Microeconomics

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Wojciech Gerson (1831-1901)

LECTURE

5

The Costs of Production

Chapter 13

ACTIVE LEARNING 1

Brainstorming costs

You run Ford Motor Company.

- List three different costs you have.
- List three different business decisions that are affected by your costs.

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Lecture Today

- What is a production function? What is marginal product? How are they related?
- What are the various costs? How are they related to each other and to output?
- How are costs different in the short run vs. the long run?
- What are “economies of scale”?

We assume that the firm's goal is to maximize profit.

Profit = Total revenue – Total cost

the amount a firm receives from the sale of its output

the market value of the inputs a firm uses in production

Explicit vs. Implicit Costs: An Example

You need $100,000 to start your business.
The interest rate is 5%.
Case 1: borrow $100,000

explicit cost = $5000 interest on loan

Case 2: use $40,000 of your savings,
borrow the other $60,000

explicit cost = $3000 (5%) interest on the loan

implicit cost = $2000 (5%) *foregone* interest you could have earned on your $40,000.

In both cases, total (exp + imp) costs are $5000.

Economic Profit vs. Accounting Profit

ACTIVE LEARNING 2

Economic profit vs. accounting profit

The equilibrium rent on office space has just increased by $500/month.

Determine the effects on accounting profit and economic profit if:

a. you rent your office space

b. you own your office space

ACTIVE LEARNING 2

Answers

The rent on office space increases $500/month.

a. You rent your office space.

Explicit costs increase $500/month.

Accounting profit & economic profit each fall $500/month.

b. You own your office space.

Explicit costs do not change,

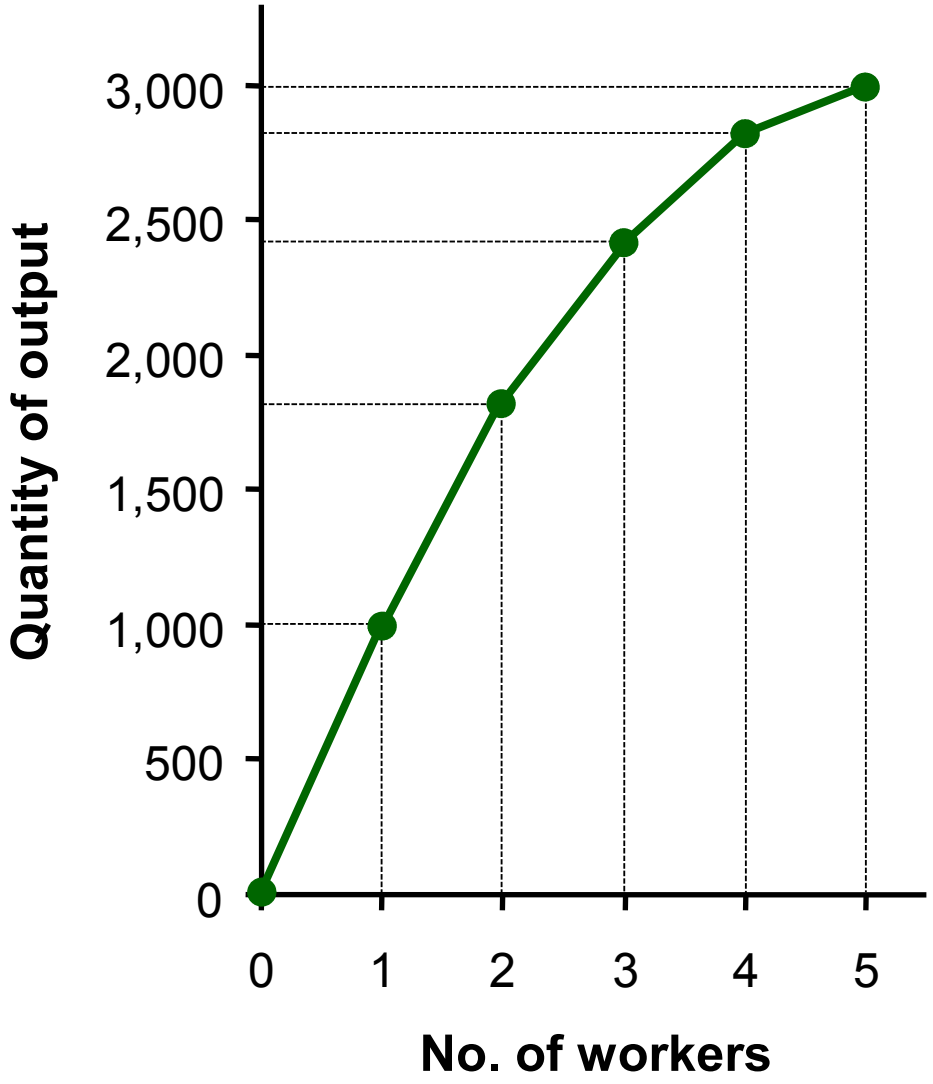
so accounting profit does not change.

Implicit costs increase $500/month (opp. cost of using your space instead of renting it)

so economic profit falls by $500/month.

EXAMPLE 1: Farmer Slavko's Production Function

L (no. of workers)	***Q*** (bushels of wheat)
0	0
1	1000
2	1800
3	2400
4	2800
5	3000



Marginal Product

If Slavko hires one more worker, his output rises by the *marginal product of labor*.

The **marginal product** of any input is the increase in output arising from an additional unit of that input, holding all other inputs constant.

Notation:

