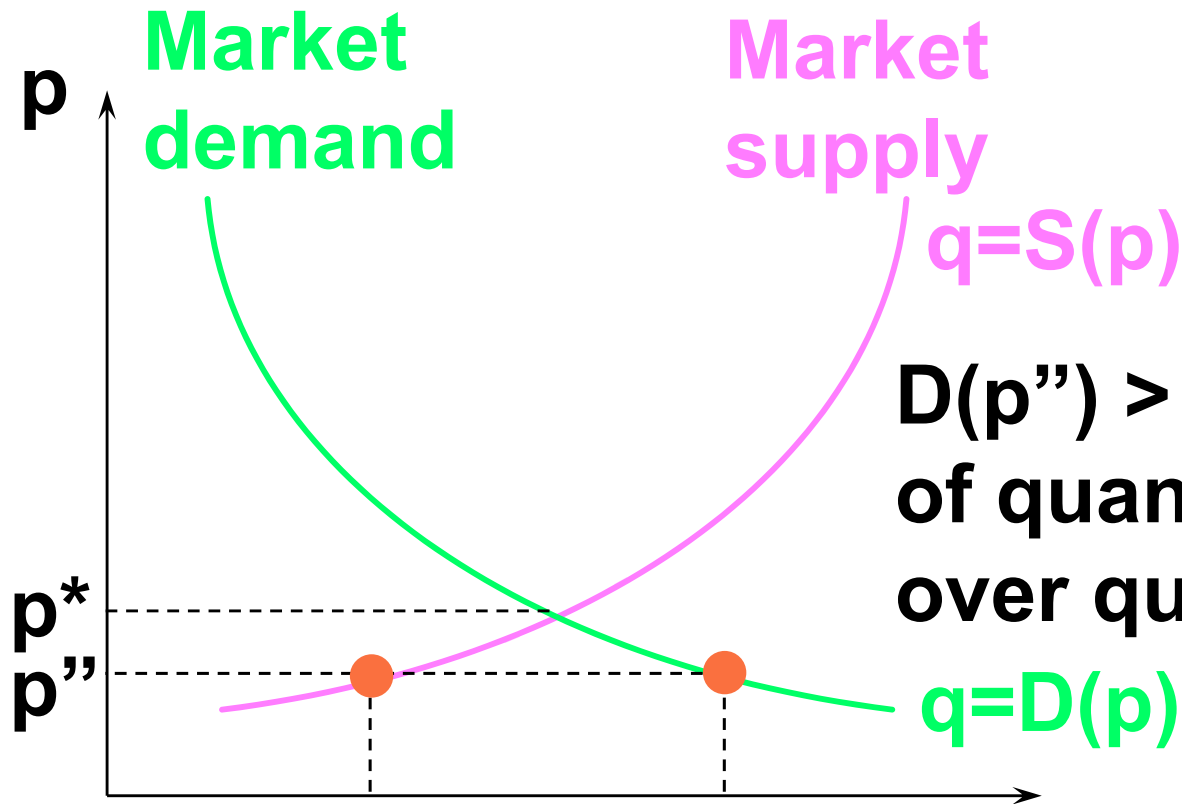
$D(p')$

$S(p')$

$D(p), S(p)$

**Market price must fall towards  $p^*$ .**

# Market Equilibrium



$D(p'') > S(p'')$ ; an excess of quantity demanded over quantity supplied.

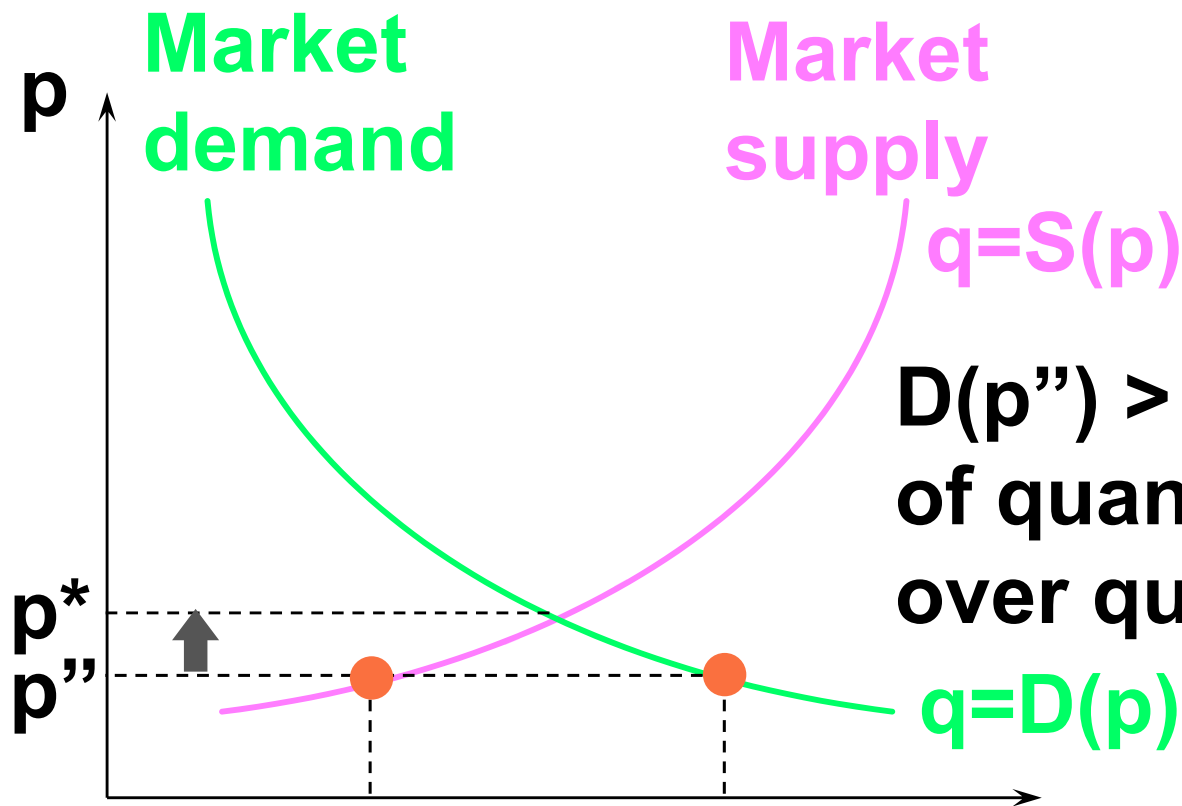
$S(p'')$

$D(p'')$

$D(p), S(p)$



# Market Equilibrium



$D(p'') > S(p'')$ ; an excess of quantity demanded over quantity supplied.

$S(p'')$

$D(p'')$

$D(p), S(p)$

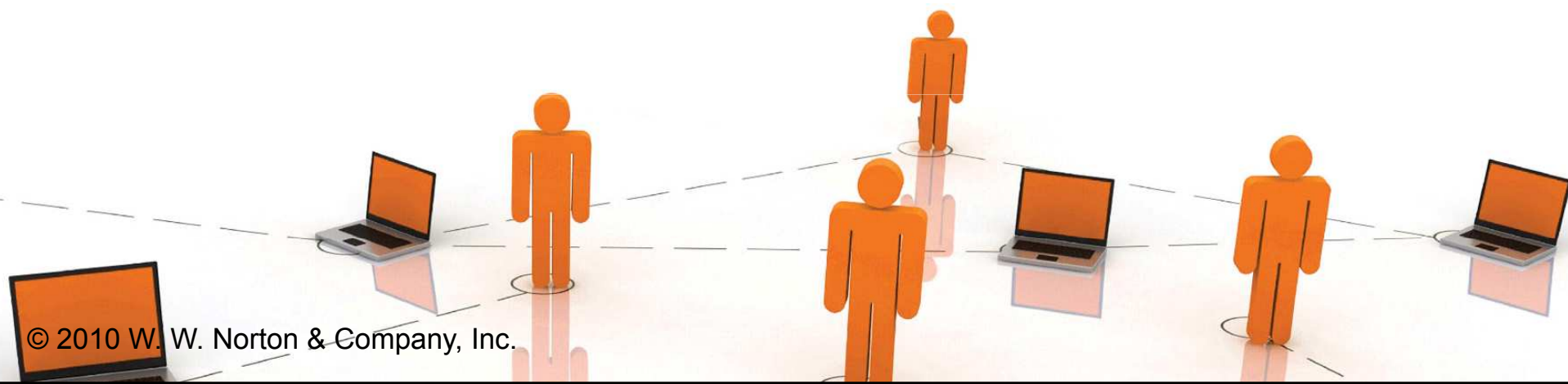
**Market price must rise towards  $p^*$ .**

# Market Equilibrium

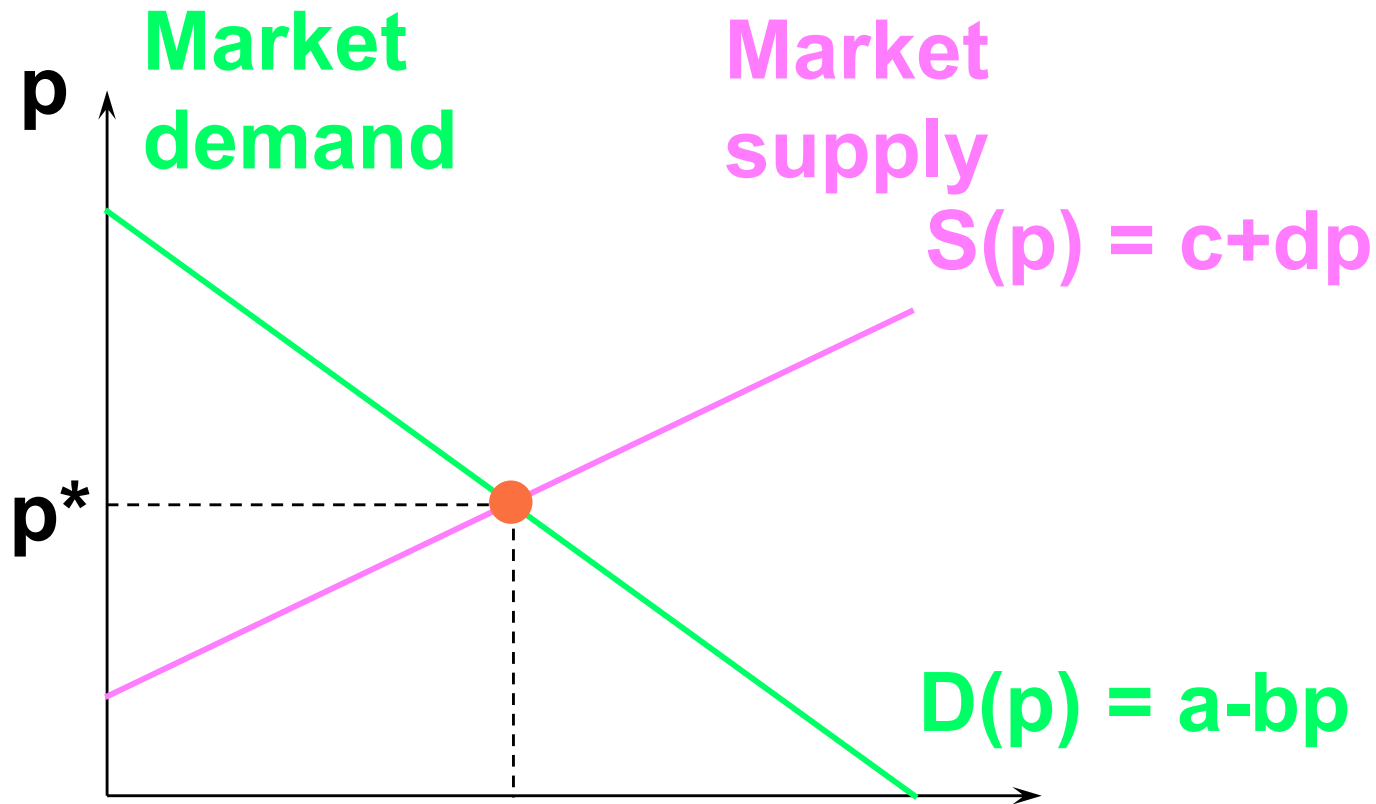
- ◆ **An example of calculating a market equilibrium when the market demand and supply curves are linear.**

$$D(p) = a - bp$$

$$S(p) = c + dp$$



# Market Equilibrium

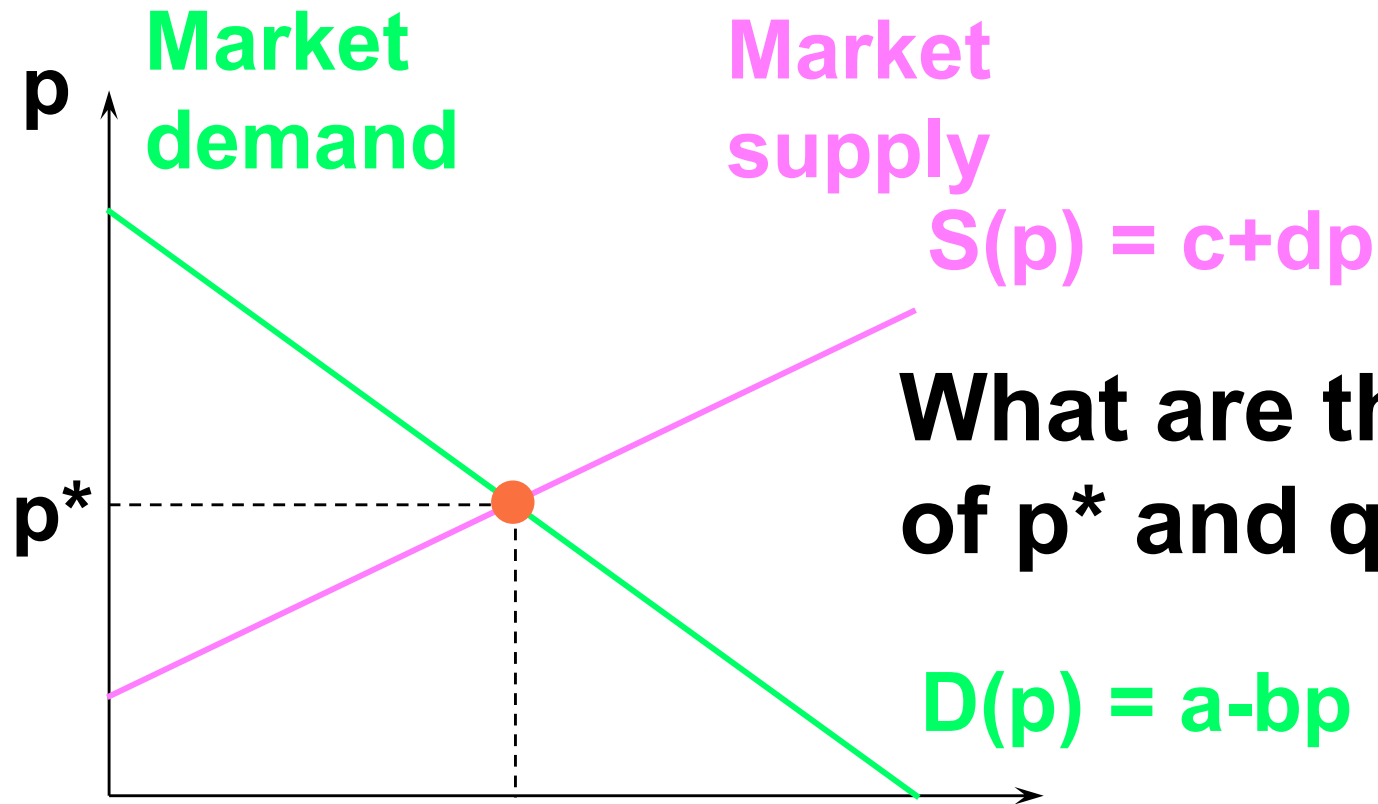


$q^*$

$D(p), S(p)$



# Market Equilibrium



What are the values of  $p^*$  and  $q^*$ ?

$$D(p) = a - bp$$

$$S(p) = c + dp$$

$q^*$

$D(p), S(p)$

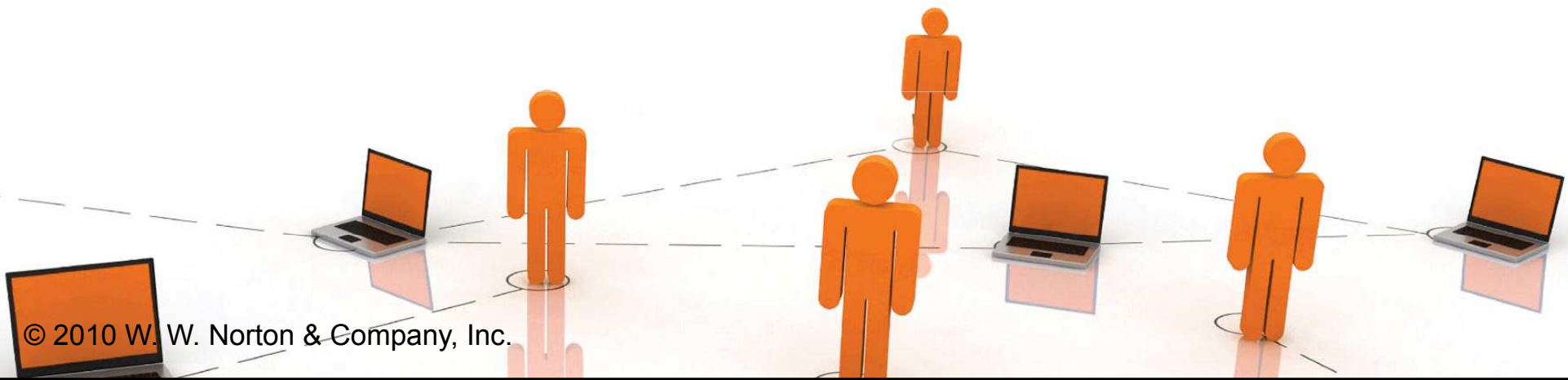


# Market Equilibrium

$$D(p) = a - bp$$

$$S(p) = c + dp$$

**At the equilibrium price  $p^*$ ,  $D(p^*) = S(p^*)$ .**



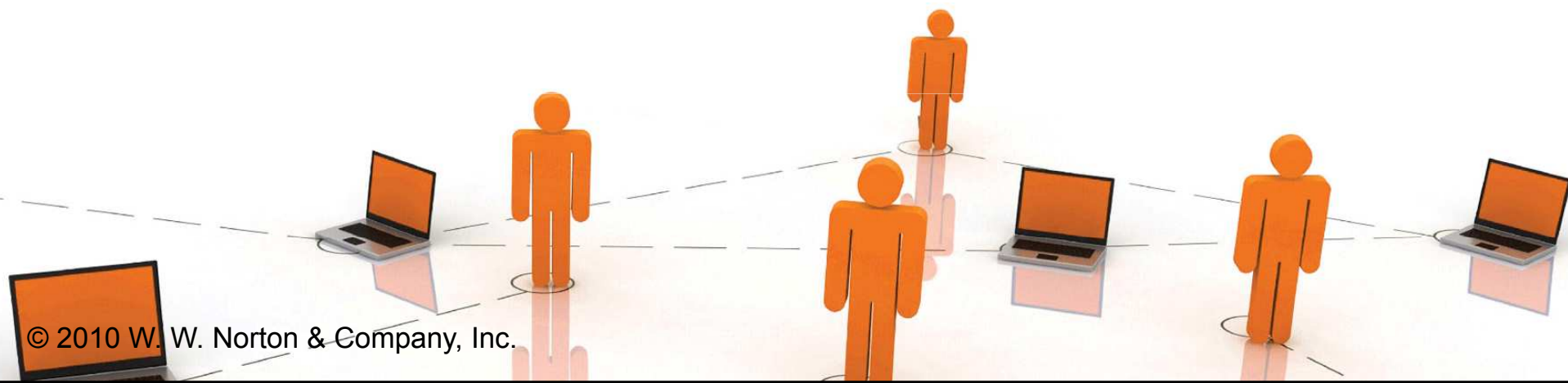
# Market Equilibrium

$$D(p) = a - bp$$

$$S(p) = c + dp$$

**At the equilibrium price  $p^*$ ,  $D(p^*) = S(p^*)$ .**

**That is,  $a - bp^* = c + dp^*$**





# Market Equilibrium

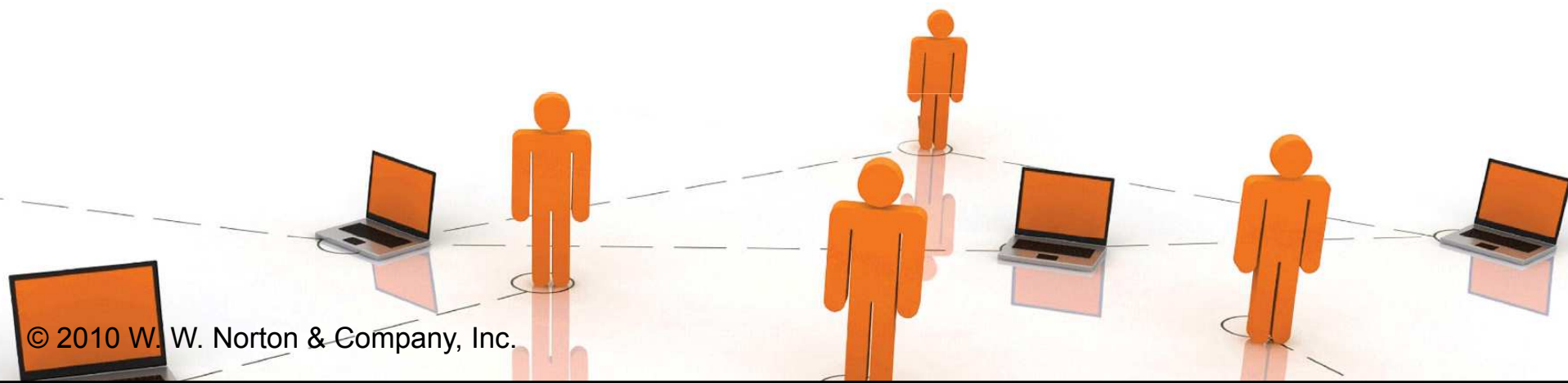
$$D(p) = a - bp$$

$$S(p) = c + dp$$

**At the equilibrium price  $p^*$ ,  $D(p^*) = S(p^*)$ .**

**That is,  $a - bp^* = c + dp^*$**

**which gives  $p^* = \frac{a - c}{b + d}$**



# Market Equilibrium

$$D(p) = a - bp$$

$$S(p) = c + dp$$

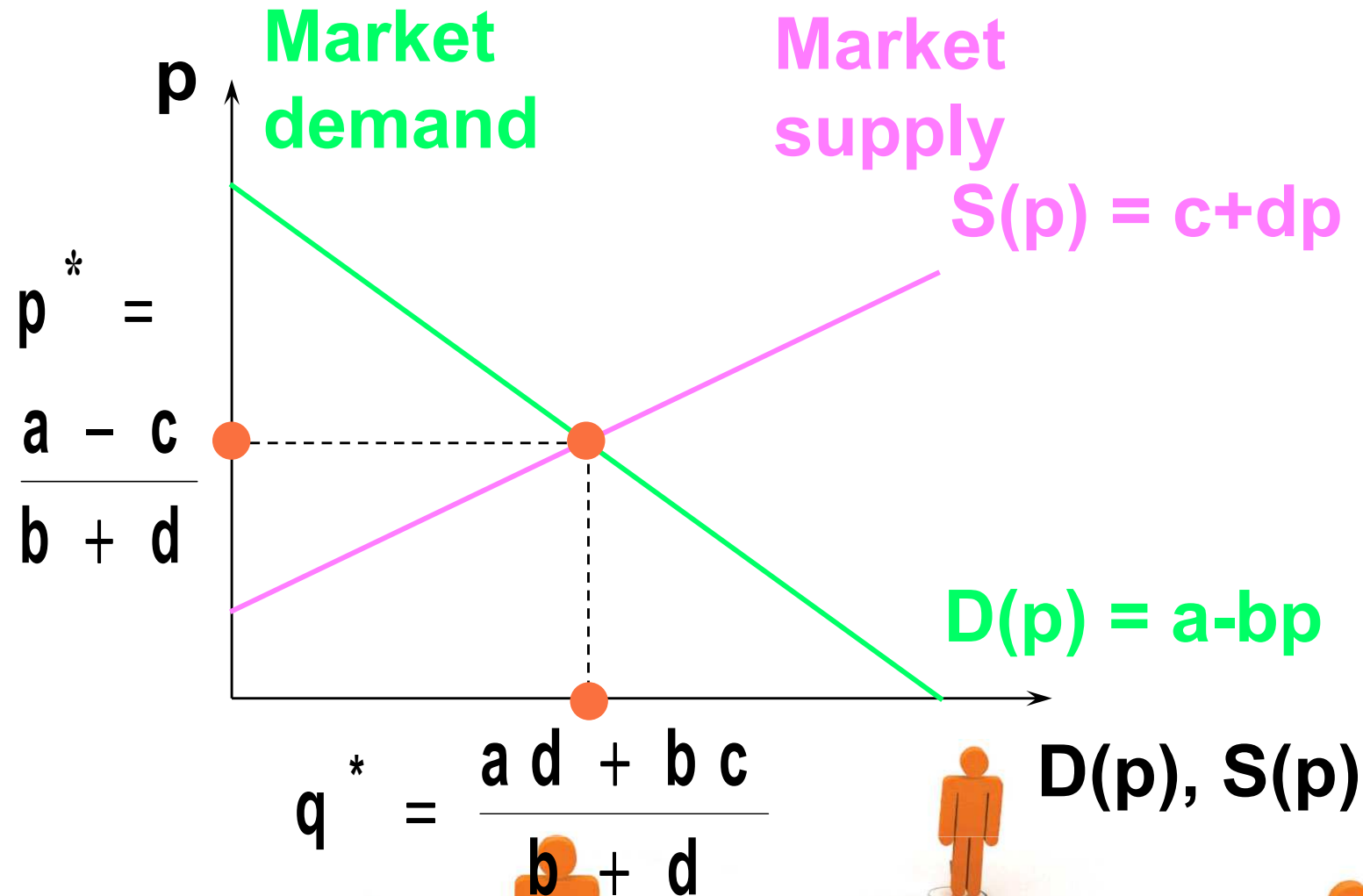
**At the equilibrium price  $p^*$ ,  $D(p^*) = S(p^*)$ .**

**That is,  $a - bp^* = c + dp^*$**

**which gives  $p^* = \frac{a - c}{b + d}$**

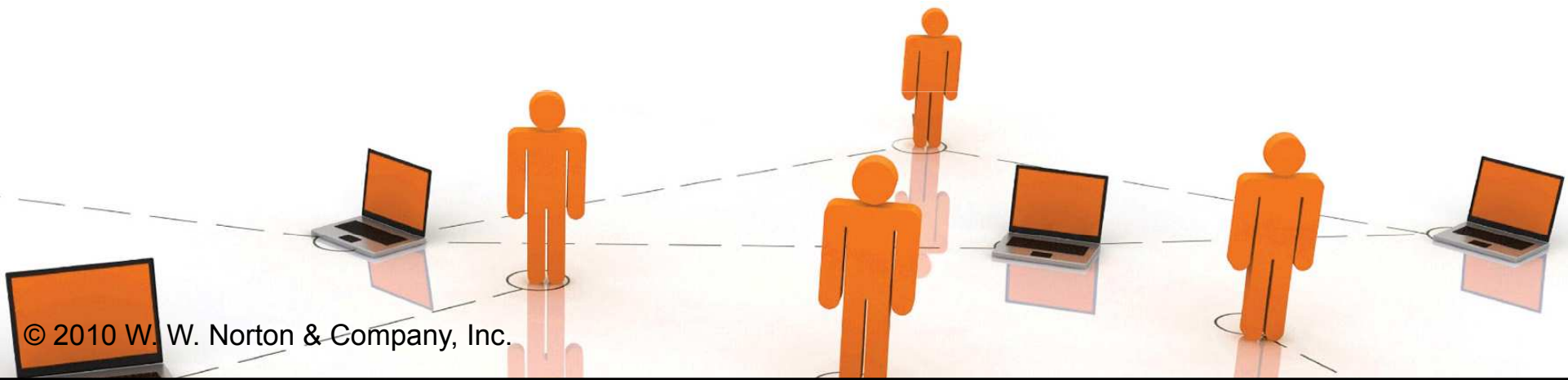
**and  $q^* = D(p^*) = S(p^*) = \frac{ad + bc}{b + d}$ .**

# Market Equilibrium



# Market Equilibrium

- ◆ **Can we calculate the market equilibrium using the inverse market demand and supply curves?**



# Market Equilibrium

- ◆ **Can we calculate the market equilibrium using the inverse market demand and supply curves?**
- ◆ **Yes, it is the same calculation.**



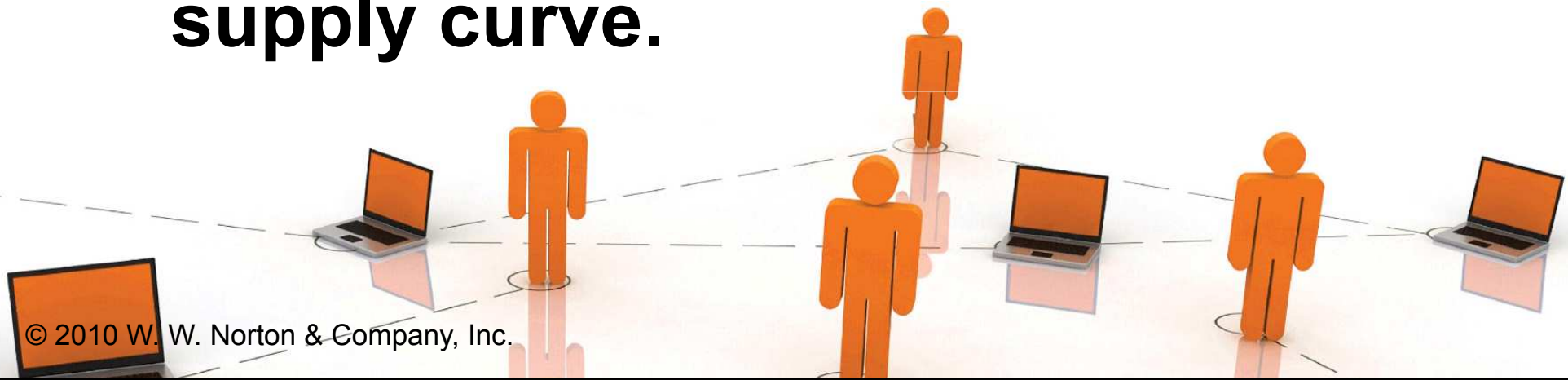
# Market Equilibrium

$$q = D(p) = a - bp \Leftrightarrow p = \frac{a - q}{b} = D^{-1}(q),$$

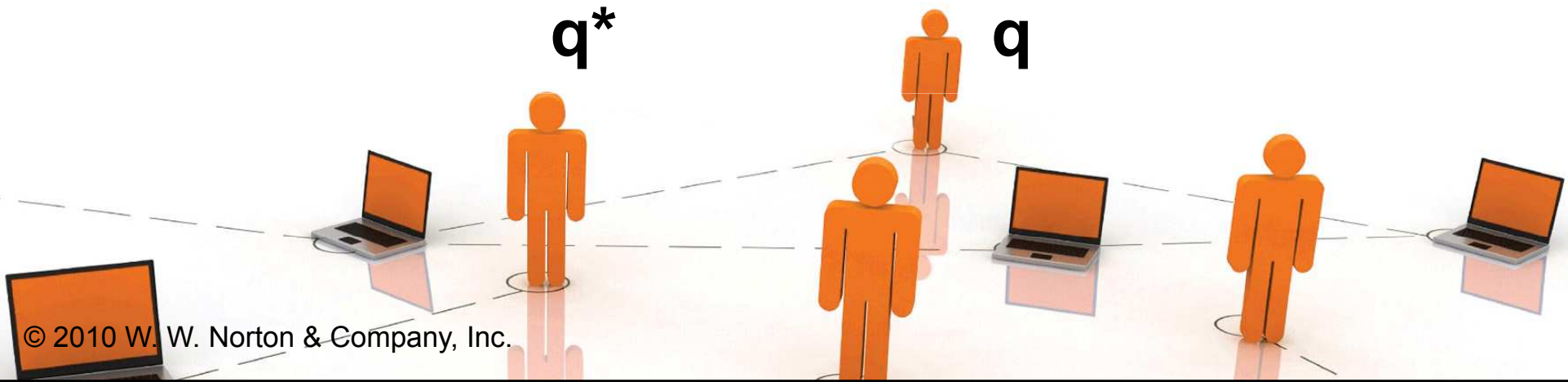
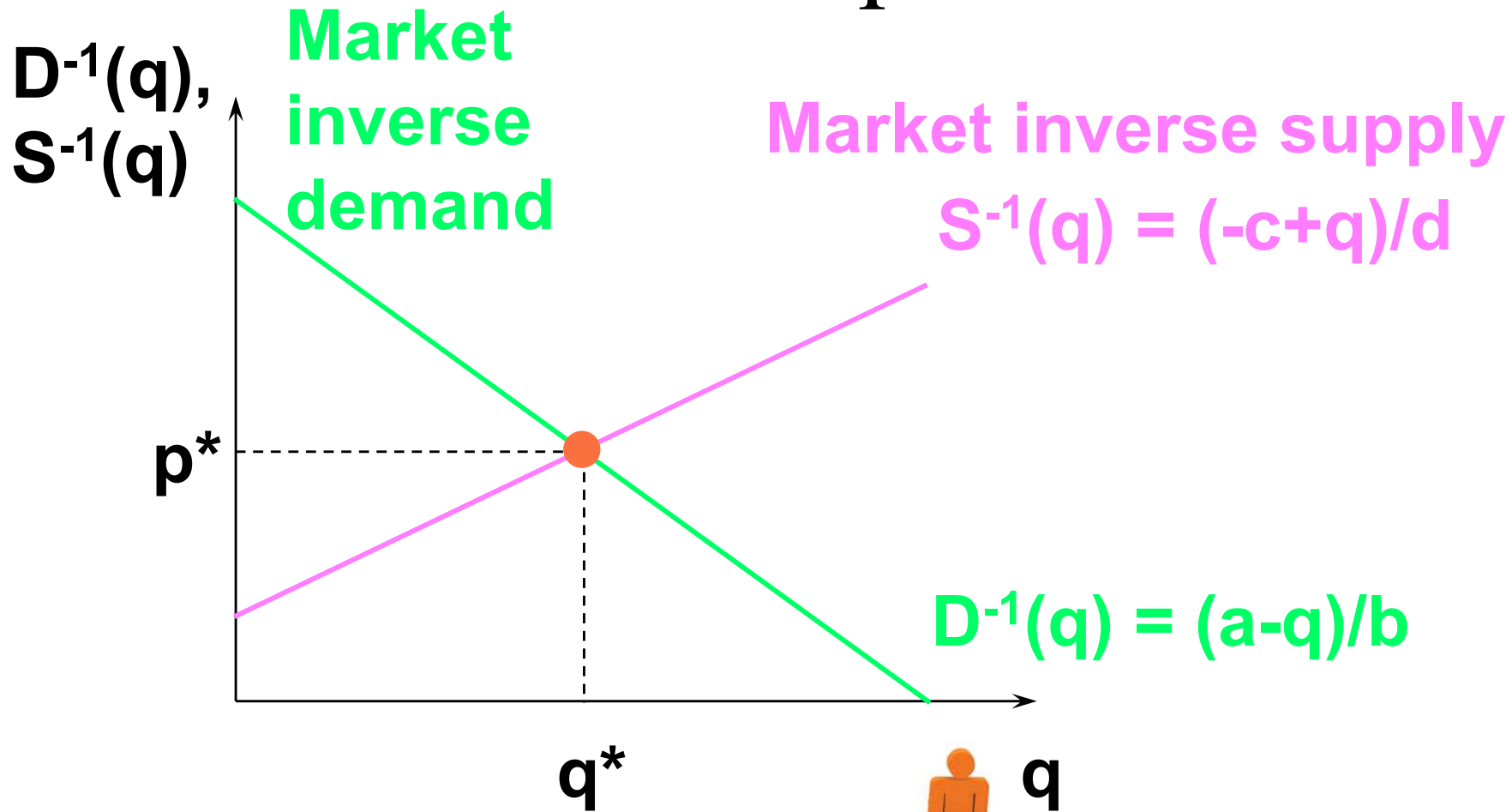
**the equation of the inverse market demand curve. And**

$$q = S(p) = c + dp \Leftrightarrow p = \frac{-c + q}{d} = S^{-1}(q),$$

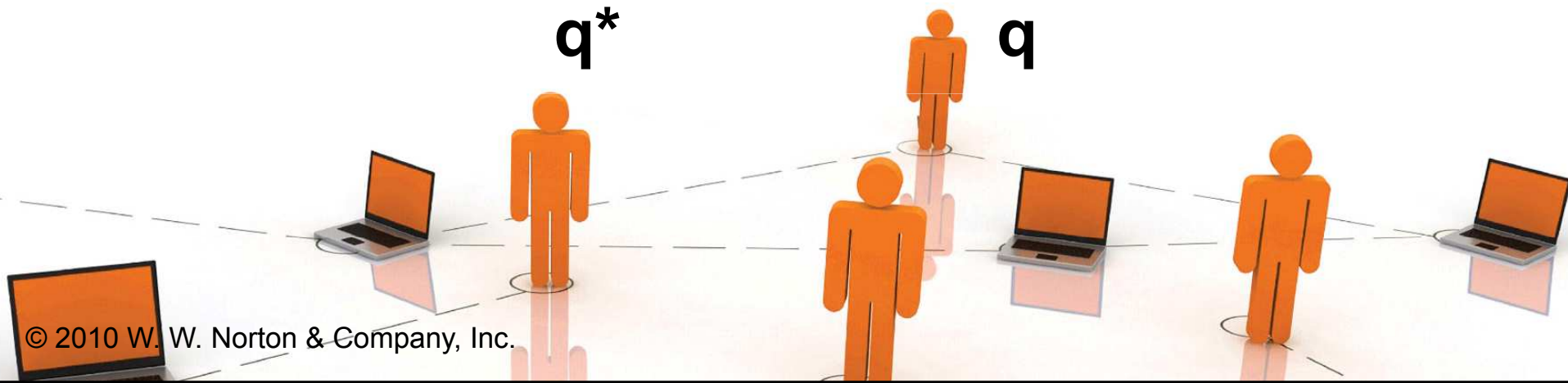
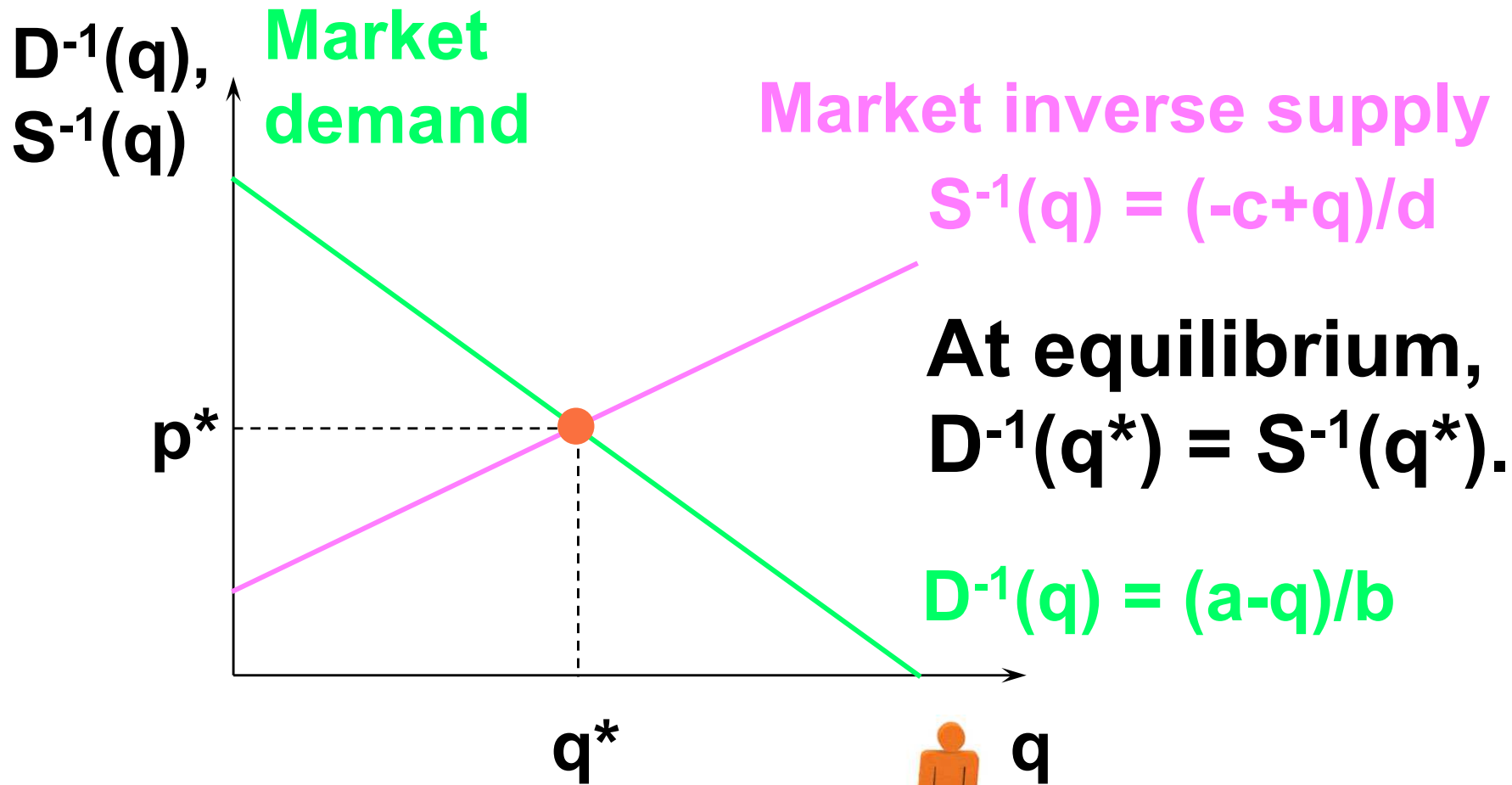
**the equation of the inverse market supply curve.**



