

A woman's silhouette is shown from the back, looking at a display of sunglasses on shelves. The shelves are filled with various styles and colors of sunglasses, including aviators, wrap-around styles, and classic frames. The background is bright, creating a high-contrast silhouette of the woman.

INTERMEDIATE

MICROECONOMICS

NINTH EDITION

HAL R. VARIAN

## Chapter 2

# Budget Constraint

# Consumption Choice Sets

- ◆ **A consumption choice set is the collection of all consumption choices available to the consumer.**
- ◆ **What constrains consumption choice?**
  - **Budgetary, time and other resource limitations.**

# Budget Constraints

- ◆ **A consumption bundle containing  $x_1$  units of commodity 1,  $x_2$  units of commodity 2 and so on up to  $x_n$  units of commodity  $n$  is denoted by the vector  $(x_1, x_2, \dots, x_n)$ .**
- ◆ **Commodity prices are  $p_1, p_2, \dots, p_n$ .**

# Budget Constraints

- ◆ **Q: When is a consumption bundle  $(x_1, \dots, x_n)$  affordable at given prices  $p_1, \dots, p_n$ ?**

# Budget Constraints

◆ **Q: When is a bundle  $(x_1, \dots, x_n)$  affordable at prices  $p_1, \dots, p_n$ ?**

◆ **A: When**

$$p_1x_1 + \dots + p_nx_n \leq m$$

**where  $m$  is the consumer's (disposable) income.**

# Budget Constraints

- ◆ **The bundles that are only just affordable form the consumer's budget constraint. This is the set**

$$\{ (x_1, \dots, x_n) \mid x_1 \geq 0, \dots, x_n \geq 0 \text{ and } p_1 x_1 + \dots + p_n x_n = m \}.$$

# Budget Constraints

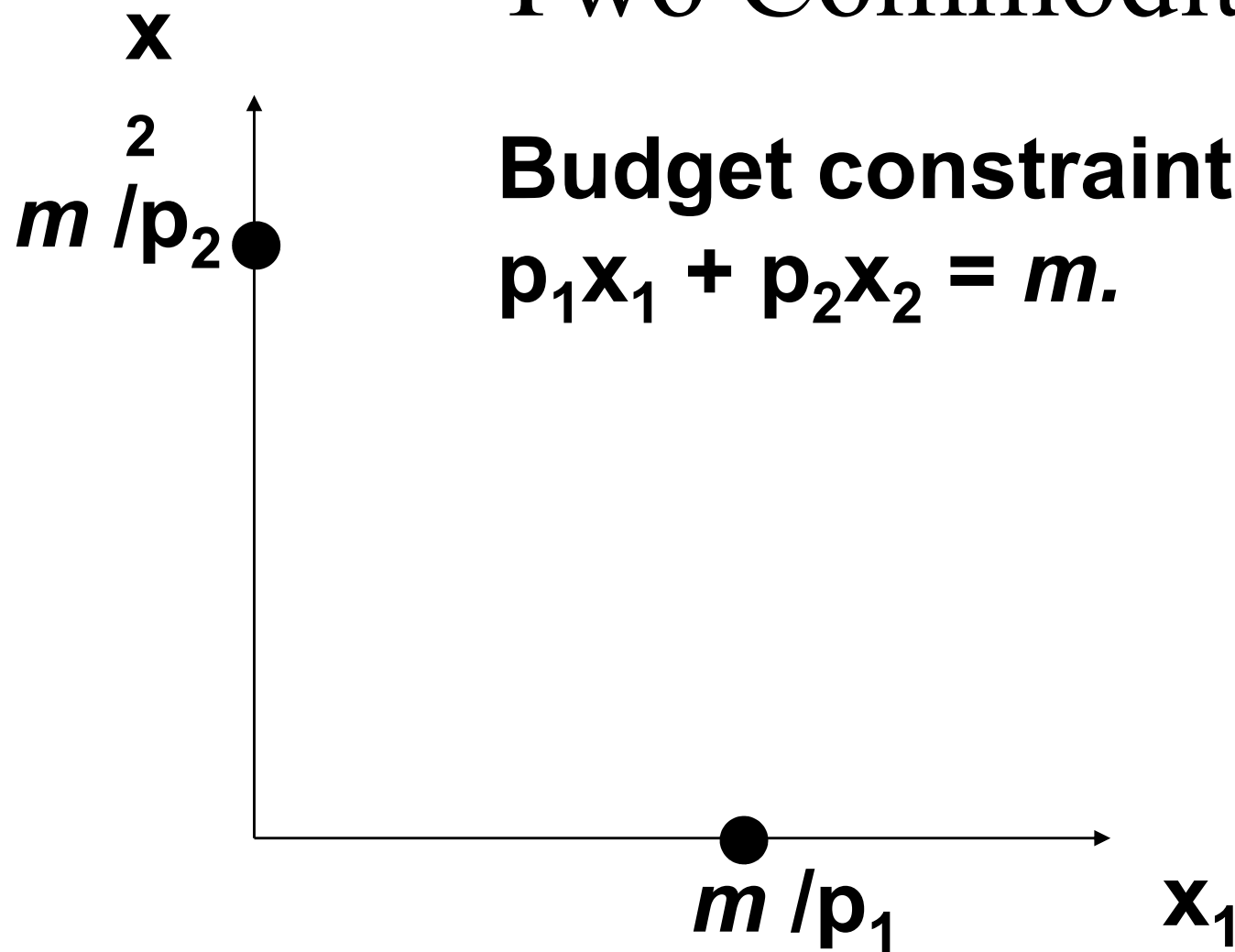
- ◆ **The consumer's budget set is the set of all affordable bundles;**