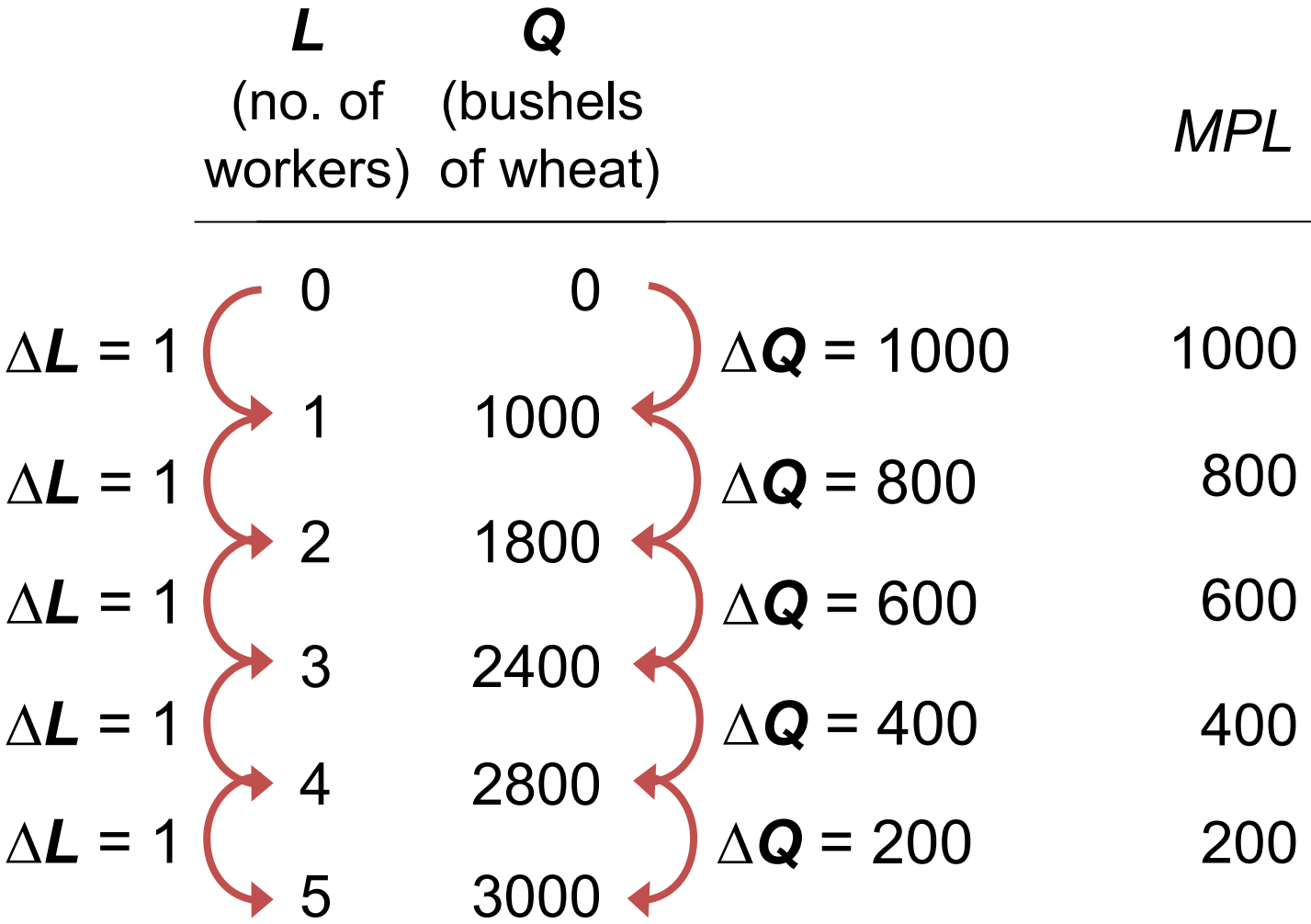
Δ (delta) = "change in…"

Examples:

Δ*Q* = change in output, **Δ*L*** = change in labor

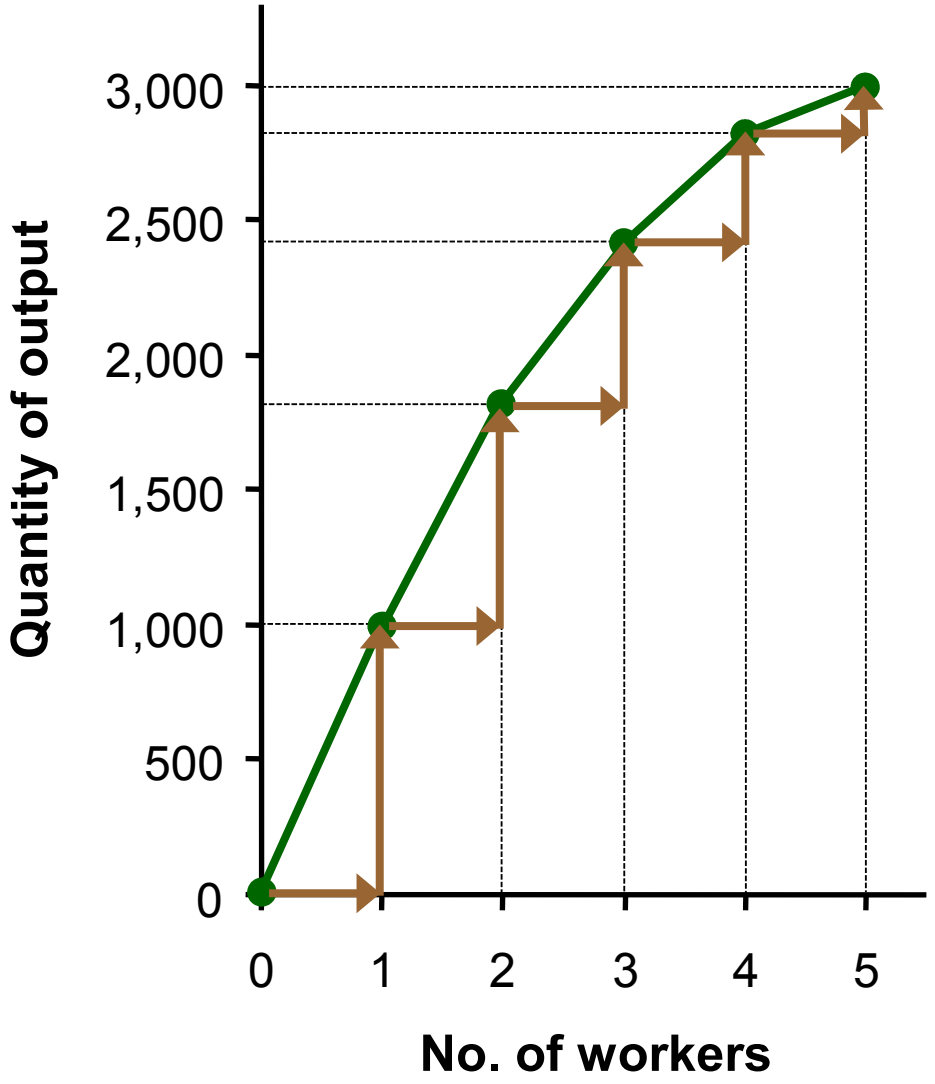
Marginal product of labor (*MPL*) =

$$\frac{\Delta Q}{\Delta L}$$



EXAMPLE 1: MPL = Slope of Prod Function

L (no. of workers)	***Q*** (bushels of wheat)	*MPL*
0	0	
		1000
1	1000	
		800
2	1800	
		600
3	2400	
		400
4	2800	
		200
5	3000	



Why MPL Is Important

- Recall one of the Ten Principles:
  Rational people think at the margin.
- When Farmer Slavko hires an extra worker,
  - his costs rise by the wage he pays the worker
  - his output rises by *MPL*
- Comparing them helps Slavko decide whether he should hire the worker.