# Market Equilibrium



# Market Equilibrium

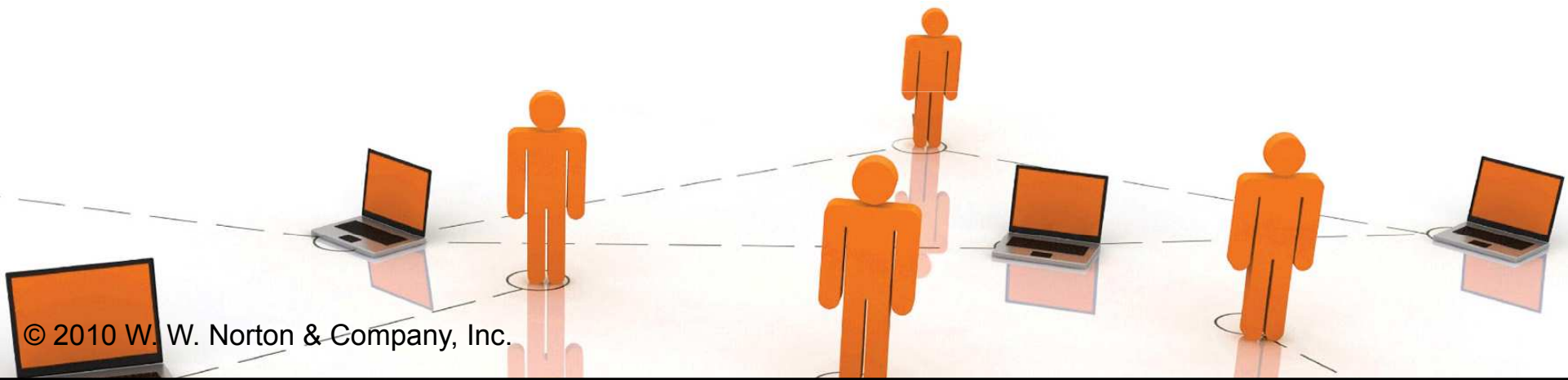




# Market Equilibrium

$$p = D^{-1}(q) = \frac{a - q}{b} \quad \text{and} \quad p = S^{-1}(q) = \frac{-c + q}{d}.$$

**At the equilibrium quantity  $q^*$ ,  $D^{-1}(p^*) = S^{-1}(p^*)$ .**



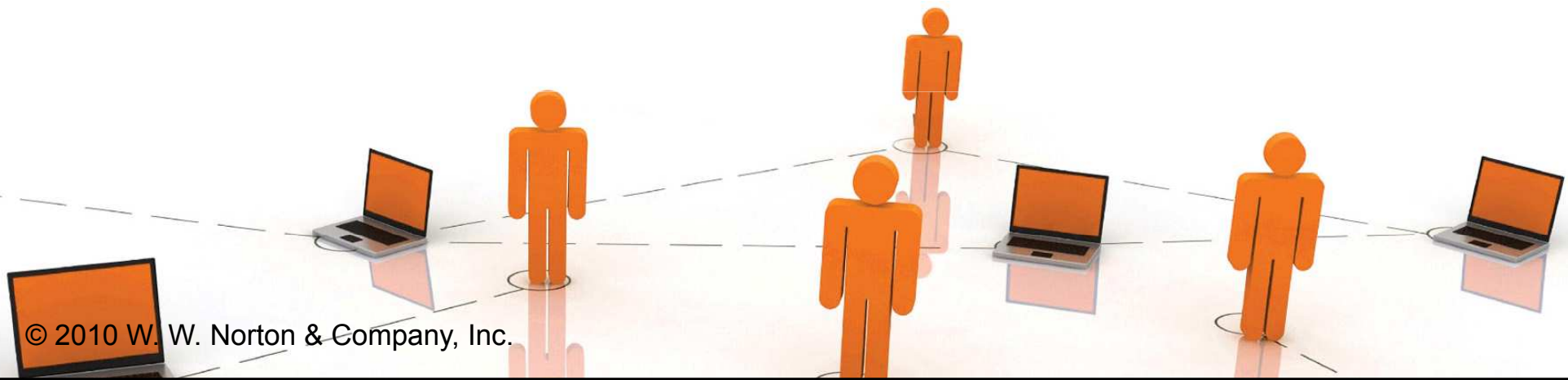
# Market Equilibrium

$$p = D^{-1}(q) = \frac{a - q}{b} \quad \text{and} \quad p = S^{-1}(q) = \frac{-c + q}{d}.$$

**At the equilibrium quantity  $q^*$ ,  $D^{-1}(p^*) = S^{-1}(p^*)$ .**

**That is,**

$$\frac{a - q^*}{b} = \frac{-c + q^*}{d}$$



# Market Equilibrium

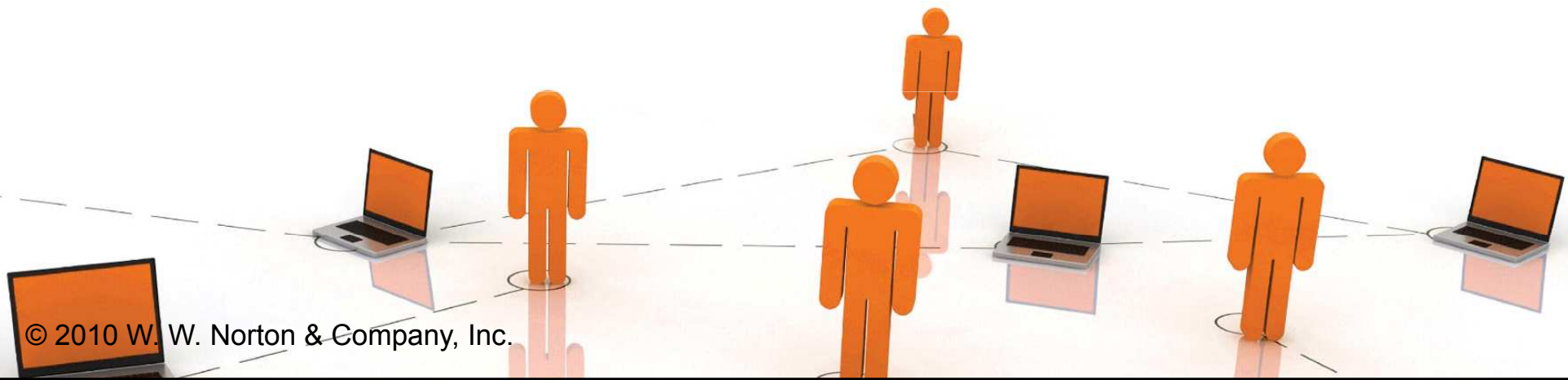
$$p = D^{-1}(q) = \frac{a - q}{b} \quad \text{and} \quad p = S^{-1}(q) = \frac{-c + q}{d}.$$

At the equilibrium quantity  $q^*$ ,  $D^{-1}(p^*) = S^{-1}(p^*)$ .

That is,

$$\frac{a - q^*}{b} = \frac{-c + q^*}{d}$$

which gives  $q^* = \frac{ad + bc}{b + d}$



# Market Equilibrium

$$p = D^{-1}(q) = \frac{a - q}{b} \quad \text{and} \quad p = S^{-1}(q) = \frac{-c + q}{d}.$$

At the equilibrium quantity  $q^*$ ,  $D^{-1}(p^*) = S^{-1}(p^*)$ .

That is,

$$\frac{a - q^*}{b} = \frac{-c + q^*}{d}$$

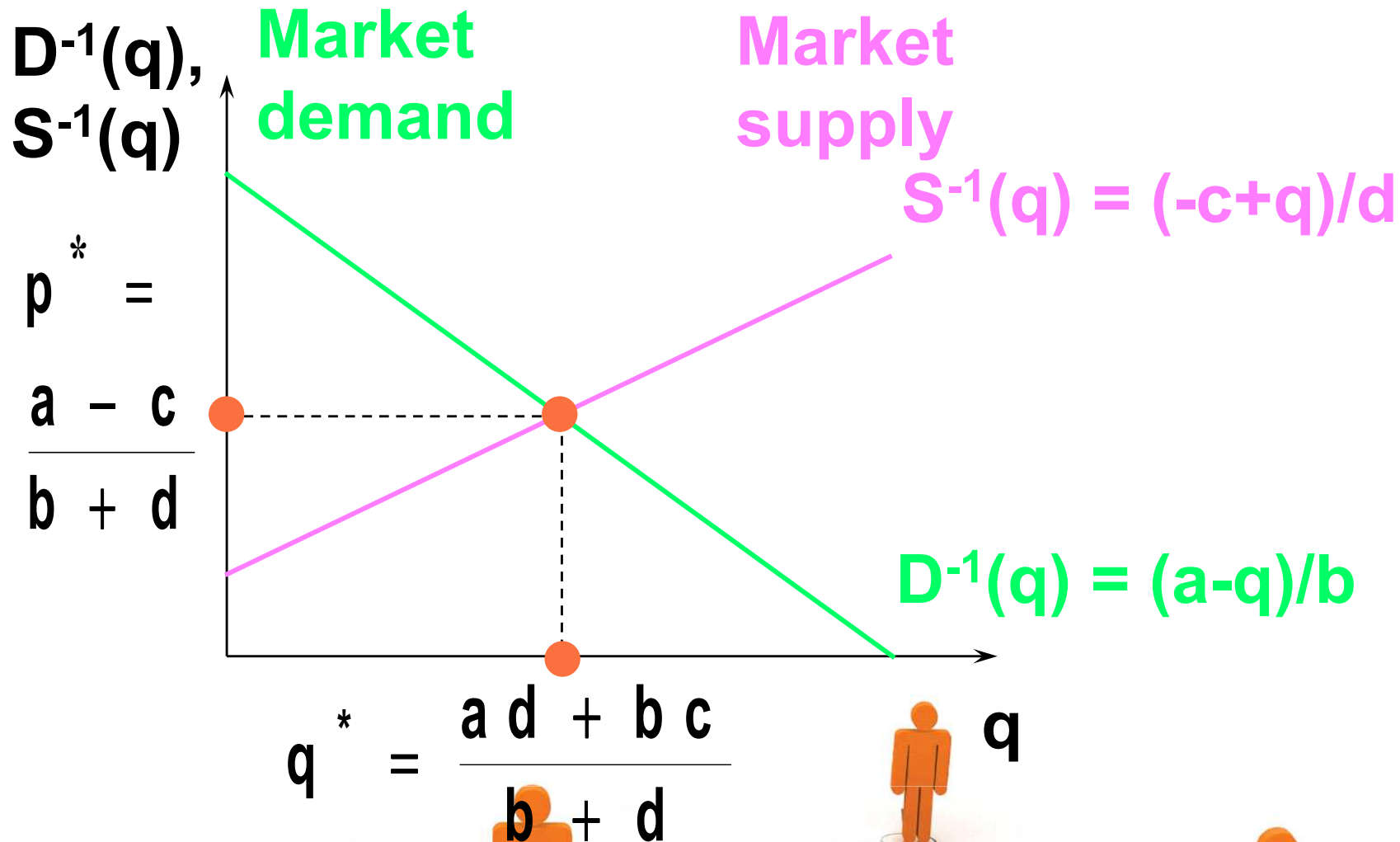
which gives

$$q^* = \frac{ad + bc}{b + d}$$

and

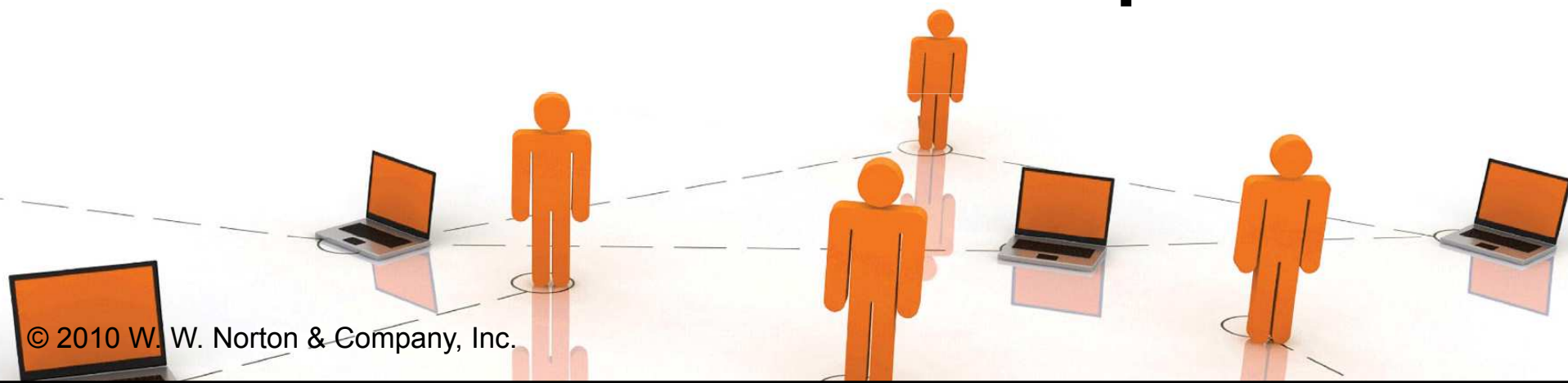
$$p^* = D^{-1}(q^*) = S^{-1}(q^*) = \frac{a - c}{b + d}.$$

# Market Equilibrium



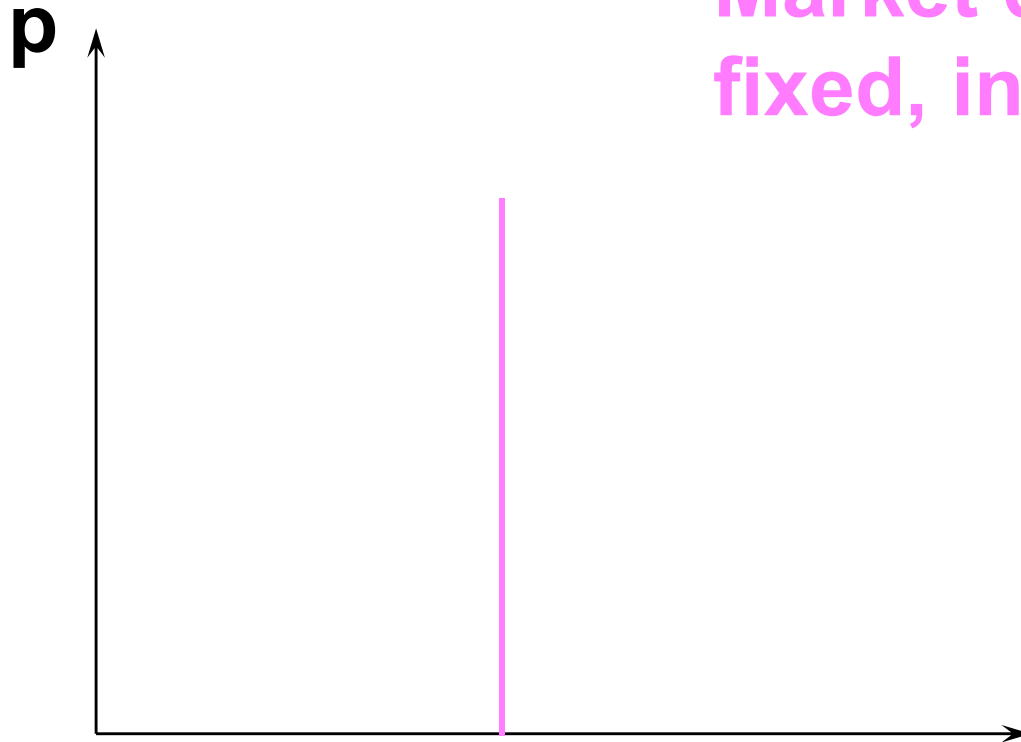
# Market Equilibrium

- ◆ **Two special cases:**
  - **quantity supplied is fixed, independent of the market price, and**
  - **quantity supplied is extremely sensitive to the market price.**



# Market Equilibrium

Market quantity supplied is fixed, independent of price.



$q^*$

$q$



# Market Equilibrium

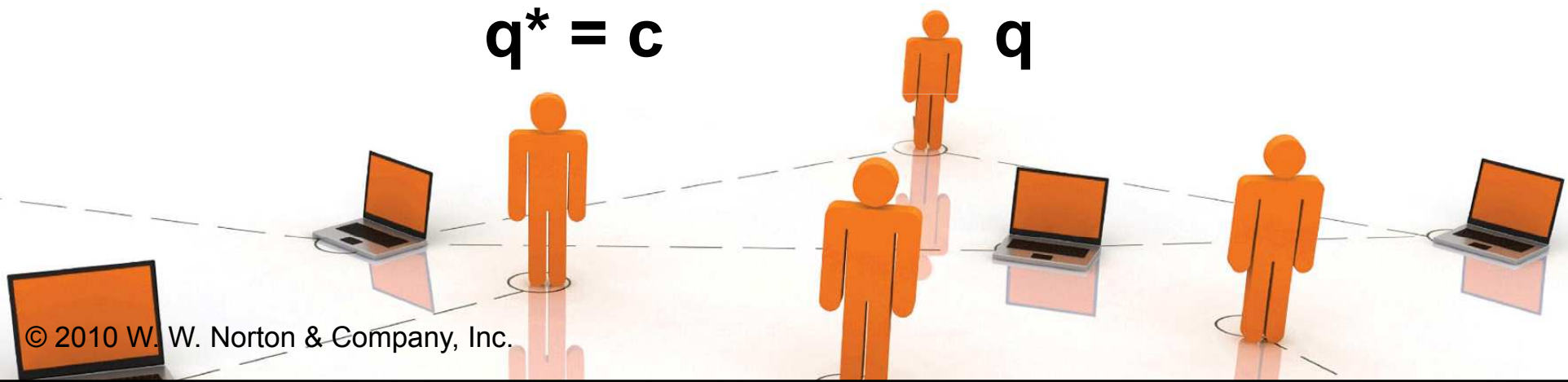
Market quantity supplied is fixed, independent of price.

$$S(p) = c + dp, \text{ so } d=0 \\ \text{and } S(p) \equiv c.$$



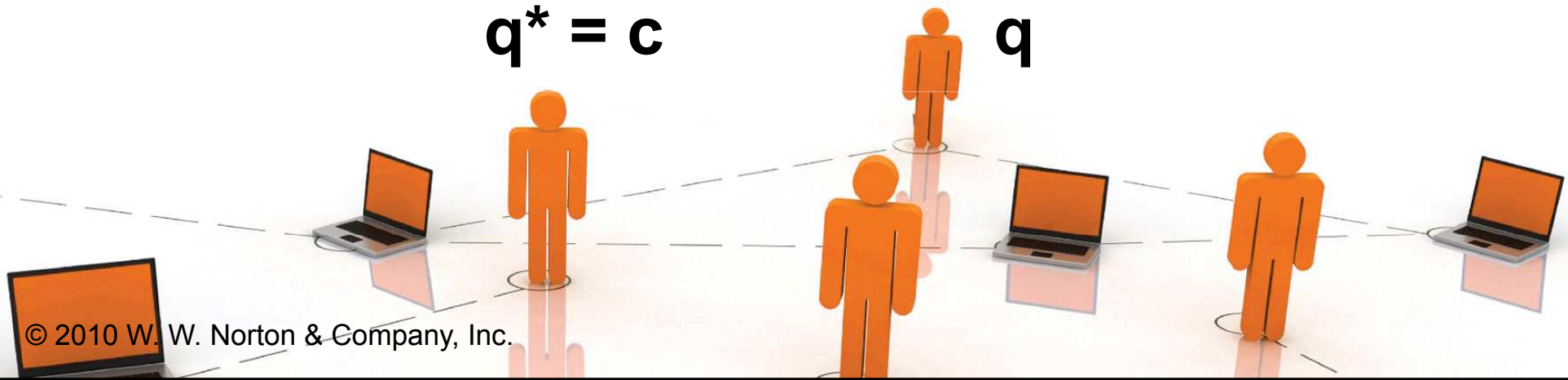
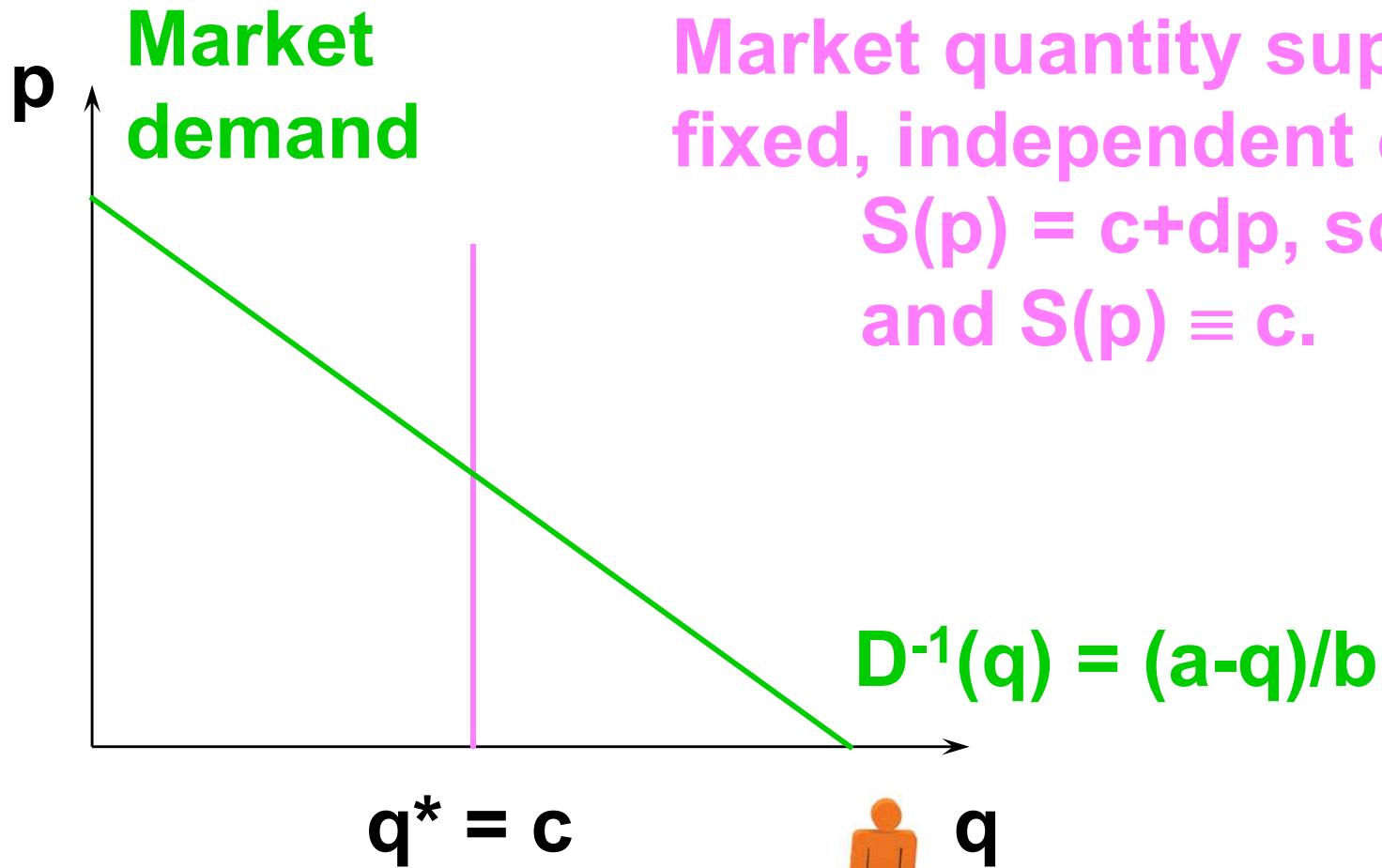
$$q^* = c$$

q

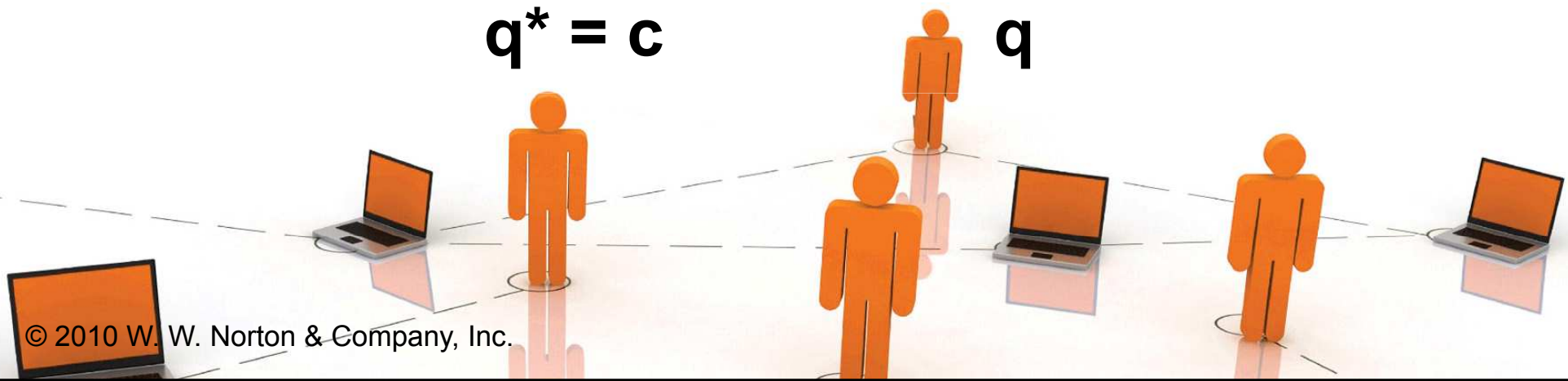
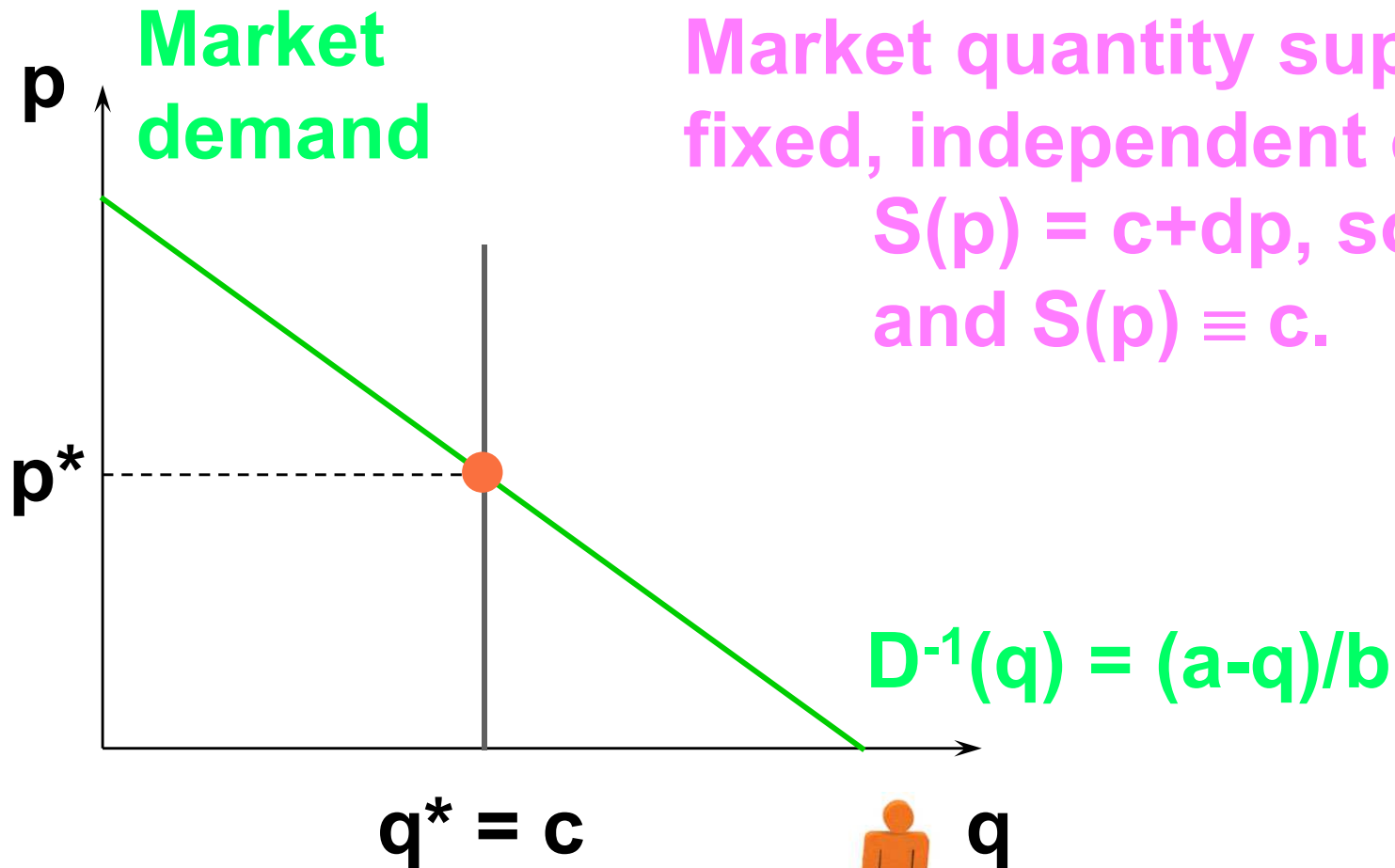




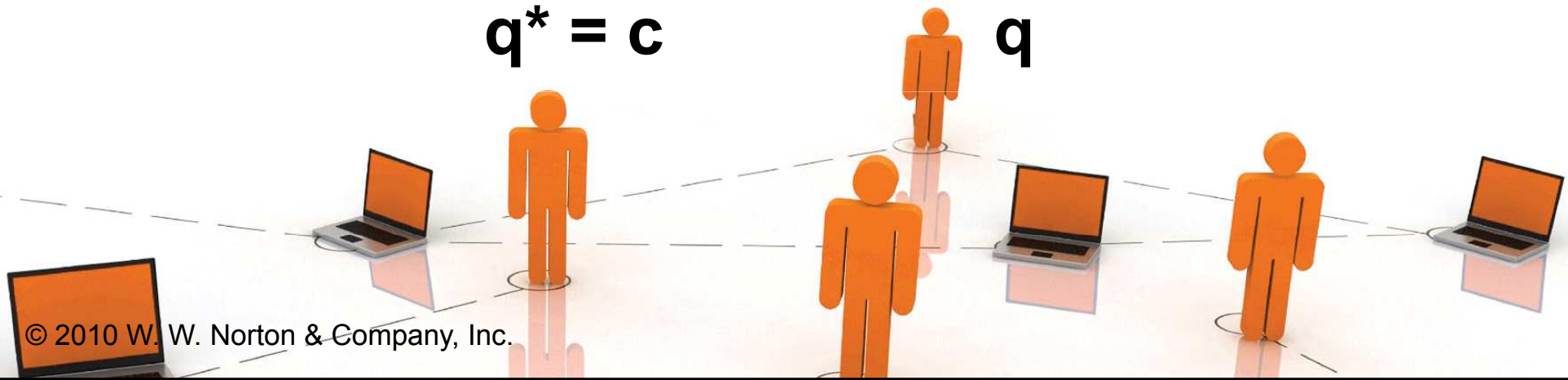
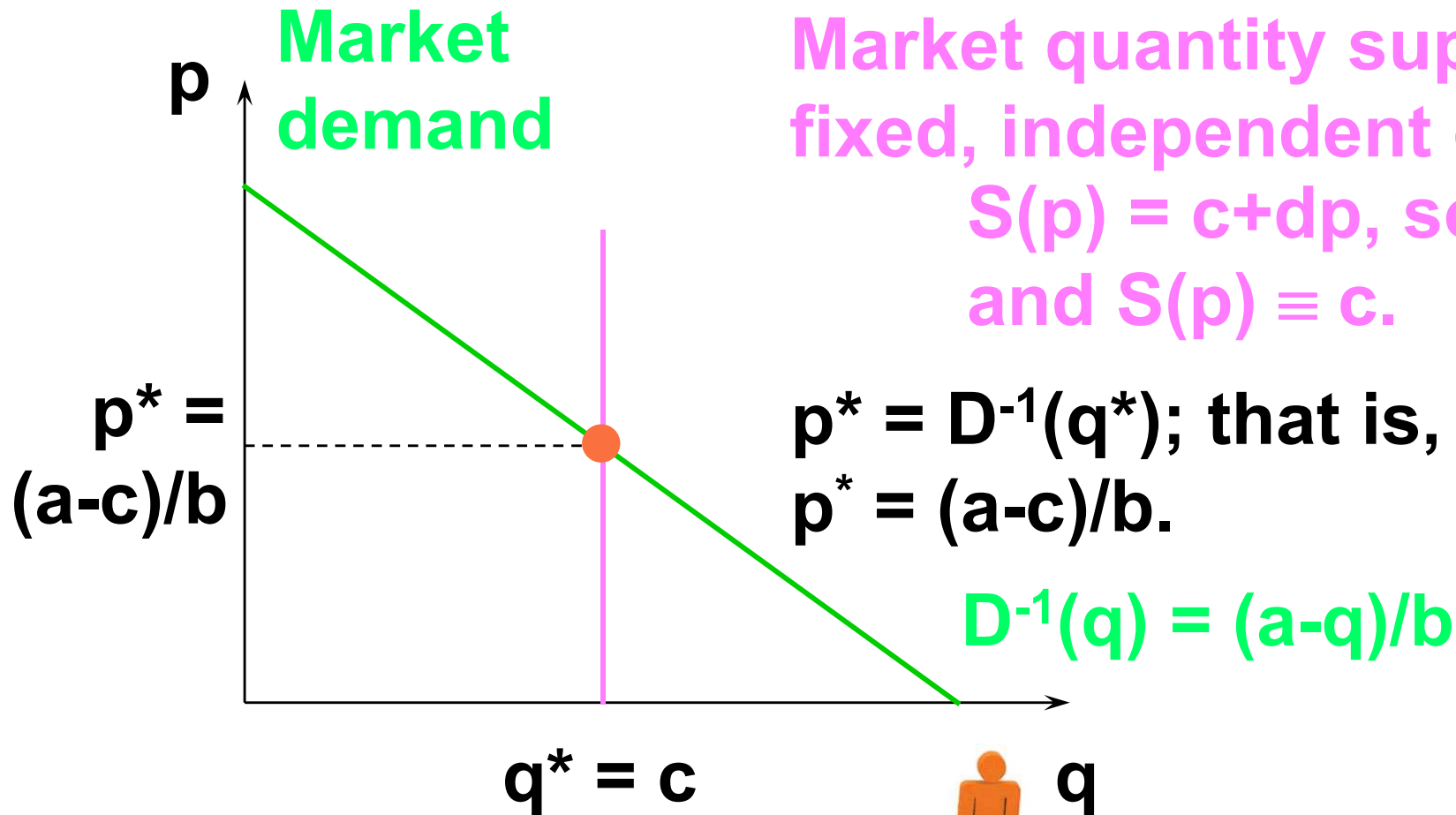
# Market Equilibrium