$$B(p_1, \dots, p_n, m) =$$

$$\{ (x_1, \dots, x_n) \mid x_1 \geq 0, \dots, x_n \geq 0 \text{ and} \\ p_1x_1 + \dots + p_nx_n \leq m \}$$

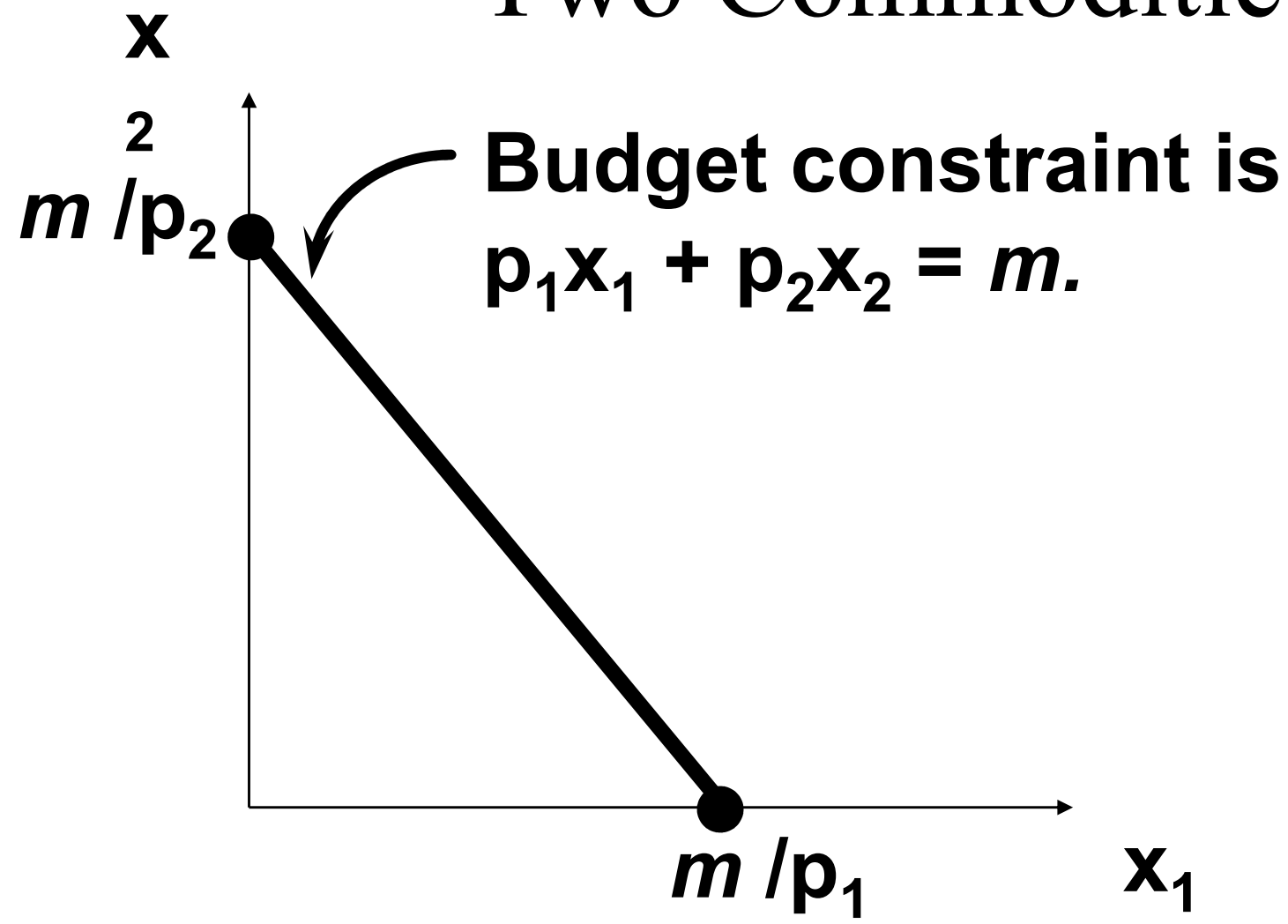
- ◆ **The budget constraint is the upper boundary of the budget set.**

