Exercise session 4

1. Your aim is to estimate how the number of prenatal examinations and several other characteristics influence the birth weight of a baby. Your initial hypothesis is that more responsible pregnant women visit the doctor more often and this leads to healthier and thus also bigger babies.
	1. In your first specification, you run the following model:

*bwght* = *β*0 + *β*1 *npvis* + *β*2 *npvis*2 + *β*3 *monpre* + *β*4 *male* + *ε ,*

where *bwght* is birth weight of the baby (in grams), *npvis* is the number of prenatal doctor’s visits, *monpre* is the month on pregnancy in which the prenatal care began and *male* is a dummy, equal to one if the baby is a boy and zero if it is a girl. You obtain the following results from Stata[[1]](#footnote-1):

|  |  |  |  |
| --- | --- | --- | --- |
| Source | SS | df | MS |
| Model | **12848047.5** | **4** | **3212011.87** |
| Residual | **570003184** | **1721** | **331204.639** |
| Total | **582851231** | **1725** | **337884.772** |

|  |  |
| --- | --- |
| Number of obs = | **1726** |
| F( 4, 1721) = | **9.70** |
| Prob > F = | **0.0000** |
| R-squared = | **0.0220** |
| Adj R-squared = | **0.0198** |
| Root MSE = | **575.5** |

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| bwght | Coef. | Std. Err. | t | P>|t| | [95% Conf. | Interval] |
| npvis | **53.50974** | **11.41313** | **4.69** | **0.000** | **31.12468** | **75.8948** |
| npvissq | **-1.173175** | **.3591552** | **-3.27** | **0.001** | **-1.877601** | **-.4687481** |
| monpre | **30.47033** | **12.40794** | **2.46** | **0.014** | **6.134091** | **54.80657** |
| male | **76.69243** | **27.76083** | **2.76** | **0.006** | **22.24391** | **131.141** |
| \_cons | **2853.196** | **101.3073** | **28.16** | **0.000** | **2654.498** | **3051.895** |

* + 1. Is there strong evidence that *npvissq* (stands for *npvis*2) should be included in the model? **The *p*-value on the coefficient on *npvissq* is very small, and hence the vari- able is strongly significant and should be included in the model.**
1. How do you interpret the negative coefficient of *npvissq*? **The negative coefficient on *npvissq* signals a concave form of the impact of the number of prenatal doctor’s visits, meaning that there are decreasing returns to visiting the doctor. A possible explanation is that some number of visits is beneficiary for all pregnant women, but higher necessity of visits could mean that the pregnancy is risky for some reasons and the woman has to go to the doctor more often than usually. Such woman is also more likely to have smaller baby.**
2. Holding *npvis* and *monpre* fixed, test the hypothesis that newborn boys weight by 100 grams more than newborn girls (at 95% confidence level).

**Such hypothesis can be stated as**

$$H\_{0}: β\_{4}=100 H\_{a}: β\_{4}\ne 100 $$

**Test statistic** $t=\frac{\hat{β\_{4}}-100}{SE(\hat{β\_{4}})}=\frac{76.69-100}{27.76}=-0.84 \~ t\_{\infty ,1721}$**=-1.96. Therefore, we failed to reject the null hypothesis that newborn boys weight by 100 grams more than newborn girls at 95% confidence level.**

1. A friend of yours, student of medicine, reminds you of the fact that the age of the parents (especially of the mother) might be a decisive factor for the health and for the weight of the baby. Therefore, in your second specification, you decide to include in your model also the age of the mother (*mage*) and of the father (*fage*). The results of your estimation are now the following:

|  |  |  |  |
| --- | --- | --- | --- |
| Source | SS | df | MS |
| Model | **16270165.8** | **6** | **2711694.3** |
| Residual | **563258231** | **1713** | **328813.912** |
| Total | **579528396** | **1719** | **337131.121** |

|  |  |
| --- | --- |
| Number of obs = | **1720** |
| F( 6, 1713) = | **8.25** |
| Prob > F = | **0.0000** |
| R-squared = | **0.0281** |
| Adj R-squared = | **0.0247** |
| Root MSE = | **573.42** |

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| bwght | Coef. | Std. Err. | t | P>|t| | [95% Conf. | Interval] |
| npvis | **52.43859** | **11.40558** | **4.60** | **0.000** | **30.06826** | **74.80891** |
| npvissq | **-1.138545** | **.3585648** | **-3.18** | **0.002** | **-1.841816** | **-.4352743** |
| monpre | **34.35661** | **12.69477** | **2.71** | **0.007** | **9.457725** | **59.2555** |
| male | **74.45482** | **27.75247** | **2.68** | **0.007** | **20.02252** | **128.8871** |
| mage | **.5285275** | **4.218069** | **0.13** | **0.900** | **-7.744582** | **8.801637** |
| fage | **8.697342** | **3.465973** | **2.51** | **0.012** | **1.899357** | **15.49533** |
| \_cons | **2592.813** | **139.6173** | **18.57** | **0.000** | **2318.974** | **2866.651** |

* + 1. Comment on the significance of the coefficients on *mage* and *fage* separately: are they in line with your friend’s claim?