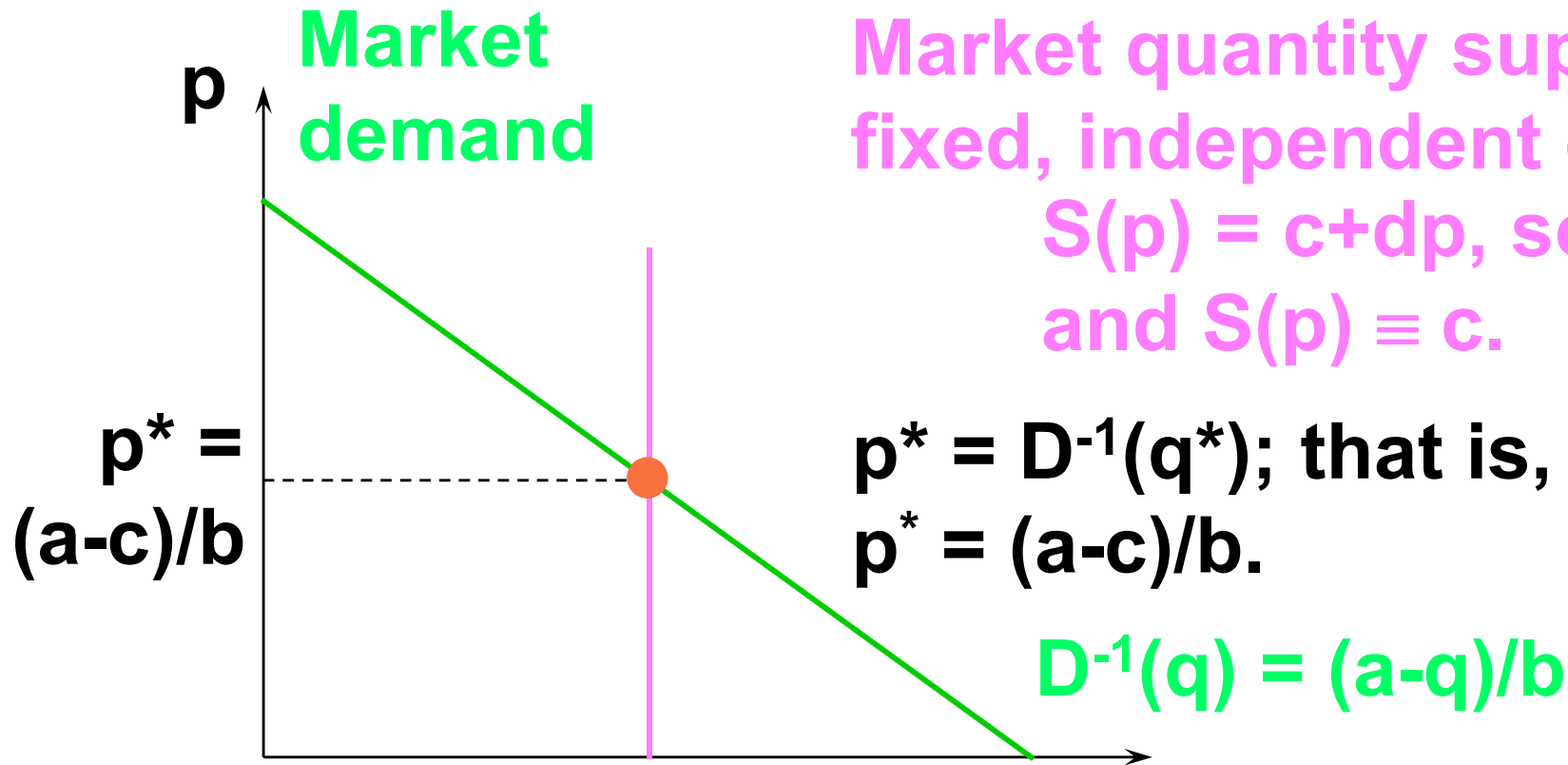
# Market Equilibrium



# Market Equilibrium

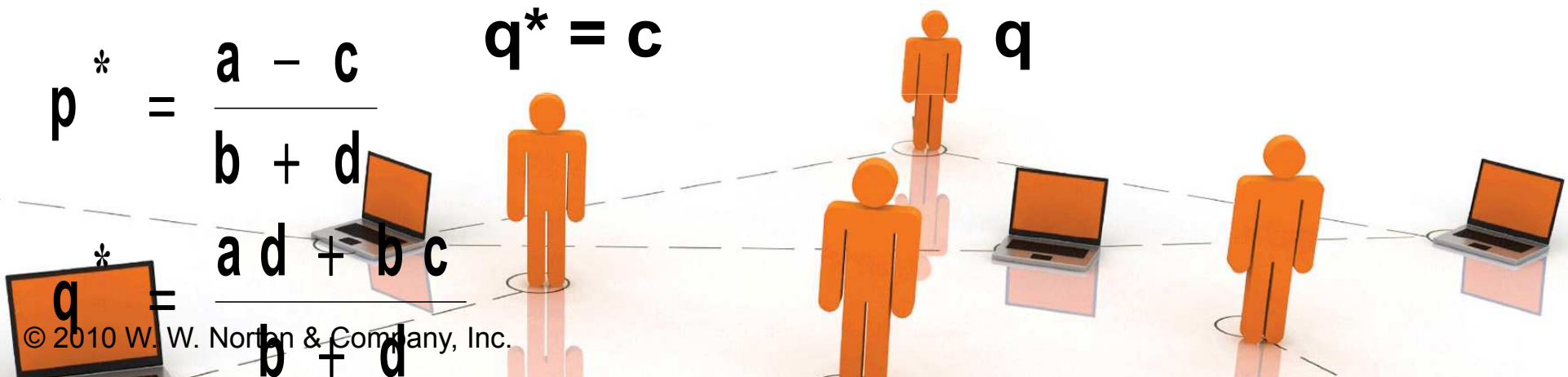


# Market Equilibrium

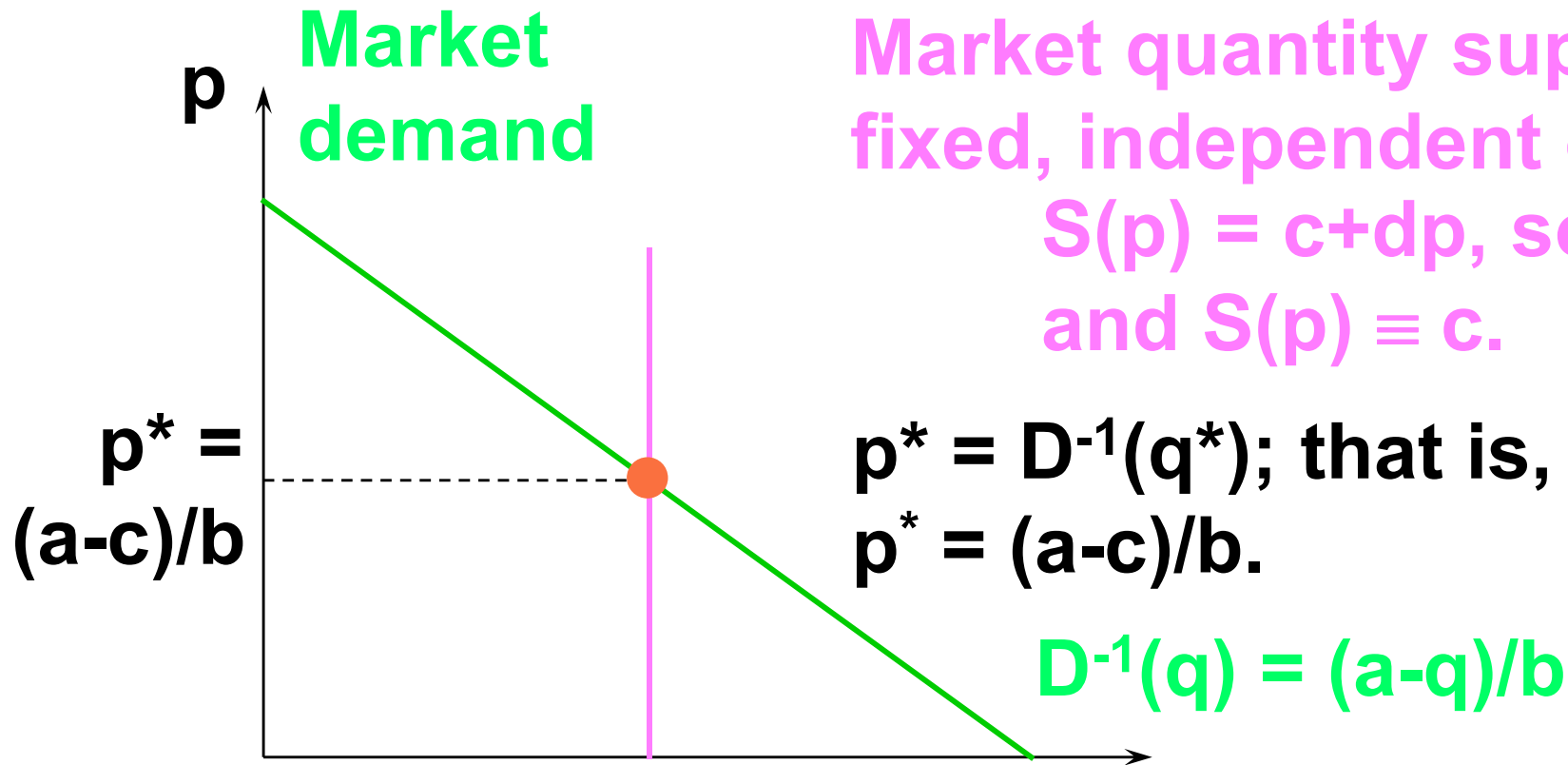


$$p^* = \frac{a - c}{b + d}$$

$$q^* = \frac{a d + b c}{b + d}$$



# Market Equilibrium



Market quantity supplied is fixed, independent of price.  
 $S(p) = c + dp$ , so  $d=0$   
 and  $S(p) \equiv c$ .

$p^* = D^{-1}(q^*)$ ; that is,  
 $p^* = \frac{a-c}{b}$ .

$$p^* = \frac{a-c}{b+d}$$

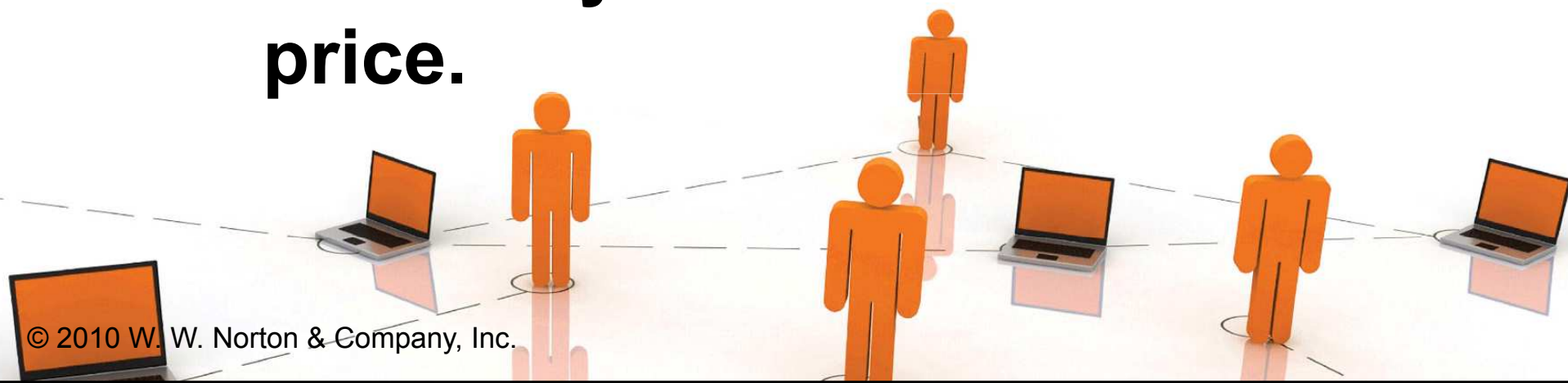
$$q^* = \frac{ad+bc}{b+d}$$
 with  $d = 0$  give
 
$$p^* = \frac{a-c}{b}$$

$$q^* = c$$

# Market Equilibrium

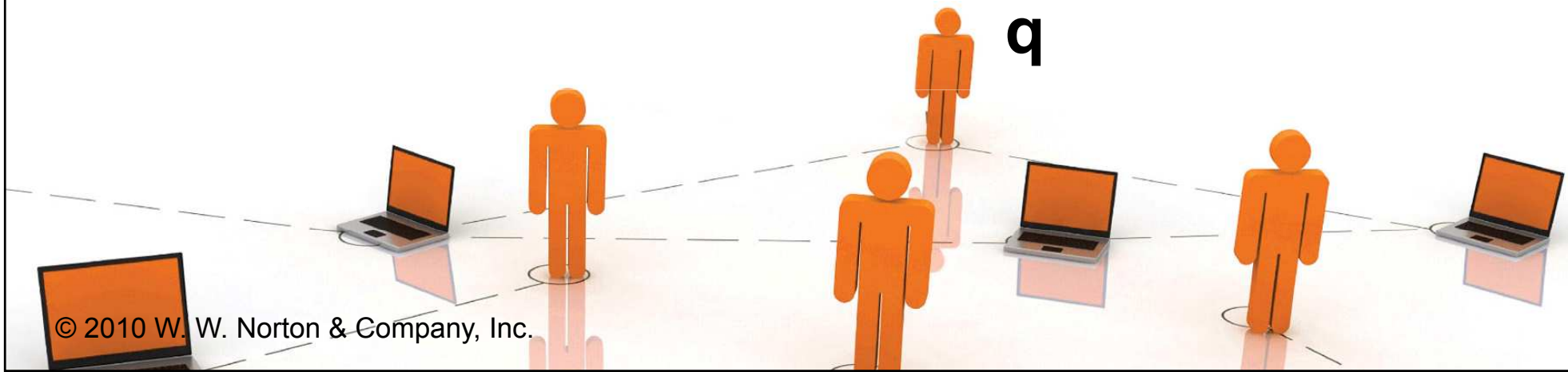
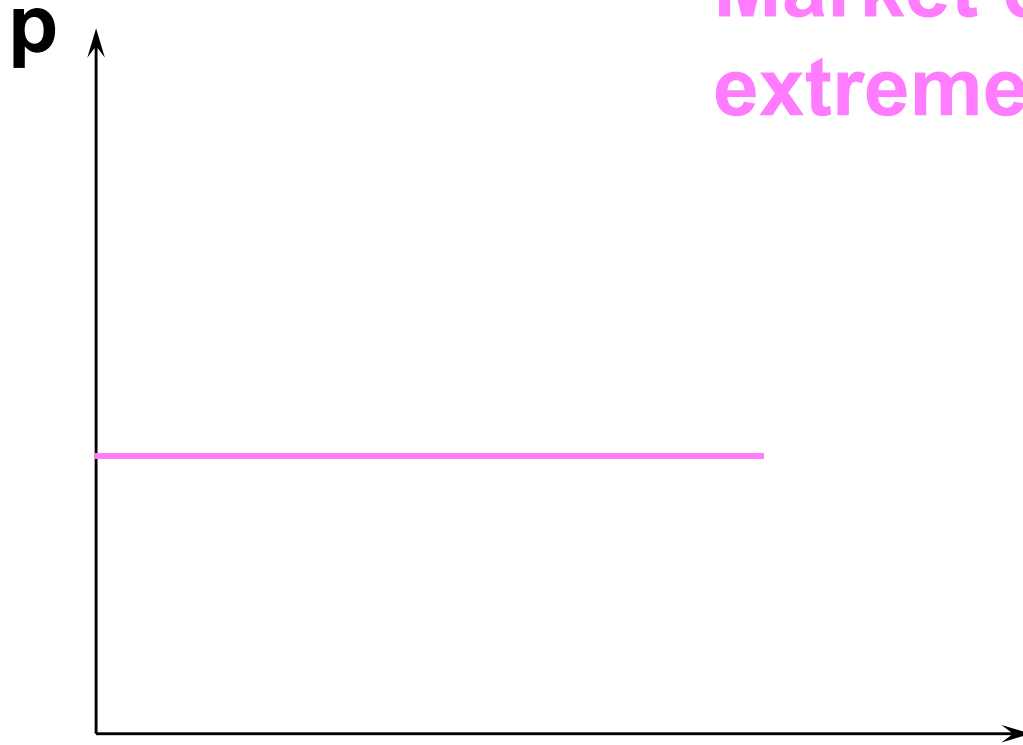
## ◆ Two special cases are

- when quantity supplied is fixed, independent of the market price, and
- when quantity supplied is extremely sensitive to the market price.



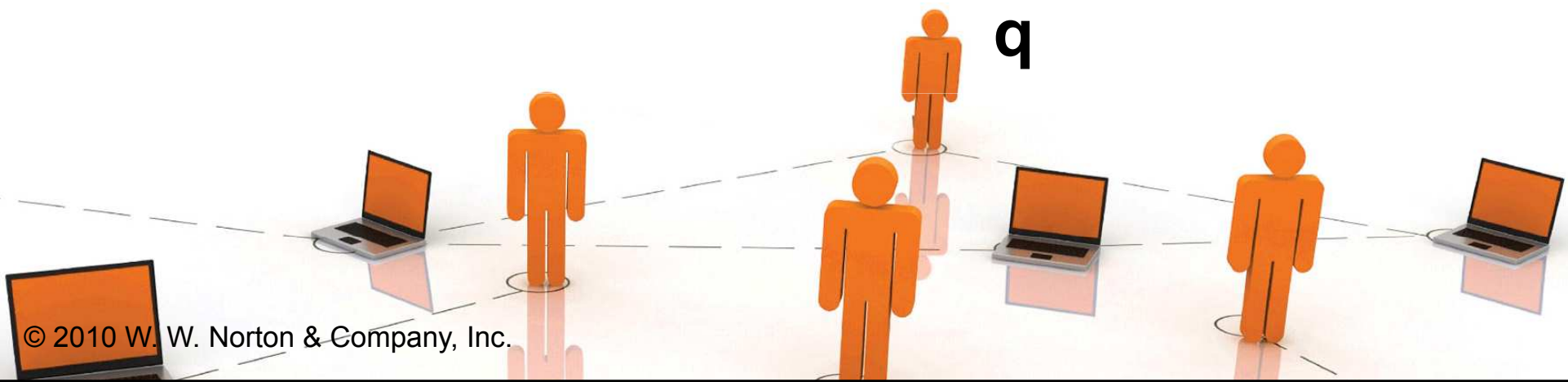
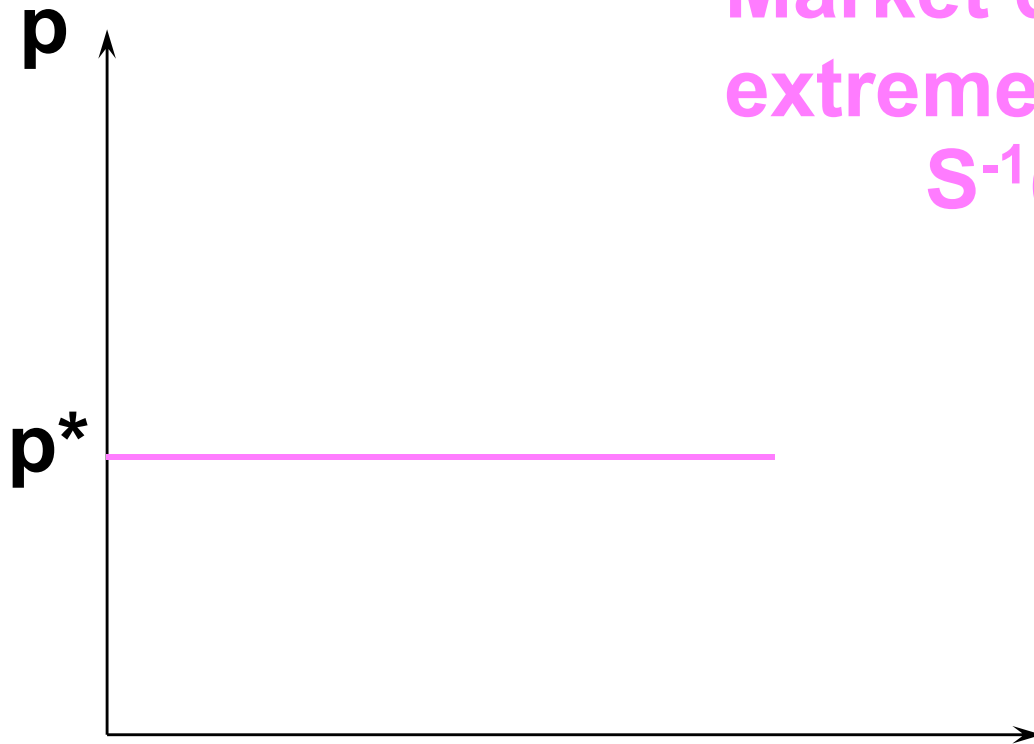
# Market Equilibrium

Market quantity supplied is extremely sensitive to price.



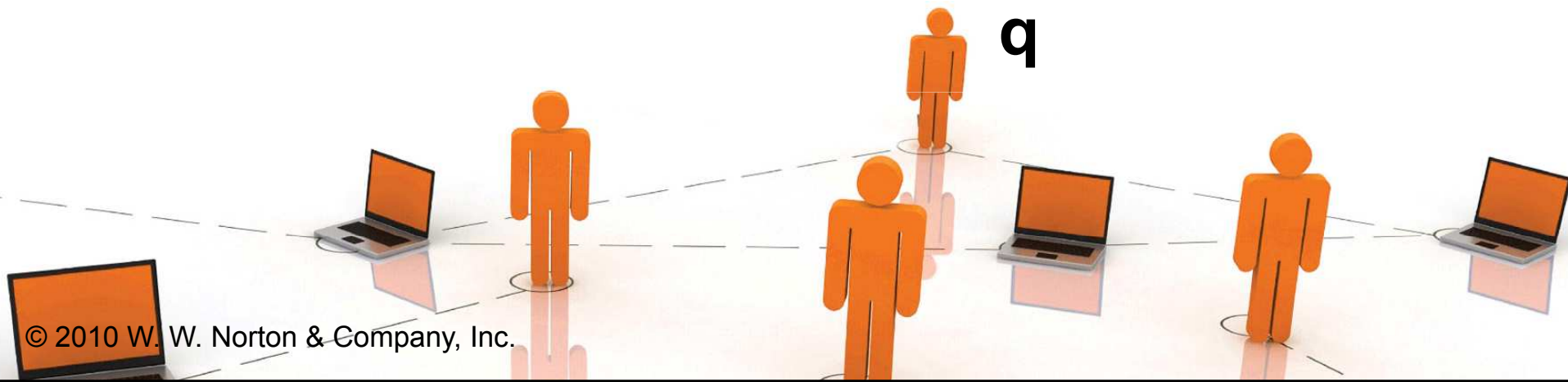
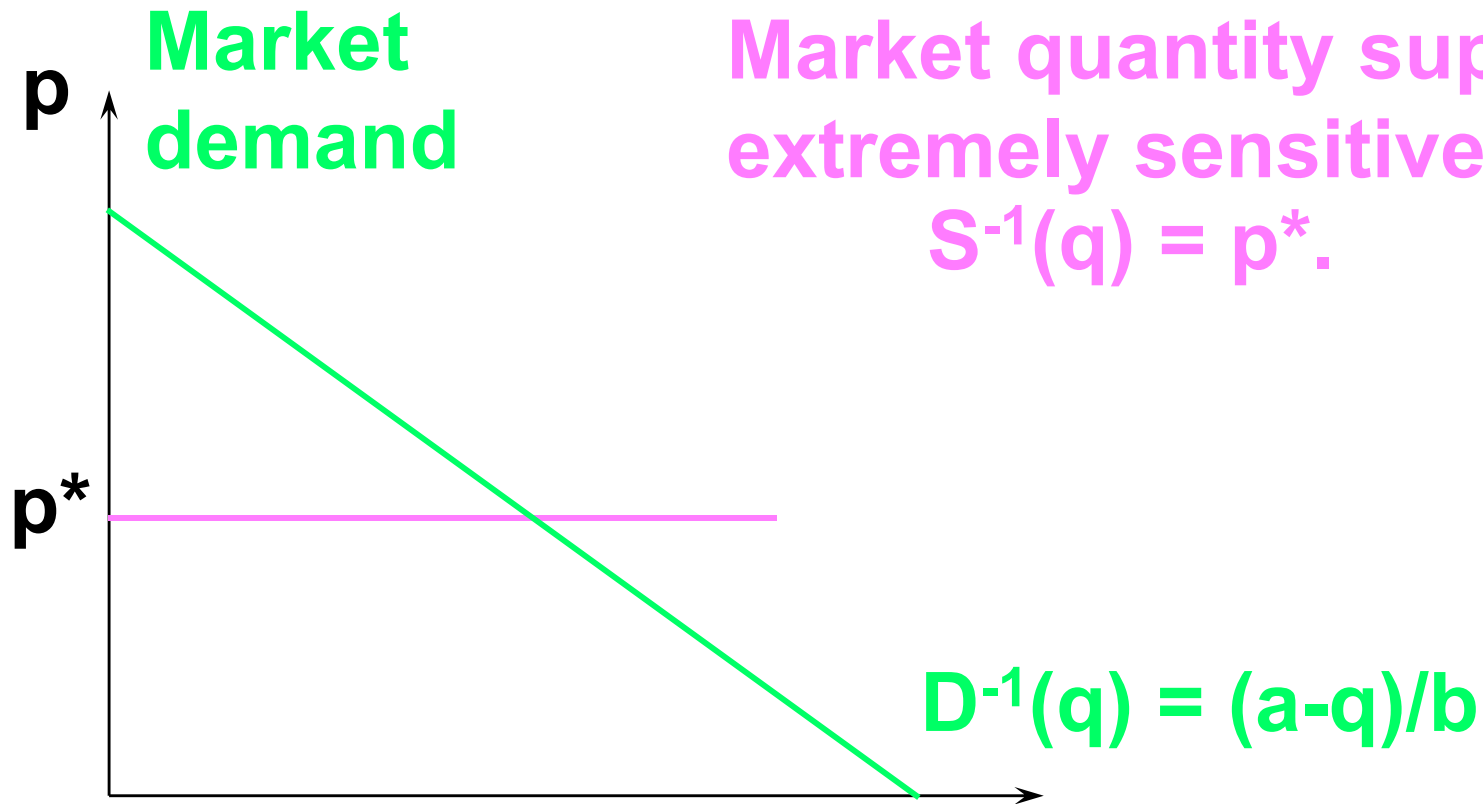
# Market Equilibrium

Market quantity supplied is extremely sensitive to price.  
 $S^{-1}(q) = p^*$ .

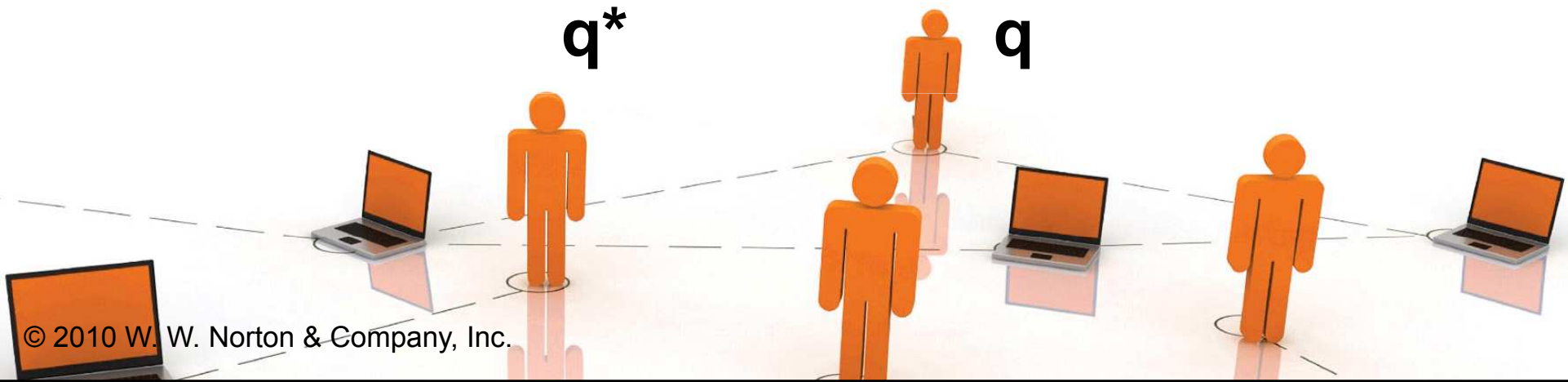
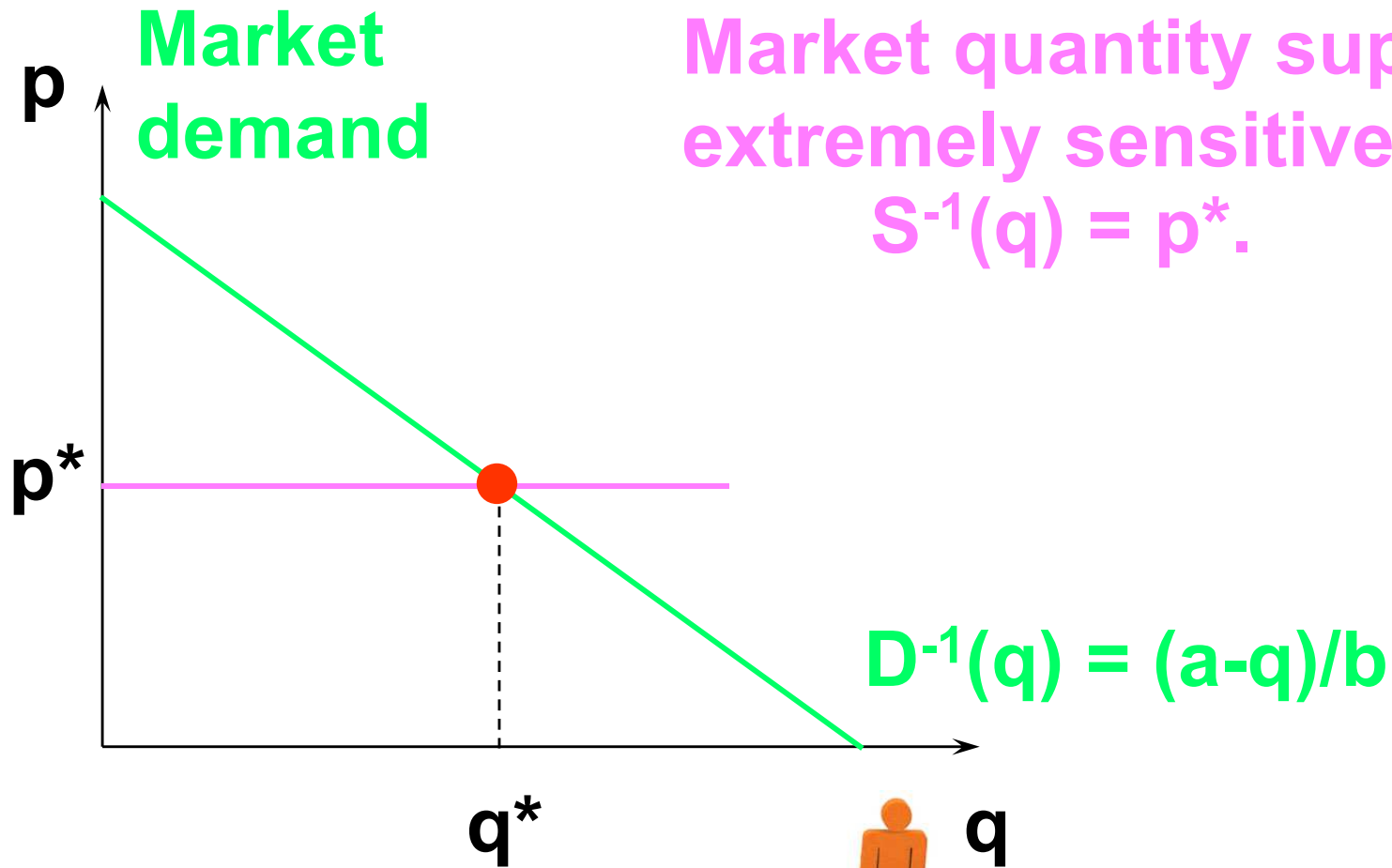




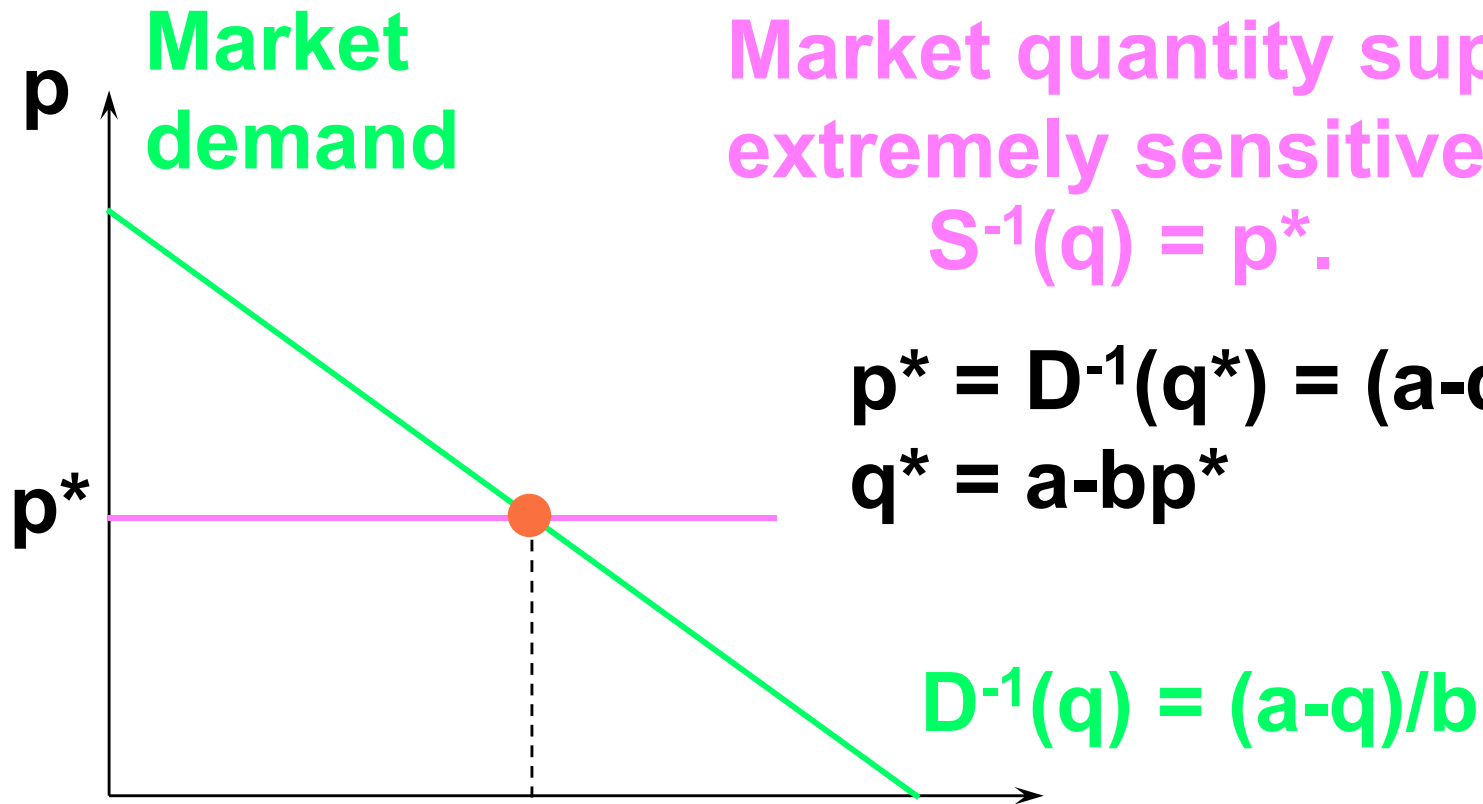
# Market Equilibrium



# Market Equilibrium



# Market Equilibrium



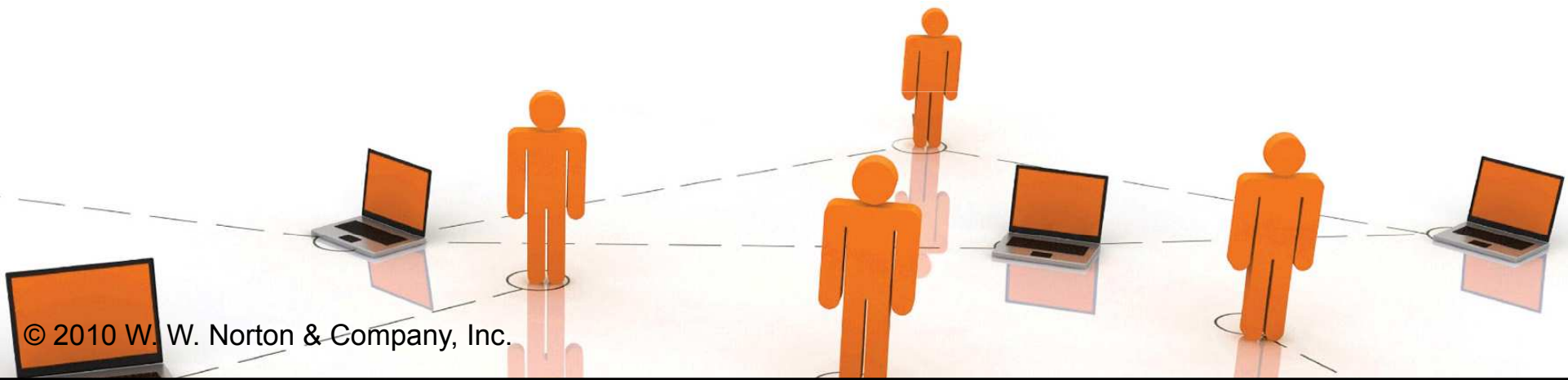
$$q^* = a - bp^*$$

$q$



# Quantity Taxes

- ◆ **A quantity tax levied at a rate of  $\$t$  is a tax of  $\$t$  paid on each unit traded.**
- ◆ **If the tax is levied on sellers then it is an excise tax.**
- ◆ **If the tax is levied on buyers then it is a sales tax.**



# Quantity Taxes

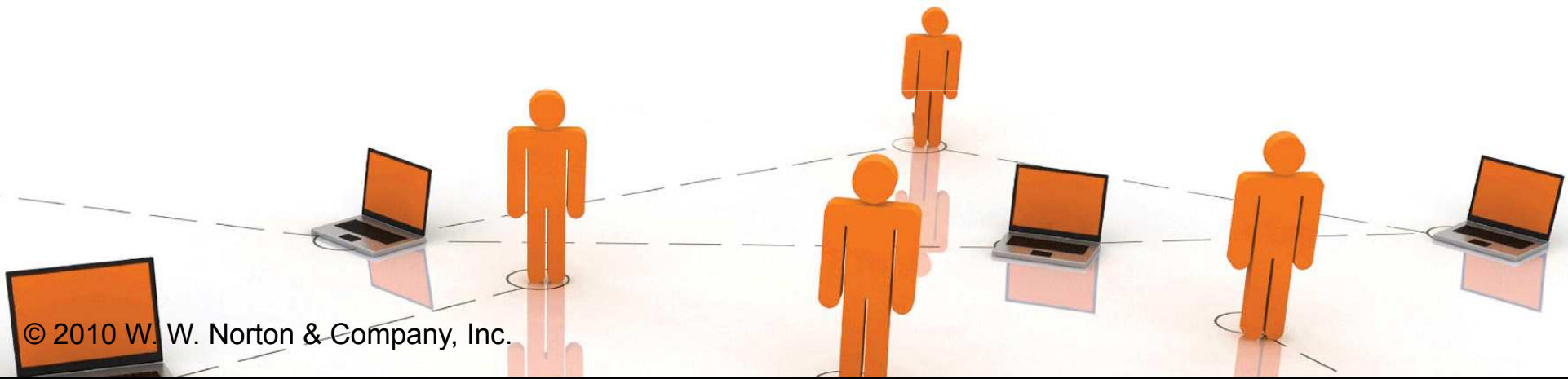
- ◆ **What is the effect of a quantity tax on a market's equilibrium?**
- ◆ **How are prices affected?**
- ◆ **How is the quantity traded affected?**
- ◆ **Who pays the tax?**
- ◆ **How are gains-to-trade altered?**



# Quantity Taxes

- ◆ A tax rate  $t$  makes the price paid by buyers,  $p_b$ , higher by  $t$  from the price received by sellers,  $p_s$ .