# Budget Set and Constraint for Two Commodities

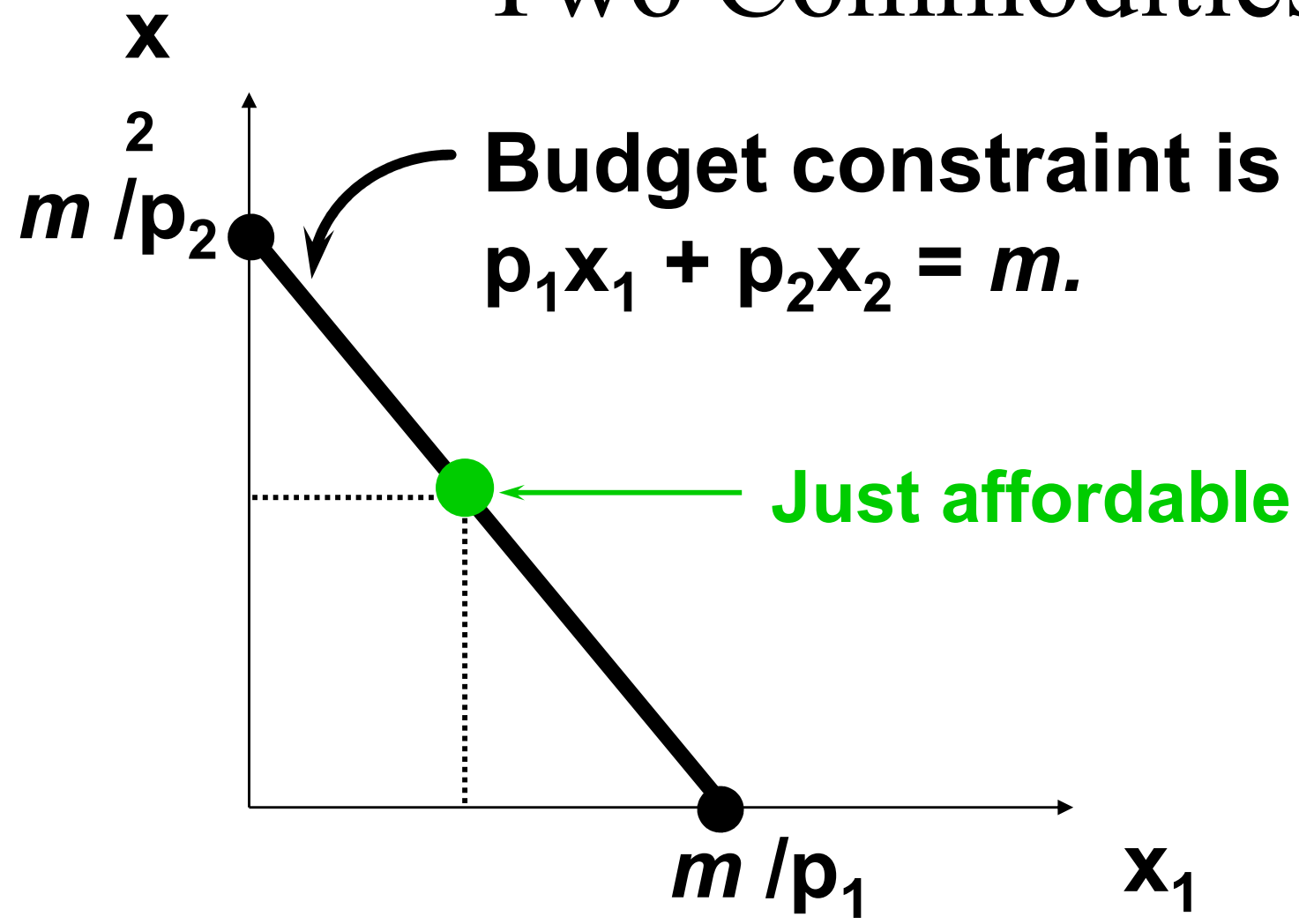




