

# Lecture 6

# Sampling

# DHX\_MET1 Methodology 1

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# SAMPLING

- Sampling strategies and representativeness
- Sample size determination

# REPRESENTATIVENESS

- Inability to collect and/or analyze ALL data – need for sampling
- Samples of units
  - people, organizations, economies, events...
- Sampling within units (in time)
  - behavior – states
- Samples represent population (~ALL data) – representativeness
- **Representativeness**
  - ideal - sample differs from population only in size (or irrelevant characteristics)
  - achievable only probabilistically
  - R in relevant characteristics – can we list them all?

# STATISTICS & PARAMETERS

**Statistics** ( $M, r, SD, B...$ ) computed on our sample are estimates of their population values – **parameters** ( $\mu, \rho, \sigma, \beta...$ )

- $\hat{b}$  is an estimate of  $b$

The difference between their values is **sampling error**

# SAMPLING ERRORS

## Random

- quantifiable, estimable from probability theory
- in the long run does not bias estimates of researched characteristics

## Systematic

- hard to control for unless we know exactly the process (variable) creating the error
- selection bias
- response bias

# SAMPLING

1. Define the **population**.
2. Choose the **sample(-ing) frame**.
3. Decide the **sampling design/strategy**.
4. Estimate the appropriate **sample size**.
5. **Execute** the sampling process.

**POPULATION**

**SAMPLING FRAME**

**SAMPLE (approached)**

**SAMPLE**



# POPULATION

- NOT necessarily population in demographic sense
- POPULATION
  - a set of all units to which I want to generalize
  - a set of all units I want to have a sample of
- Widely/vaguely defined populations hard to sample
- Better to have a representative sample of a narrowly defined population than a biased sample of a wide one.



# SAMPLING FRAMES

- LISTS, SETS of (all) units in a population from which we **can** select
  - SETS of approachable units in some communication channel, place...
  - Registries of all kind
- Function of sampling frames
  - Allow sampling, allow for a level of control over sampling strategy
  - Allow reasoning about external validity - generalization
- First, come up with a frame, second, consider its limitations

# SAMPLING STRATEGIES

## NON-STRATEGIES

- Convenience samples
- Self-selected samples
- Naive snow-ball

## PURPOSIVE, NON-PROBABILISTIC STRATEGIES

- Careful creation of a sample making it representative in relevant variables
- Quota sample

## PROBABILISTIC STRATEGIES

- Strategies based on random selection

# SAMPLING – NON-STRATEGIES

## (convenience sampling)

We have little to no control (or knowledge) over the processes leading to including a particular unit in or sample

- Difficult to argue about bias
- Difficult to argue the processes are the same as in other studies
- Difficult to apply statistical inference
  
- „Heterogeneity“ nor „homogeneity“ are not the solution if not considered systematically
- Making the sample bigger makes it worse – false confidence
  
- If it *must* be used, strive for maximum randomness

# SAMPLING – NON-PROBABILISTIC

## QUOTA SAMPLING

- building the sample so that it is representative in particular characteristics
- typically demographics – settlement, age, race, gender...
- quota = proportion of units in each category found in **population**
- unless the quota variables are super-relevant it may not be worth the effort

## PURPOSIVE SAMPLING, THEORETICAL SAMPLING

- selection of individual units based on current needs of a (qualitative) study
- to compare, contrast...
- Emmel, N. (2013). *Sampling and choosing cases in qualitative research. A realist approach.* Sage.

# SAMPLING – PROBABILISTIC STRATEGIES

Probabilistically unbiased estimates of parameters

- SIMPLE RANDOM, SYSTEMATIC
- STRATIFIED – let's assist probability; need for sub-population parameters
  - PROPORTIONAL (proportionate)
  - NON-PROPORTIONAL (disproportionate), e.g. oversampling rare subgroups
- CLUSTER (MULTISTAGE) – let's make it more practical
  - Hierarchical sampling procedure – higher-order units, lower-order units, individuals
  - At all levels we need sufficient numbers of units
- SNOW-BALL (probabilistic)
  - network sampling, link-tracing