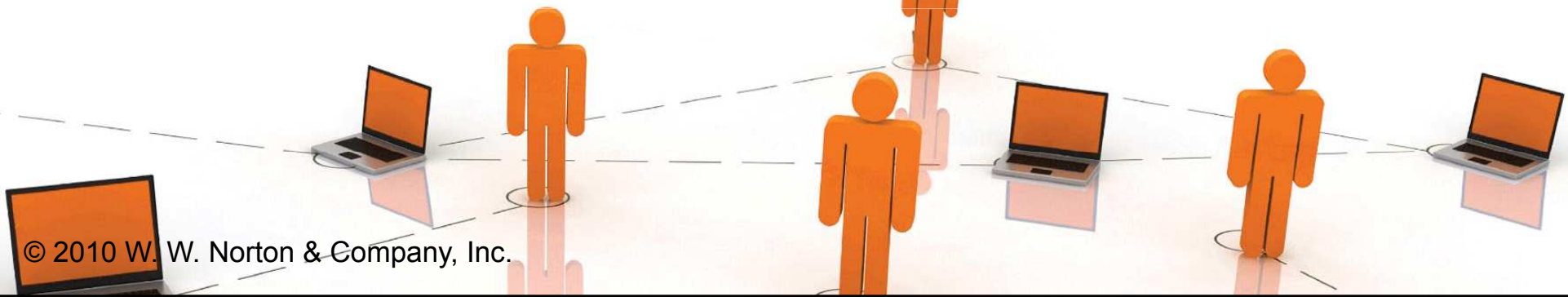
$$p_b - p_s = t$$



# Quantity Taxes

- ◆ **Even with a tax the market must clear.**
- ◆ **I.e. quantity demanded by buyers at price  $p_b$  must equal quantity supplied by sellers at price  $p_s$ .**

$$D(p_b) = S(p_s)$$

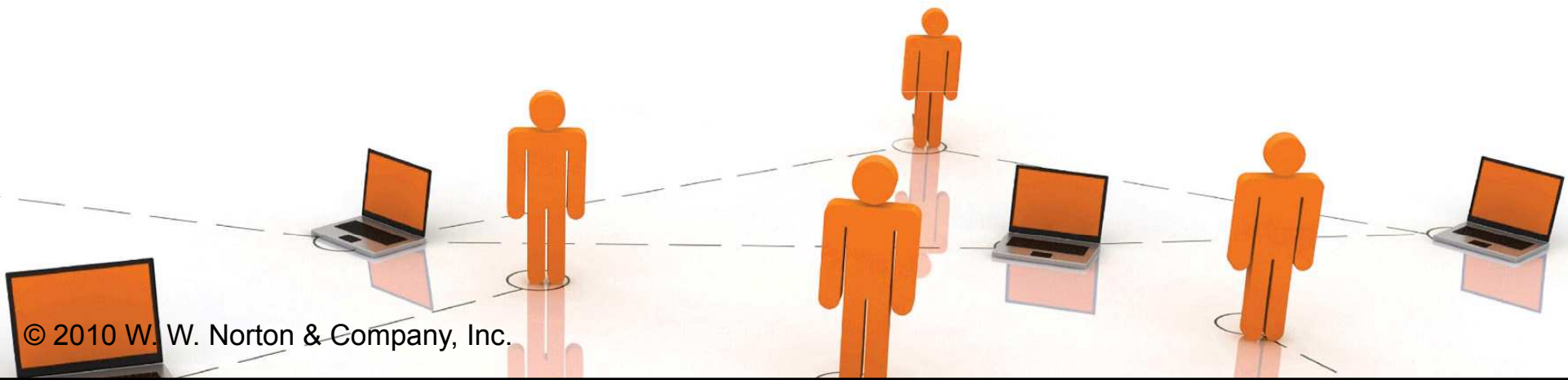


# Quantity Taxes

$$p_b - p_s = t \quad \text{and} \quad D(p_b) = S(p_s)$$

**describe the market's equilibrium.**

**Notice these conditions apply no matter if the tax is levied on sellers or on buyers.**





# Quantity Taxes

$$p_b - p_s = t \quad \text{and} \quad D(p_b) = S(p_s)$$

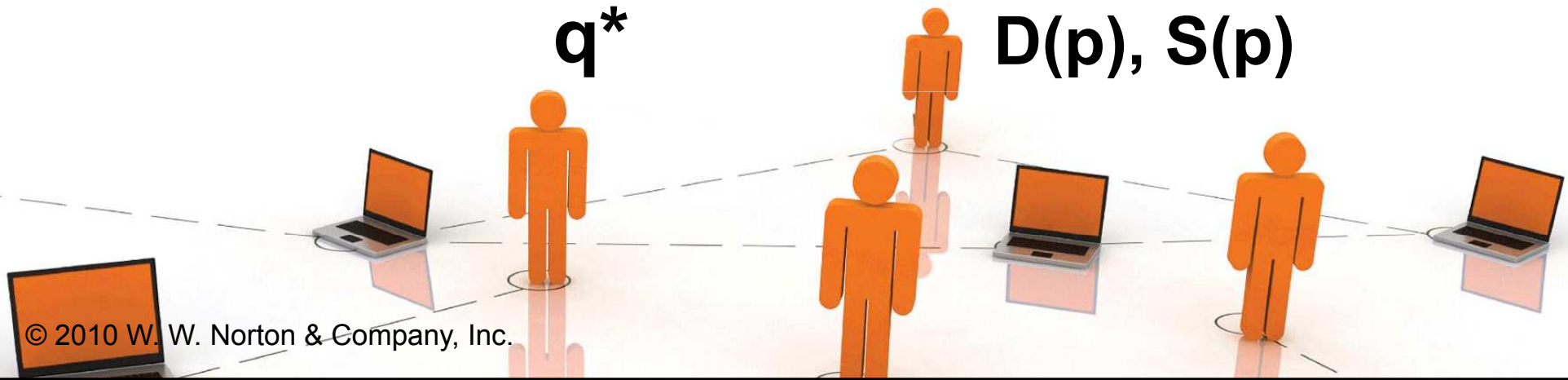
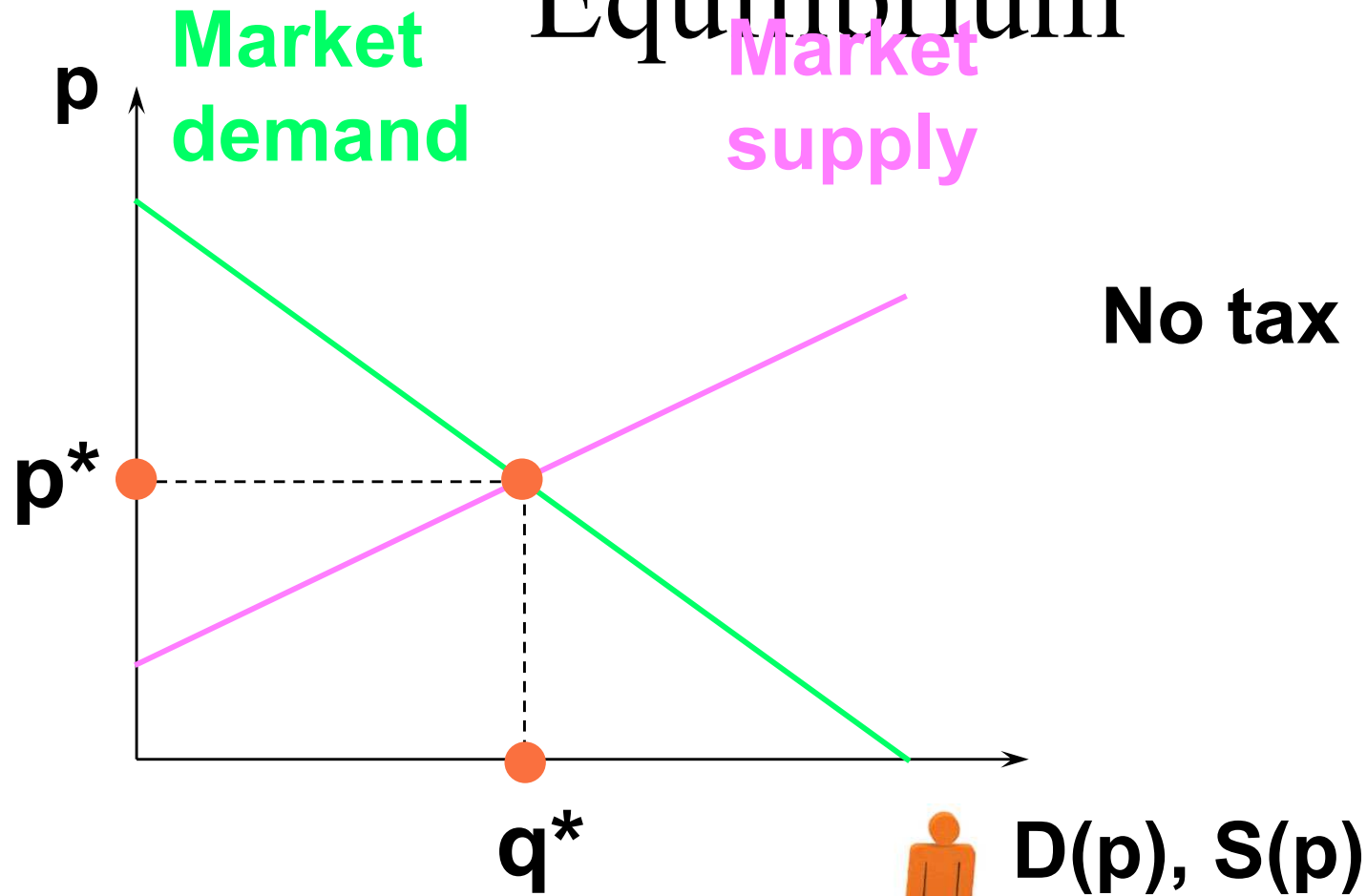
**describe the market's equilibrium.**

**Notice that these two conditions apply no matter if the tax is levied on sellers or on buyers.**

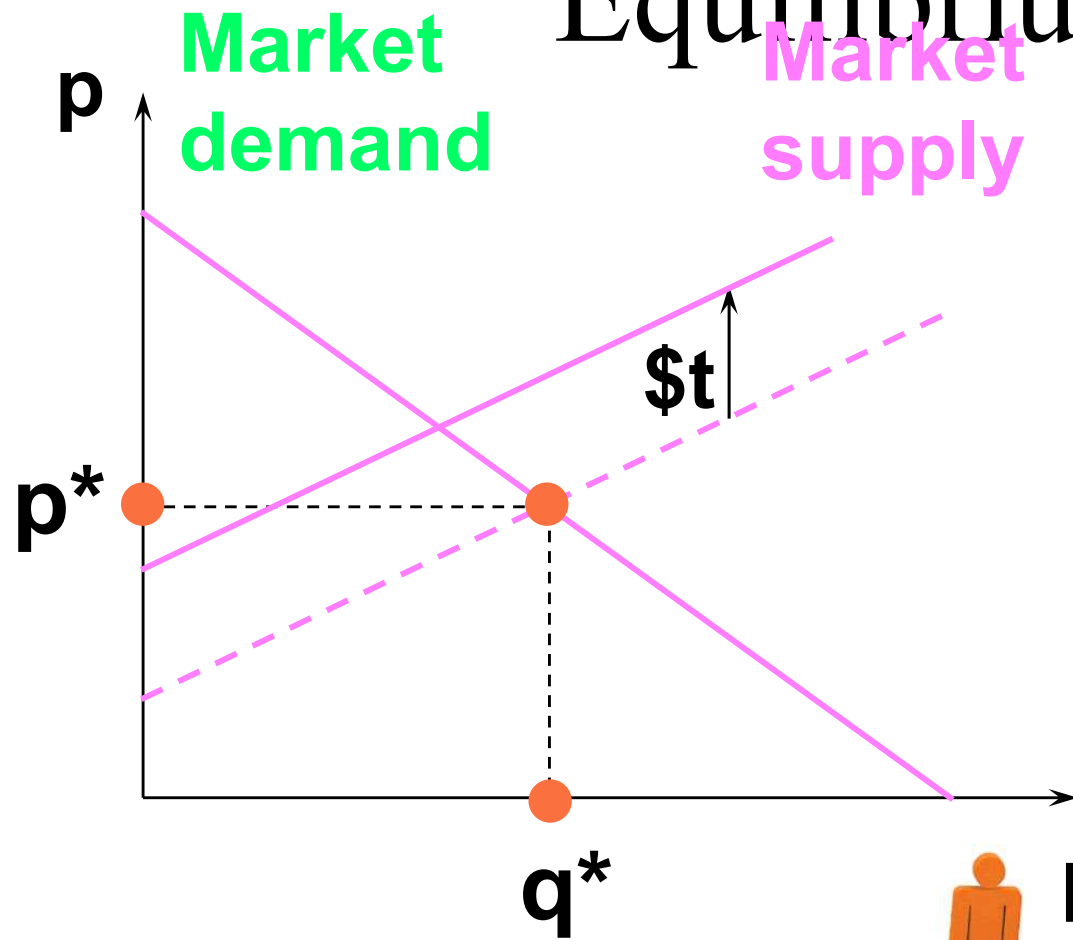
**Hence, a sales tax rate \$t\$ has the same effect as an excise tax rate \$t\$.**



# Quantity Taxes & Market Equilibrium



# Quantity Taxes & Market Equilibrium

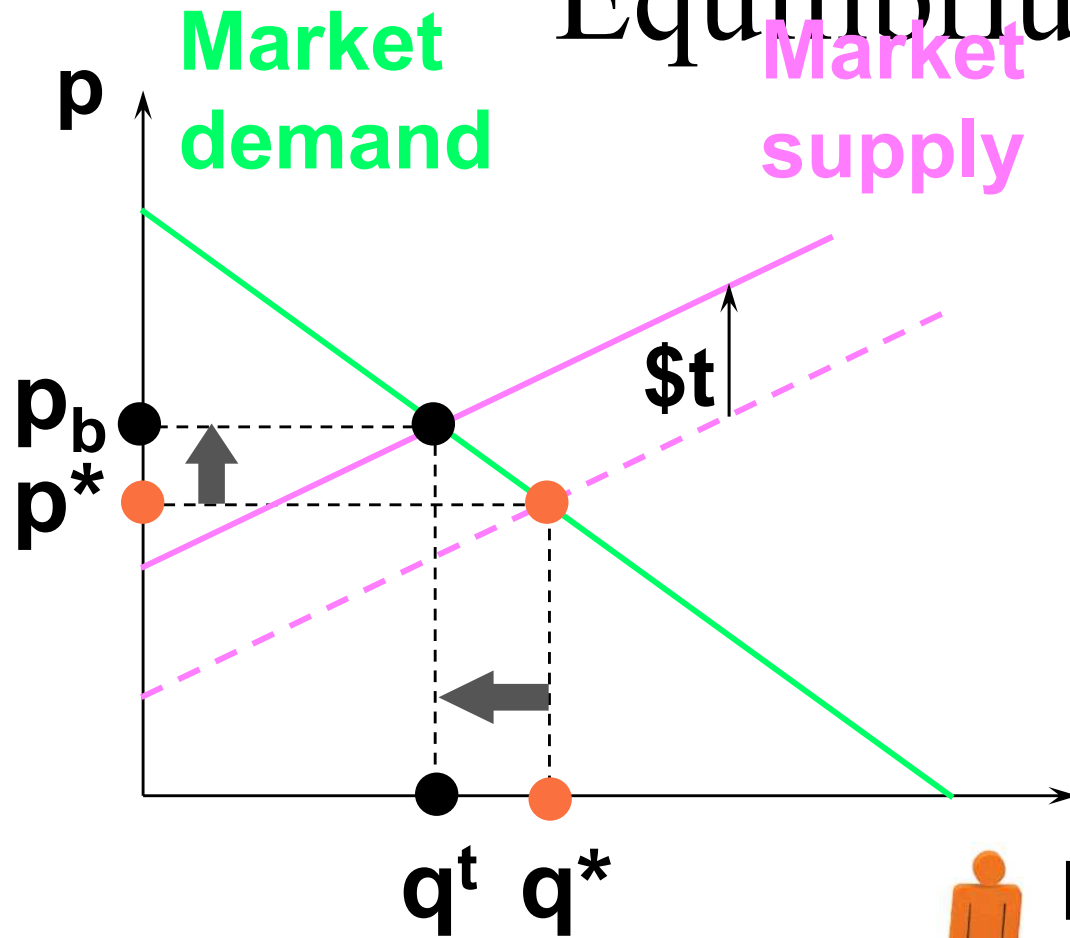


**An excise tax raises the market supply curve by  $\$t$**

$D(p), S(p)$



# Quantity Taxes & Market Equilibrium

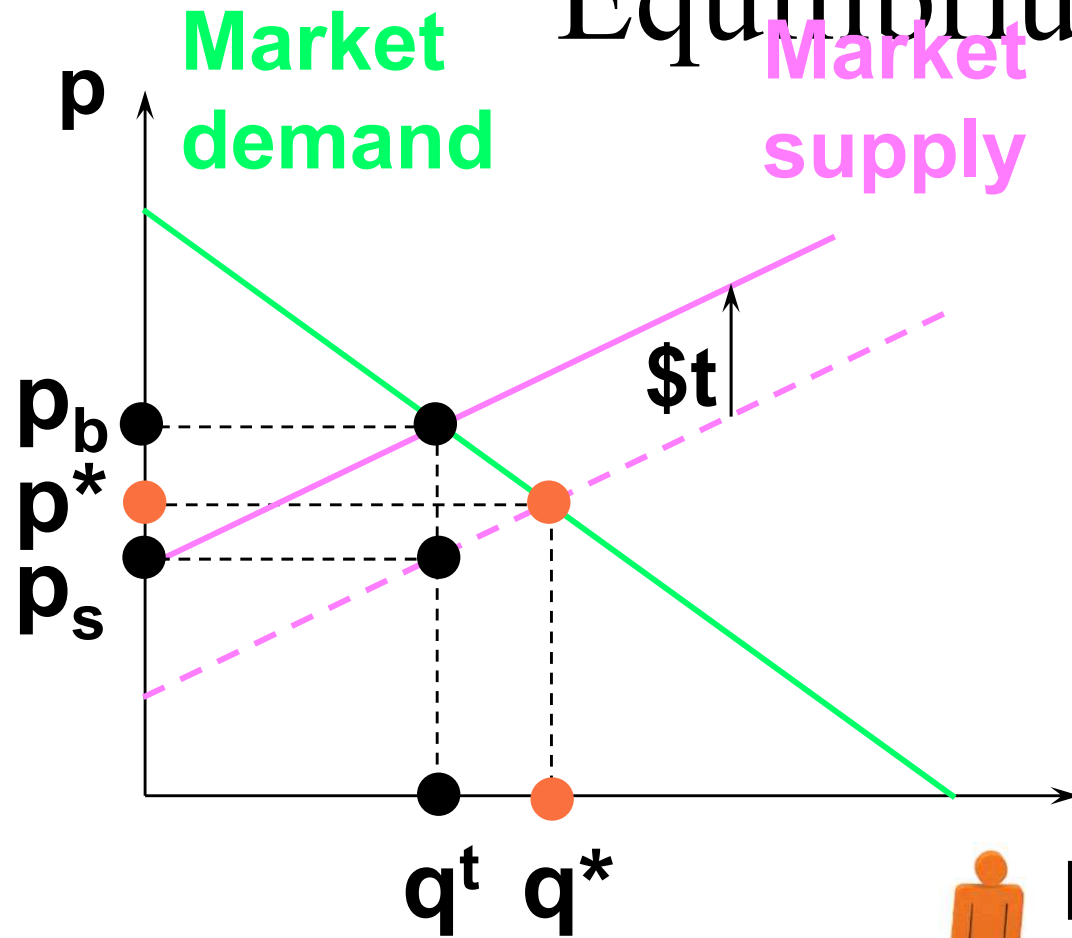


**An excise tax raises the market supply curve by  $\$t$ , raises the buyers' price and lowers the quantity traded.**

$D(p), S(p)$



# Quantity Taxes & Market Equilibrium

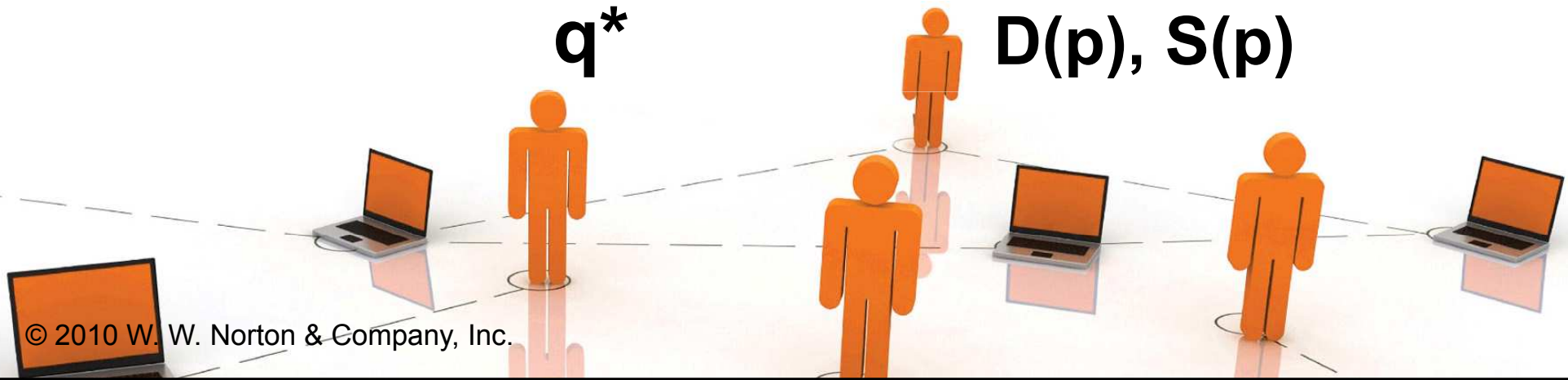
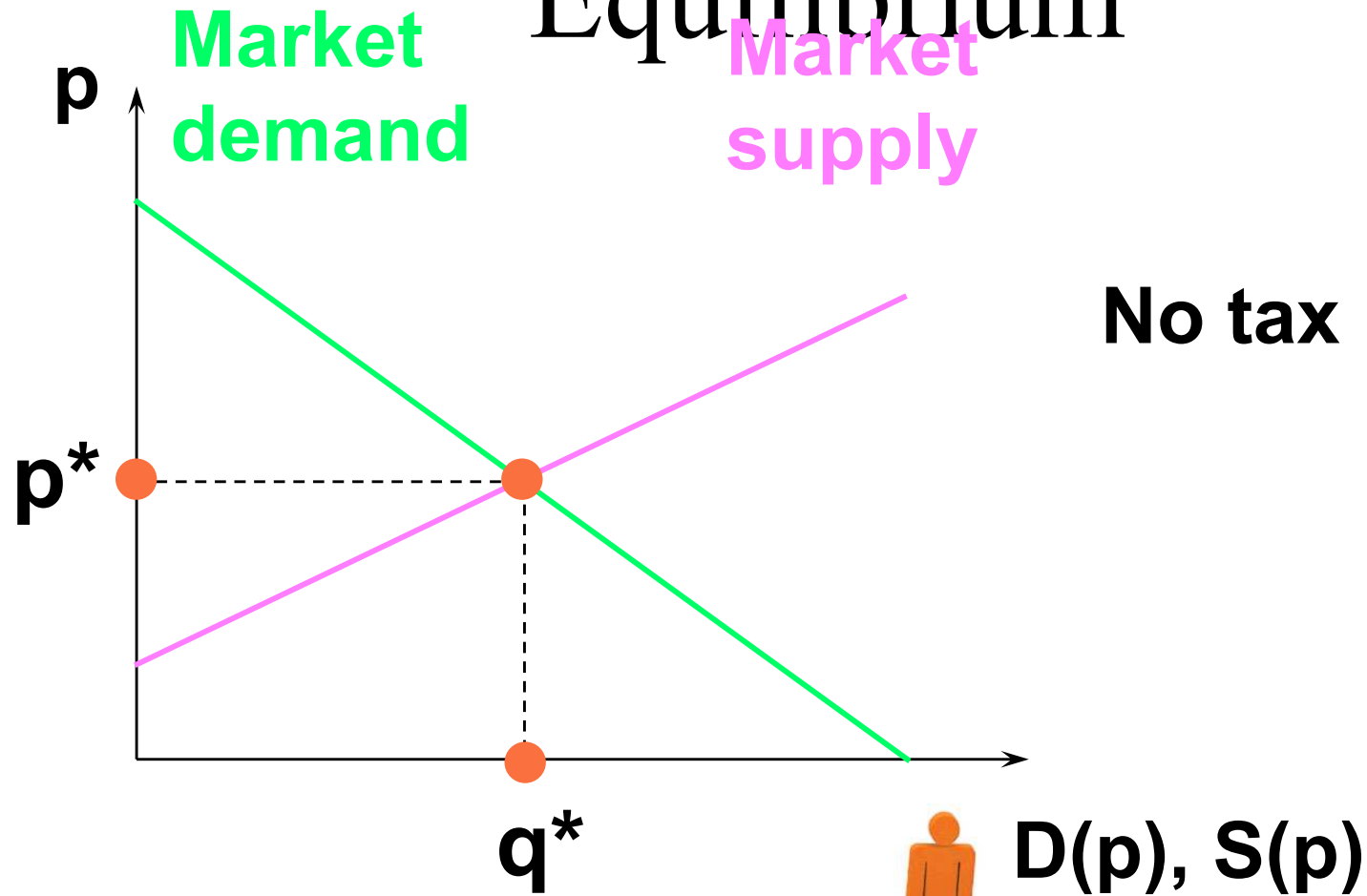


An excise tax raises the market supply curve by  $\$t$ , raises the buyers' price and lowers the quantity traded.

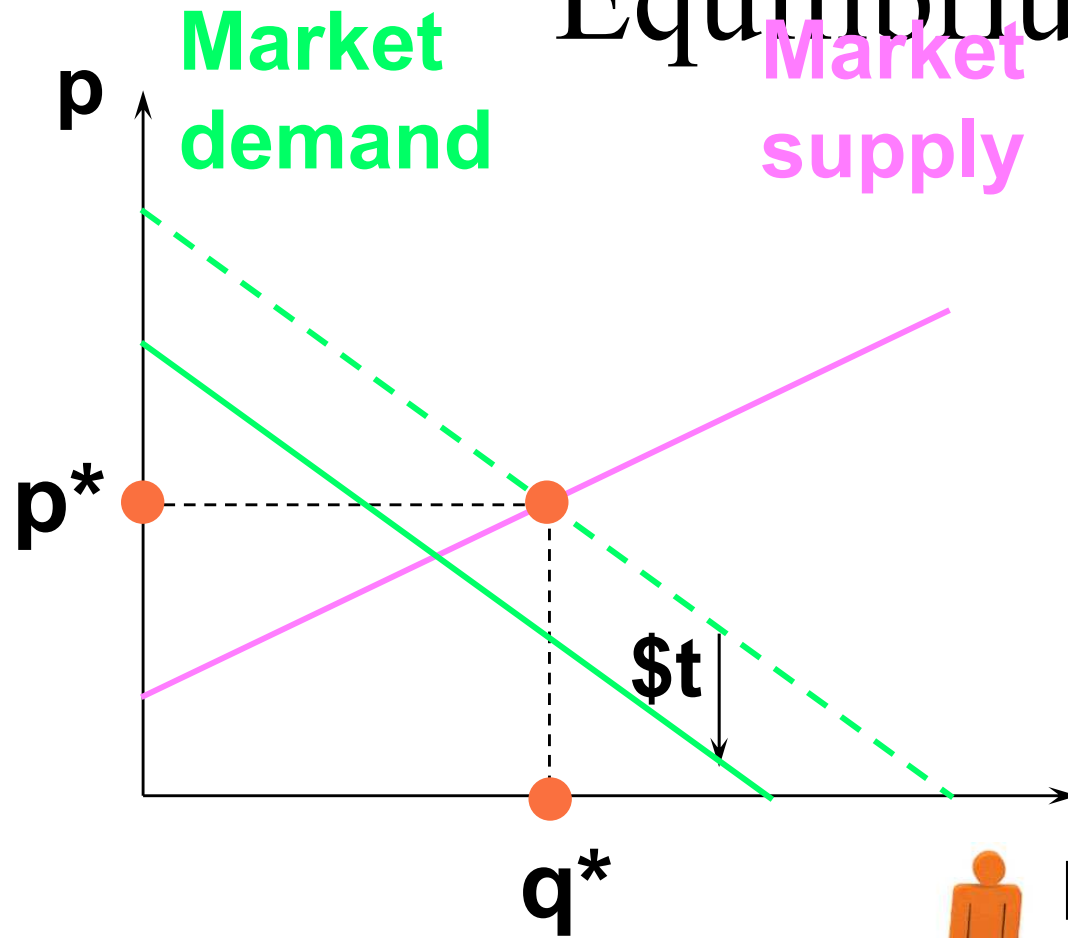
$D(p), S(p)$

And sellers receive only  $p_s = p_b - t$ .

# Quantity Taxes & Market Equilibrium



# Quantity Taxes & Market Equilibrium

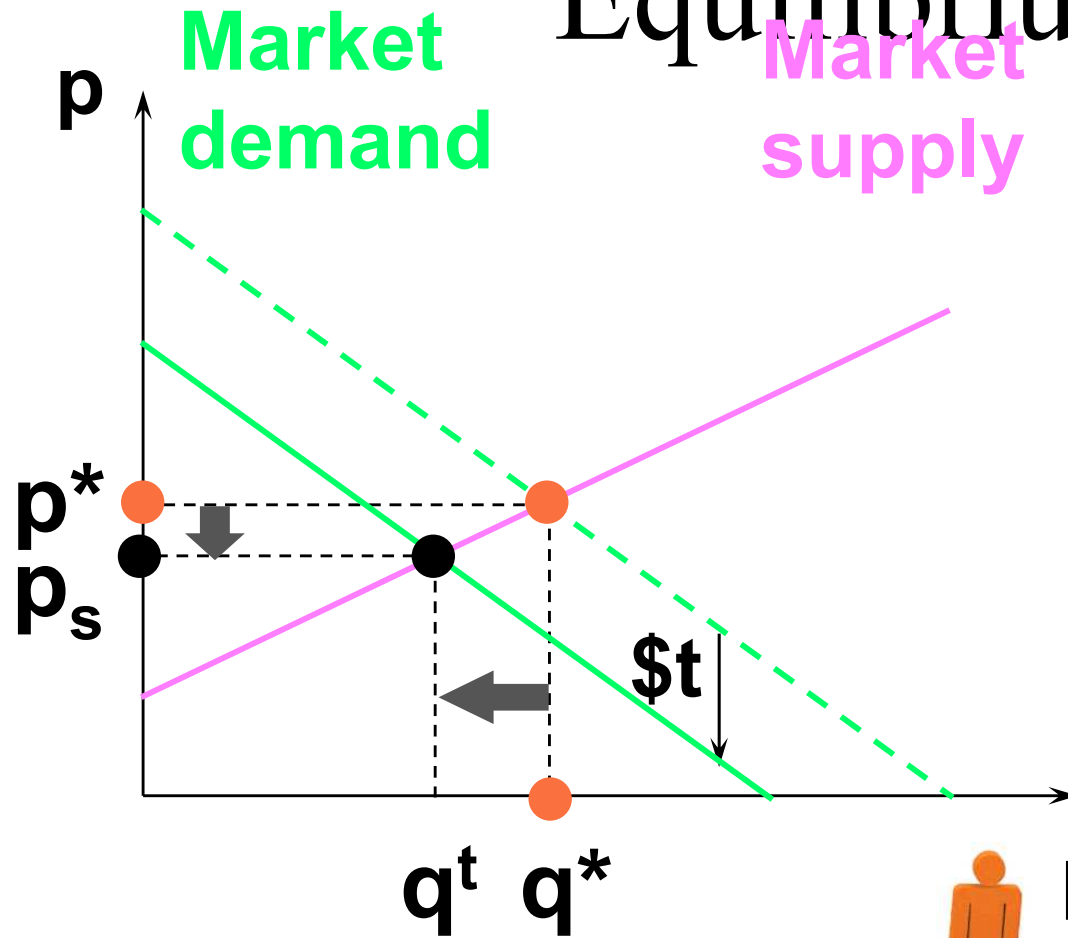


An sales tax lowers the market demand curve by  $\$t$

$D(p), S(p)$



# Quantity Taxes & Market Equilibrium

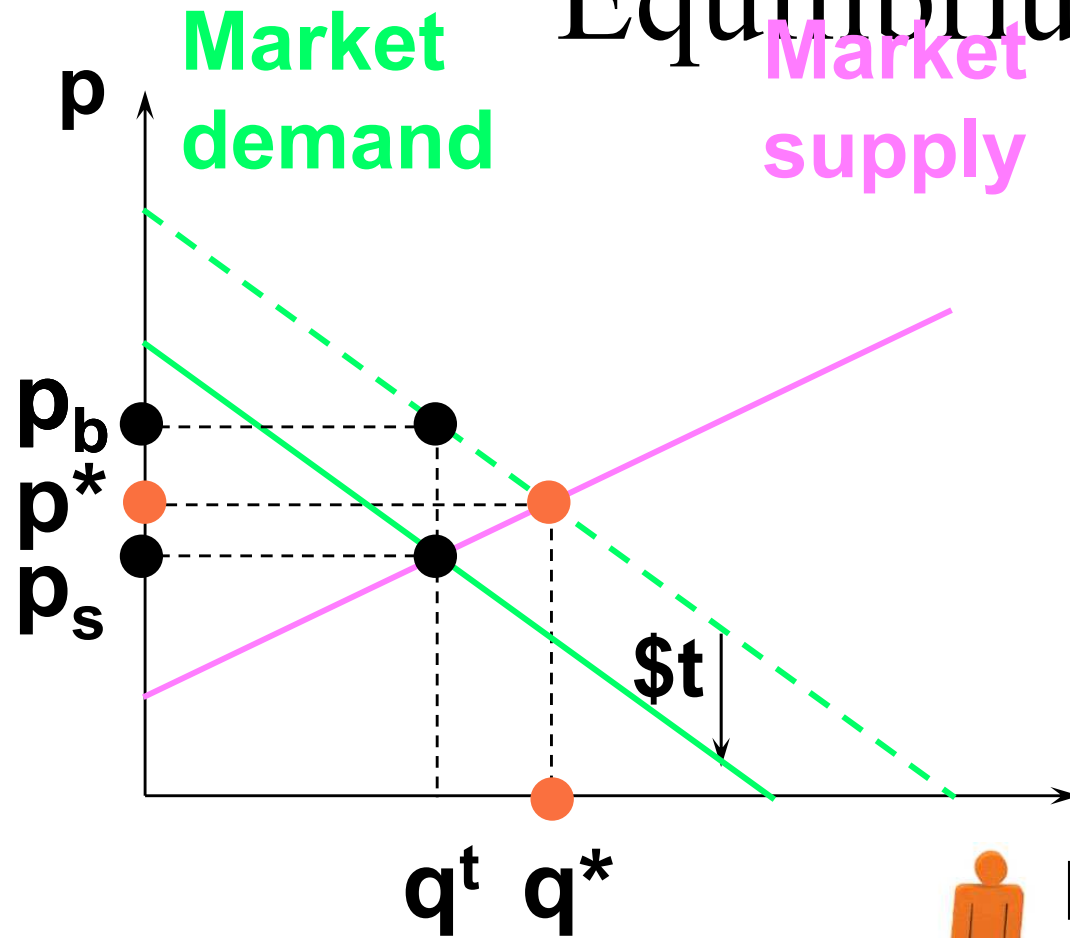


An sales tax lowers the market demand curve by  $\$t$ , lowers the sellers' price and reduces the quantity traded.





# Quantity Taxes & Market Equilibrium

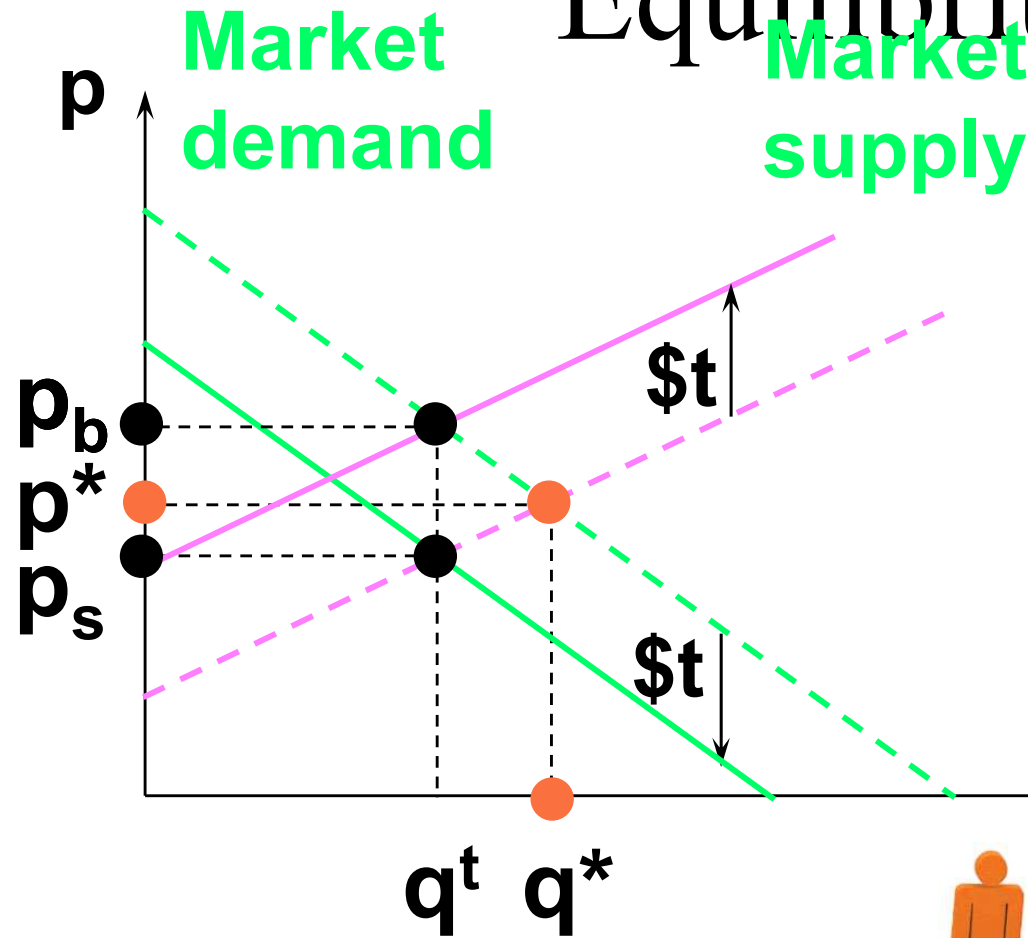


An sales tax lowers the market demand curve by  $\$t$ , lowers the sellers' price and reduces the quantity traded.

And buyers pay  $p_b = p_s + t$ .

# Quantity Taxes & Market

## Equilibrium



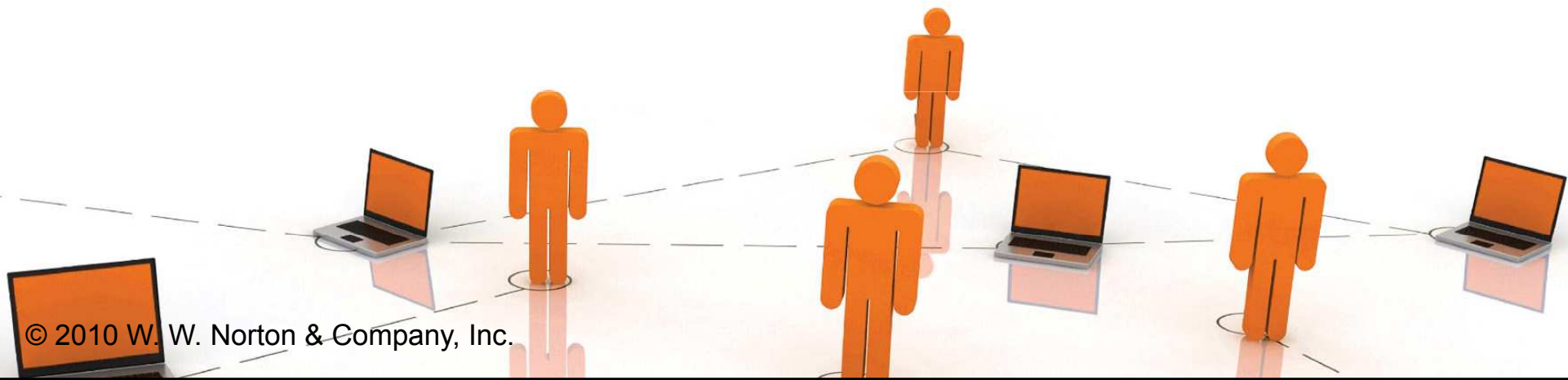
A sales tax levied at rate  $\$t$  has the same effects on the market's equilibrium as does an excise tax levied at rate  $\$t$ .