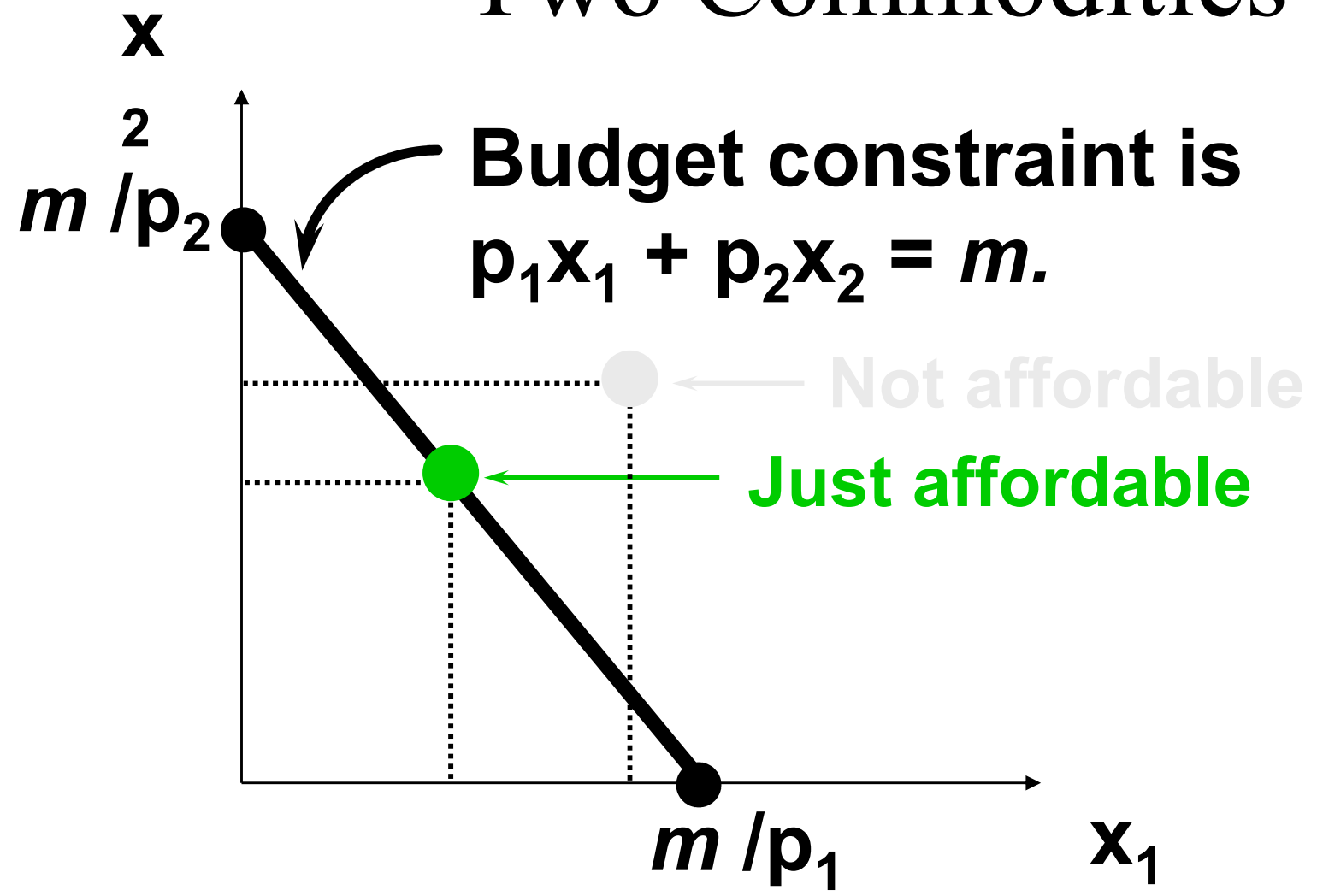
# Budget Set and Constraint for Two Commodities