**When we look on the *p*-values of the corresponding coefficients, we see that whereas *fage* is significant at 99% confidence level, *mage* is insignificant. This is not in line with our friend’s claim, who says that especially the age of the mother should be an important factor.**

* + 1. Test the hypothesis that *mage* and *fage* are jointly significant (at 95% confidence level). Is the result in line with your friend’s claim? **To test joint significance, we need restricted and unrestricted models. In the regression in part (b) we have included *mage* and *fage* while they are not included in the regression in part (a). Therefore, we can use SSR from both regression outputs in order to judge the joint significance of the *mage* and *fage* variables. According to output in part (a) SSRr=570003184, According to output in part (b) SSRur=563258231. We construct F test based on the formula:** $F=\frac{(SSR\_{r}-SSR\_{ur})/q}{SSR\_{ur}/df}$**, where q is the number of restrictions in this case q=2 (mage and fage) and df is degrees of freedom.**

**Df=n-k-1=1720-7**

**Therefore,** $F=\frac{(570003184-563258231)/2}{563258231/1713}=10.36$ **in the F-table we will find a critical value at 5% it will be** $F\_{2,\infty }=3.00$**.**

**10.36>3, hence, we can reject the null hypothesis and we conclude that mage and fage are jointly significant.**

* + 1. How can you reconcile you findings from the two previous questions?

**The finding about the joint significance from the second question is not surprising, since we know already from the first question that *fage* is individually significant. If a variable is significant, then the *HA* of the test of the joint significance has to be valid and so the variables have to be jointly significant.**

**c) I**n your third specification, you decide to drop *fage* and you get the following results:

|  |  |  |  |
| --- | --- | --- | --- |
| Source | SS | df | MS |
| Model | **14451685.6** | **5** | **2890337.13** |
| Residual | **568399545** | **1720** | **330464.852** |
| Total | **582851231** | **1725** | **337884.772** |

|  |  |
| --- | --- |
| Number of obs = | **1726** |
| F( 5, 1720) = | **8.75** |
| Prob > F = | **0.0000** |
| R-squared = | **0.0248** |
| Adj R-squared = | **0.0220** |
| Root MSE = | **574.86** |

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| bwght | Coef. | Std. Err. | t | P>|t| | [95% Conf. | Interval] |
| npvis | **52.27885** | **11.41406** | **4.58** | **0.000** | **29.89196** | **74.66575** |
| npvissq | **-1.142647** | **.3590214** | **-3.18** | **0.001** | **-1.846811** | **-.4384821** |
| monpre | **35.25912** | **12.58328** | **2.80** | **0.005** | **10.57898** | **59.93927** |
| male | **79.38175** | **27.75667** | **2.86** | **0.004** | **24.94136** | **133.8221** |
| mage | **-6.91257** | **3.137972** | **-2.20** | **0.028** | **-13.06721** | **-.757928** |
| \_cons | **2648.851** | **137.2778** | **19.30** | **0.000** | **2379.602** | **2918.1** |

Comment on the significance of the coefficient on *mage*, compared to the results from part (b). Is your finding in line with your reasoning in part (b)? Does it confirm your friend’s claim?

**Now, the *p*-value of the coefficient on *mage* is very low and so the coefficient is strongly significant. When we compare this finding to part (b), we realize that the insignificance of this coefficient in that part was probably given by a strong correlation between *mage* and *fage*, leading to the multicollinearity problem, which increases the standard errors and decreases thus the significance of the coefficients. When we drop *fage*, the multicollinearity problem is solved and we see that our friend’s claim was true.**