$D(p), S(p)$

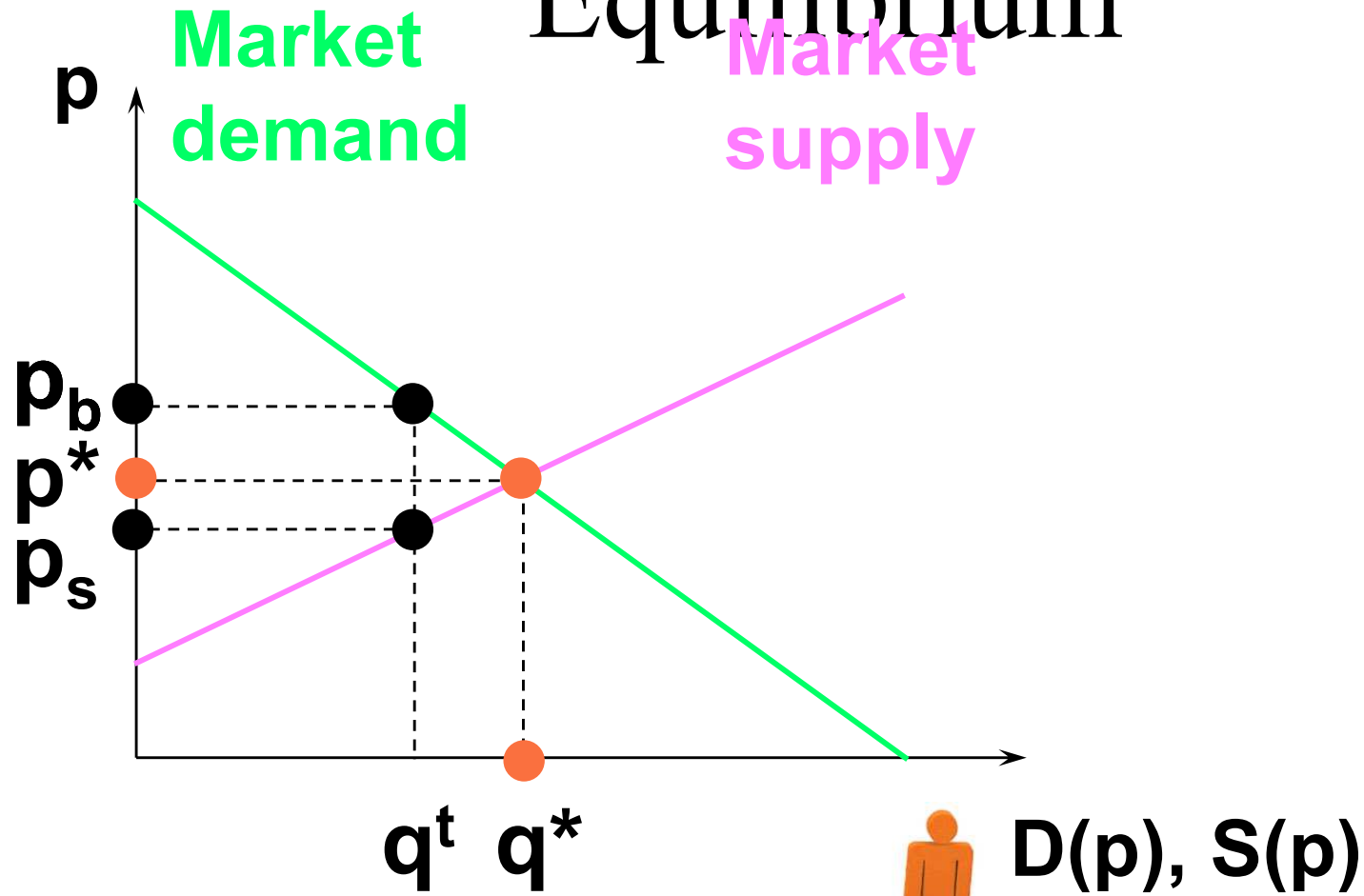


# Quantity Taxes & Market Equilibrium

- ◆ **Who pays the tax of \$t per unit traded?**
- ◆ **The division of the \$t between buyers and sellers is the incidence of the tax.**

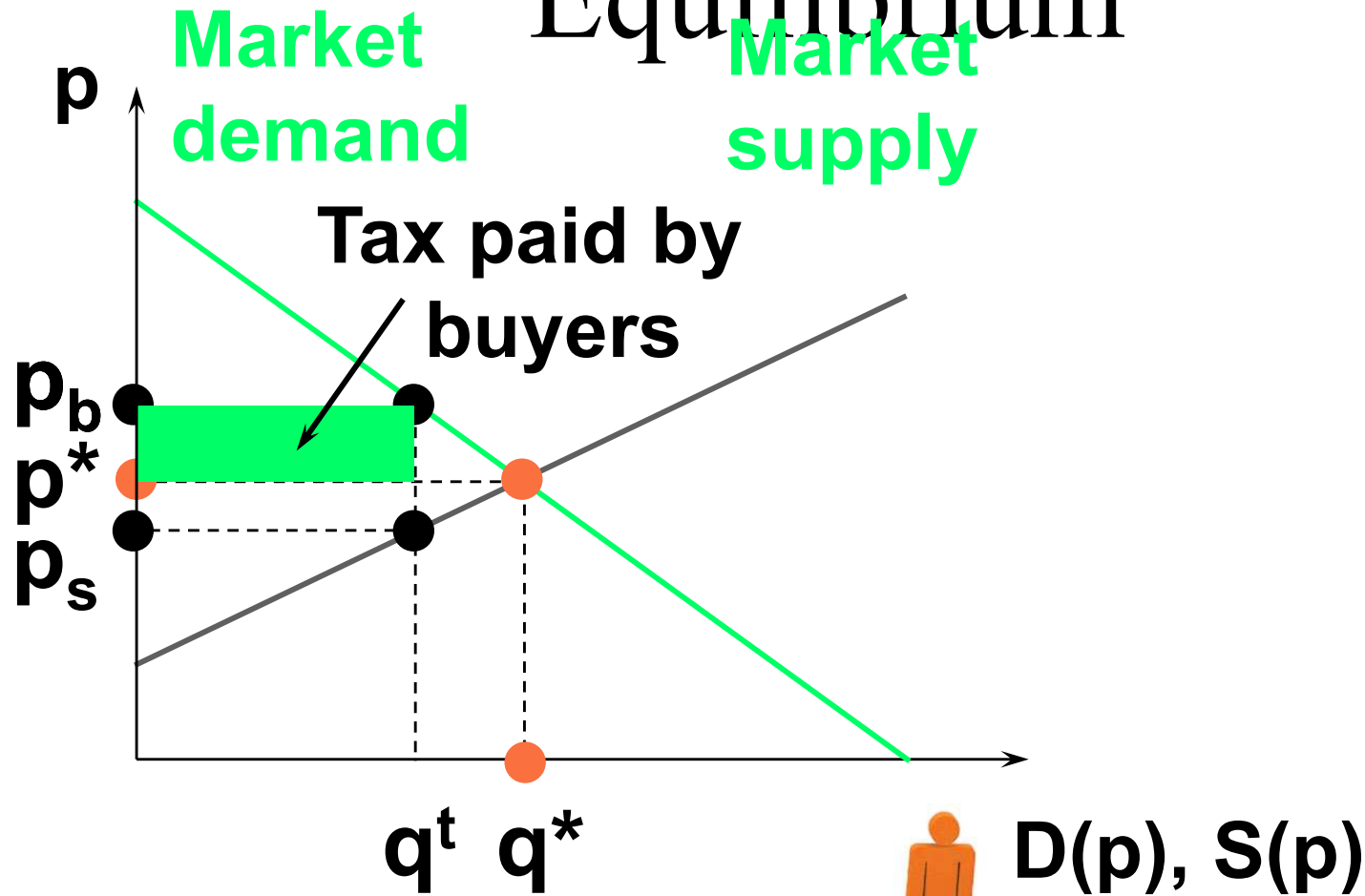


# Quantity Taxes & Market Equilibrium

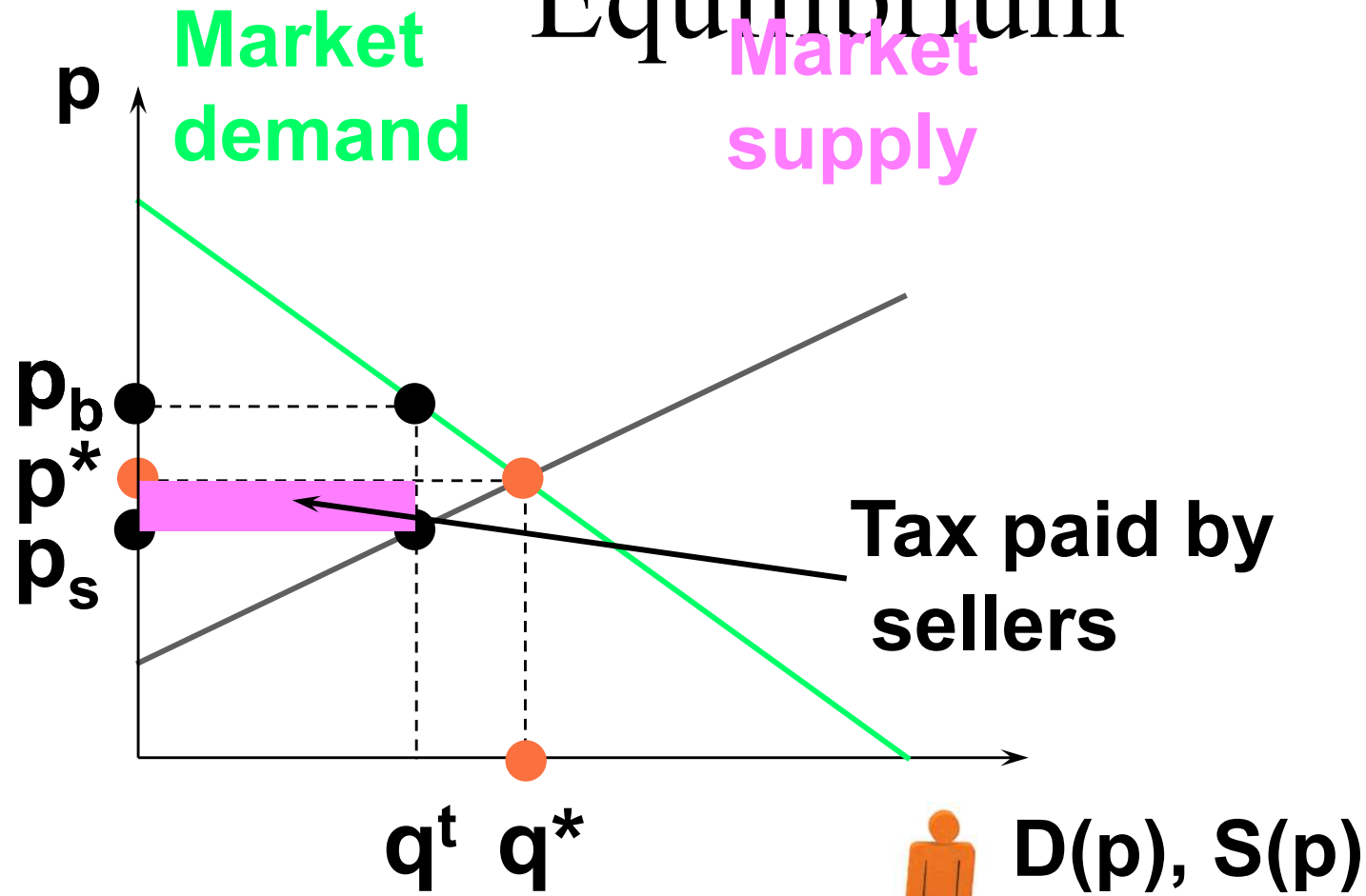


# Quantity Taxes & Market

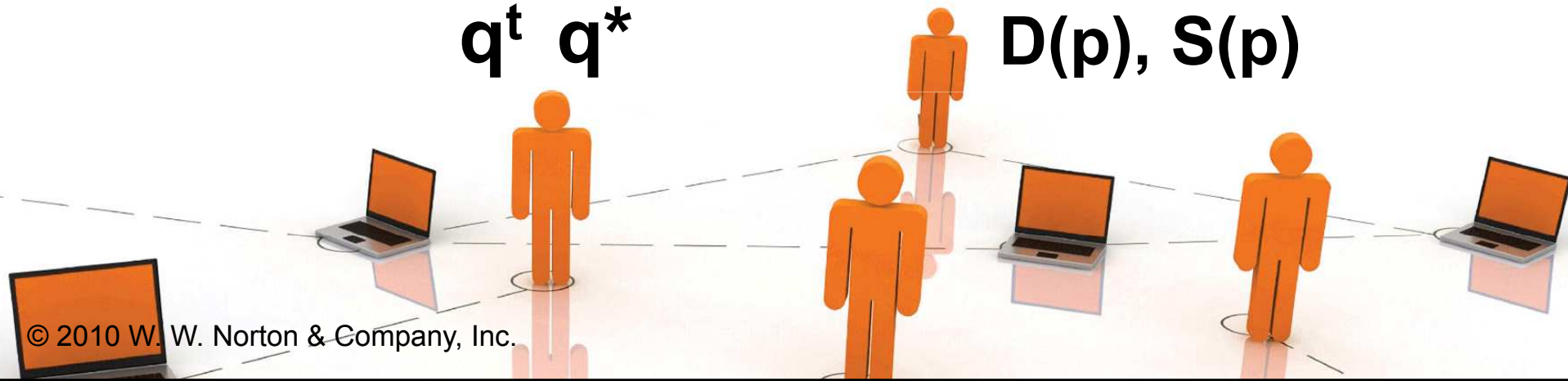
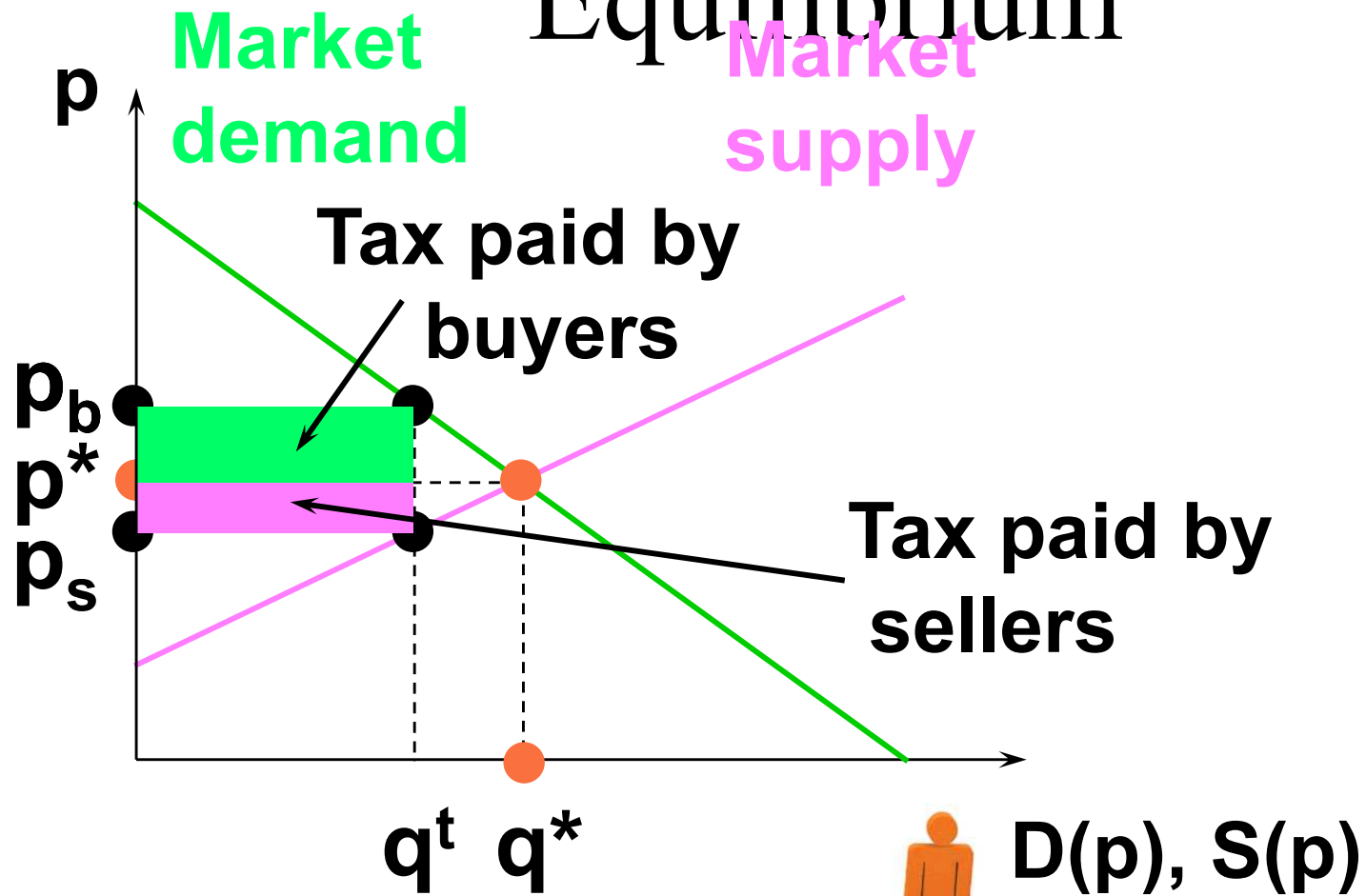
## Equilibrium



# Quantity Taxes & Market Equilibrium



# Quantity Taxes & Market Equilibrium

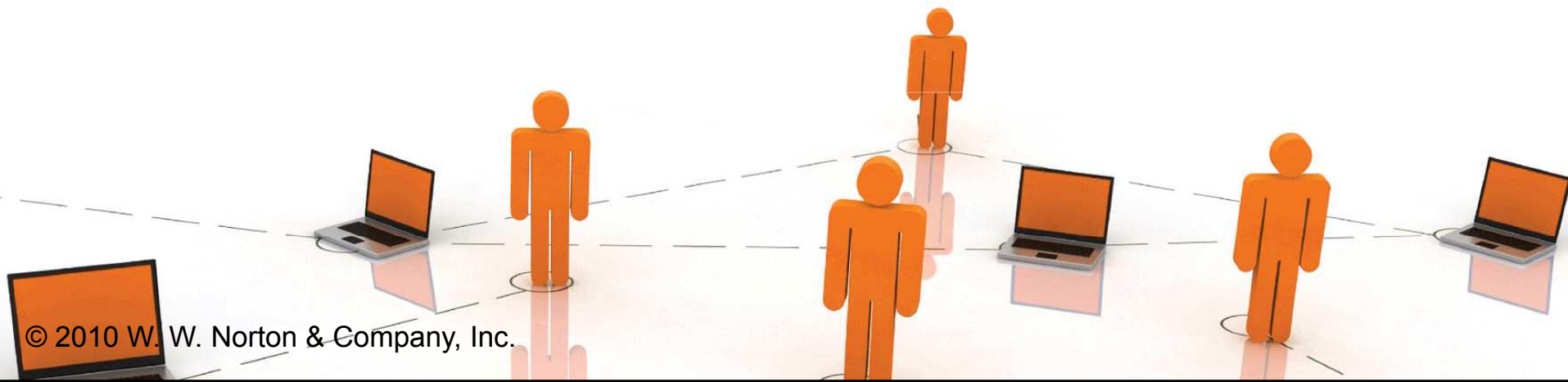


# Quantity Taxes & Market Equilibrium

- ◆ E.g. suppose the market demand and supply curves are linear.

$$D(p_b) = a - b p_b$$

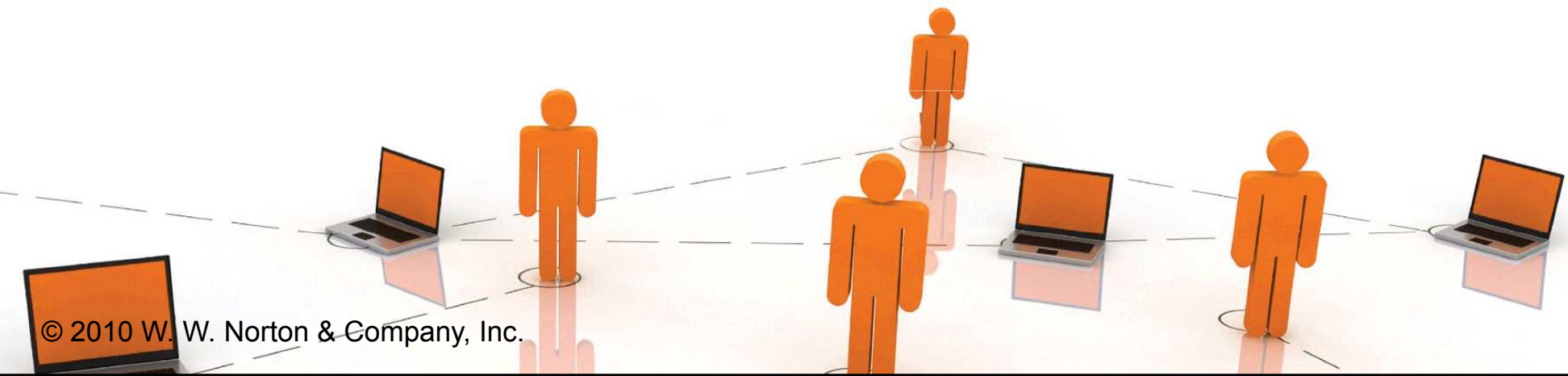
$$S(p_s) = c + d p_s$$





# Quantity Taxes & Market

$$D(p_b) = a - b p_b \quad \text{and} \quad S(p_s) = c + d p_s.$$



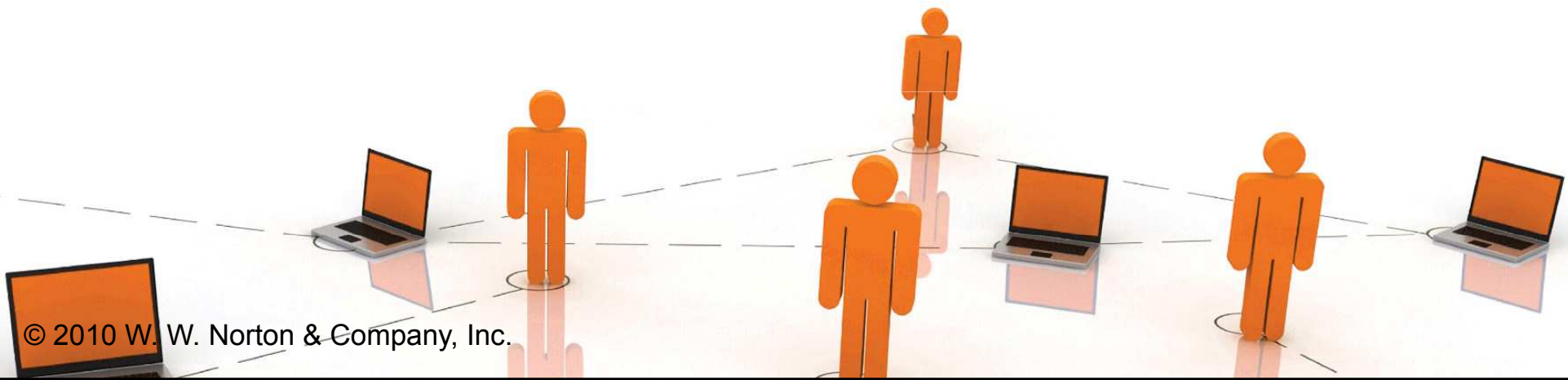
# Quantity Taxes & Market

$$D(p_b) = a - b p_b \quad \text{and} \quad S(p_s) = c + d p_s.$$

**With the tax, the market equilibrium satisfies**

$$p_b = p_s + t \quad \text{and} \quad D(p_b) = S(p_s) \quad \text{so}$$

$$p_b = p_s + t \quad \text{and} \quad a - b p_b = c + d p_s.$$



# Quantity Taxes & Market

**Equilibrium**  
 $D(p_b) = a - b p_b$  and  $S(p_s) = c + d p_s$ .

**With the tax, the market equilibrium satisfies**

$$p_b = p_s + t \quad \text{and} \quad D(p_b) = S(p_s) \quad \text{so}$$

$$p_b = p_s + t \quad \text{and} \quad a - b p_b = c + d p_s.$$

**Substituting for  $p_b$  gives**

$$a - b(p_s + t) = c + d p_s \Rightarrow p_s = \frac{a - c - b t}{b + d}.$$

# Quantity Taxes & Market

## Equilibrium

$$p_s = \frac{a - c - b t}{b + d} \quad \text{and} \quad p_b = p_s + t \quad \text{give}$$

$$p_b = \frac{a - c + d t}{b + d}$$

**The quantity traded at equilibrium is**

$$q^t = D(p_b) = S(p_s)$$

$$= a + b p_b = \frac{a d + b c - b d t}{b + d}$$



# Quantity Taxes & Market Equilibrium

$$p_s = \frac{a - c - b t}{b + d}$$

$$q^t = \frac{a d + b c - b d t}{b + d}$$

$$p_b = \frac{a - c + d t}{b + d}$$

**As  $t \rightarrow 0$ ,  $p_s$  and  $p_b \rightarrow \frac{a - c}{b + d} = p^*$ , the equilibrium price if**

**there is no tax ( $t = 0$ ) and  $q^t \rightarrow$  \_\_\_\_\_**

**the quantity traded at equilibrium**

**when there is no tax.**



# Quantity Taxes & Market Equilibrium

$$p_s = \frac{a - c - b t}{b + d}$$

$$q^t = \frac{a d + b c - b d t}{b + d}$$

$$p_b = \frac{a - c + d t}{b + d}$$

**As  $t$  increases,**

**$p_s$  falls,**

**$p_b$  rises,**

**and**

**$q^t$  falls.**



# Quantity Taxes & Market Equilibrium

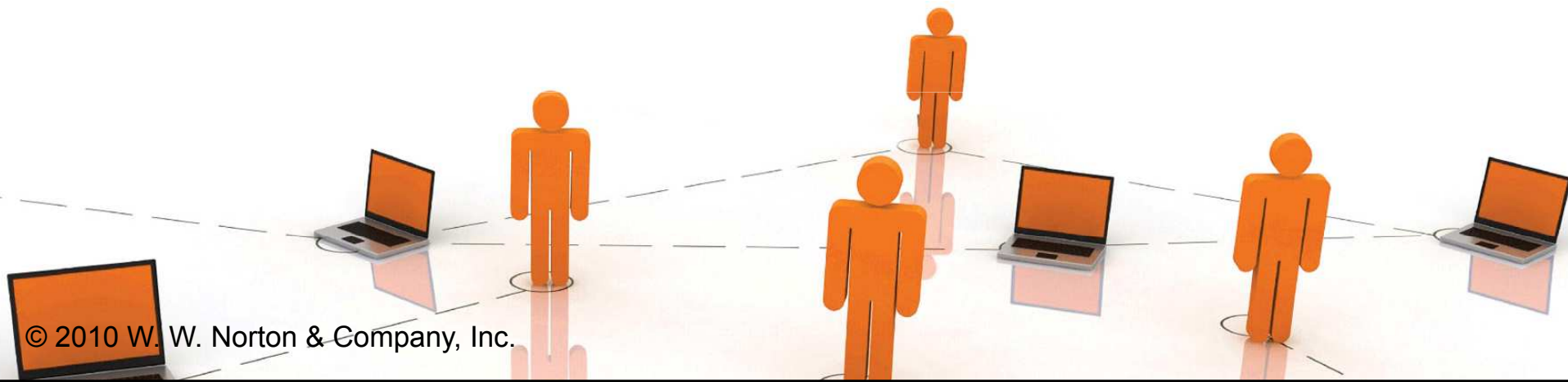
$$p_s = \frac{a - c - b t}{b + d}$$

$$q^t = \frac{a d + b c - b d t}{b + d}$$

$$p_b = \frac{a - c + d t}{b + d}$$

**The tax paid per unit by the buyer is**

$$p_b - p^* = \frac{a - c + d t}{b + d} - \frac{a - c}{b + d} = \frac{d t}{b + d}.$$



# Quantity Taxes & Market Equilibrium

$$p_s = \frac{a - c - b t}{b + d}$$

$$q^t = \frac{a d + b c - b d t}{b + d}$$

$$p_b = \frac{a - c + d t}{b + d}$$

**The tax paid per unit by the buyer is**

$$p_b - p^* = \frac{a - c + d t}{b + d} - \frac{a - c}{b + d} = \frac{d t}{b + d}$$

**The tax paid per unit by the seller is**

$$p^* - p_s = \frac{a - c}{b + d} - \frac{a - c - b t}{b + d} = \frac{b t}{b + d}$$



# Quantity Taxes & Market Equilibrium

$$p_s = \frac{a - c - b t}{b + d}$$

$$q^t = \frac{a d + b c - b d t}{b + d}$$

$$p_b = \frac{a - c + d t}{b + d}$$

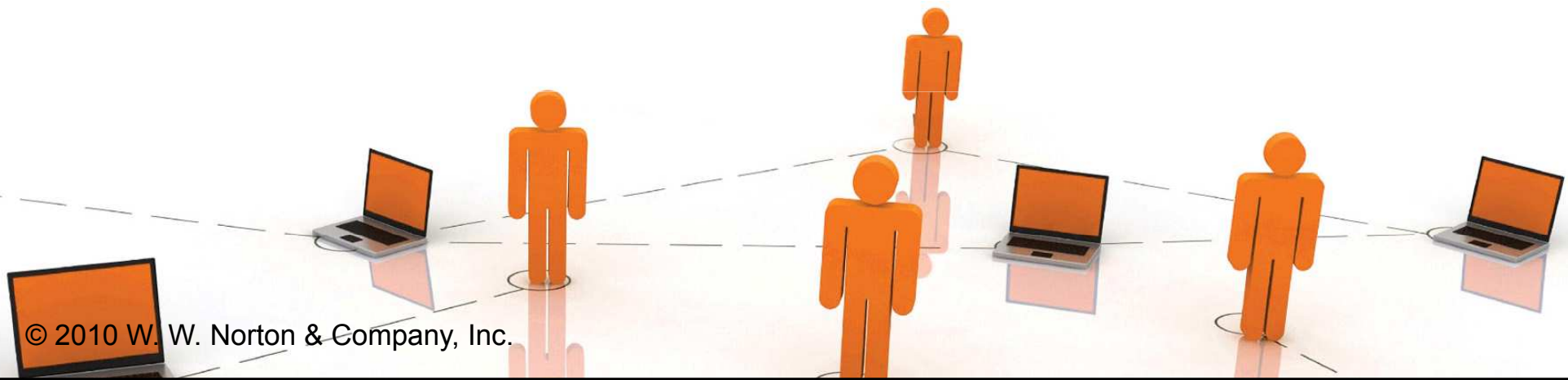
**The total tax paid (by buyers and sellers combined) is**

$$T = t q^t = t \frac{a d + b c - b d t}{b + d}.$$



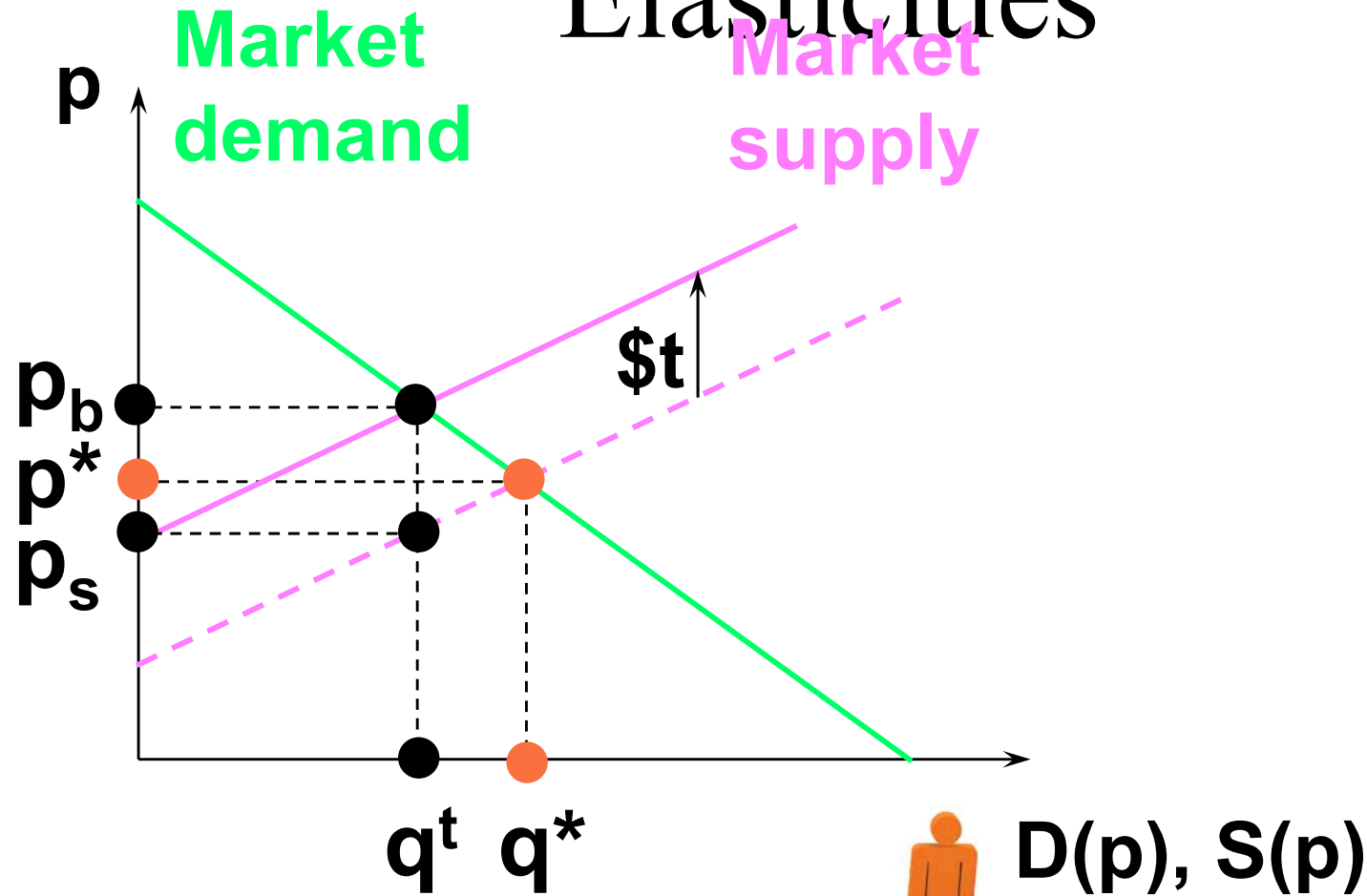
# Tax Incidence and Own-Price Elasticities

- ◆ **The incidence of a quantity tax depends upon the own-price elasticities of demand and supply.**



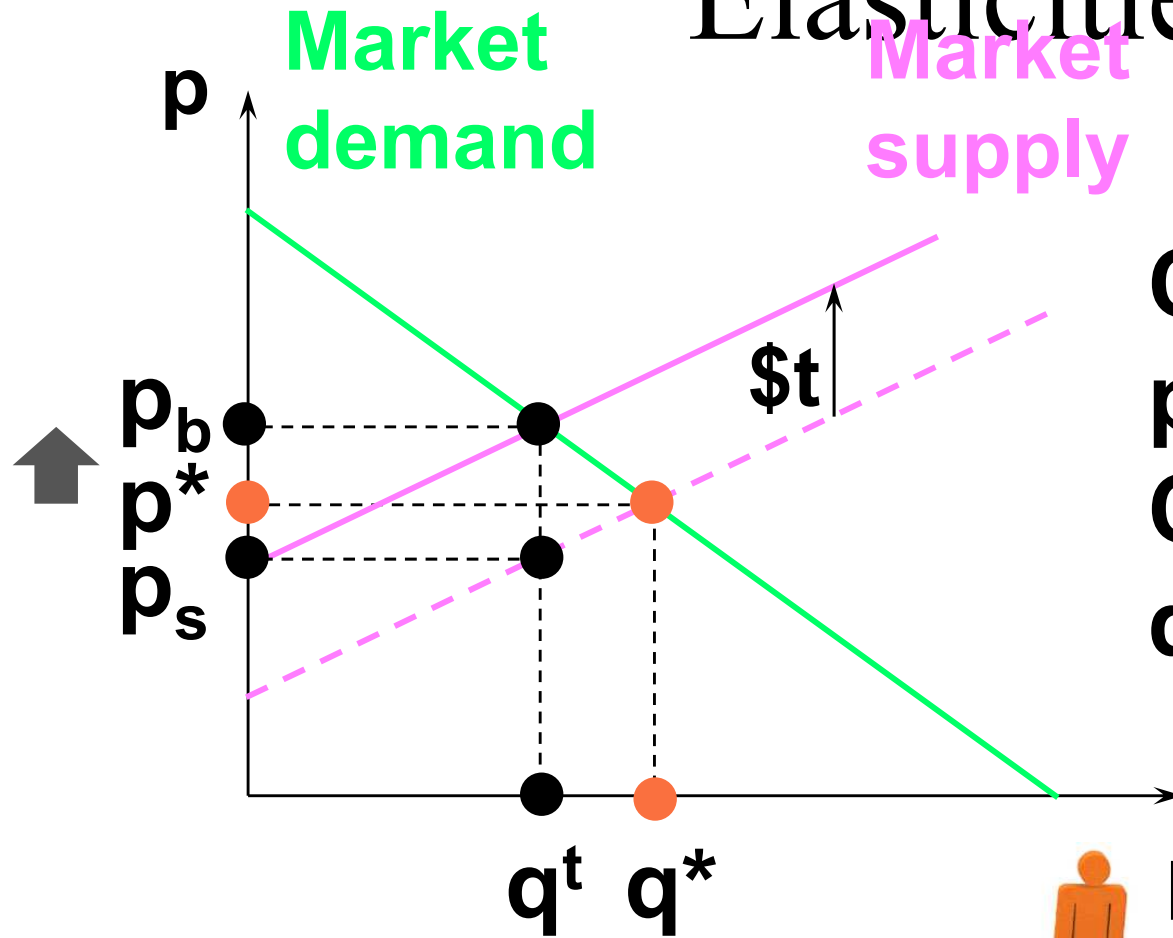
# Tax Incidence and Own-Price

## Elasticities



# Tax Incidence and Own-Price

## Elasticities



**Change to buyers' price is  $p_b - p^*$ .**  
**Change to quantity demanded is  $\Delta q$ .**

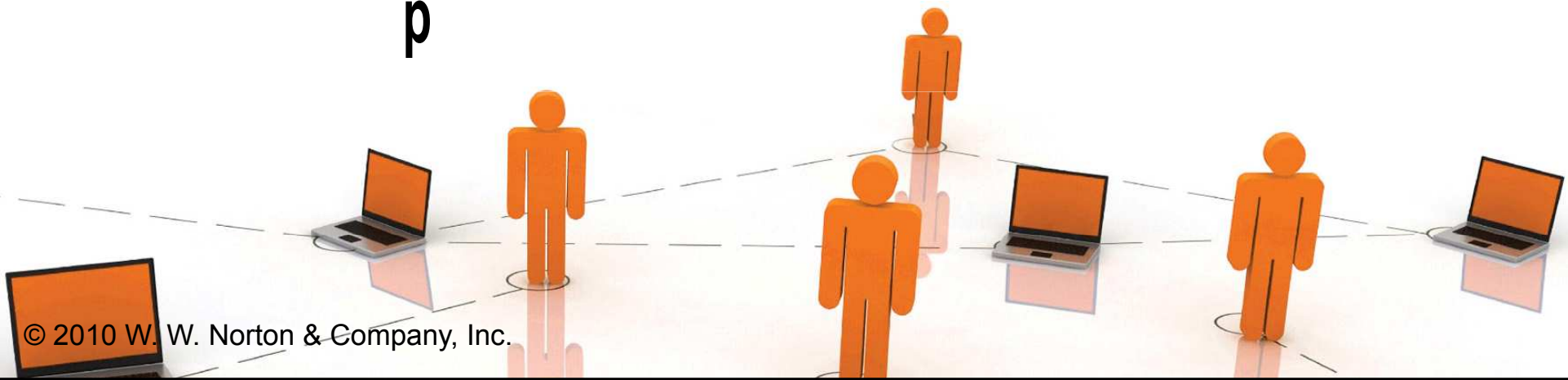
$D(p), S(p)$

$\Delta q$

# Tax Incidence and Own-Price Elasticities

**Around  $p = p^*$  the own-price elasticity of demand is approximately**

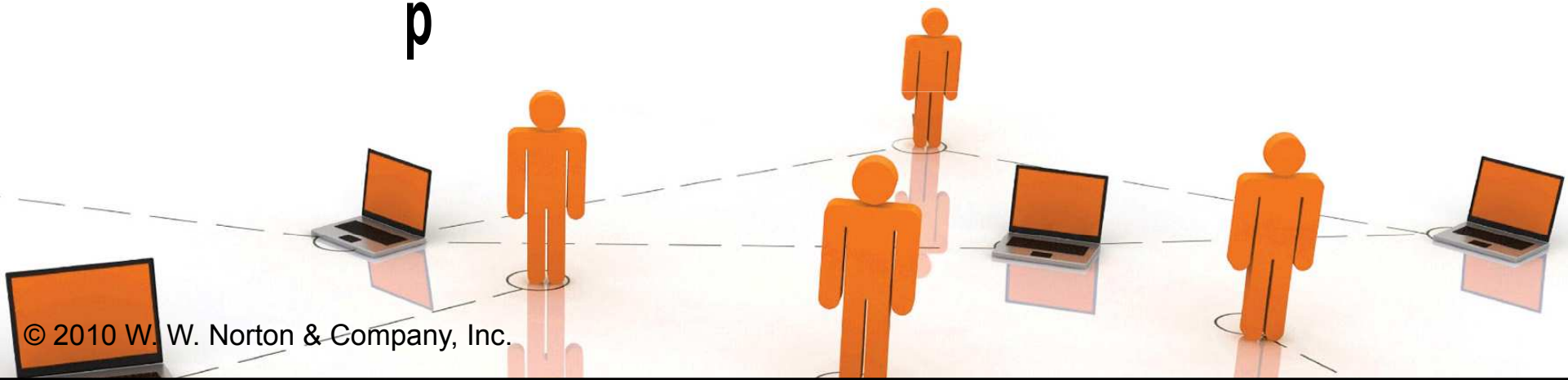
$$\epsilon_D \approx \frac{\frac{\Delta q}{q^*}}{\frac{p_b - p^*}{p^*}}$$