Why MPL Diminishes

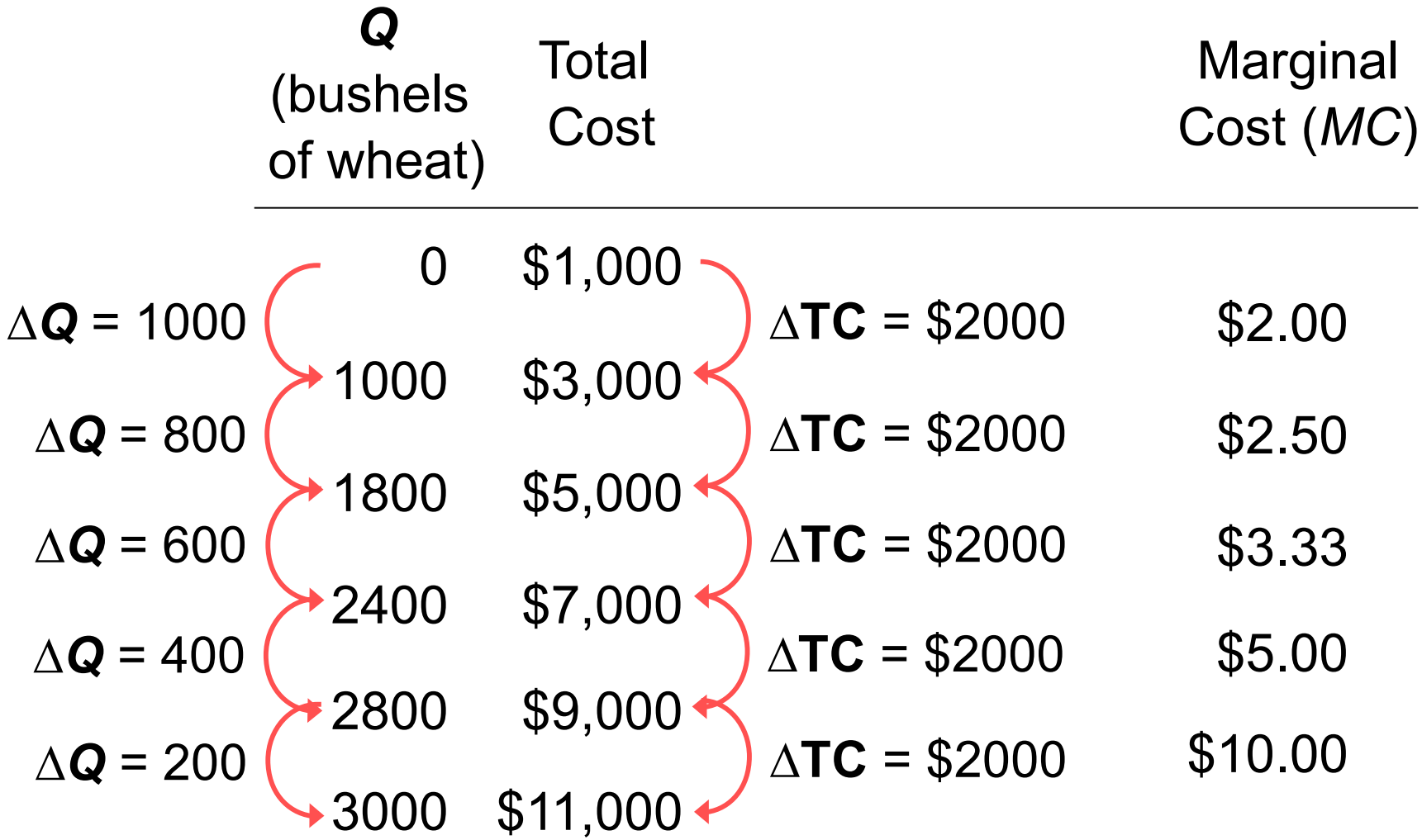
- Farmer Slavko's output rises by a smaller and smaller amount for each additional worker. Why?
- As he adds workers, the average worker has less land to work with and will be less productive.
- In general, *MPL* diminishes as ***L*** rises whether the fixed input is land or capital (equipment, machines, etc.).
- **Diminishing marginal product**: The marginal product of an input declines as the quantity of the input increases (other things equal).

L (no. of workers)	***Q*** (bushels of wheat)	Cost of land	Cost of labor	Total cost
0	0	$1,000	$0	$1,000
1	1000	$1,000	$2,000	$3,000
2	1800	$1,000	$4,000	$5,000
3	2400	$1,000	$6,000	$7,000
4	2800	$1,000	$8,000	$9,000
5	3000	$1,000	$10,000	$11,000

EXAMPLE 1: Slavko's Total Cost Curve

Q (bushels of wheat)	Total Cost
0	$1,000
1000	$3,000
1800	$5,000
2400	$7,000
2800	$9,000
3000	$11,000

$$MC = \frac{\Delta TC}{\Delta \mathbf{Q}}$$



EXAMPLE 1: The Marginal Cost Curve

Q (bushels of wheat)	*TC*	*MC*
0	$1,000	
		$2.00
1000	$3,000	
		$2.50
1800	$5,000	
		$3.33
2400	$7,000	
		$5.00
2800	$9,000	
		$10.00
3000	$11,000	

MC usually rises
as ***Q*** rises,
as in this example.

Why MC Is Important

- Farmer Slavko is rational and wants to maximize his profit. To increase profit, should he produce more or less wheat?
- To find the answer, he needs to "think at the margin."
- If the cost of an additional wheat (*MC*) is less than the revenue he would get from selling it, then Alejandro's profits rise if he produces more.

Fixed and Variable Costs

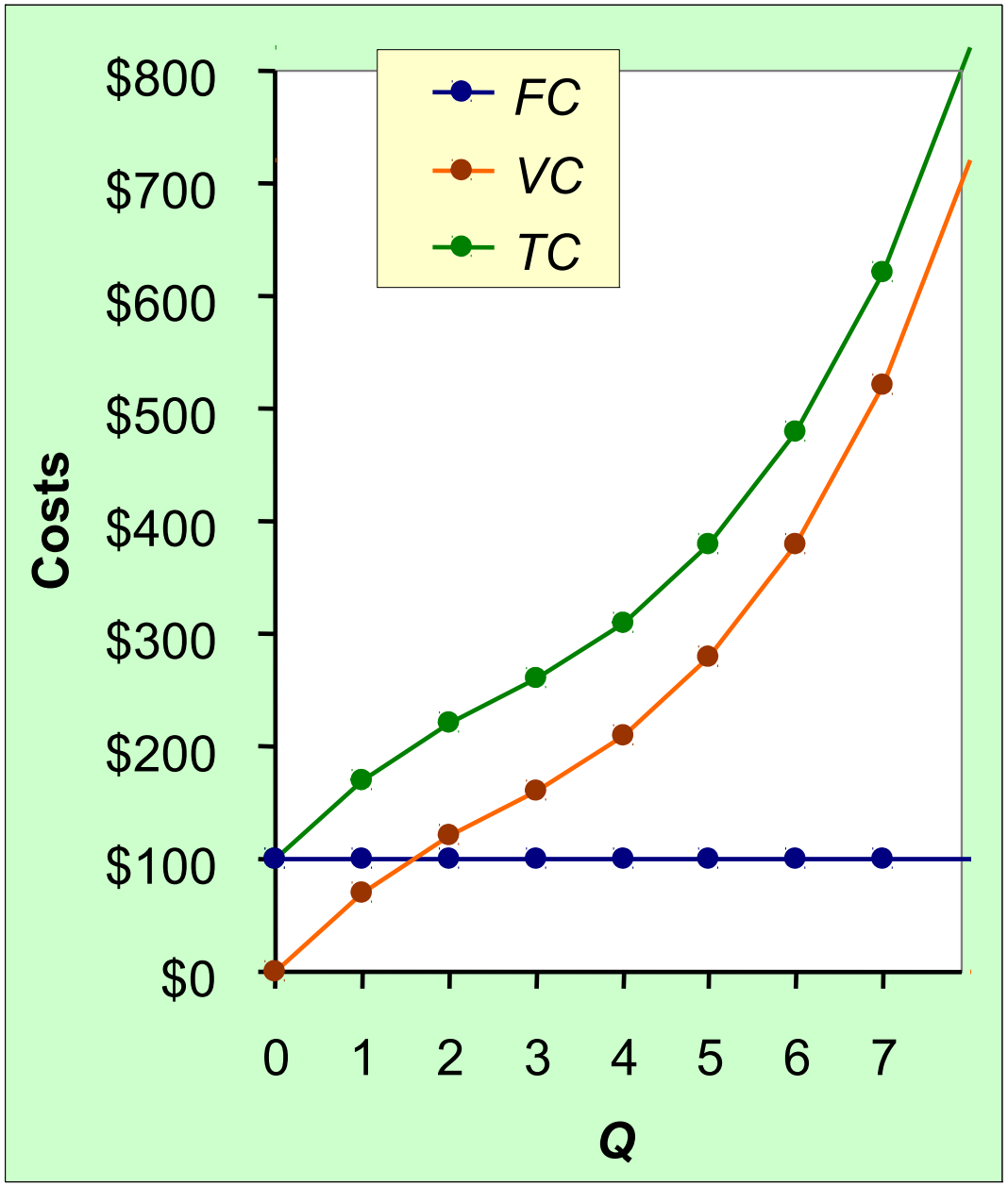
- **Fixed costs (*FC*)** do not vary with the quantity of output produced.
  - For Farmer Slavko, *FC* = $1000 for his land
  - Other examples:
    cost of equipment, loan payments, rent
- **Variable costs (*VC*)** vary with the quantity produced.
  - For Farmer Slavko, *VC* = wages he pays workers
  - Other example: cost of materials
- **Total cost (*TC*)** = *FC* + *VC*