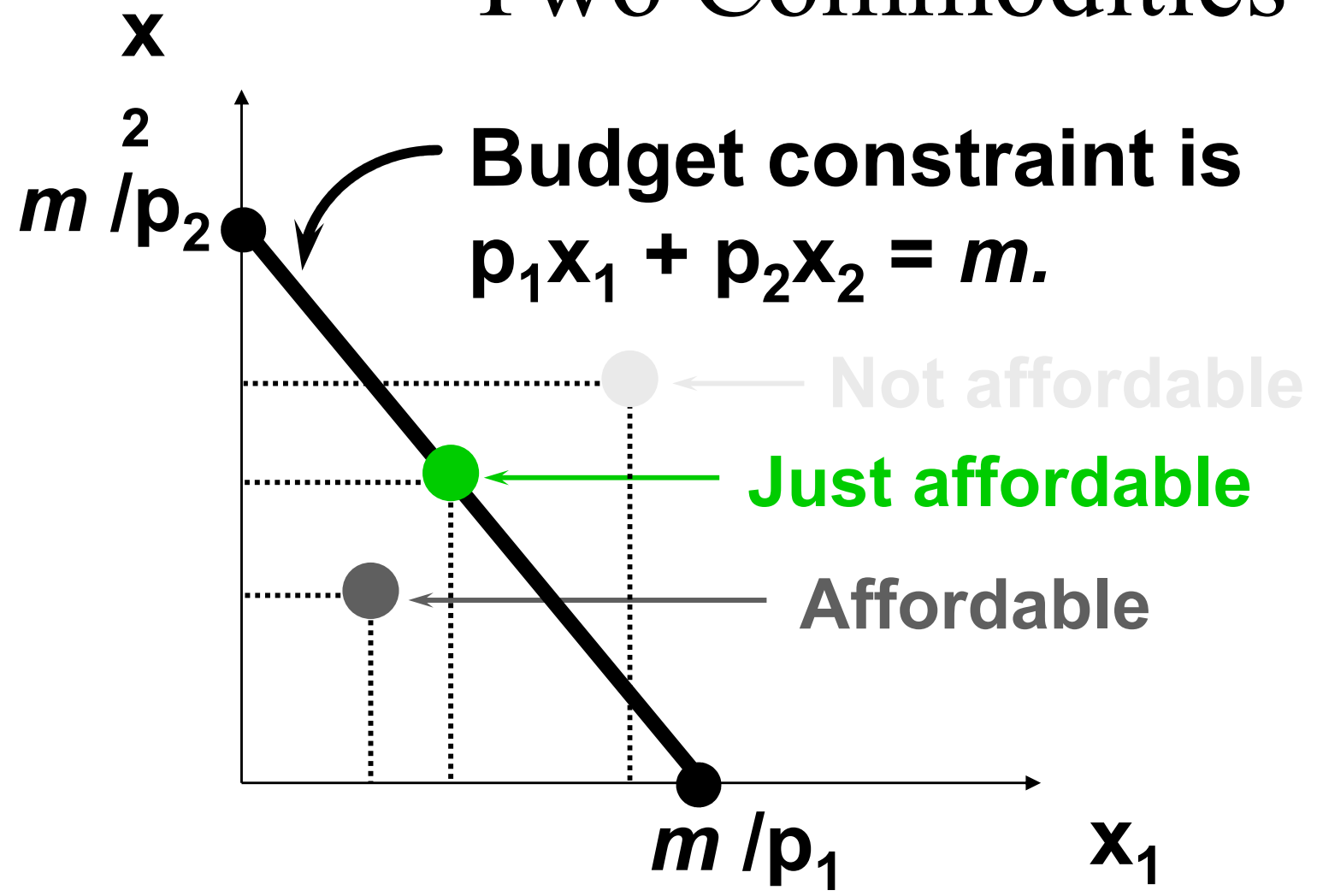
# Budget Set and Constraint for Two Commodities