# Tax Incidence and Own-Price Elasticities

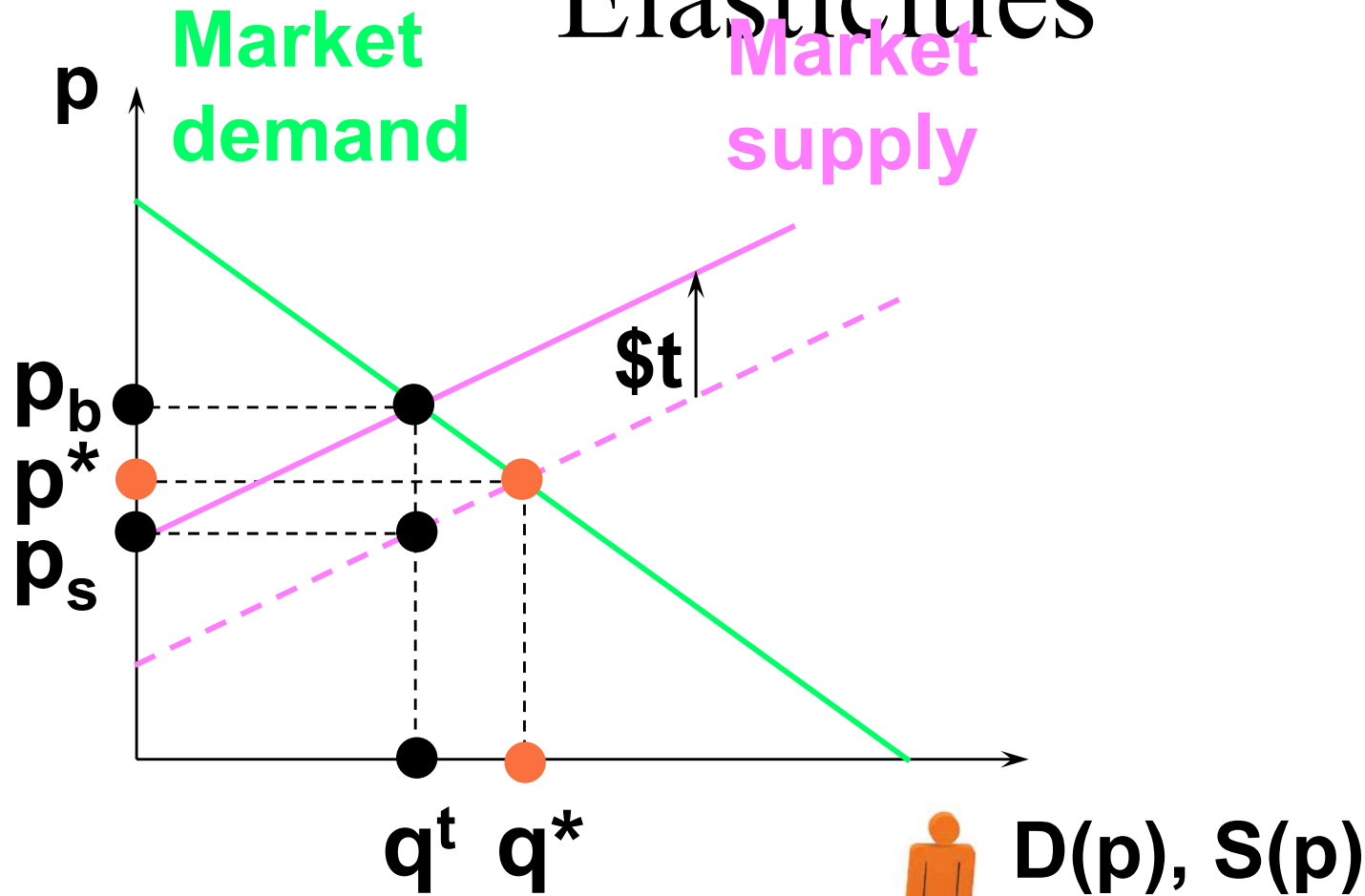
**Around  $p = p^*$  the own-price elasticity of demand is approximately**

$$\epsilon_D \approx \frac{\frac{\Delta q}{q^*}}{\frac{p_b - p^*}{p^*}} \Rightarrow p_b - p^* \approx \frac{\Delta q \times p^*}{\epsilon_D \times q^*}.$$



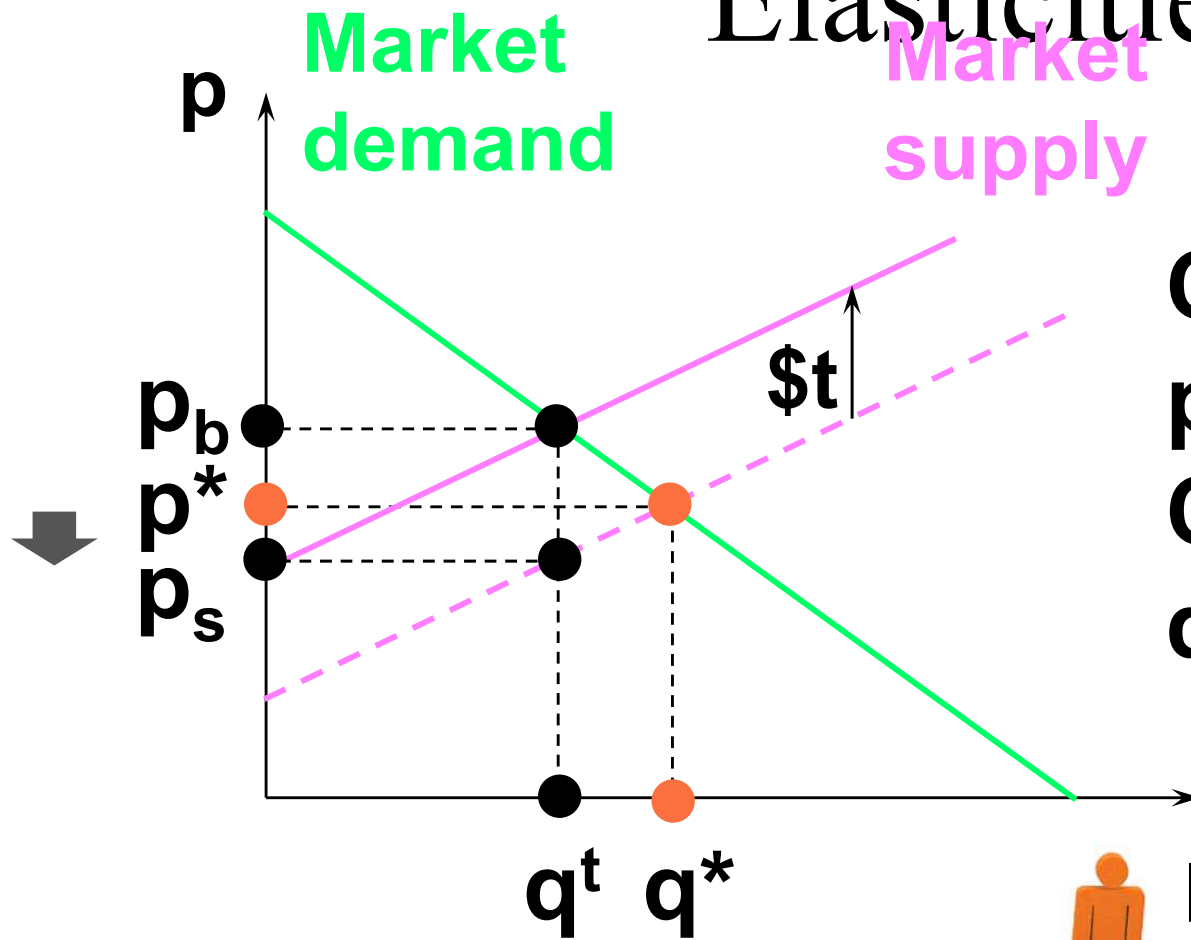
# Tax Incidence and Own-Price

## Elasticities



# Tax Incidence and Own-Price

## Elasticities



**Change to sellers' price is  $p_s - p^*$ .**  
**Change to quantity demanded is  $\Delta q$ .**

$D(p), S(p)$

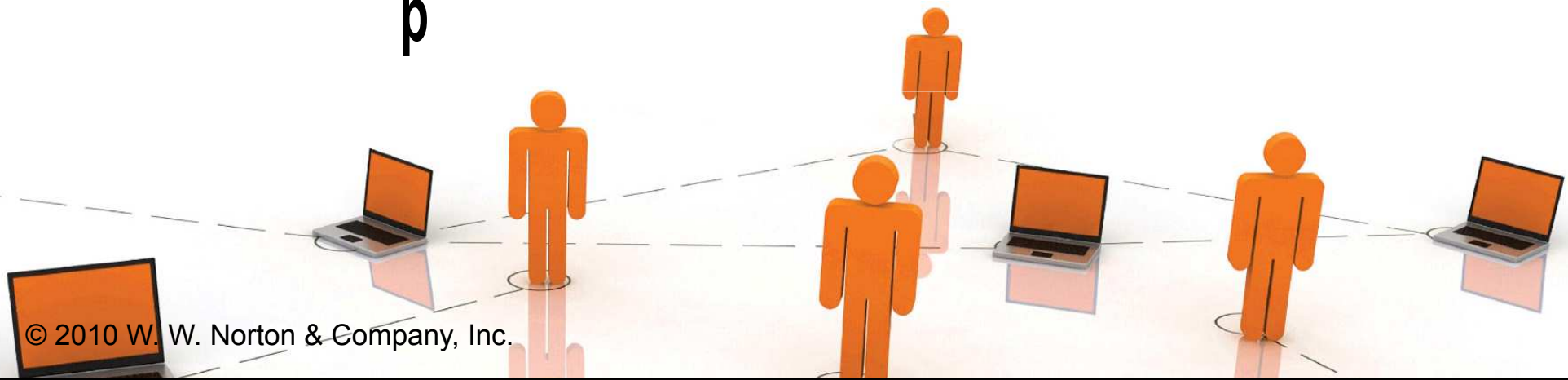
$\Delta q$



# Tax Incidence and Own-Price Elasticities

**Around  $p = p^*$  the own-price elasticity of supply is approximately**

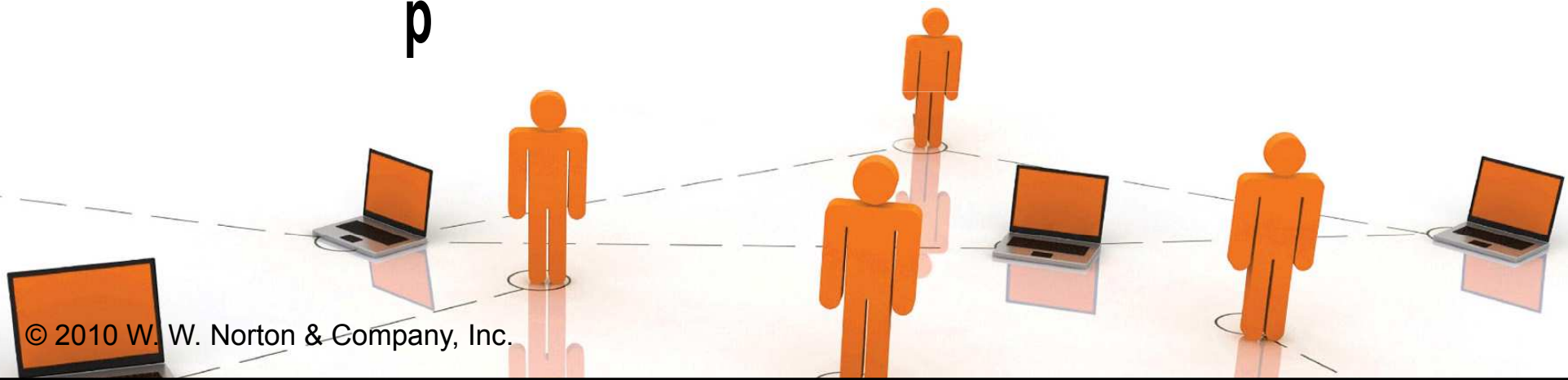
$$\epsilon_s \approx \frac{\frac{\Delta q}{q^*}}{\frac{p_s - p^*}{p^*}}$$



# Tax Incidence and Own-Price Elasticities

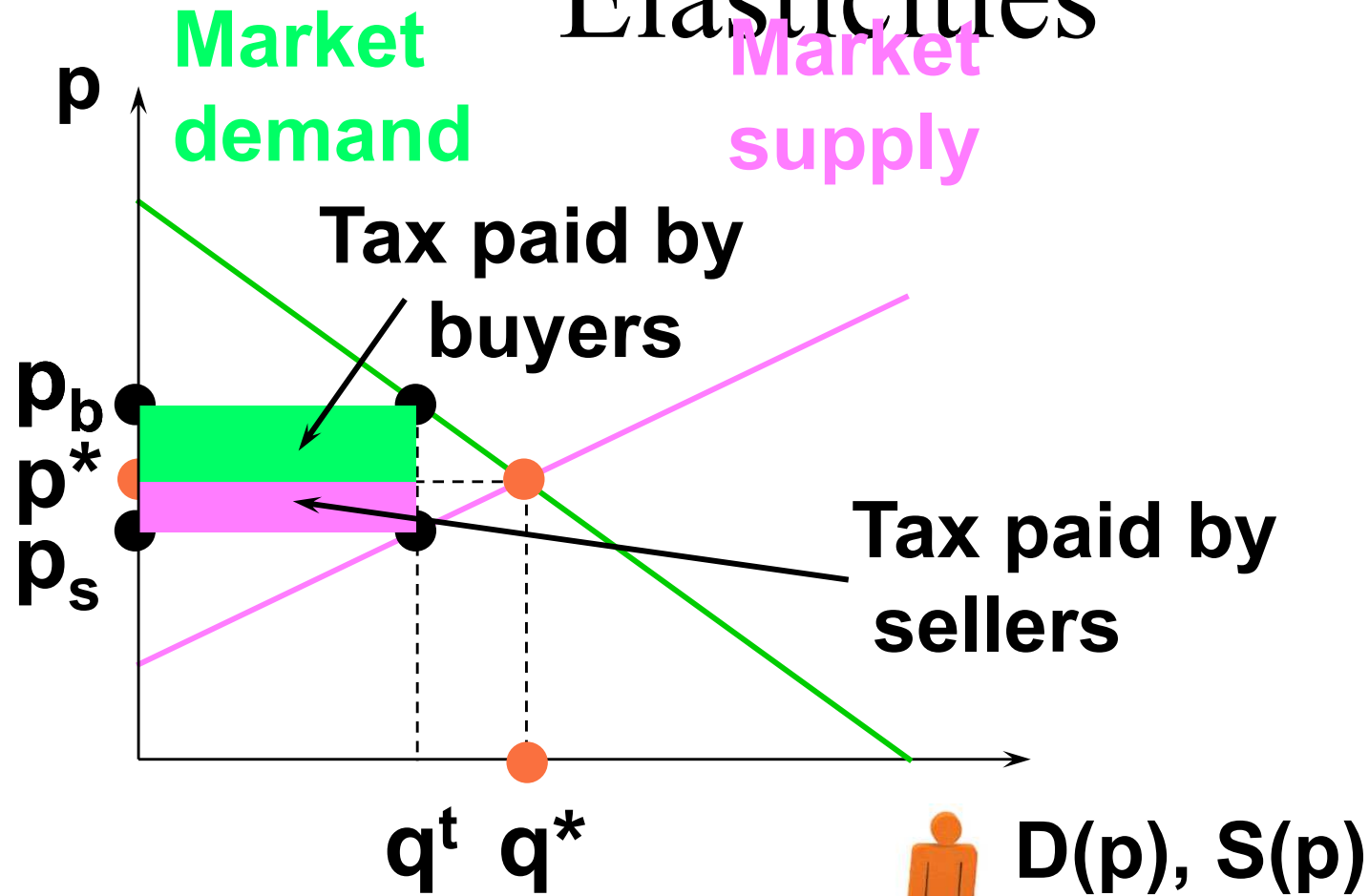
**Around  $p = p^*$  the own-price elasticity of supply is approximately**

$$\epsilon_s \approx \frac{\frac{\Delta q}{q^*}}{\frac{p_s - p^*}{p^*}} \Rightarrow p_s - p^* \approx \frac{\Delta q \times p^*}{\epsilon_s \times q^*}.$$



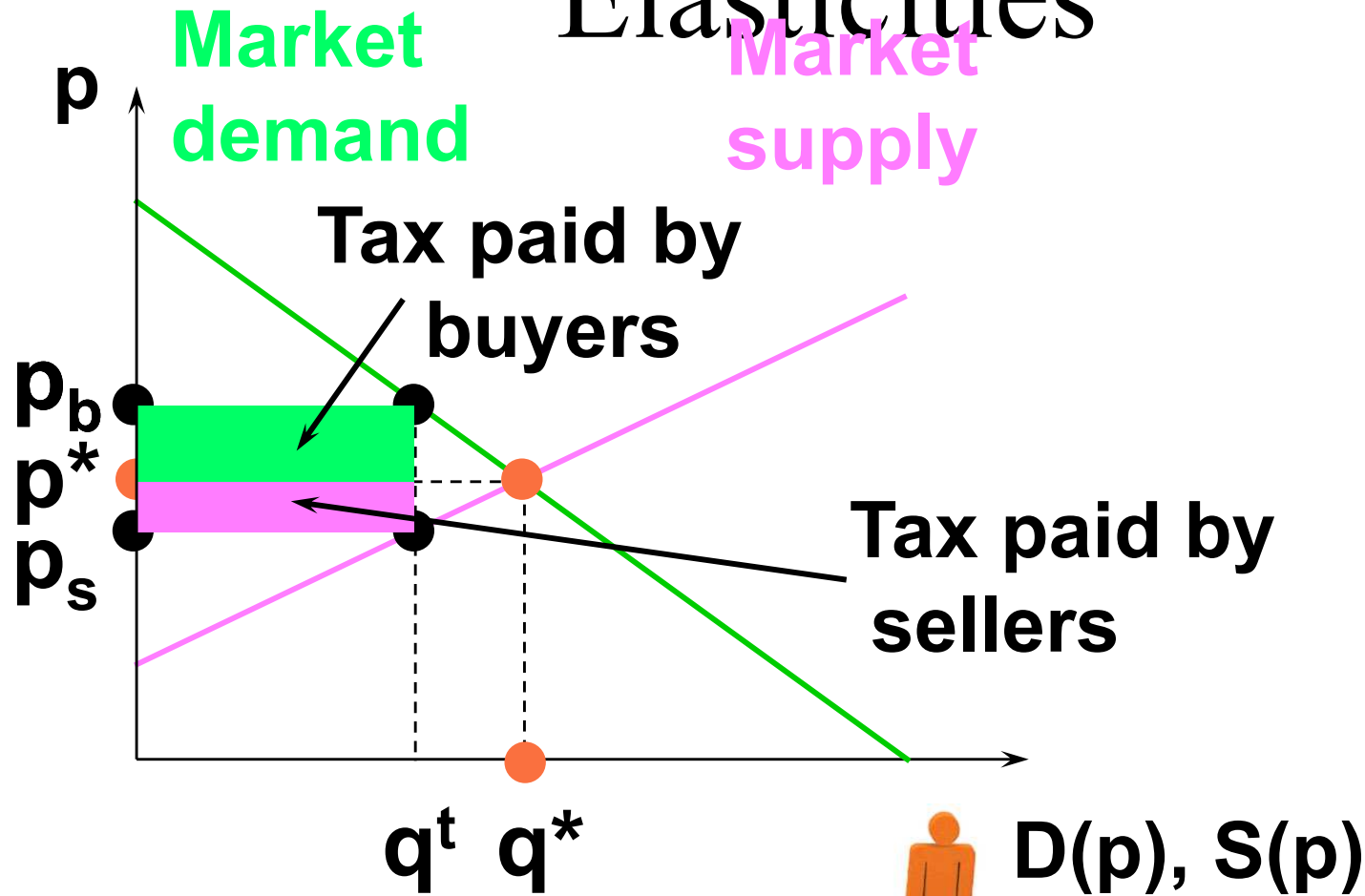
# Tax Incidence and Own-Price

## Elasticities



# Tax Incidence and Own-Price

## Elasticities



**Tax incidence** =  $\frac{p_b - p^*}{p^* - p_s}$

# Tax Incidence and Own-Price Elasticities

$$\text{Tax incidence} = \frac{p_b - p^*}{p^* - p_s}$$

$$p_b - p^* \approx \frac{\Delta q \times p^*}{\varepsilon_D \times q^*}$$

$$p_s - p^* \approx \frac{\Delta q \times p^*}{\varepsilon_S \times q^*}$$



# Tax Incidence and Own-Price Elasticities

$$\text{Tax incidence} = \frac{p_b - p^*}{p^* - p_s}$$

$$p_b - p^* \approx \frac{\Delta q \times p^*}{\epsilon_D \times q^*}$$

$$p_s - p^* \approx \frac{\Delta q \times p^*}{\epsilon_S \times q^*}$$

So

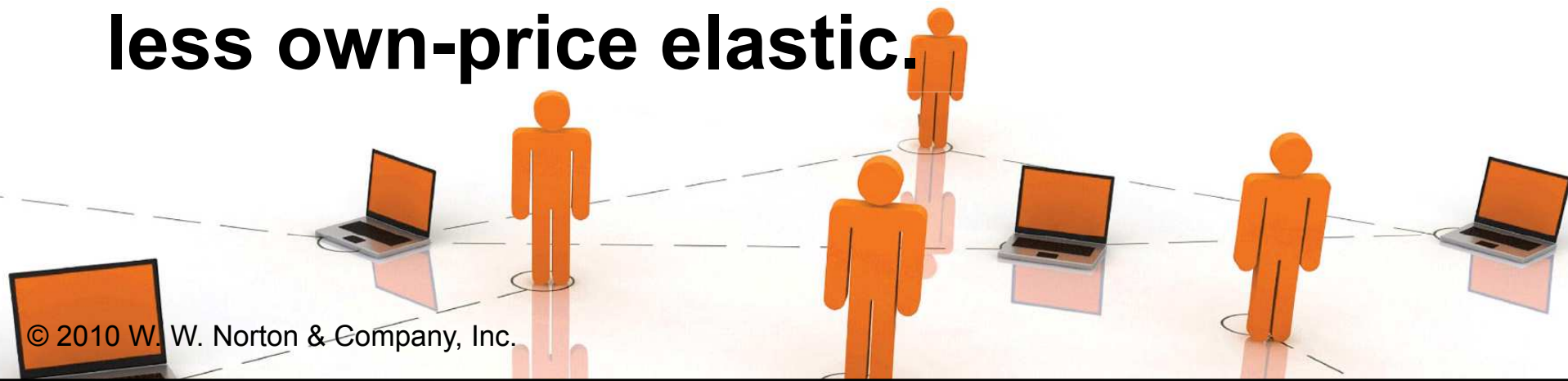
$$\frac{p_b - p^*}{p^* - p_s} \approx \frac{\epsilon_S}{\epsilon_D}$$



# Tax Incidence and Own-Price Elasticities

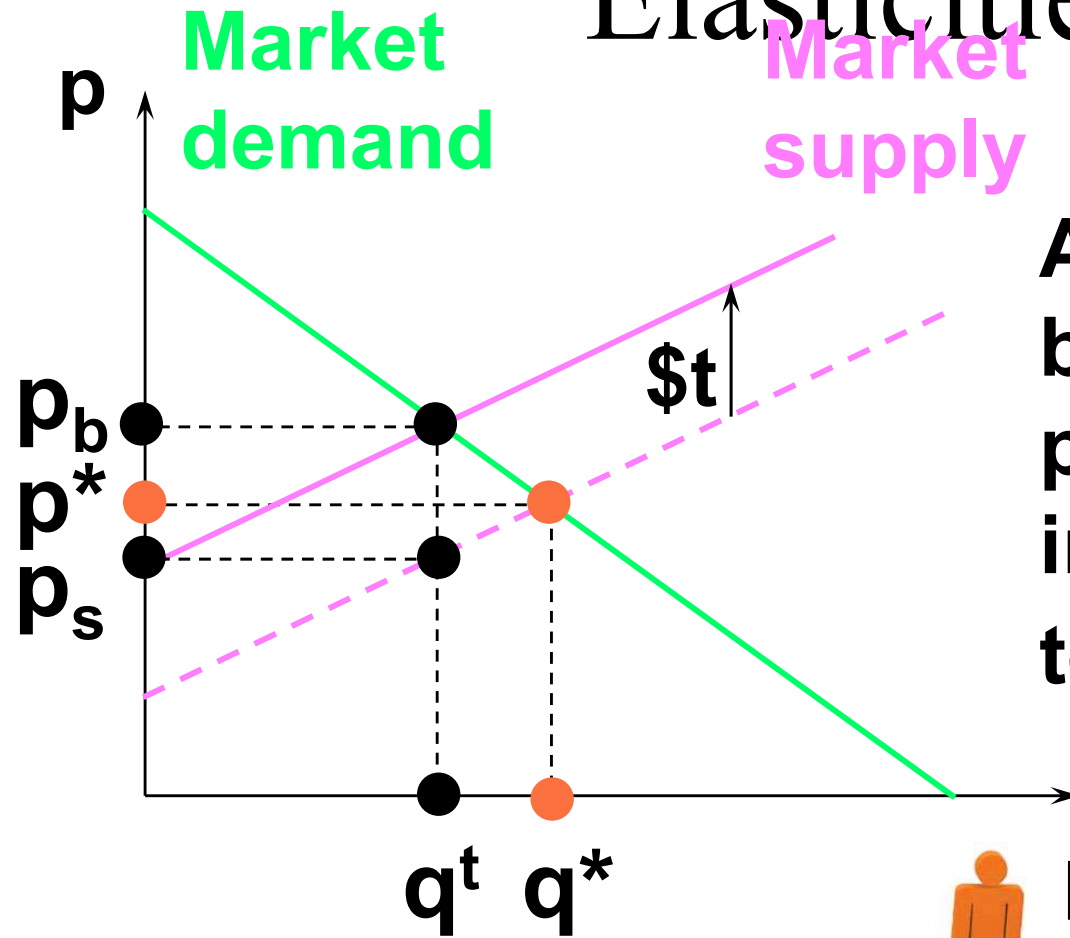
**Tax incidence is** 
$$\frac{p_b - p^*}{p^* - p_s} \approx -\frac{\epsilon_s}{\epsilon_D}.$$

**The fraction of a \$t quantity tax paid by buyers rises as supply becomes more own-price elastic or as demand becomes less own-price elastic.**



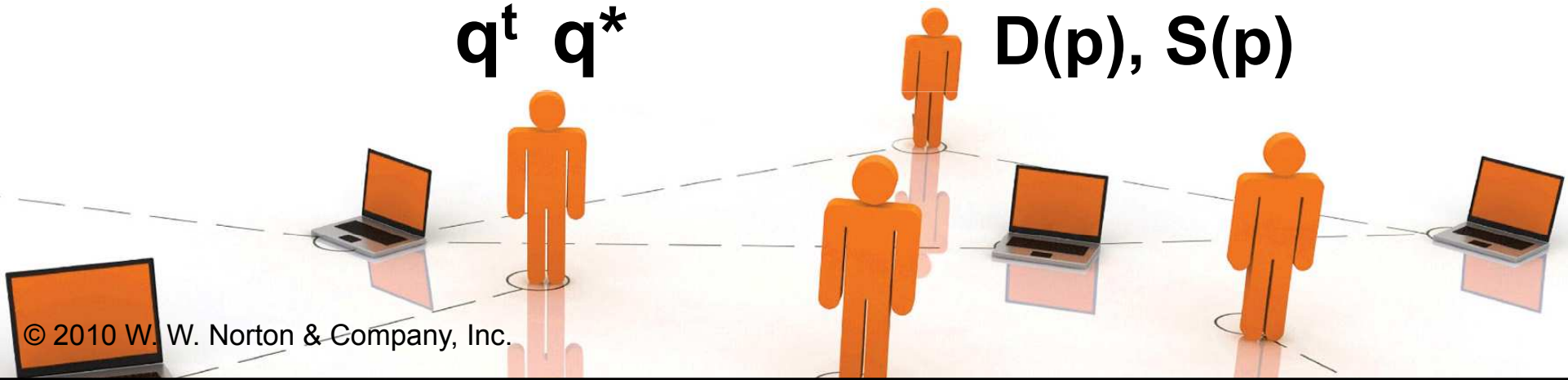
# Tax Incidence and Own-Price

## Elasticities



**As market demand becomes less own-price elastic, tax incidence shifts more to the buyers.**

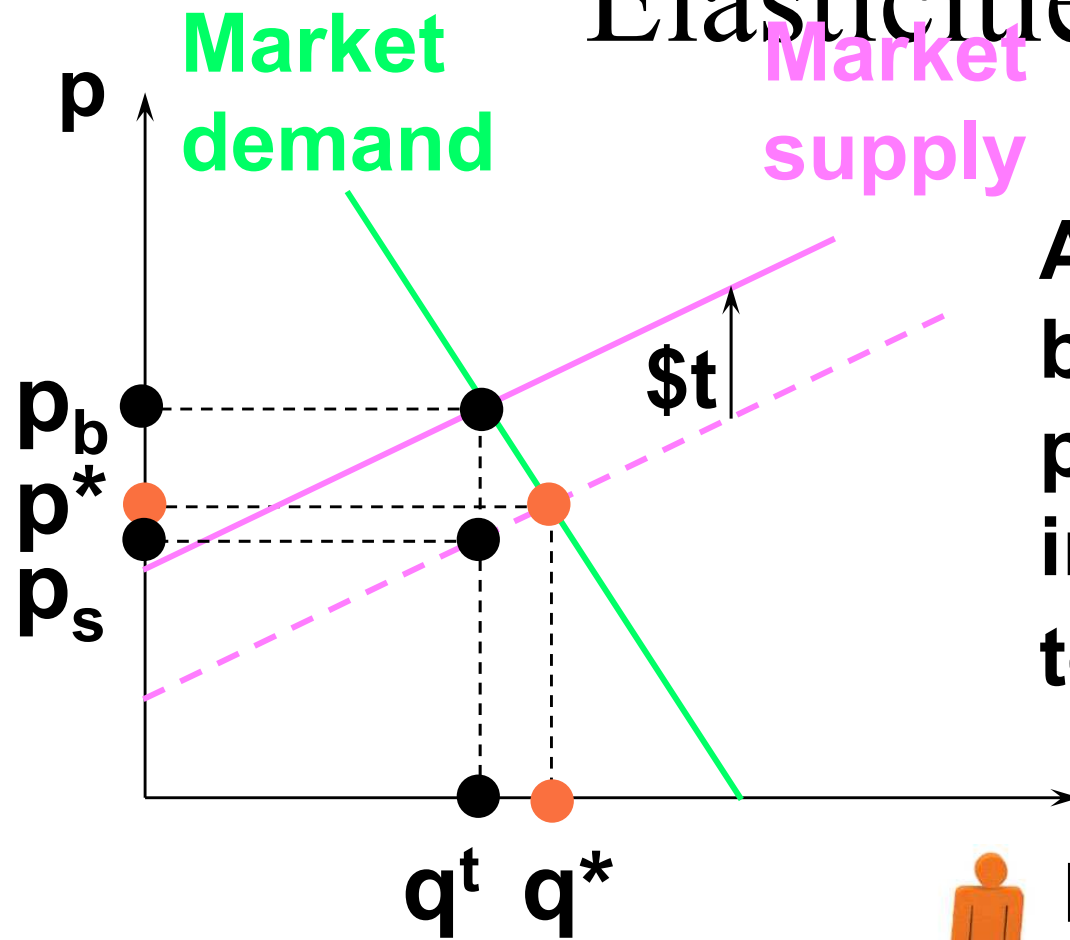
$D(p), S(p)$



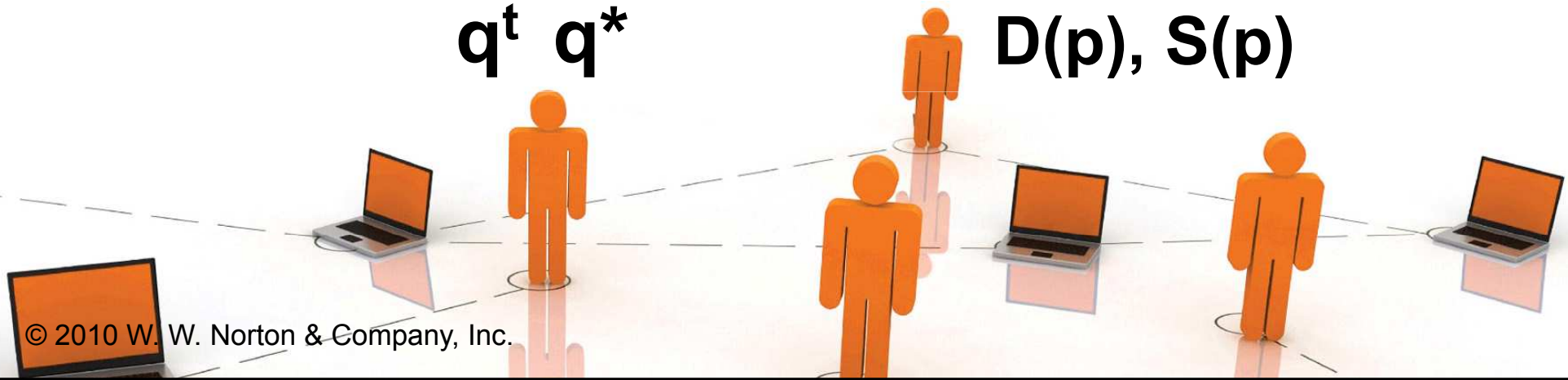


# Tax Incidence and Own-Price

## Elasticities

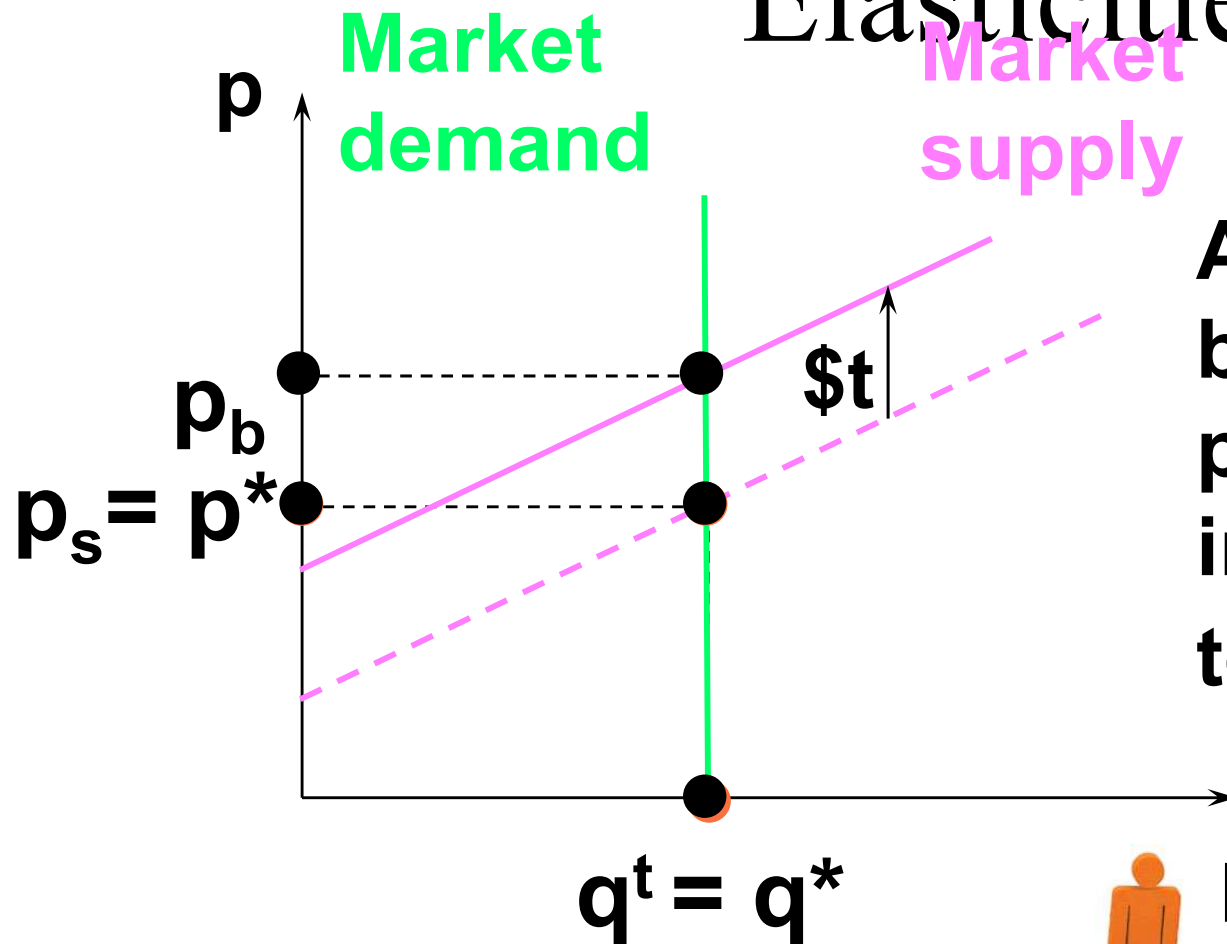


**As market demand becomes less own-price elastic, tax incidence shifts more to the buyers.**



# Tax Incidence and Own-Price

## Elasticities



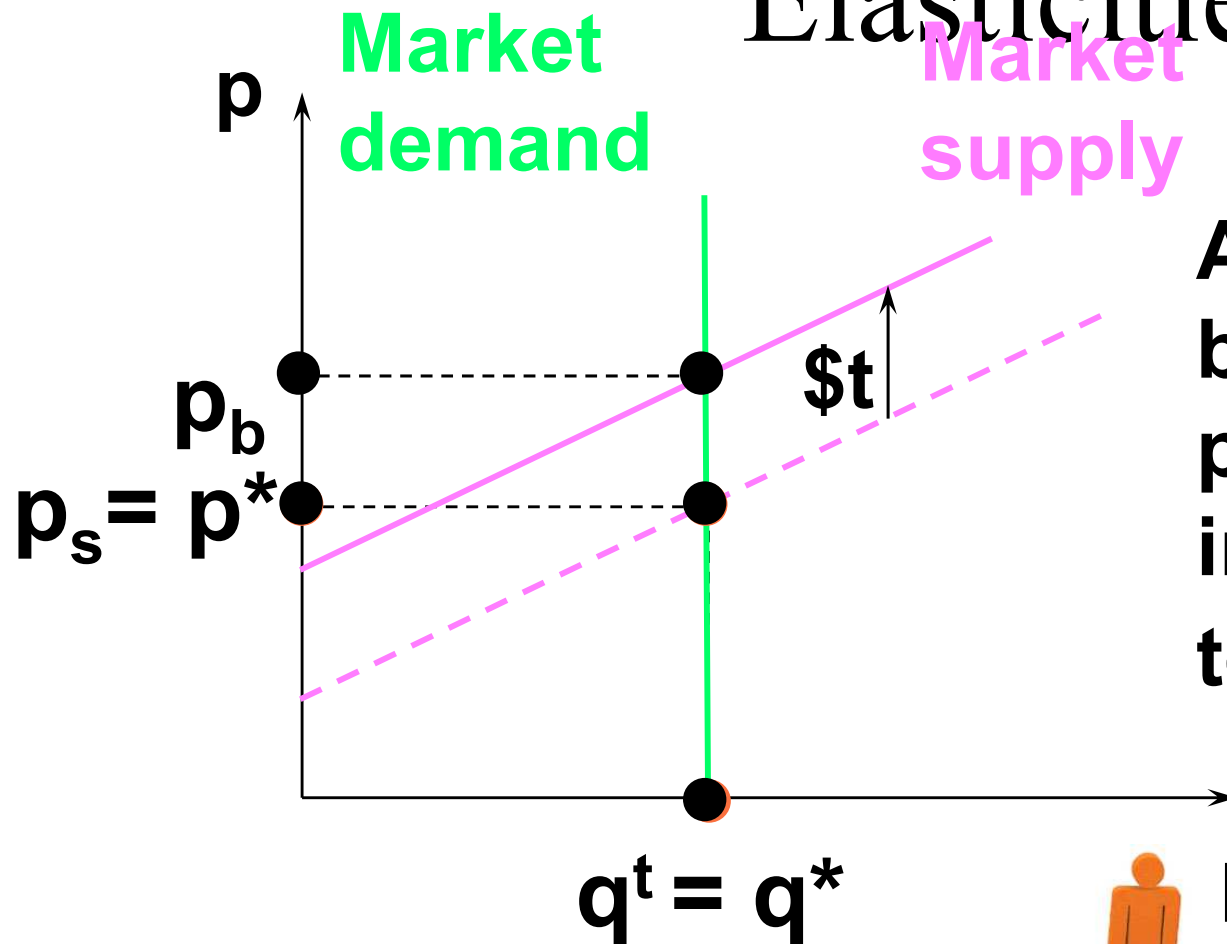
**As market demand becomes less own-price elastic, tax incidence shifts more to the buyers.**

$D(p), S(p)$



# Tax Incidence and Own-Price

## Elasticities



As market demand becomes less own-price elastic, tax incidence shifts more to the buyers.