EXAMPLE 2

- Our second example is more general, applies to any type of firm producing any good with any types of inputs.

EXAMPLE 2: Costs

Q	FC	VC	TC
0	$100	$0	$100
1	100	70	170
2	100	120	220
3	100	160	260
4	100	210	310
5	100	280	380
6	100	380	480
7	100	520	620



EXAMPLE 2: Marginal Cost

Q	*TC*	*MC*
0	$100	
		$70
1	170	
		50
2	220	
		40
3	260	
		50
4	310	
		70
5	380	
		100
6	480	
		140
7	620	

Recall, **Marginal Cost (*MC*)** is the change in total cost from producing one more unit:

$$MC = \frac{\Delta TC}{\Delta \boldsymbol{Q}}$$

Usually, *MC* rises as ***Q*** rises, due to diminishing marginal product.

Sometimes (as here), *MC* falls before rising.

(In other examples, *MC* may be constant.)

EXAMPLE 2: Average Fixed Cost

Q	*FC*	*AFC*
0	$100	n/a
1	100	$100
2	100	50
3	100	33.33
4	100	25
5	100	20
6	100	16.67
7	100	14.29

Average fixed cost (*AFC*) is fixed cost divided by the quantity of output:

$$AFC = FC/\mathbf{Q}$$

Notice that *AFC* falls as ***Q*** rises: The firm is spreading its fixed costs over a larger and larger number of units.

EXAMPLE 2: Average Variable Cost

Q	*VC*	*AVC*
0	$0	n/a
1	70	$70
2	120	60
3	160	53.33
4	210	52.50
5	280	56.00
6	380	63.33
7	520	74.29

Average variable cost (*AVC*) is variable cost divided by the quantity of output:

$$AVC = VC/Q$$

As ***Q*** rises, *AVC* may fall initially. In most cases, *AVC* will eventually rise as output rises.

EXAMPLE 2: Average Total Cost

Q	*TC*	*ATC*	*AFC*	*AVC*
0	$100	n/a	n/a	n/a
1	170	$170	$100	$70
2	220	110	50	60
3	260	86.67	33.33	53.33
4	310	77.50	25	52.50
5	380	76	20	56.00
6	480	80	16.67	63.33
7	620	88.57	14.29	74.29

Average total cost (*ATC*)/cost per unit/unit cost equals total cost divided by the quantity of output:

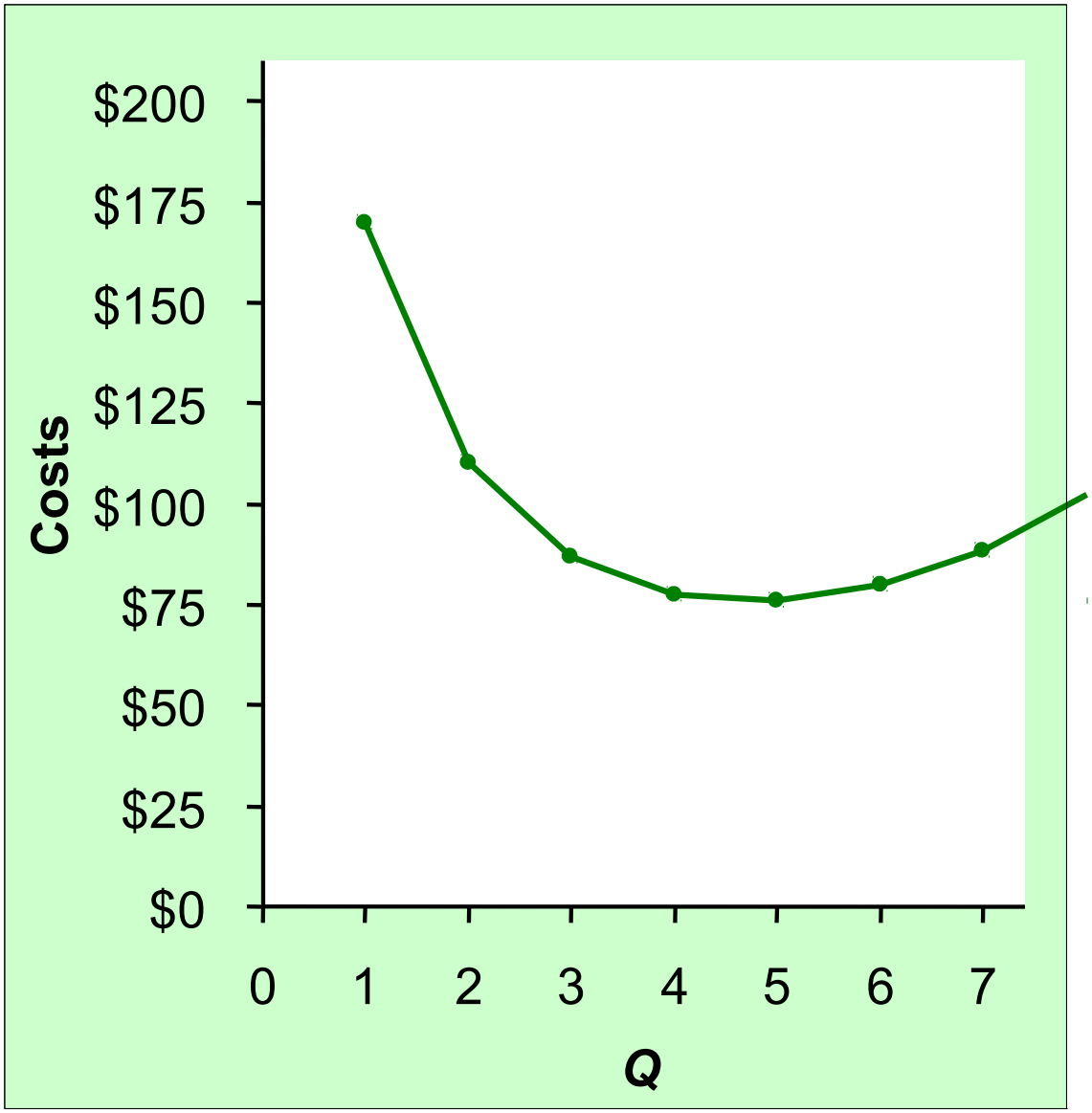
$$ATC = TC/\mathbf{Q}$$

Also,

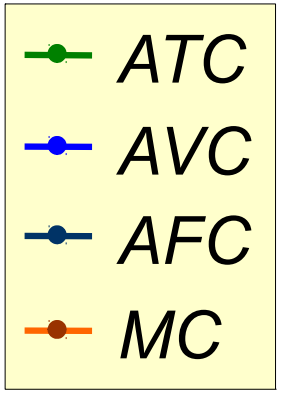
$$ATC = AFC + AVC$$

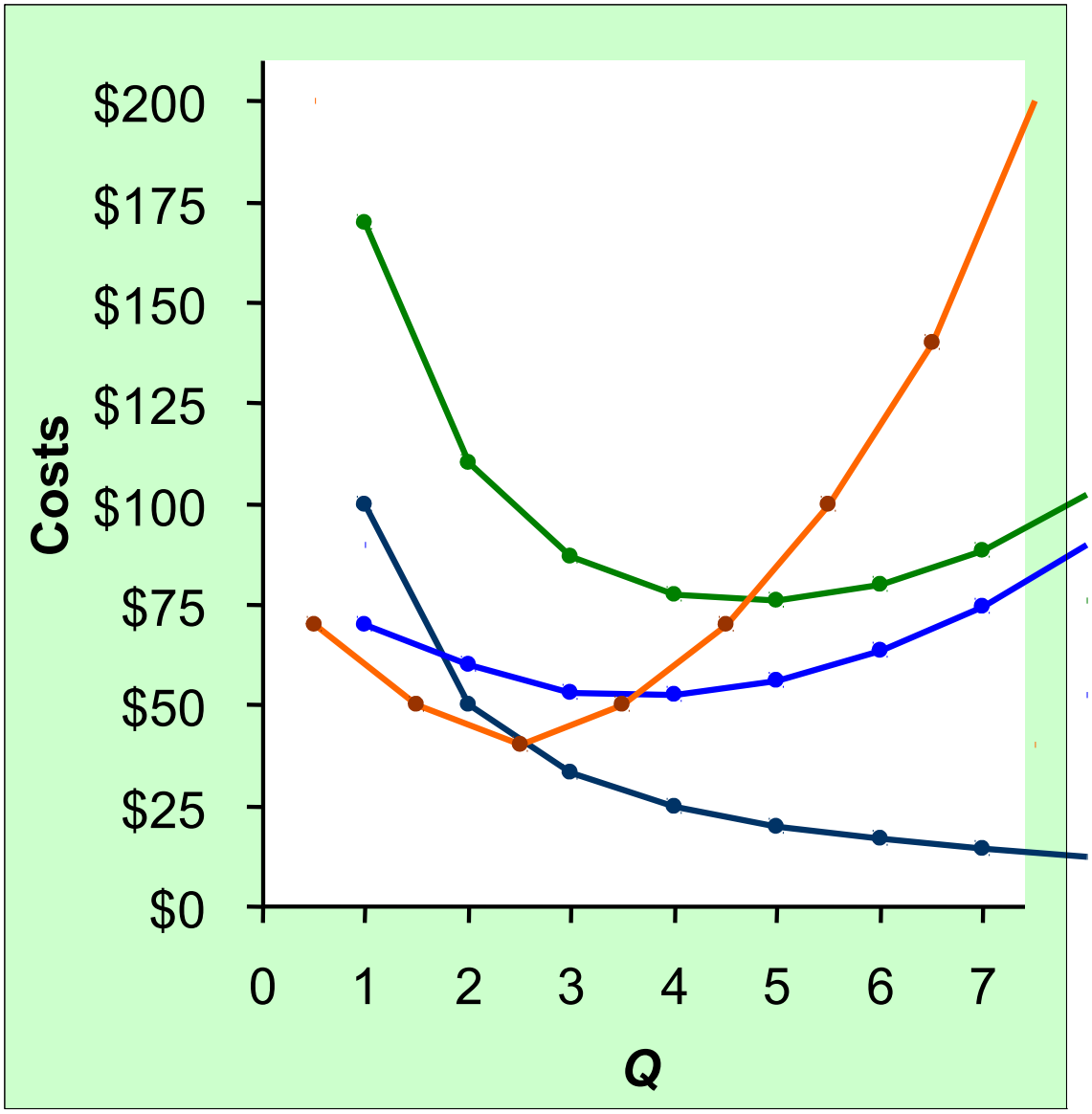
EXAMPLE 2: Average Total Cost

Q	*TC*	*ATC*
0	$100	n/a
1	170	$170
2	220	110
3	260	86.67
4	310	77.50
5	380	76
6	480	80
7	620	88.57



EXAMPLE 2: The Various Cost Curves Together





ACTIVE LEARNING 3

Calculating costs

Fill in the blank spaces of this table.

Q	*VC*	*TC*	*AFC*	*AVC*	*ATC*	*MC*
0		$50	*n/a*	*n/a*	*n/a*	
1	10			$10	$60.00	$10
2	30	80				
3			16.67	20	36.67	30
4	100	150	12.50		37.50	
5	150			30		
6	210	260	8.33	35	43.33	60

ACTIVE LEARNING 3

Answers

First, deduce *FC* = $50 and use *FC* + *VC* = *TC*.

Q	*VC*	*TC*	*AFC*	*AVC*	*ATC*	*MC*
0	$0	$50	*n/a*	*n/a*	*n/a*	
1	10	60	$50.00	$10	$60.00	$10
2	30	80	25.00	15	40.00	20
3	60	110	16.67	20	36.67	30
4	100	150	12.50	25	37.50	40
5	150	200	10.00	30	40.00	50
6	210	260	8.33	35	43.33	60