d) Having regained trust in your friend, you consult your results once more with him. Together, you come up with an interesting question: whether smoking during pregnancy can affect the weight of the baby. Fortunately, you have at your disposition the variable *cigs*, standing for the average number of cigarettes each woman in your sample smokes per day during the pregnancy, and so you can include it in your model. However, your friend warns you that women who smoke during pregnancy are in general less responsible than those who do not smoke, and that these women also tend to visit the doctor less often. (In other words, the more the women smokes, the less prenatal doctor’s visits she has). This is an important fact that you have to take into consideration while interpreting your final results, which are:

|  |  |  |  |
| --- | --- | --- | --- |
| Source | SS | df | MS |
| Model | **14560828.9** | **6** | **2426804.81** |
| Residual | **523281374** | **1615** | **324013.235** |
| Total | **537842203** | **1621** | **331796.547** |

|  |  |
| --- | --- |
| Number of obs = | **1622** |
| F( 6, 1615) = | **7.49** |
| Prob > F = | **0.0000** |
| R-squared = | **0.0271** |
| Adj R-squared = | **0.0235** |
| Root MSE = | **569.22** |

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| bwght | Coef. | Std. Err. | t | P>|t| | [95% Conf. | Interval] |
| npvis | **42.43442** | **11.59582** | **3.66** | **0.000** | **19.68999** | **65.17885** |
| npvissq | **-.8948737** | **.3624432** | **-2.47** | **0.014** | **-1.605782** | **-.1839653** |
| monpre | **31.77658** | **12.78156** | **2.49** | **0.013** | **6.706395** | **56.84676** |
| male | **82.39438** | **28.34937** | **2.91** | **0.004** | **26.78897** | **137.9998** |
| mage | **-6.980738** | **3.227181** | **-2.16** | **0.031** | **-13.31064** | **-.6508356** |
| cigs | **-10.209** | **3.398309** | **-3.00** | **0.003** | **-16.87456** | **-3.54344** |
| \_cons | **2748.856** | **141.868** | **19.38** | **0.000** | **2470.591** | **3027.12** |

1. Interpret the coefficient on *cigs*.

**The coefficient on *cigs* tells us that with each additional cigarette smoked by the pregnant woman on average per day, the weight of the baby is smaller by 10 grams, ceteris paribus.**

1. What evidence do you find that *cigs* really should be included in the model? List at least two arguments.

**We can see from the *p*-value that the coefficient on *cigs* is strongly signifi- cant. We can also see that the *R*2 as well as the adjusted *R*2 are higher than in the model without this variable (in part (c)). Moreover, we see that the coefficient on *npvis* has changed quite a lot once we included *cigs*, which is a signal of an omitted variable bias in part (c) and a proof that *cigs* indeed should be included in the model.**

1. Compare the coefficient on *npvis* with the one you obtained in part (c). Do you think there was a bias? If yes, explain where it came from and interpret its sign.

**In part (c), the coefficient on *npvis* was approximatively equal to 52, now it is equal to 42. This shows there was a positive bias in part (c): the coefficient was overestimated there. We know that the sign of this bias is the sign of the product of two correlations: the correlation between the omitted variable *cigs* and the variable *npvis* and the correlation between *cigs* and the dependent variable *bwght*. The correlation between *cigs* and the dependent variable *bwght* is negative as we can see from the negative coefficient on *cigs* in the model estimated in part (d), the correlation between *cigs* and *npvis* is negative as we learn from our friend (women who smoke tend to visit the doctor less often). The product of these two correlations is thus positive and so is the bias in part (c).**

**Intuitively, we can say that when *cigs* was omitted, everything that could measure the degree of responsibility of pregnant women in our model was the variable *npvis*. Once we included *cigs*, we can measure separately the responsibility of going to the doctor and the responsibility of not smoking, and so the coefficient on *npvs* is reflecting only the correct part of this influence and it is not overestimated.**

**Problem 2**

Suppose that you have a sample of *n* individuals who apart from their mother tongue (Czech) can speak English, German, or are trilingual (i.e., all individuals in your sample speak in addition to their mother tongue at least one foreign language). You estimate the following model:

*wage* = *β*0 + *β*1*educ* + *β*2*IQ* + *β*3*exper* + *β*4*DM* + *β*5*Germ* + *β*6*Engl* + *ε ,*

where

|  |  |  |
| --- | --- | --- |
| *educ* | *. . .* | years of education |
| *IQ* | *. . .* | IQ level |
| *exper* | *. . .* | years of on-the-job experience |
| *DM* | *. . .* | dummy, equal to one for males and zero for females |
| *Germ* | *. . .* | dummy, equal to one for German speakers and zero otherwise |
| *Engl* | *. . .* | dummy, equal to one for English speakers and zero otherwise |

* 1. Explain why a dummy equal to one for trilingual people and zero otherwise is not included in the model.