When  $\varepsilon_D = 0$ , buyers pay the entire tax, even though it is levied on the sellers.

# Tax Incidence and Own-Price Elasticities

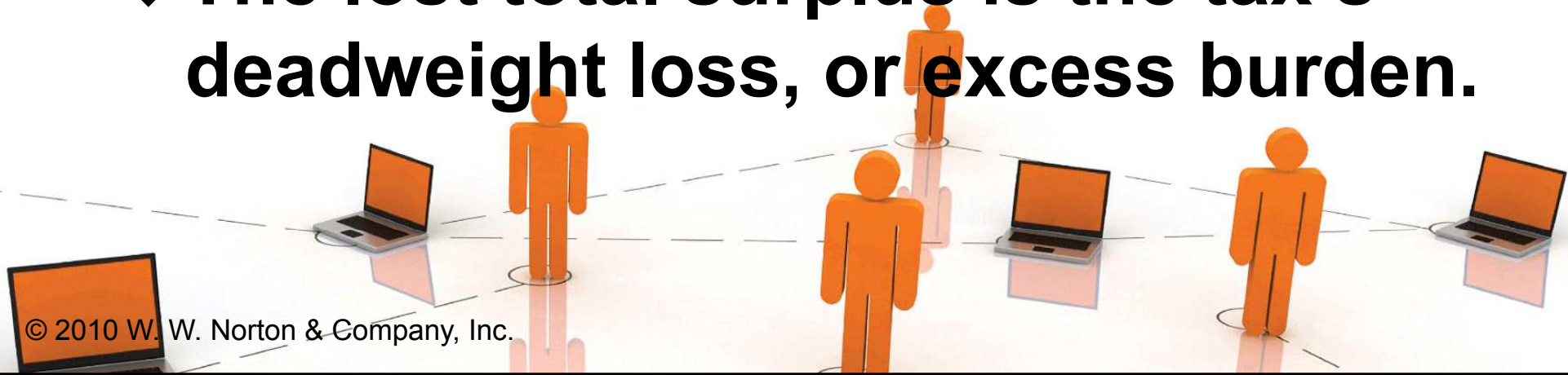
**Tax incidence is** 
$$\frac{p_b - p^*}{p^* - p_s} \approx - \frac{\epsilon_s}{\epsilon_D}.$$

**Similarly, the fraction of a \$t quantity tax paid by sellers rises as supply becomes less own-price elastic or as demand becomes more own-price elastic.**



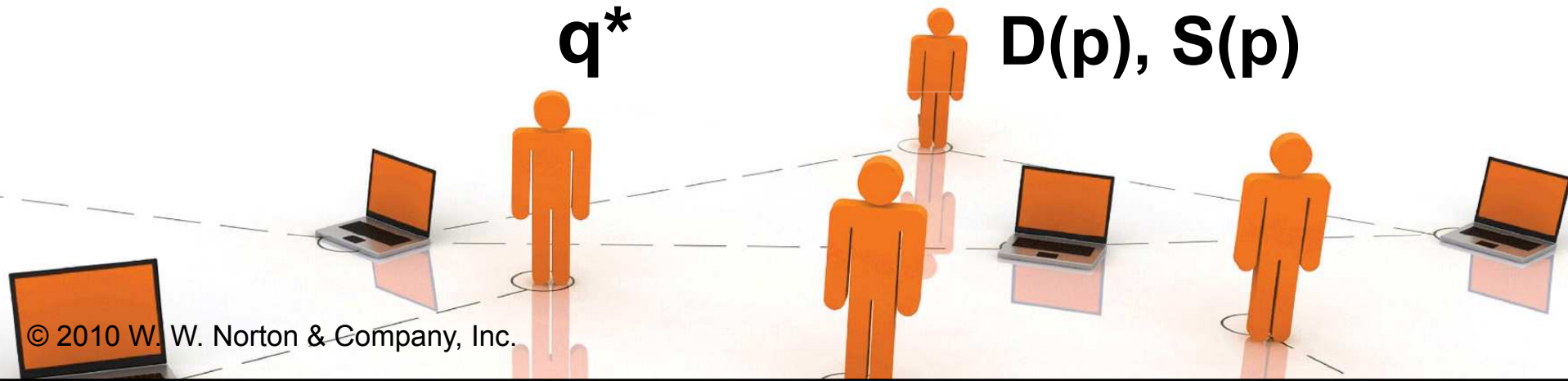
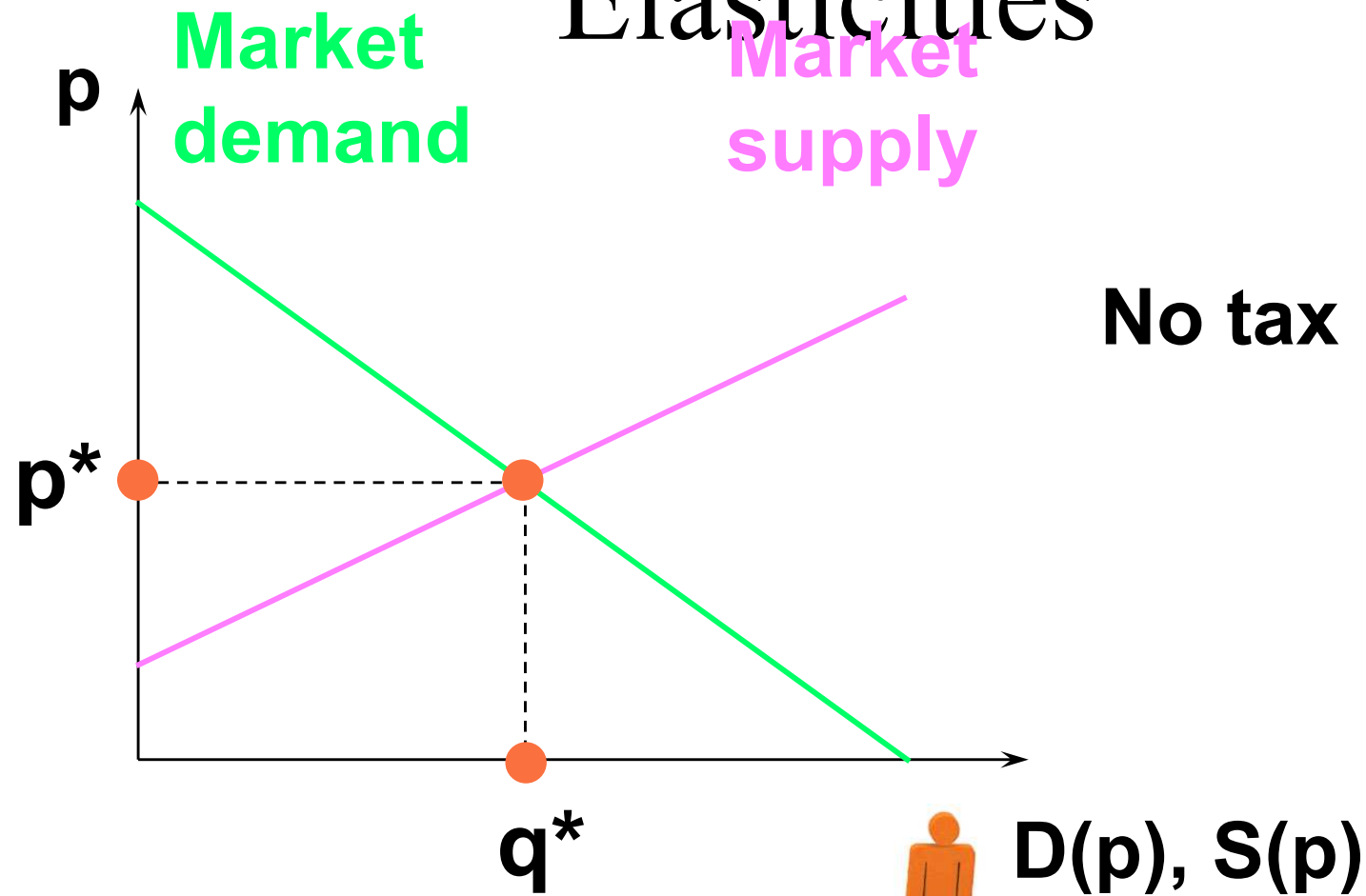
# Deadweight Loss and Own-Price Elasticities

- ◆ **A quantity tax imposed on a competitive market reduces the quantity traded and so reduces gains-to-trade (*i.e.* the sum of Consumers' and Producers' Surpluses).**
- ◆ **The lost total surplus is the tax's deadweight loss, or excess burden.**



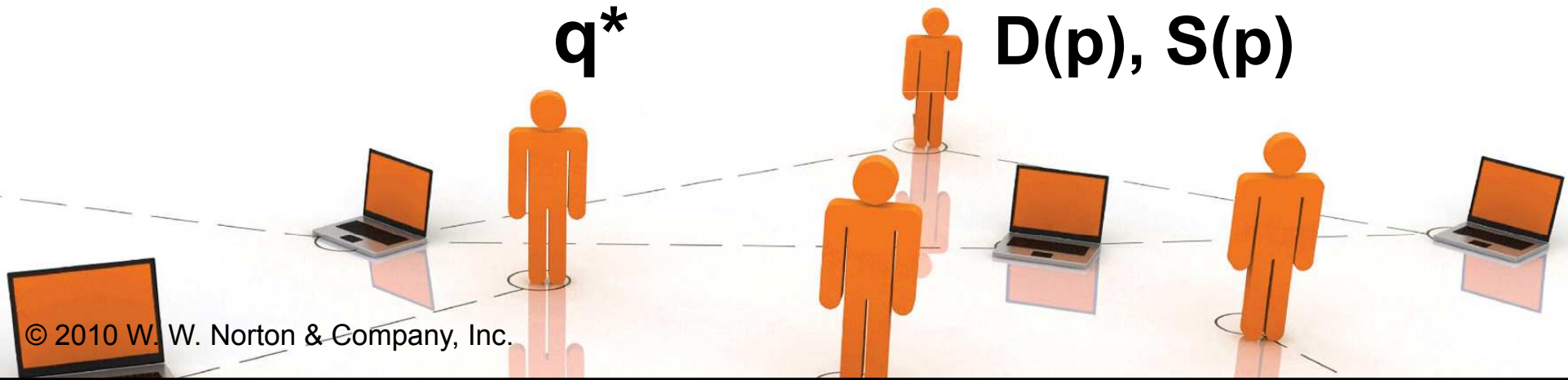
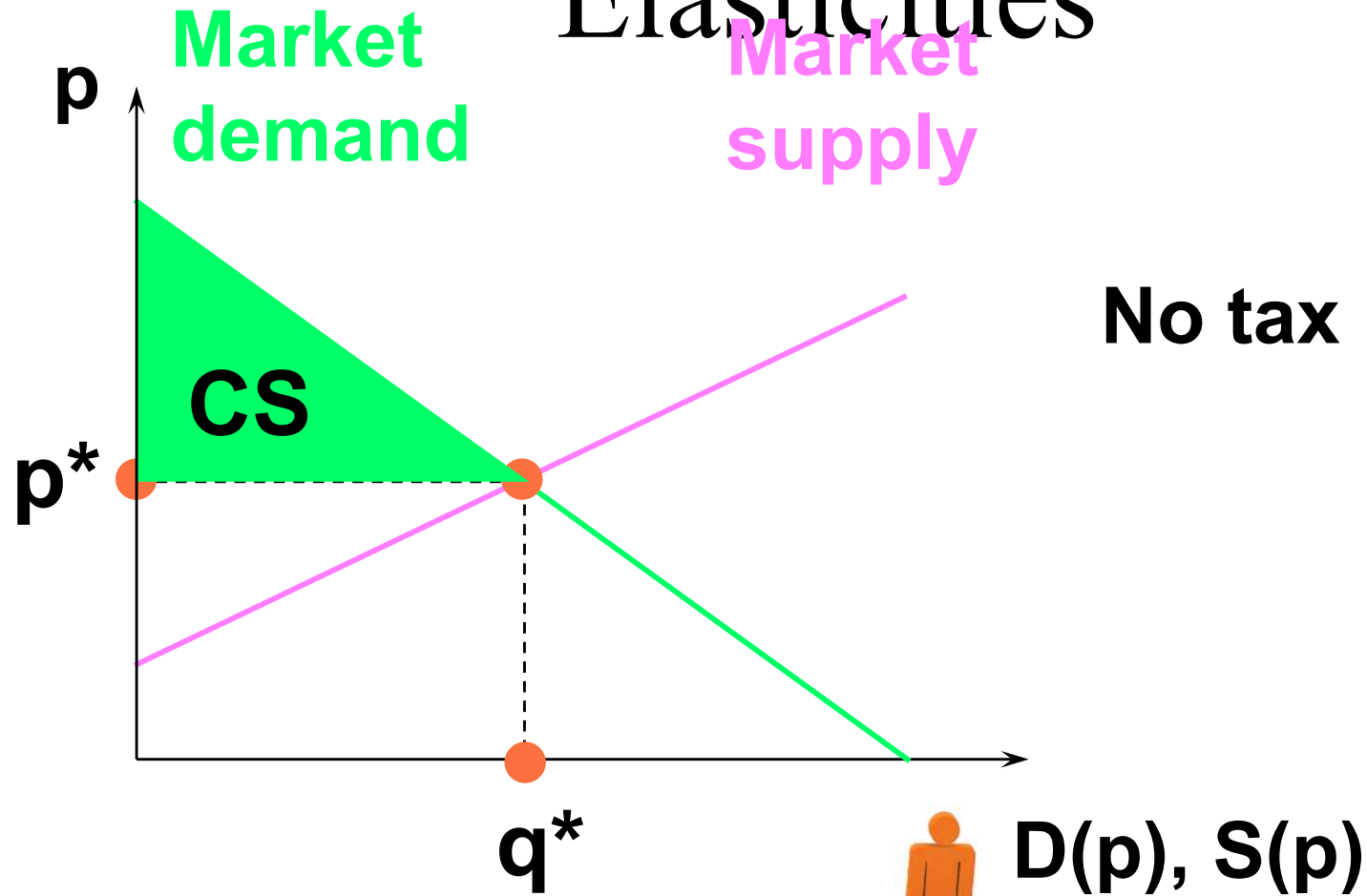
# Deadweight Loss and Own-Price

## Elasticities



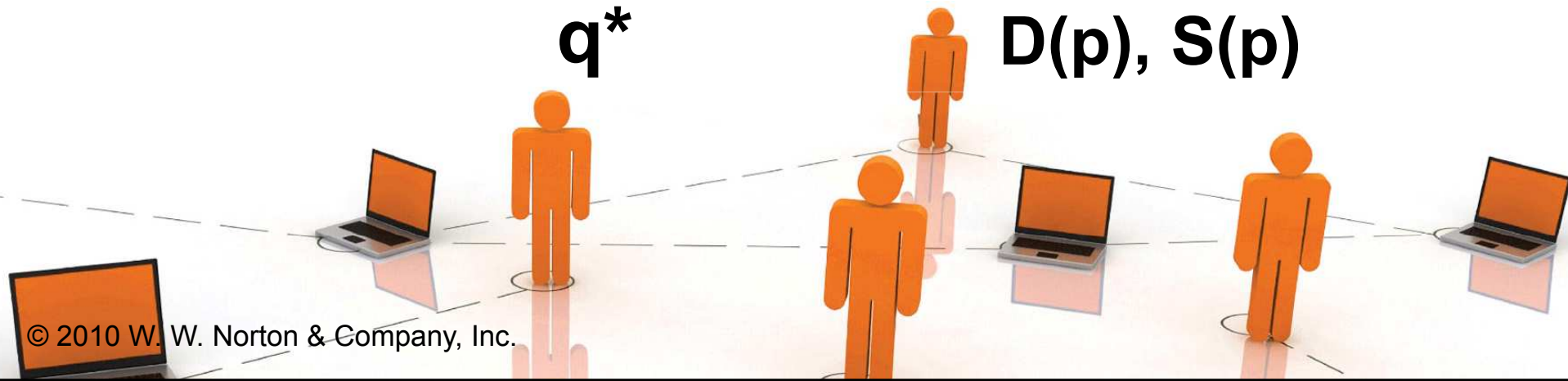
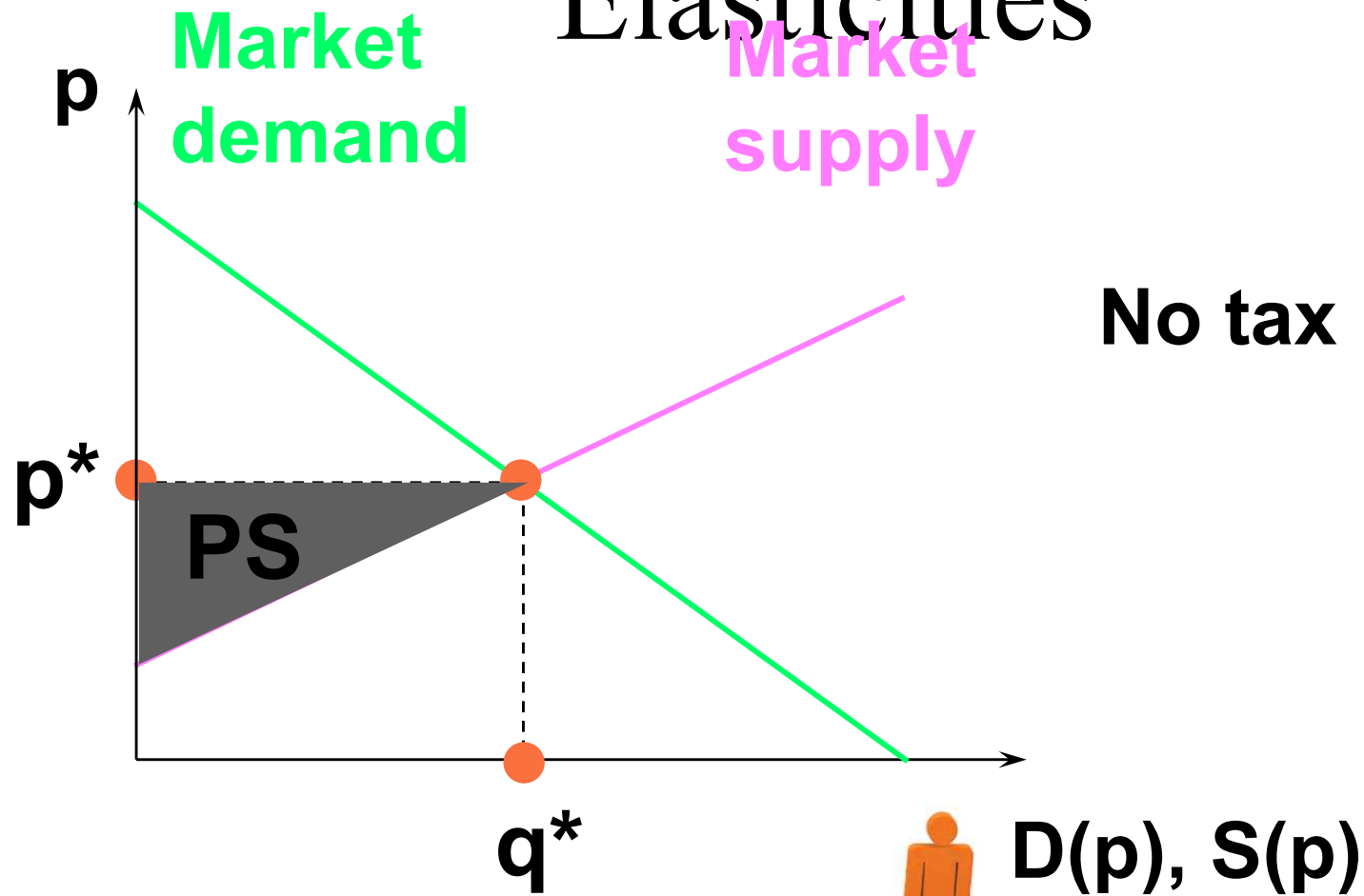
# Deadweight Loss and Own-Price

## Elasticities



# Deadweight Loss and Own-Price

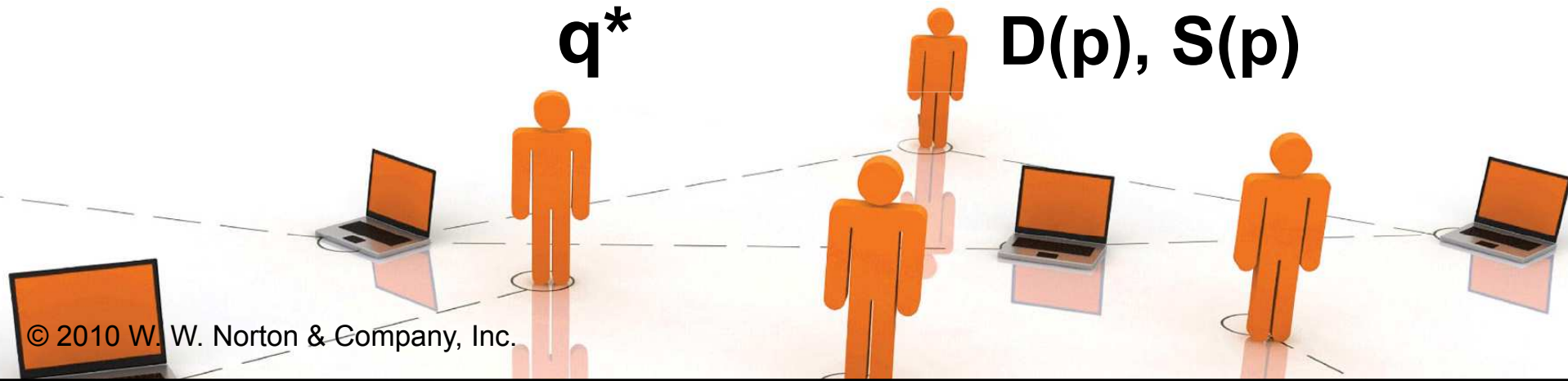
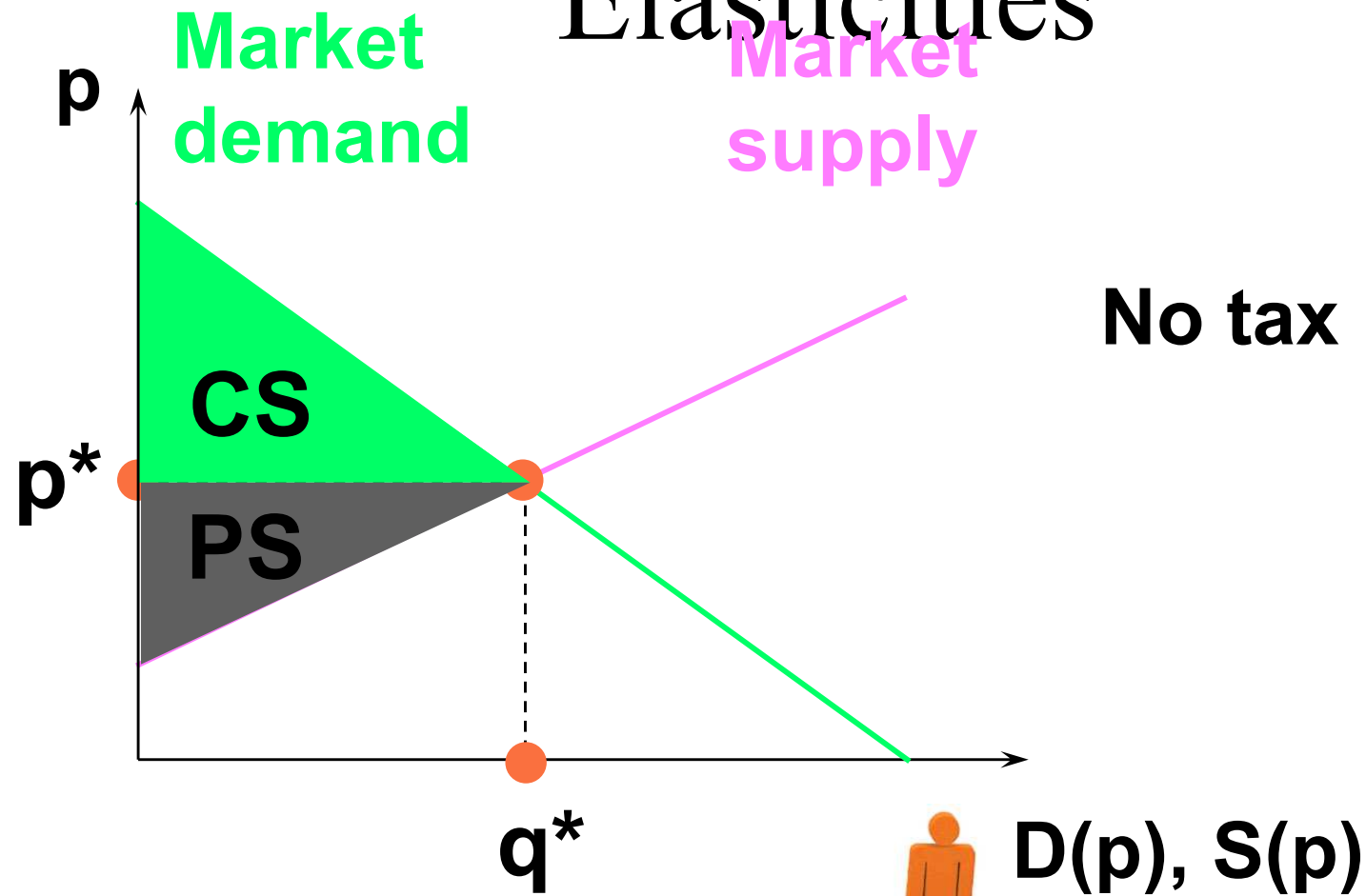
## Elasticities





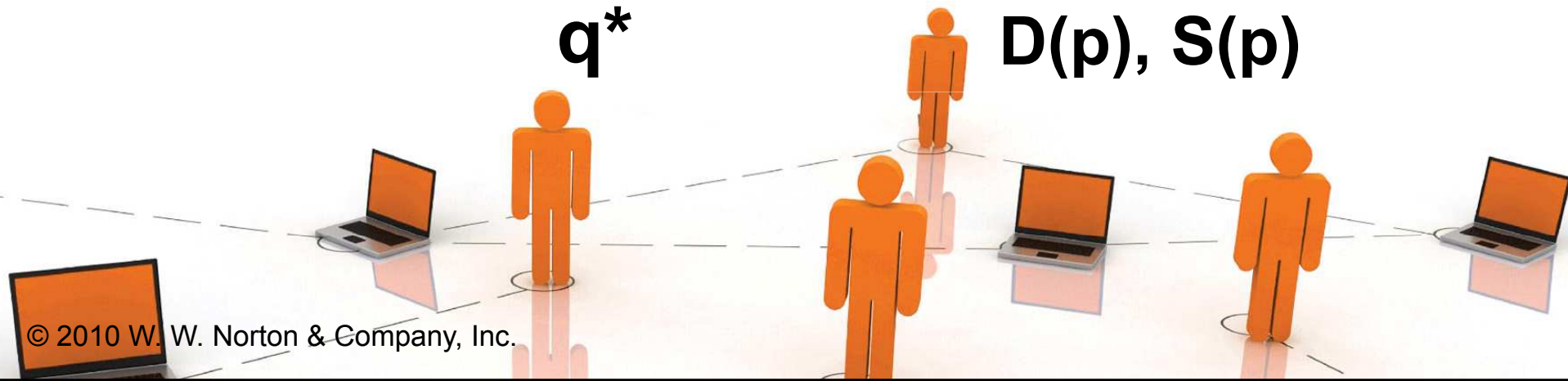
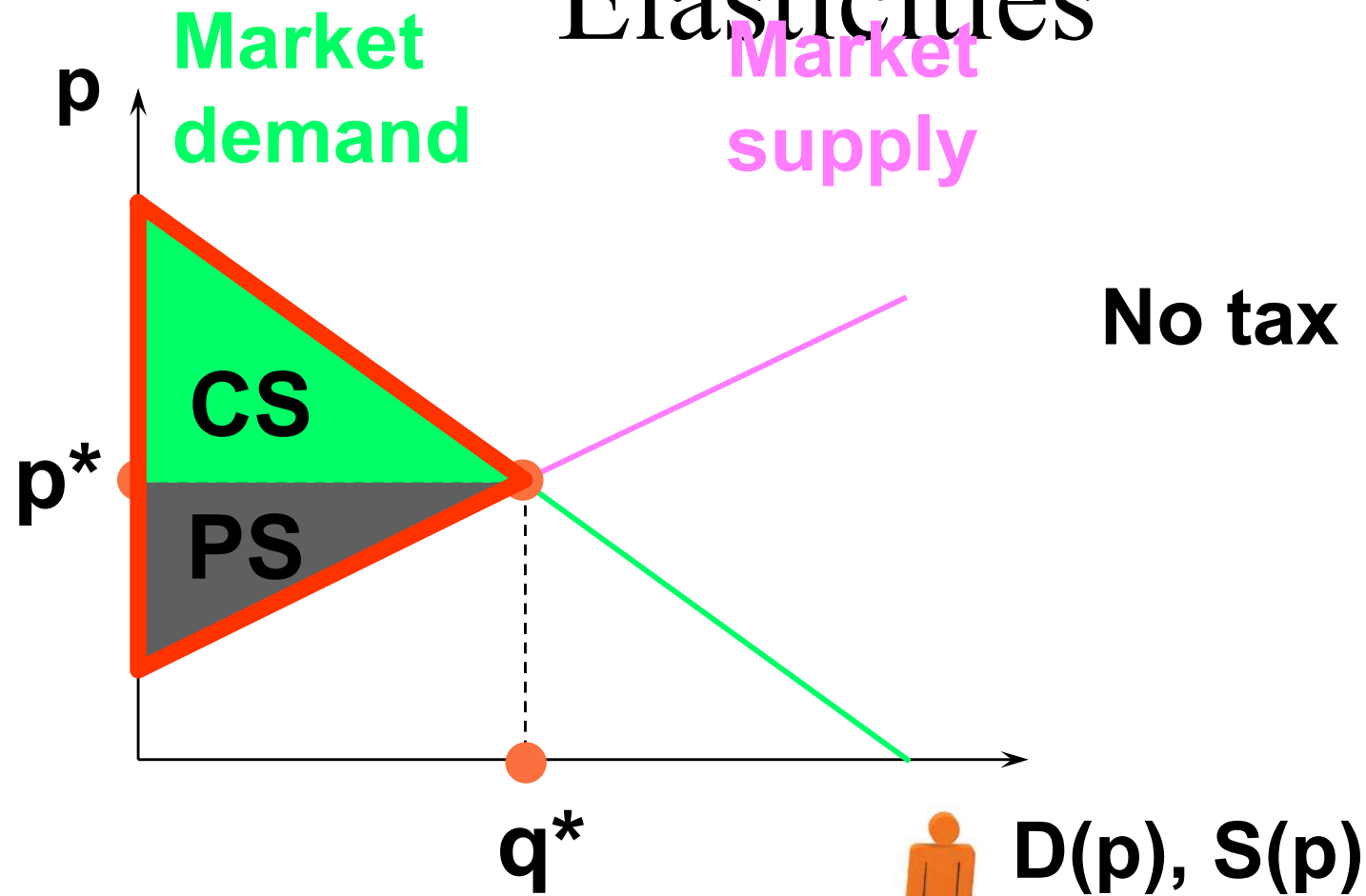
# Deadweight Loss and Own-Price