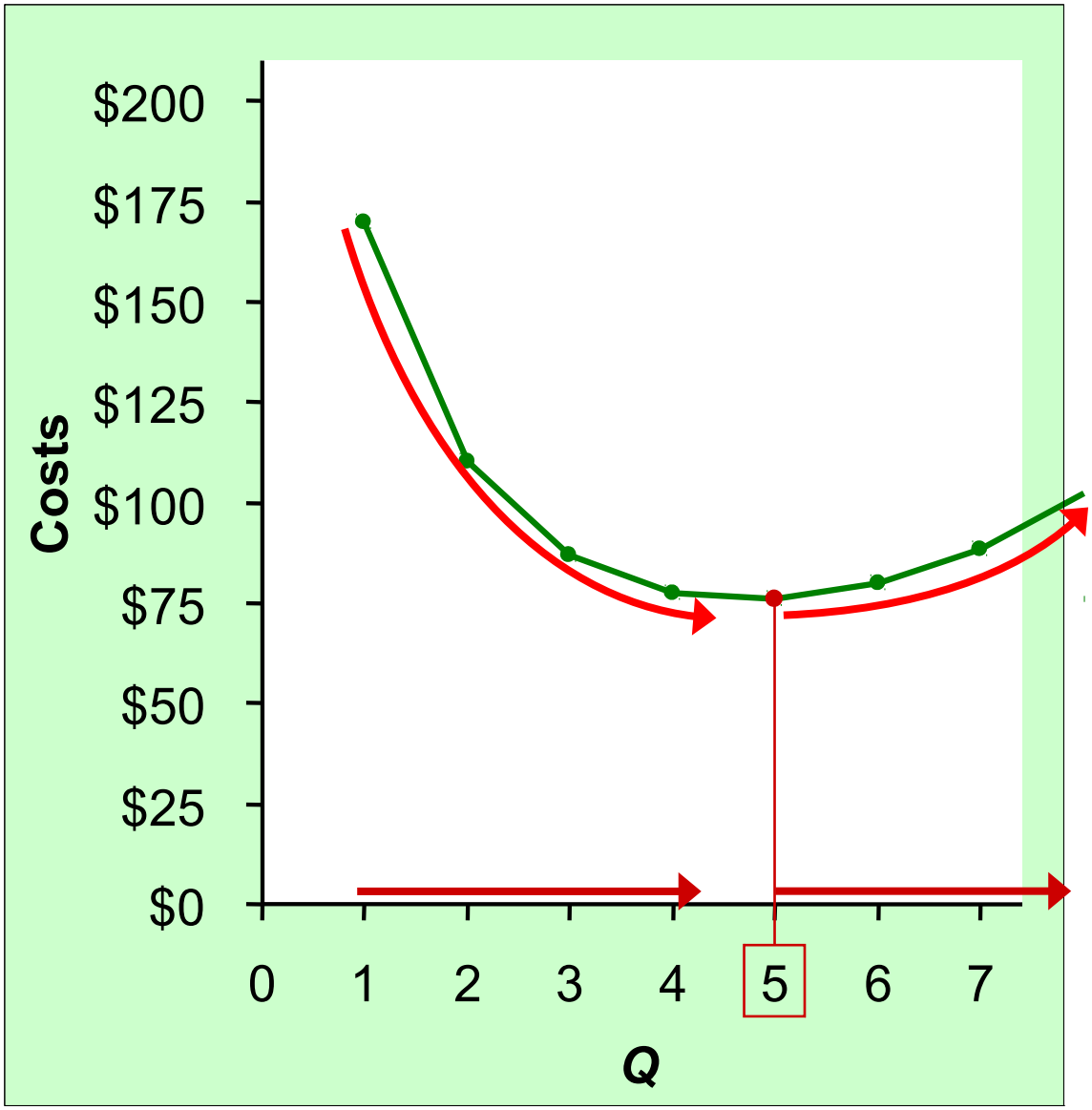
EXAMPLE 2: Why ATC Is Usually U-Shaped

As ***Q*** rises:

Initially,
falling *AFC*
pulls *ATC* down.

Eventually,
rising *AVC*
pulls *ATC* up.

Efficient scale:
The quantity that
minimizes ATC.

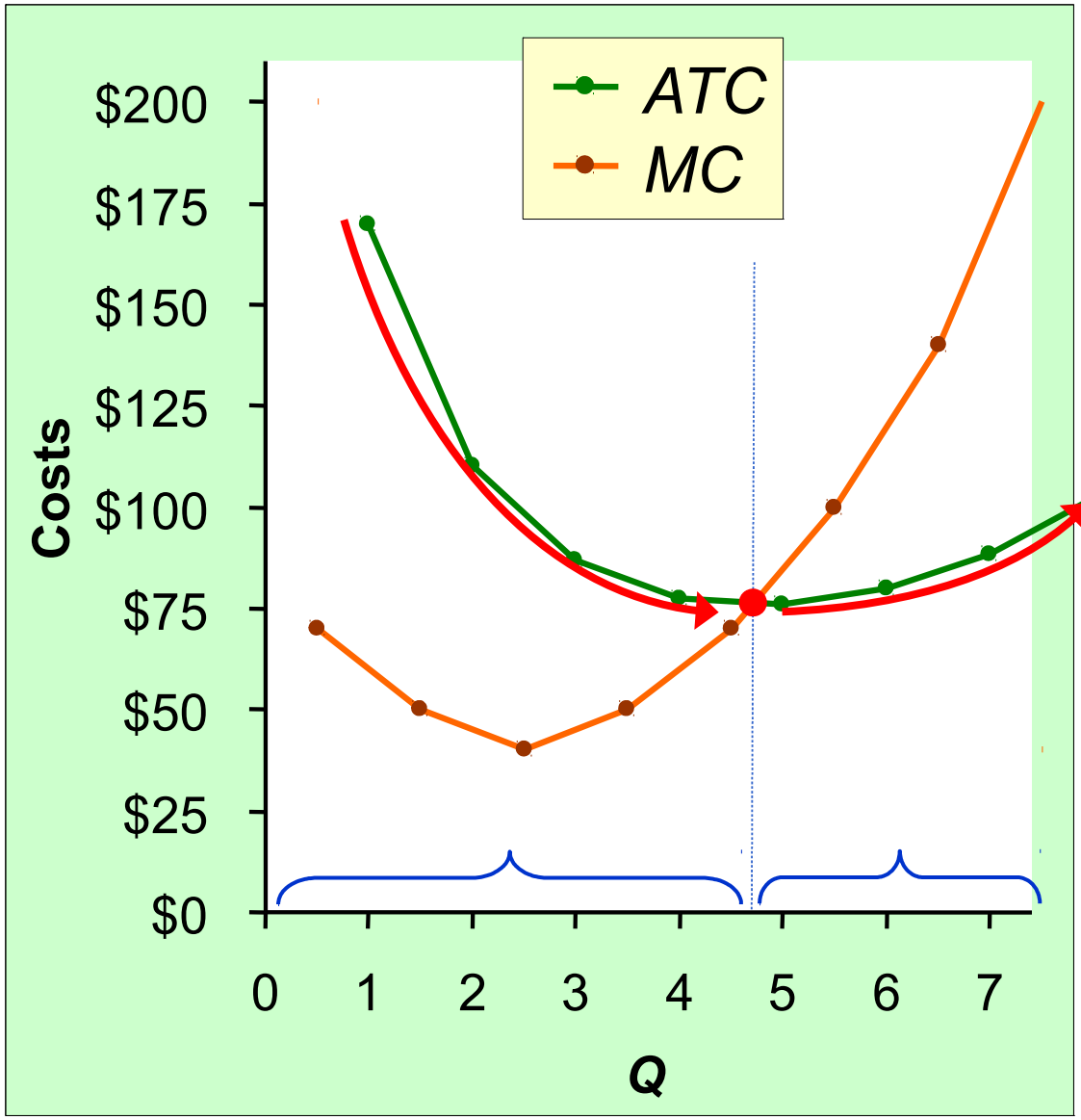


EXAMPLE 2: ATC and MC

When *MC* < *ATC*, *ATC* is falling.

When *MC* > *ATC*, *ATC* is rising.

The *MC* curve crosses the *ATC* curve at the *ATC* curve's minimum.

