

Worksheet week # 7

1. Consider the following model describing the corporate investment behavior

$$I_t = \beta_0 + \beta_1 F_{t-1} + \beta_2 K_{t-1} + \varepsilon_t \quad , \quad t = 1935, \dots, 1953 \quad ,$$

where I_t = current gross investment, F_{t-1} = end-of-period value of outstanding shares, and K_{t-1} = end-of-period capital stock. The regression was estimated from the data for General Motors Corporation (standard errors in parentheses):

$$\hat{I}_t = - \begin{matrix} 109.8 \\ (97.436) \end{matrix} + \begin{matrix} 0.1142 \\ (0.0235) \end{matrix} F_{t-1} + \begin{matrix} 0.3261 \\ (0.0394) \end{matrix} K_{t-1} \quad , \quad R^2 = 0.8907 \quad .$$

- (a) Test that the amount of capital stock affects positively future investment behavior.
- (b) Explain how you would test the hypothesis that no relevant explanatory variables have been omitted using the RESET test.
2. Imagine that you want to estimate the race-specific crime rates. Given the data on over 2000 criminals (*crime2.gdt*), estimate the relationship between the race and the number of crimes committed. The dataset contains the following variables:

crime86 - number of crimes committed in 1986

race - race (=1 if black, =2 if Hispanic, =0 otherwise)

tottime - total number of months spent in prison since 18 years old

pcnv - proportion of prior convictions

qemp86 - number of quarters employed in 1986

inc86 - legal income in 1986, \$100s

- (a) Estimate the baseline model of the impact of race on number of crimes committed in 1986:

$$crime86_i = \alpha_0 + \alpha_1 race_i + \varepsilon_i \quad .$$

- (b) Interpret the results. Do you believe that the coefficient α_1 is correctly estimated? Under what assumptions would it be?
- (c) Create two dummy variables for black and Hispanic individuals. Estimate the equation again with these two variables. Interpret the results.

$$crime86_i = \beta_0 + \beta_1 black_i + \beta_2 hispanic_i + v_i \quad .$$

- (d) Is there anything that could still create a bias in this equation? If yes, how would you solve for this problem? What direction of bias do you expect?
- (e) Re-estimate the equation with variables controlling for crime history of a person:

$$crime86_i = \gamma_0 + \gamma_1 black_i + \gamma_2 hispanic_i + \gamma_3 tottime_i + \gamma_4 pcnv_i + e_i .$$

- (f) Control further for a current employment status and income of an individual:

$$crime86_i = \delta_0 + \delta_1 black_i + \delta_2 hispanic_i + \delta_3 tottime_i + \delta_4 pcnv_i + \delta_5 qemp86_i + \delta_6 inc86_i + u_i .$$

- (g) Interpret the results from part e and f (in comparison with c). How did the coefficients of *black* and *hispanic* change? Did you expect this direction of potential bias? Would you conclude that the additional variables indeed belong to the model?
- (h) Test the hypothesis that no relevant explanatory variables have been omitted using the RESET test in Gretl (test for the model from part f).

3. Use data *wage.gdt* to estimate the returns to education equation.

- (a) Estimate the baseline model of the impact of education and experience on wages:

$$\ln(wage_i) = \beta_0 + \beta_1 educ_i + \beta_2 exper_i + \varepsilon_i .$$

Interpret the meaning of the coefficient β_1 .

- (b) Reestimate the model using robust standard errors, comment on the differences.
- (c) Test for heteroskedasticity in the model in part (a). Is it necessary to use robust standard errors in this case?
- (d) Estimate the model with quadratic specification of experience:

$$\ln(wage_i) = \beta_0 + \beta_1 educ_i + \beta_2 exper_i + \beta_3 exper_i^2 + \varepsilon_i .$$

Comment on how and why the coefficient β_2 changed with respect to part (a). Did the coefficient β_1 change as well? Why or why not?

- (e) Do you believe that the coefficient β_1 is correctly estimated? Is there anything that could create a bias in this equation? If yes, how would you solve for this problem?
- (f) Include in the model the education of the mother and of the father of the observed individuals:

$$\ln(wage_i) = \beta_0 + \beta_1 educ_i + \beta_2 exper_i + \beta_3 exper_i^2 + \beta_4 motheduc_i + \beta_5 fatheduc_i + \varepsilon_i .$$

- i. Is there an impact on the coefficient β_1 ? Does this signal there was a bias in the model from part (d)? Comment on the sign of this bias.

- ii. Are both *motheduc* and *fatheduc* individually significant? Are they jointly significant?
 - iii. What happens if you exclude one these variables from the regression? Which one would you keep?
- (g) Instead of the education of parents, include the variable measuring ability in the model:

$$\ln(\text{wage}_i) = \beta_0 + \beta_1 \text{educ}_i + \beta_2 \text{exper}_i + \beta_3 \text{exper}^2 + \beta_4 \text{abil} + \varepsilon_i \ .$$

Is there an impact on the coefficient β_1 ? Does this signal there was a bias in the model from part (d)? Comment on the sign of this bias.