DILBERT By SCOTT ADAMS



## Normality of Distributions

Attributes or characteristics of the population are generally not normally distributed. For instance, when attributes such as height and weight are considered, most people will be clustered around the mean, leaving only a small number at the extremes who are either very tall or very short, very heavy or very light, and so on, as indicated in Figure 13.3. If we are to estimate the population parameters from those represented in a sample with reasonable accuracy, the sample has to be chosen so that the distribution of the characteristics of interest follows the same pattern of normal distribution in the sample that describes the population. From the central limit theorem, we know that the sampling distribution of the sample mean is normally distributed. As the **sample size**  $n$  increases, the means of the random samples taken from practically any population approach a normal distribution with

# SAMPLING – WHAT SAMPLE SIZE DO WE NEED?

- Large enough to make sure that relevant observed properties of the sample are unlikely to be due to sampling error
  - High „signal-to-noise ratio“
- QUAN - Power analysis, precision analysis
- QUAL – Saturation

Often seems difficult to determine beforehand – rules of thumb, e.g.

- high tens of participants for each group for a between-subject experiment
- hundreds of participants for regression models
- low tens for a within-subject experiment
- 3-5 cases for IPA
- about 10 for a GT

**Rules of thumb (like p.264) should be avoided – world is just not that simple.**

# PRECISION

At a preferred level of confidence we want our (confidence) interval estimates to be as narrow as possible.

- For mean  $S. E. = SD/\sqrt{N}$  and  $95\%CI = M \mp 1.96S. E.$ 
  - The higher SD, the wider the interval estimator
  - The higher N, the narrower – precise the interval estimate
- **How large a sample do I need to have a certain level of precision and confidence?**
  - $N = \frac{2 \times 1.96SD^2}{width\ of\ CI}$  where 1,96 can be replaced by an appropriate quantile of normal or t distribution
- With other statistics and more complicated sampling designs such estimate is more difficult to compute



# STATISTICAL POWER ( $1-\beta$ )

- In the context of statistical hypothesis testing – the probability that an effect will be found statistically significant (provided it exists)
  - $P(p < \alpha | H_0)$
  - Probability of avoiding Type II error
- Factors affecting power
  - (signal) – effect size, measurement reliability
  - (noise) – standard error ... sample size, design
  - (required certainty) - alpha
- [Simulation: https://rpsychologist.com/d3/NHST/](https://rpsychologist.com/d3/NHST/)

# CONSEQUENCES...

- ...OF INSUFFICIENT POWER (eg. 60%)
- even if you are right about your hypothesis & have designed your study well, the data may not support your hypothesis
- gambling with funding money & participants time -> ethics
- effect size inflation
  - in confirmatory studies due to publication bias
  - in exploratory studies due to publication bias, fishing and insufficient correction of p-values for multiple tests
- ... OF EXTREMELY HIGH POWER (eg. > 95%)
  - may be just an inefficient use of research budget
  - combined with fishing and other methodological *sins* (QRPs) allows to identify very small significant effects - artefacts

## Practically - 2 big questions:

### 1. What is the expected effect size?

- Many standardized measures of effect size
  - distance based – Cohen's  $d$ , Hedges'  $g$ ...
  - based on explained variance –  $R^2$ ,  $r$ ,  $\eta^2$ ,  $\omega^2$ ...
- It is safer to consider published effect sizes inflated, unless they come from meta-analysis

### 2. How to do power analysis for more complicated analyses than a $t$ -test?

- G\*Power: <http://www.gpower.hhu.de/>
- Dattalo, P. (2008). *Determining sample size: balancing power, precision, and practicality*. OUP.

# SAMPLING IN QUALITATIVE RESEARCH

- Representativeness – what is to be represented?
- If there are relevant phenomena in the the studied population we want to be fairly confident they could have been encountered during study.
- Purposive sampling
  - careful selection of each case based on accumulated knowledge and immediate needs
  - Some selected before analysis, some after analyses of first cases
  - Often return to cases
- (Theoretical) Saturation – subjective belief that adding further cases would not improve the theory enough to be justifiable
- Both the reasons for selecting each case and reasons behind saturation are reported/discussed in the research report.
- Again, rules of thumb should be avoided

# Sampling from finite populations

- Finite and fairly small - when it makes sense to think about the percentage of population in the sample
- *fpc* - finite population correction to standard error
- $SE_{fpc} = SE \sqrt{\frac{N-n}{N-1}}$  where  $N$  is population size and  $n$  sample size
- Rarely used bc the population is often thought to be more general than we initially see
- Eg. Current employees are only a sampling frame from possible employees or employees over some time period