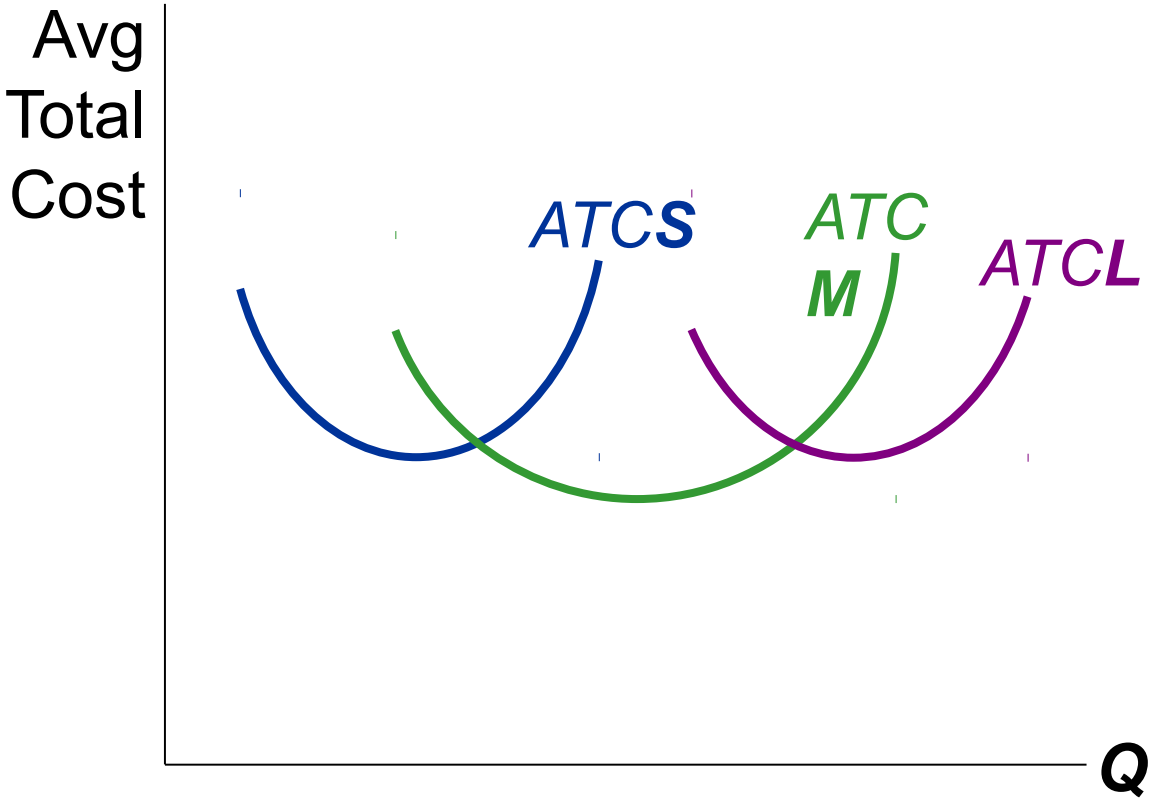


EXAMPLE 3: LRATC with 3 factory sizes

Firm can choose from three factory sizes: **S**, **M**, **L**.

Each size has its own *SRATC* curve.

The firm can change to a different factory size in the long run, but not in the short run.

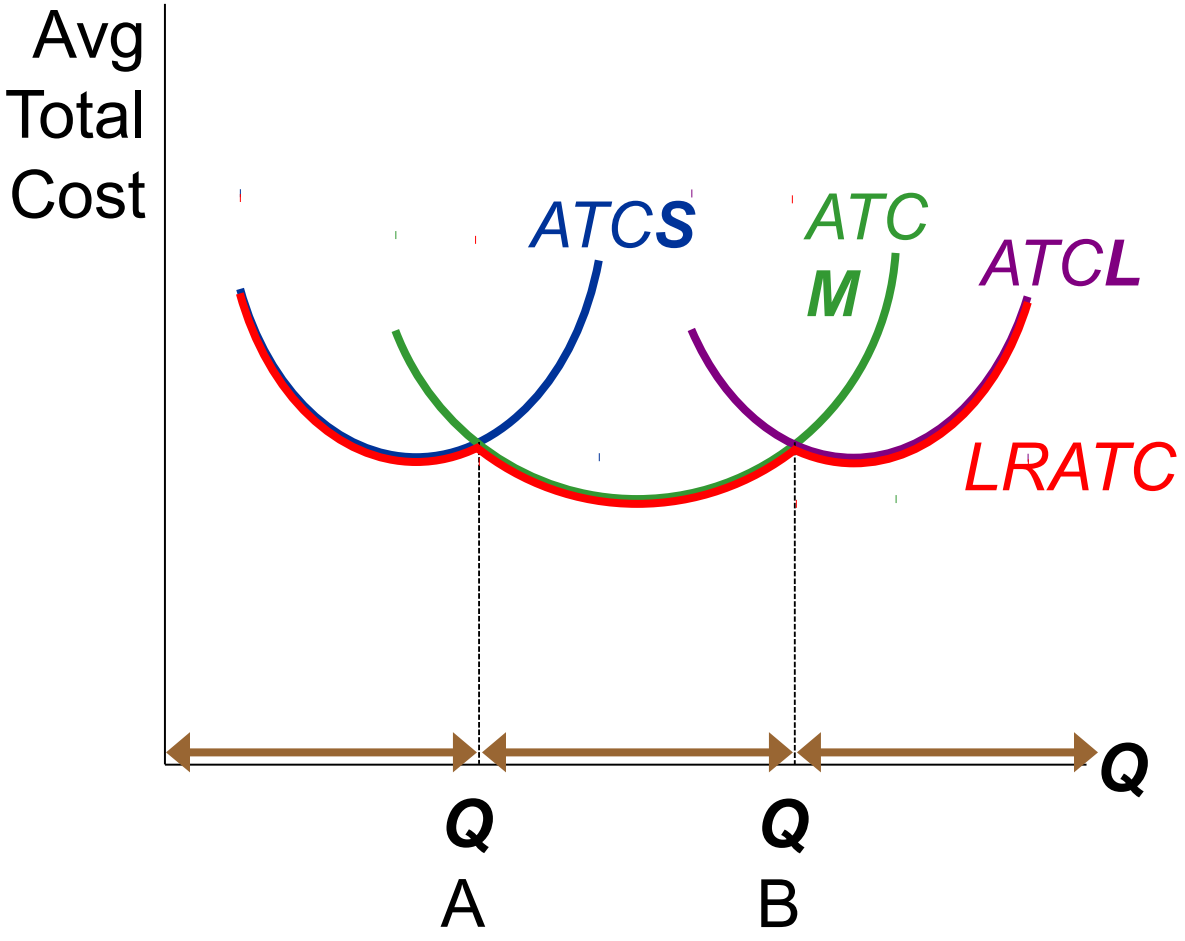


EXAMPLE 3: LRATC with 3 factory sizes

To produce less than ***Q***A, firm will choose size **S** in the long run.

To produce between ***Q***A and ***Q***B, firm will choose size **M** in the long run.