## Elasticities



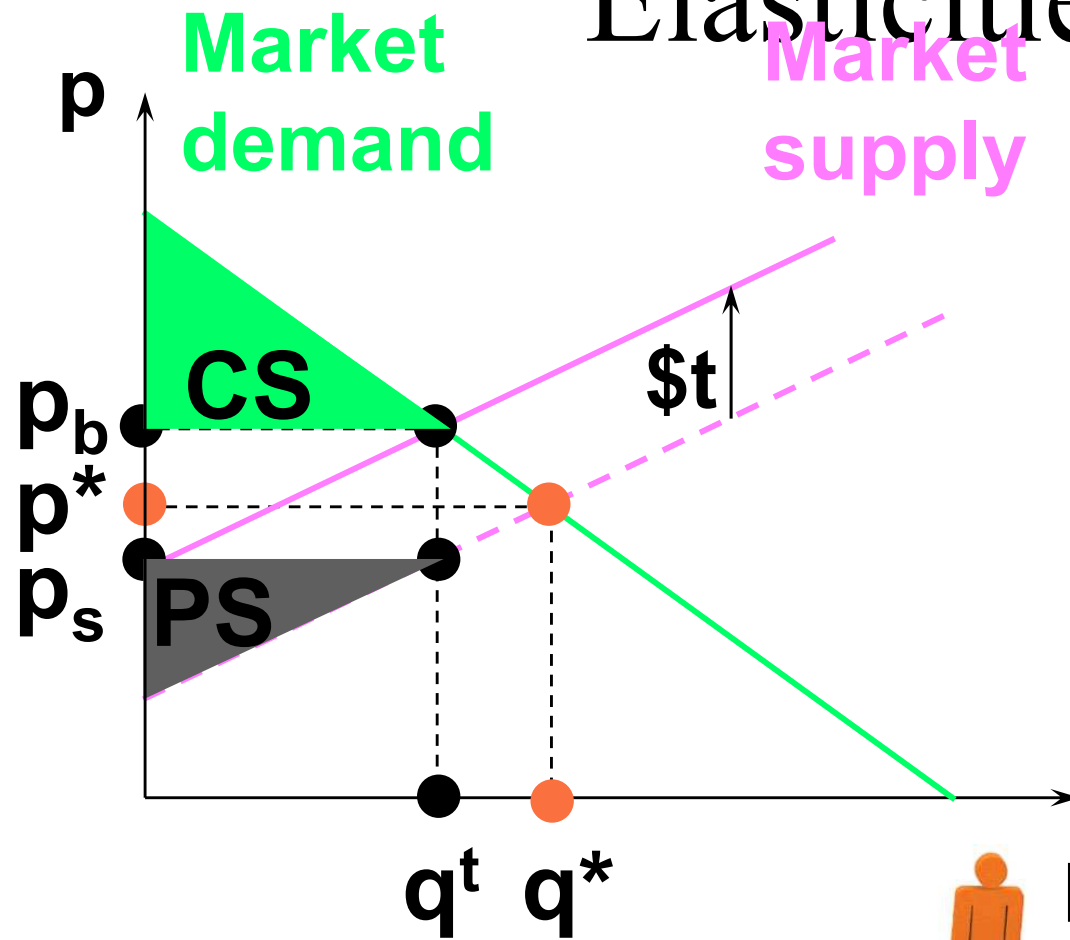
# Deadweight Loss and Own-Price

## Elasticities

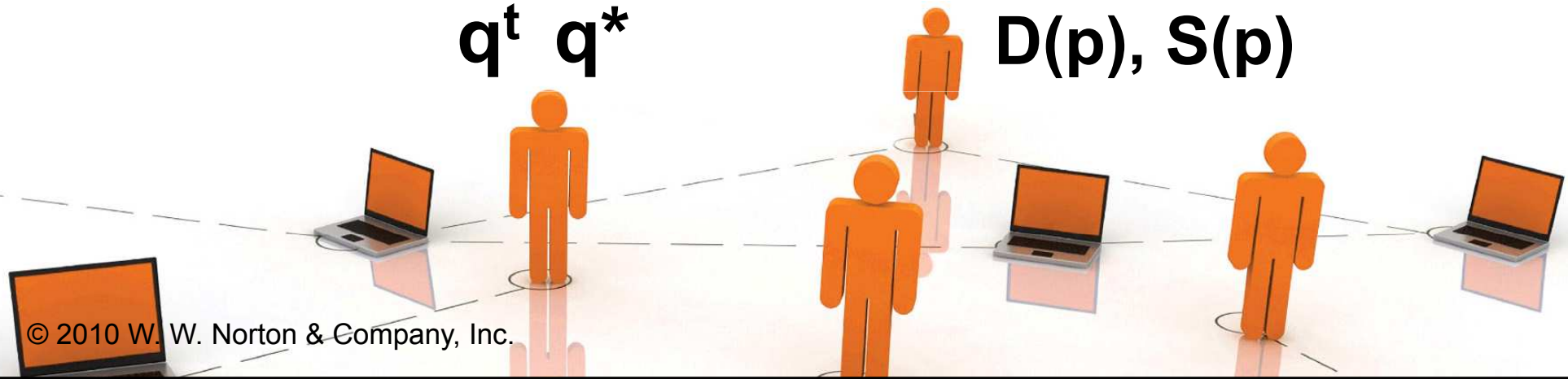


# Deadweight Loss and Own-Price

## Elasticities

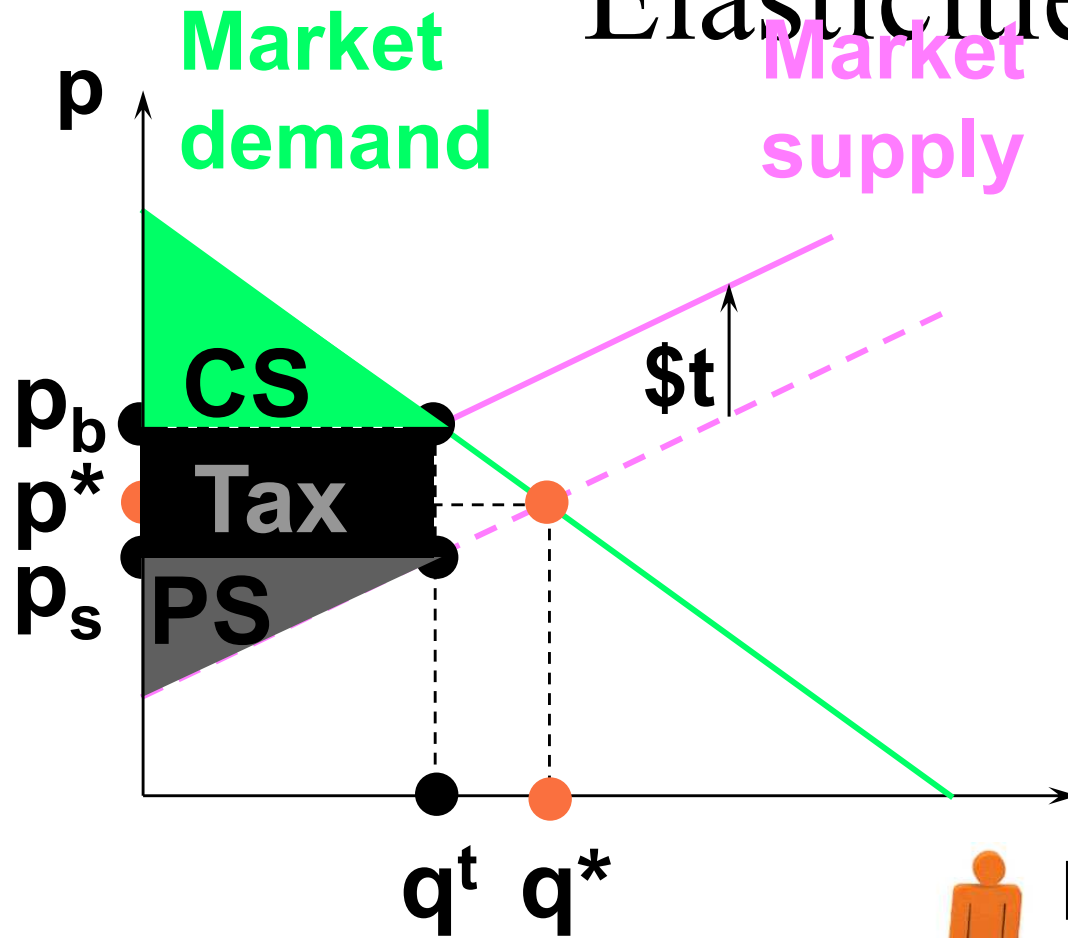


The tax reduces both CS and PS



# Deadweight Loss and Own-Price

## Elasticities

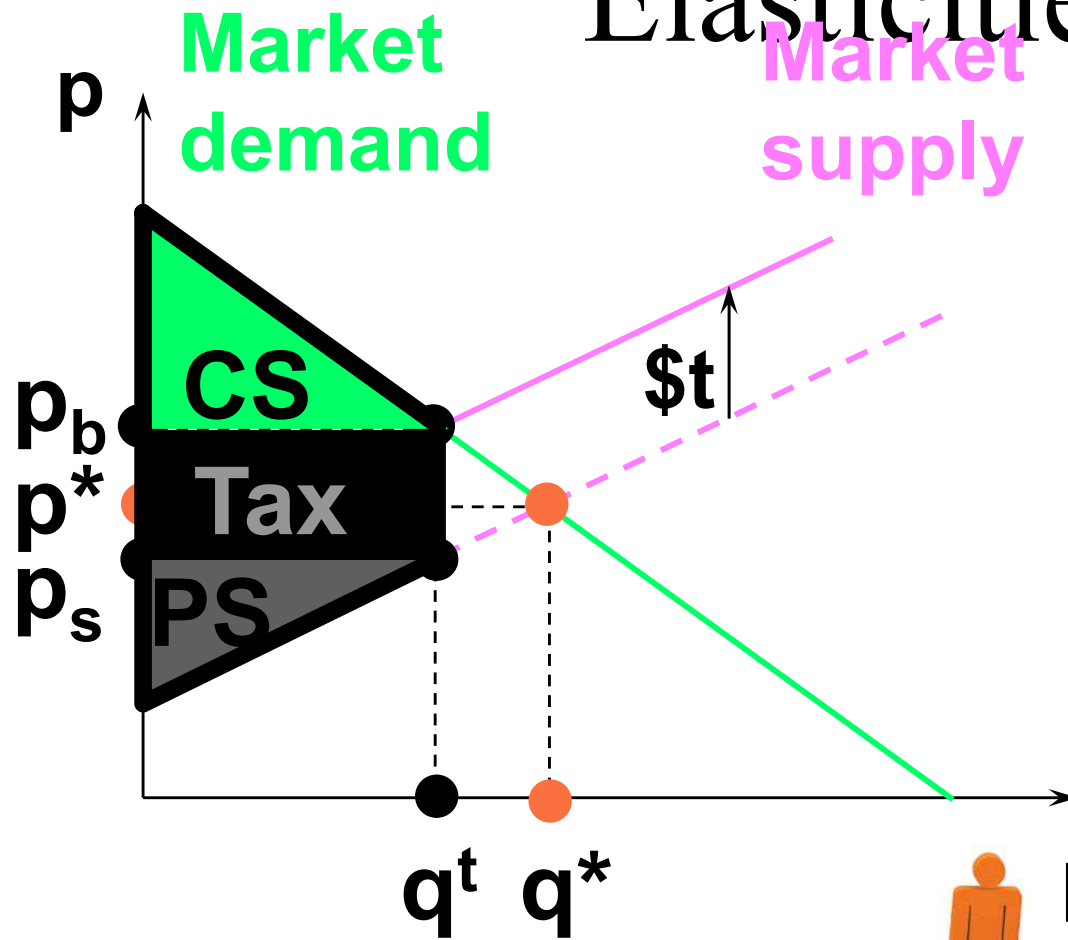


The tax reduces both CS and PS, transfers surplus to government



# Deadweight Loss and Own-Price

## Elasticities

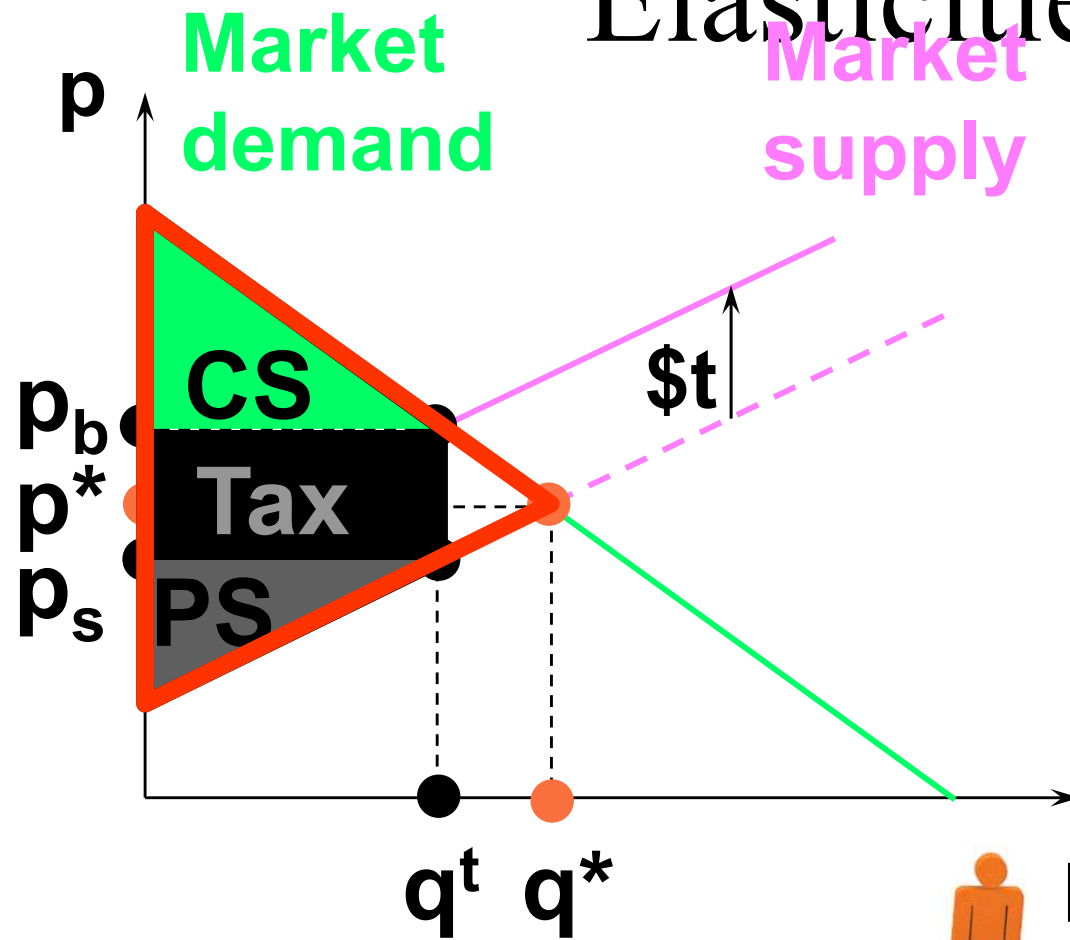


The tax reduces both CS and PS, transfers surplus to government

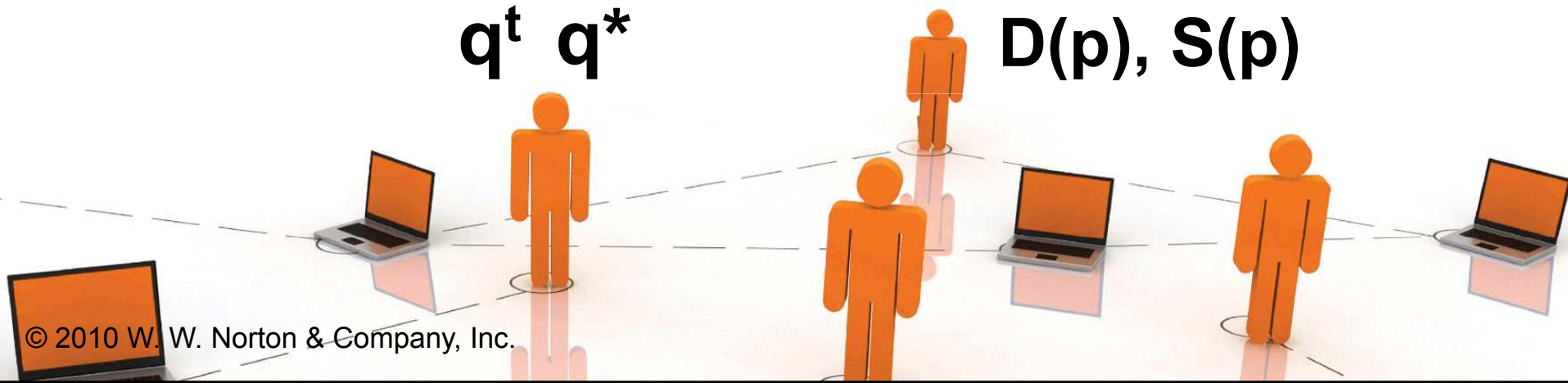


# Deadweight Loss and Own-Price

## Elasticities

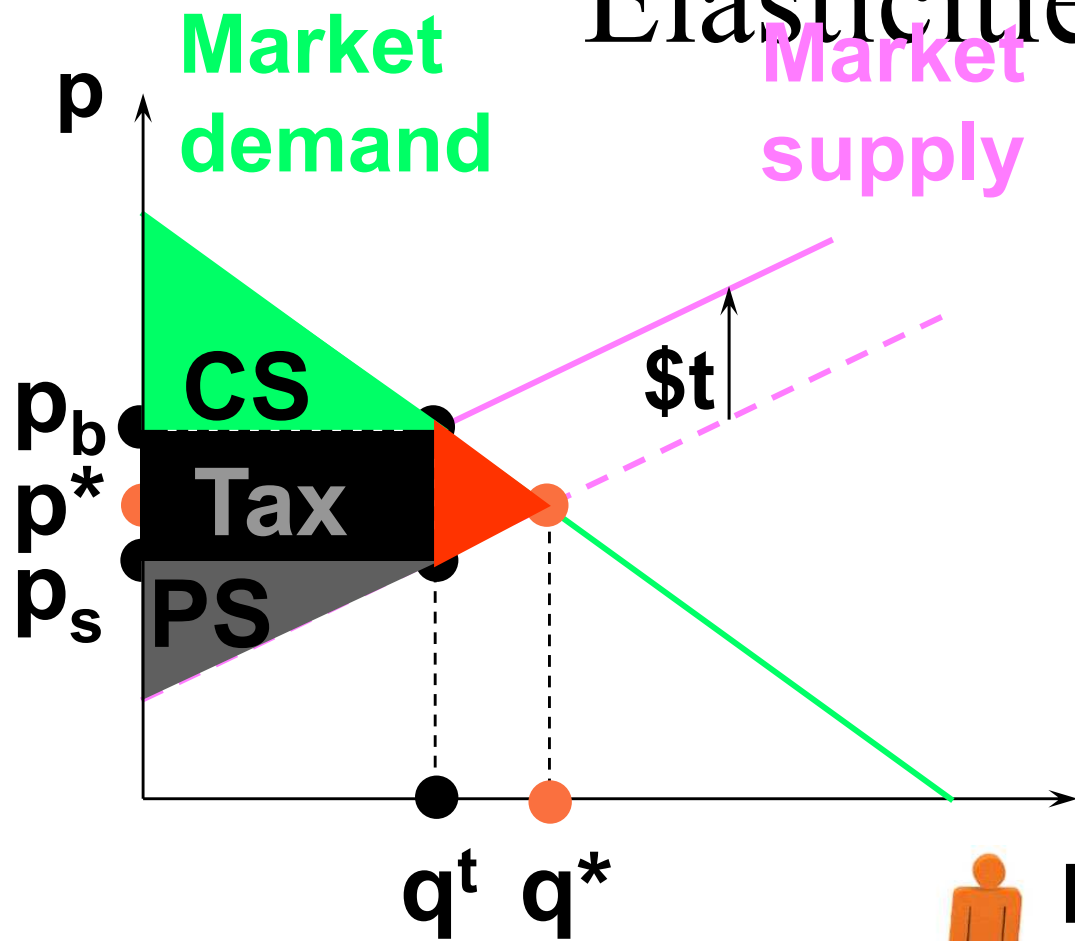


The tax reduces both CS and PS, transfers surplus to government



# Deadweight Loss and Own-Price

## Elasticities



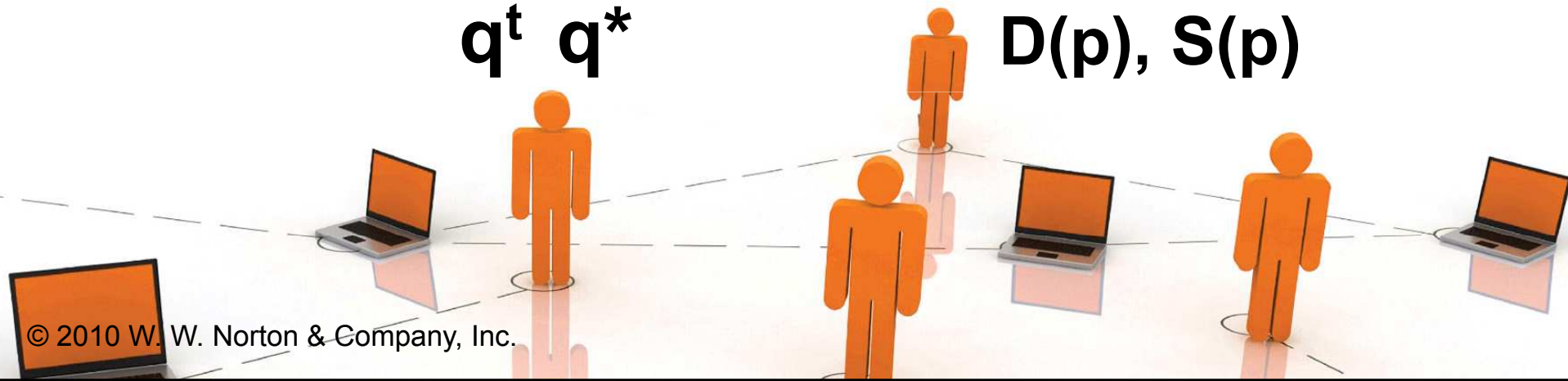
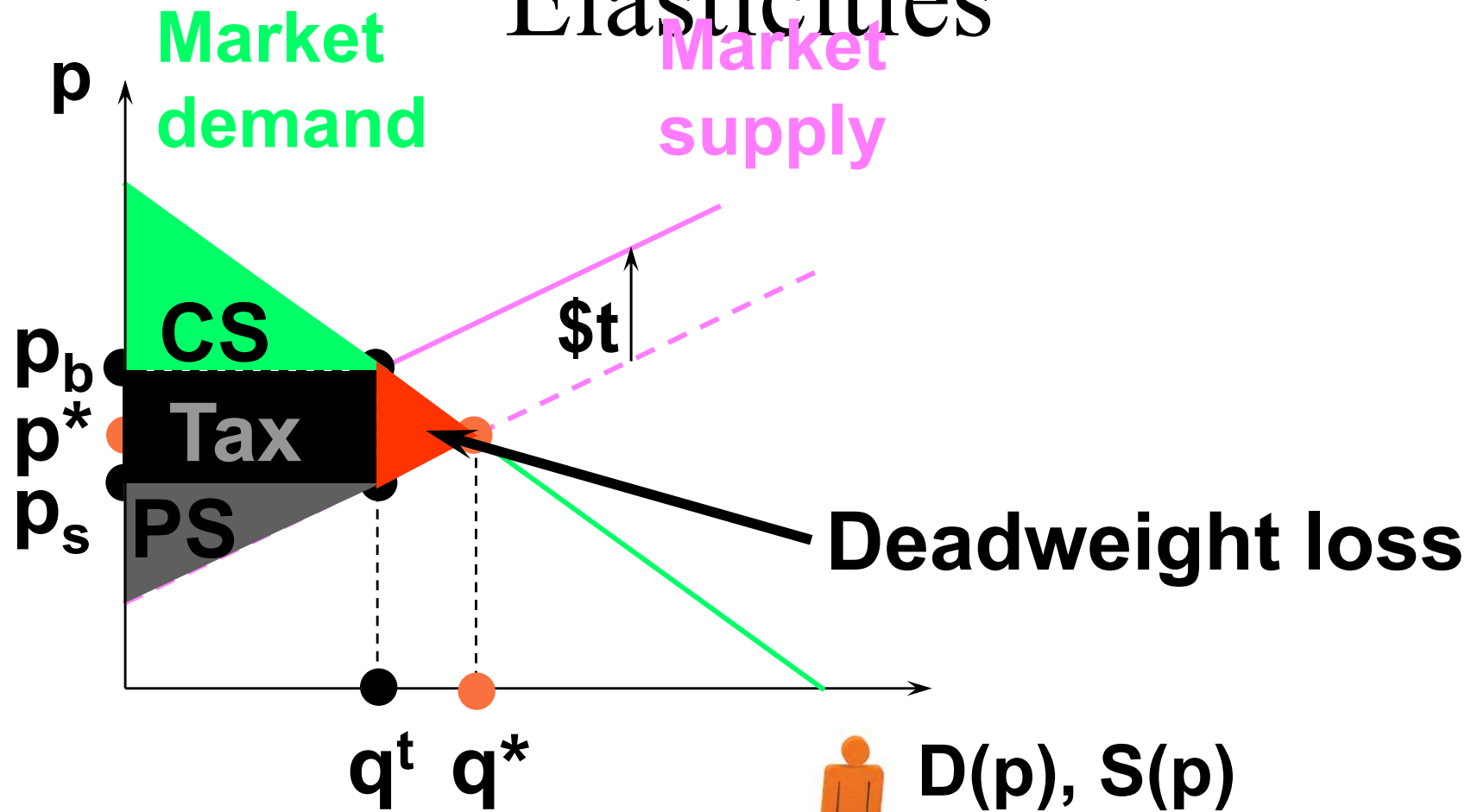
The tax reduces both CS and PS, transfers surplus to government, and lowers total surplus.

$D(p), S(p)$



# Deadweight Loss and Own-Price

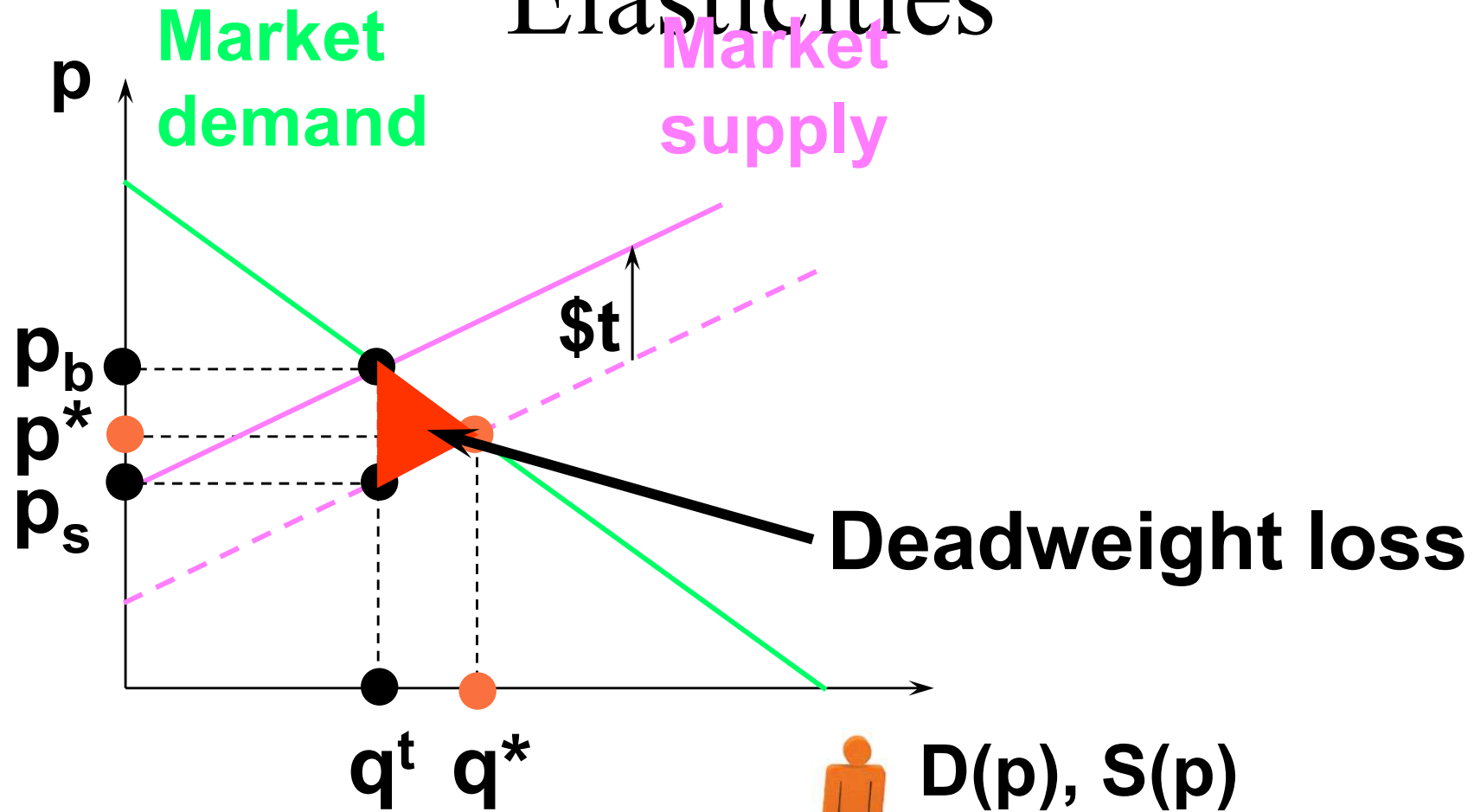
## Elasticities



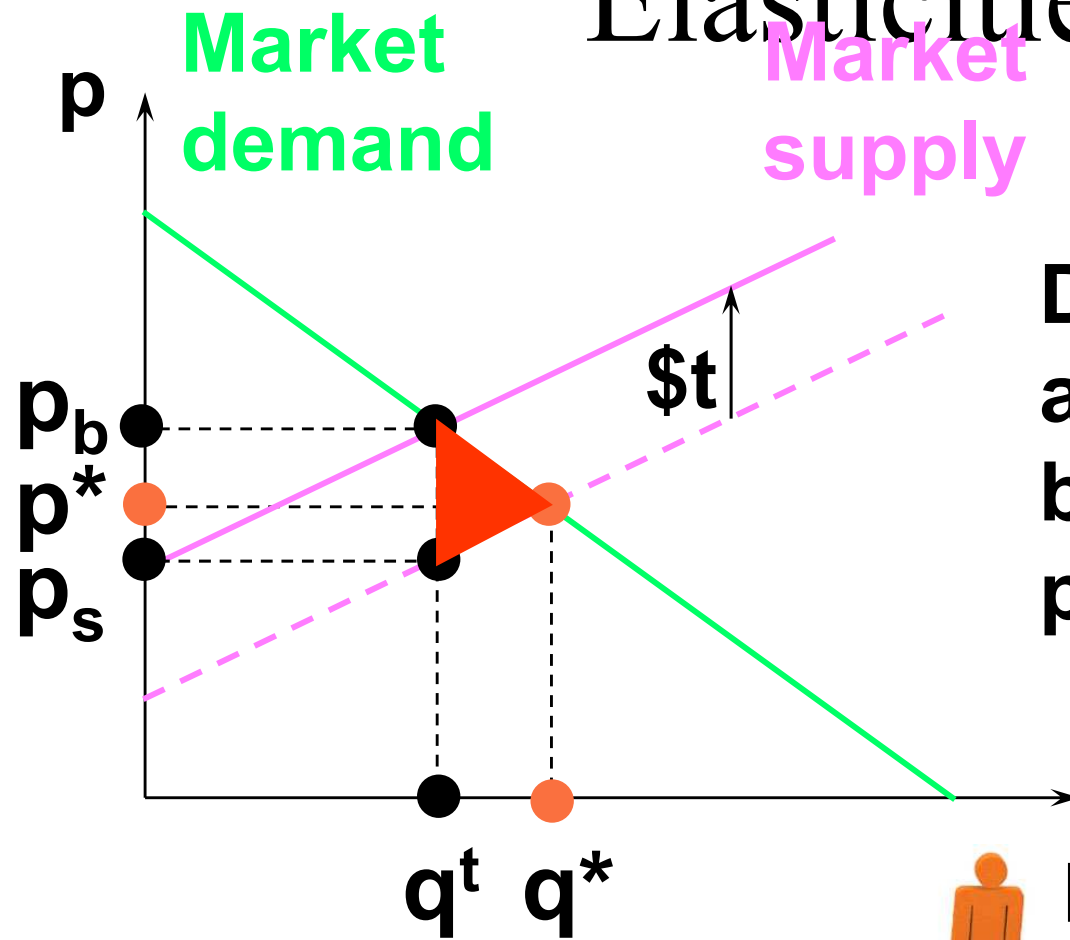


# Deadweight Loss and Own-Price

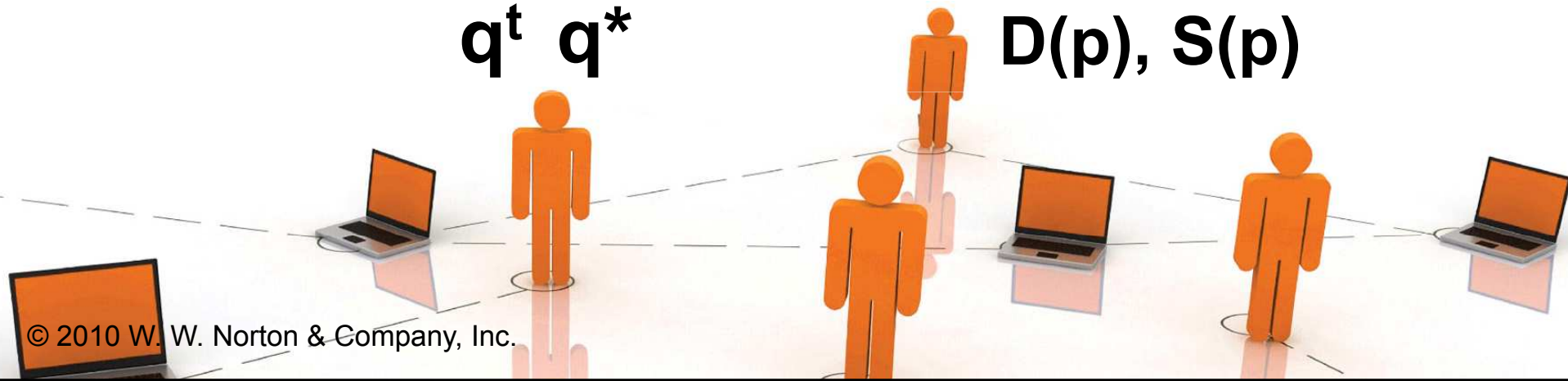
## Elasticities



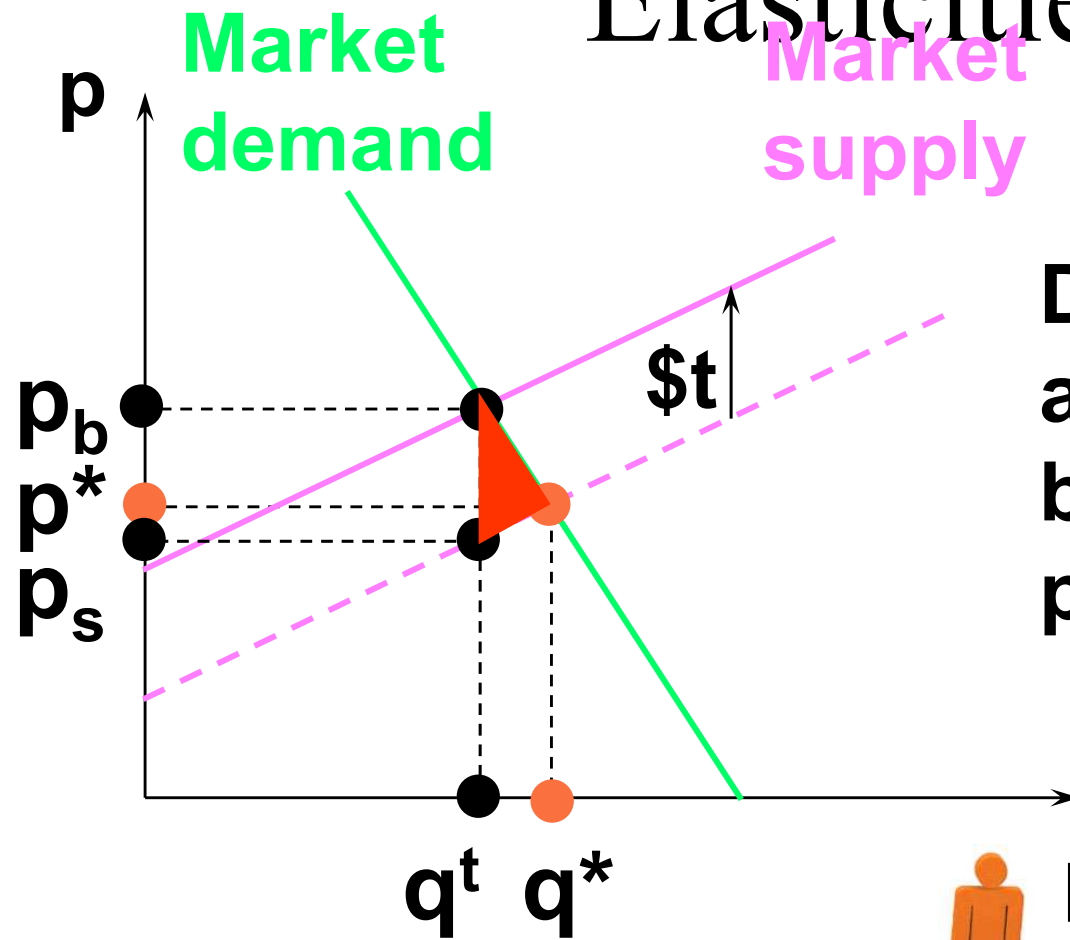
# Deadweight Loss and Own-Price Elasticities



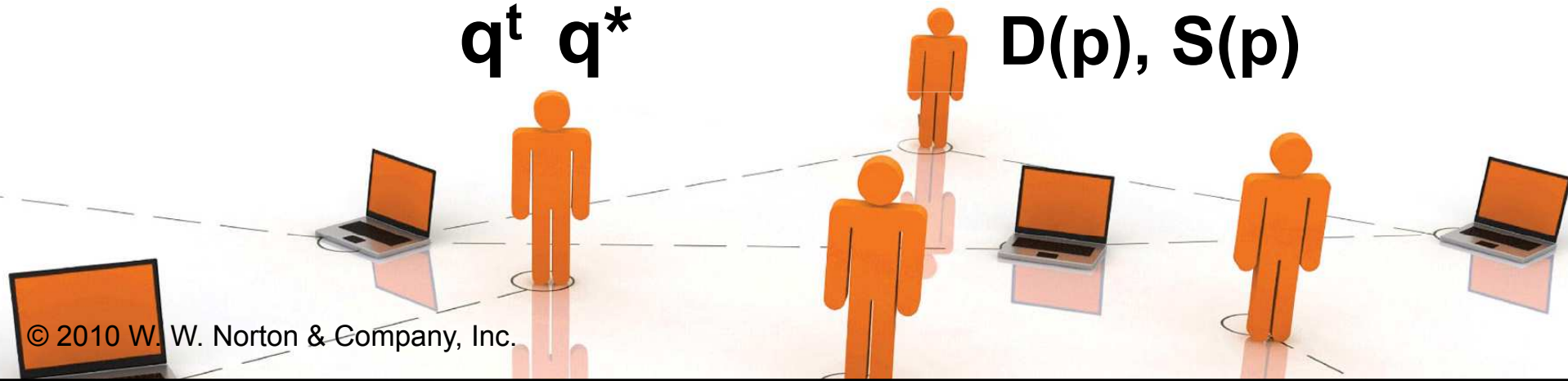
**Deadweight loss falls as market demand becomes less own-price elastic.**



# Deadweight Loss and Own-Price Elasticities

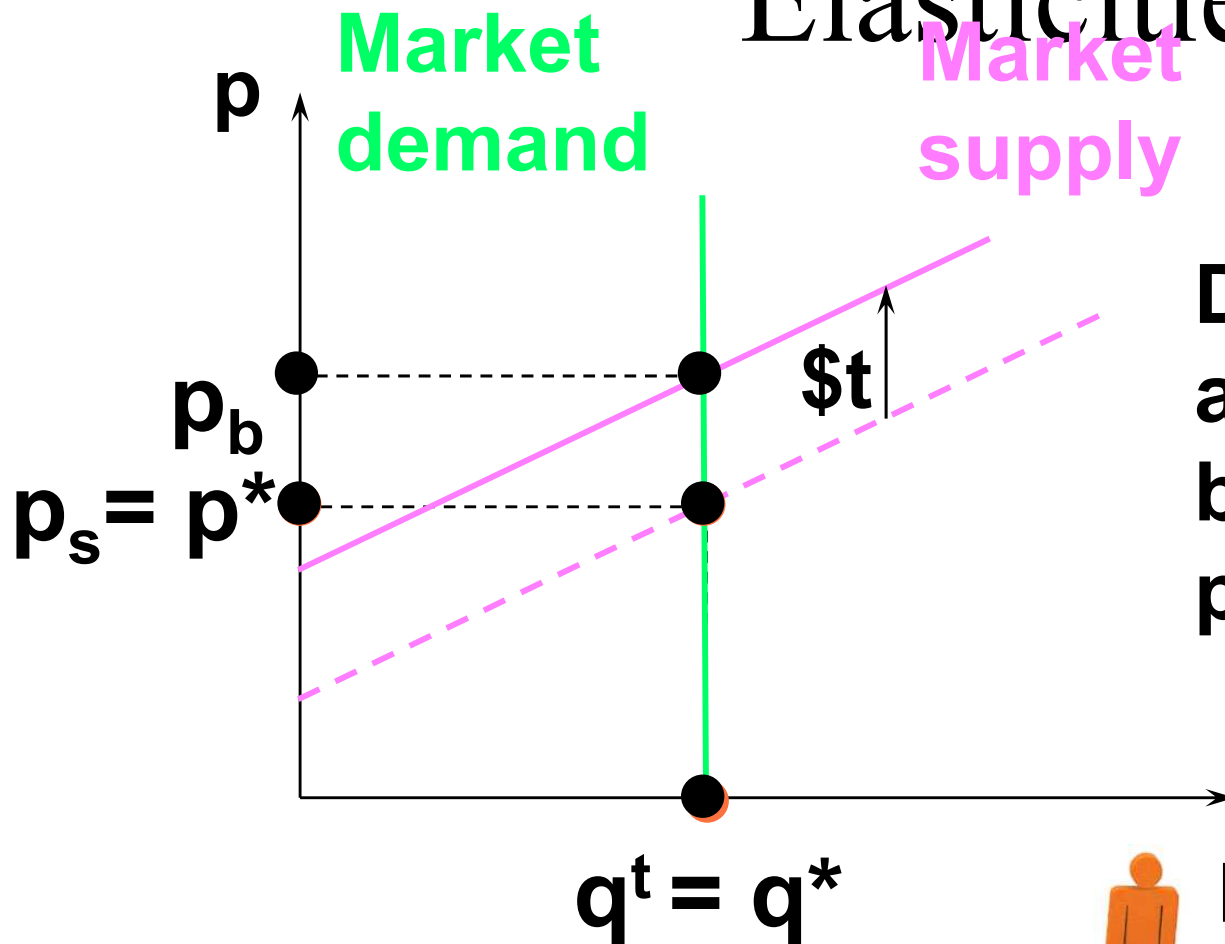


**Deadweight loss falls as market demand becomes less own-price elastic.**



# Deadweight Loss and Own-Price

## Elasticities



**Deadweight loss falls as market demand becomes less own-price elastic.**

**When  $\epsilon_D = 0$ , the tax causes no deadweight loss.**

$D(p), S(p)$

# Deadweight Loss and Own-Price Elasticities

- ◆ **Deadweight loss due to a quantity tax rises as either market demand or market supply becomes more own-price elastic.**
- ◆ **If either  $\varepsilon_D = 0$  or  $\varepsilon_S = 0$  then the deadweight loss is zero.**