**If we included the dummy for people who are trilingual, we would have the complete set of dummies in the model (describing all three possible options - German speaker, English speaker, both foreign languages). Since we have the intercept in the model, this would lead to perfect multicollinearity.**

* 1. Explain how you would test for discrimination against females (in the sense that *ceteris paribus* females earn less than males). Be specific: state the hypothesis, give the test statistic and its distribution.

**For women, the dummy *DM* is equal to 0 and the model stands as follows:**

***wage* = *β*0 + *β*1*educ* + *β*2*IQ* + *β*3*exper* + *β*5*Germ* + *β*6*Engl* + *ε .***

**For men, the dummy *DM* is equal to 1 and the model stands as follows:**

***wage* = *β*0 + *β*1*educ* + *β*2*IQ* + *β*3*exper* + *β*4 + *β*5*Germ* + *β*6*Engl* + *ε .***

**Therefore, ceteris paribus, the difference between the wage of men and the wage of women is equal to *β*4. If this coefficient is positive, then men earn more than women. Hence, our hypothesis to be tested is**

*H*0 : *β*4 ≤ 0 vs *HA* : *β*4 *>* 0 *.*

**This leads to a one-sided *t*-test with the test statistic**

$$t=\frac{\hat{β\_{4}}}{SE(\hat{β\_{4}})}\~t\_{n-k}$$

**where *k* = 7 in this case. When we compute this test statistic, we compare it to the critical value *tn-7,0.95*. If the test statistic is larger than this critical value, then we reject the *H*0 at 95% confidence level and we conclude that there is discrimination against females. where *k* = 7 in this case. When we compute this test statistic, we compare it to the critical value *tn-7,0.95*. If the test statistic is larger than this critical value, then we reject the *H*0 at 95% confidence level and we conclude that there is discrimination against females.**

* 1. Explain how you would measure the payoff (in terms of wage) to someone of becoming trilingual given that he can already speak (i) English, (ii) German.

**The payoff of a trilingual person is**

*wage* = *β*0 + *β*1*educ* + *β*2*IQ* + *β*3*exper* + *β*4*DM* + *β*5 + *β*6 + *ε ,*

**the payoff of a German speaking person is**

*wage* = *β*0 + *β*1*educ* + *β*2*IQ* + *β*3*exper* + *β*4*DM* + *β*5 + *ε ,*

**and the payoff of an English speaking person is**

*wage* = *β*0 + *β*1*educ* + *β*2*IQ* + *β*3*exper* + *β*4*DM* + *β*6 + *ε .*

**Hence, by becoming trilingual, a person who can already speak English gains *β*5 and a person who can already speak German gains *β*6. If we assume that both coefficients are positive, this payoff should be positive.**

* 1. Explain how you would test if the influence of on-the-job experience is greater for males than for females. Be specific: specify the model, state the hypothesis, give the test statistic and its distribution.

**To allow the on-the-job experience to be greater for males than for females, we have to define a slope coefficient on *exper* that would be different for males and for females. We can do so using the following model:**

*wage* = *β*0+*β*1*educ*+*β*2*IQ*+*β*3*exper*+*β*4*DM* +*β*5*Germ*+*β*6*Engl*+*β*7*exper*·*DM* +*ε .*

**Where we have vcreated an interaction term exper\*DM. In this case, the impact of on the on-the-job experience on wage would be *β*3 for females and *β*3 + *β*7 for males. Hence, if *β*7 is positive, then men gain more from experience than women. Hence, our hypothesis to be tested is**

*H*0 : *β*7 ≤ 0 vs *HA* : *β*7 *>* 0 *.*

$$t=\frac{\hat{β\_{7}}}{SE(\hat{β\_{7}})}\~t\_{n-k}$$

**where *k* = 8 in this case. When we compute this test statistic, we compare it to the critical value *tn−*8*,*0*.*95. If the test statistic is larger than this critical value, then we reject the *H*0 at 95% confidence level and we conclude that the influence of on-the-job experience is greater for males than for females.**

1. Stata is a statistical software, which can be used to for econometric purposes. The Stata output

is quite similar to the Gretl output you are familiar with. In particular, *Coef.* denotes the estimated coefficients, *Std.Err.* denotes the standard errors of these coefficients, *t* denotes the *t*-statistic of the test of significance of the coefficients, *P > |t|* denotes the corresponding *p*-value. [↑](#footnote-ref-1)