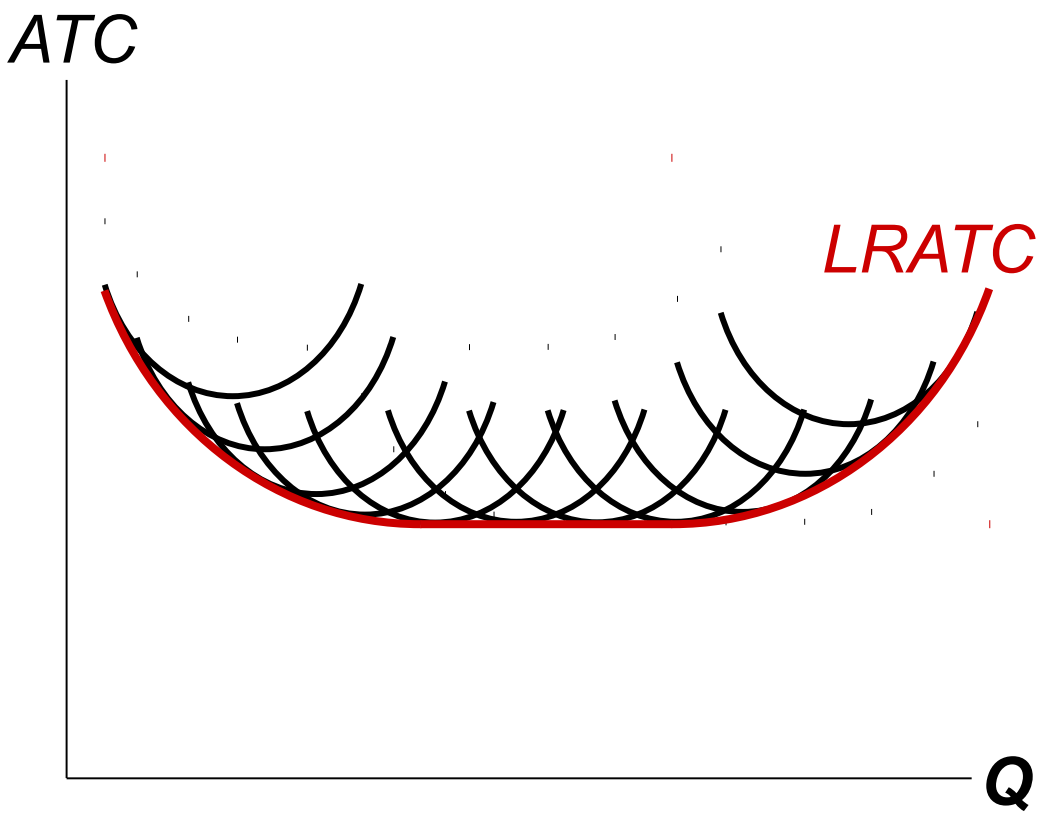
To produce more than ***Q***B, firm will choose size **L** in the long run.



A Typical LRATC Curve

In the real world, factories come in many sizes, each with its own *SRATC* curve.

So a typical *LRATC* curve looks like this:

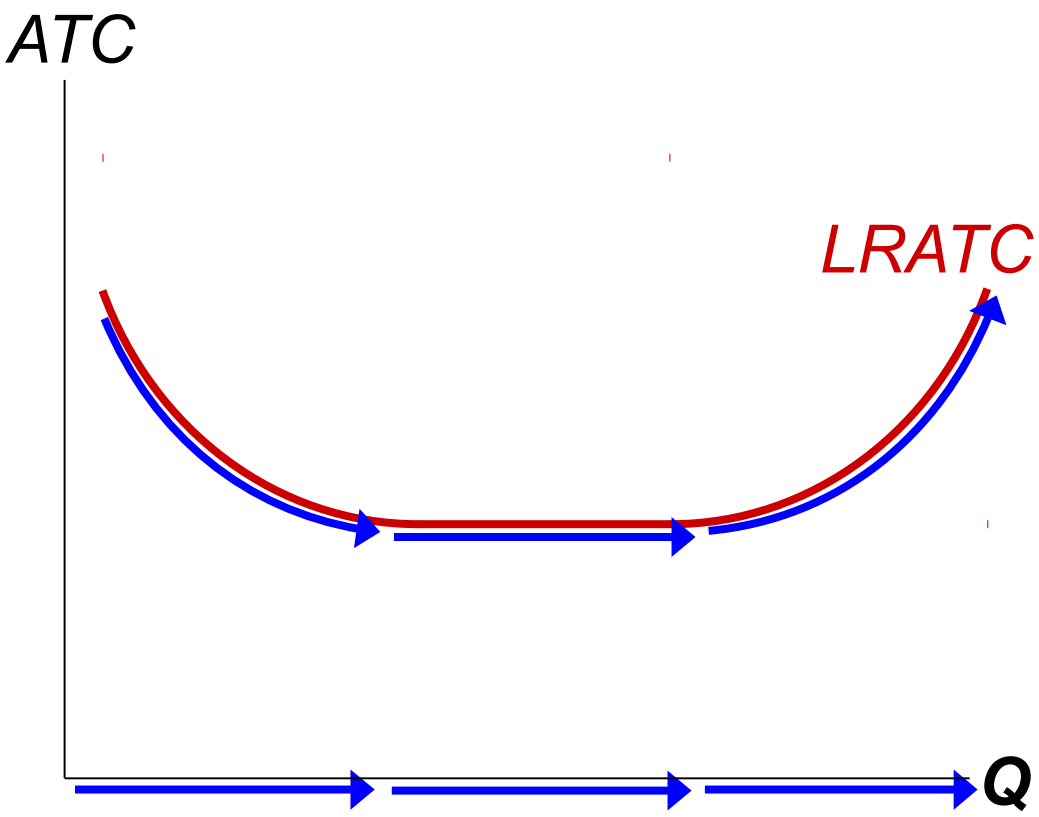


How ATC Changes as the Scale of Production Changes

Economies of scale: *ATC* falls as ***Q*** increases.

Constant returns to scale: *ATC* stays the same as ***Q*** increases.

Diseconomies of scale: *ATC* rises as ***Q*** increases.



How ATC Changes as the Scale of Production Changes

Economies of scale occur when increasing production allows greater specialization:
workers are more efficient when focusing on a narrow task.
More common when ***Q*** is low.

Diseconomies of scale are due to coordination problems in large organizations.
E.g., management becomes stretched, can't control costs.
More common when ***Q*** is high.

Summary

- Implicit costs do not involve a cash outlay, yet are just as important as explicit costs to firms' decisions.
- Accounting profit is revenue minus explicit costs. Economic profit is revenue minus total (explicit + implicit) costs.
- The production function shows the relationship between output and inputs.

Summary

- The marginal product of labor is the increase in output from a one-unit increase in labor, holding other inputs constant. The marginal products of other inputs are defined similarly.
- Marginal product usually diminishes as the input increases. Thus, as output rises, the production function becomes flatter and the total cost curve becomes steeper.
- Variable costs vary with output; fixed costs do not.

Summary

- Marginal cost is the increase in total cost from an extra unit of production. The *MC* curve is usually upward-sloping.
- Average variable cost is variable cost divided by output.
- Average fixed cost is fixed cost divided by output. *AFC* always falls as output increases.
- Average total cost (sometimes called “cost per unit”) is total cost divided by the quantity of output. The *ATC* curve is usually U-shaped.

Summary

- The *MC* curve intersects the *ATC* curve at minimum average total cost.
  When *MC* < *ATC*, *ATC* falls as *Q* rises.
  When *MC* > *ATC*, *ATC* rises as *Q* rises.
- In the long run, all costs are variable.
- Economies of scale: *ATC* falls as *Q* rises.
  Diseconomies of scale: *ATC* rises as *Q* rises.
  Constant returns to scale: *ATC* remains constant as *Q* rises.