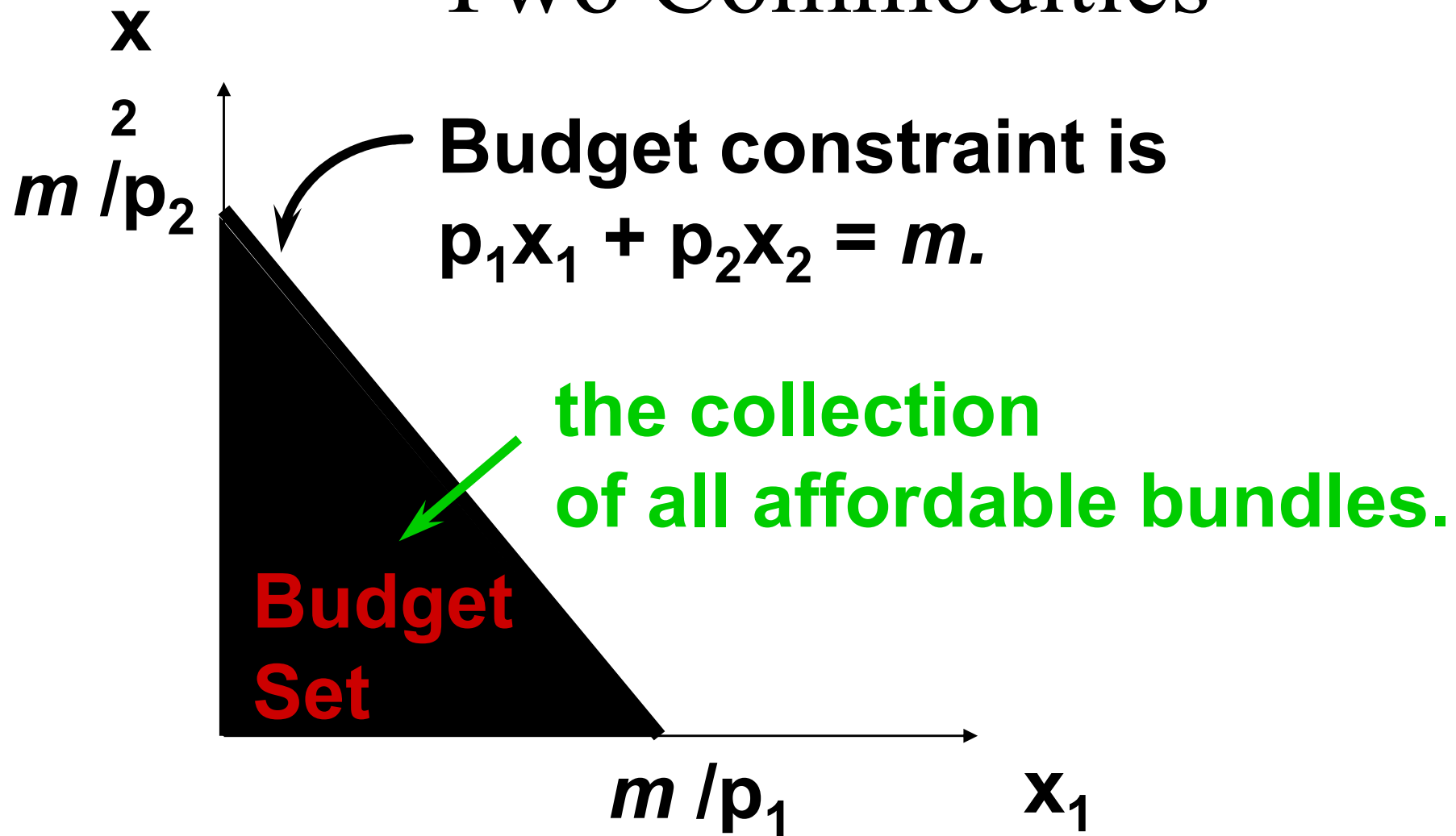
# Budget Set and Constraint for Two Commodities



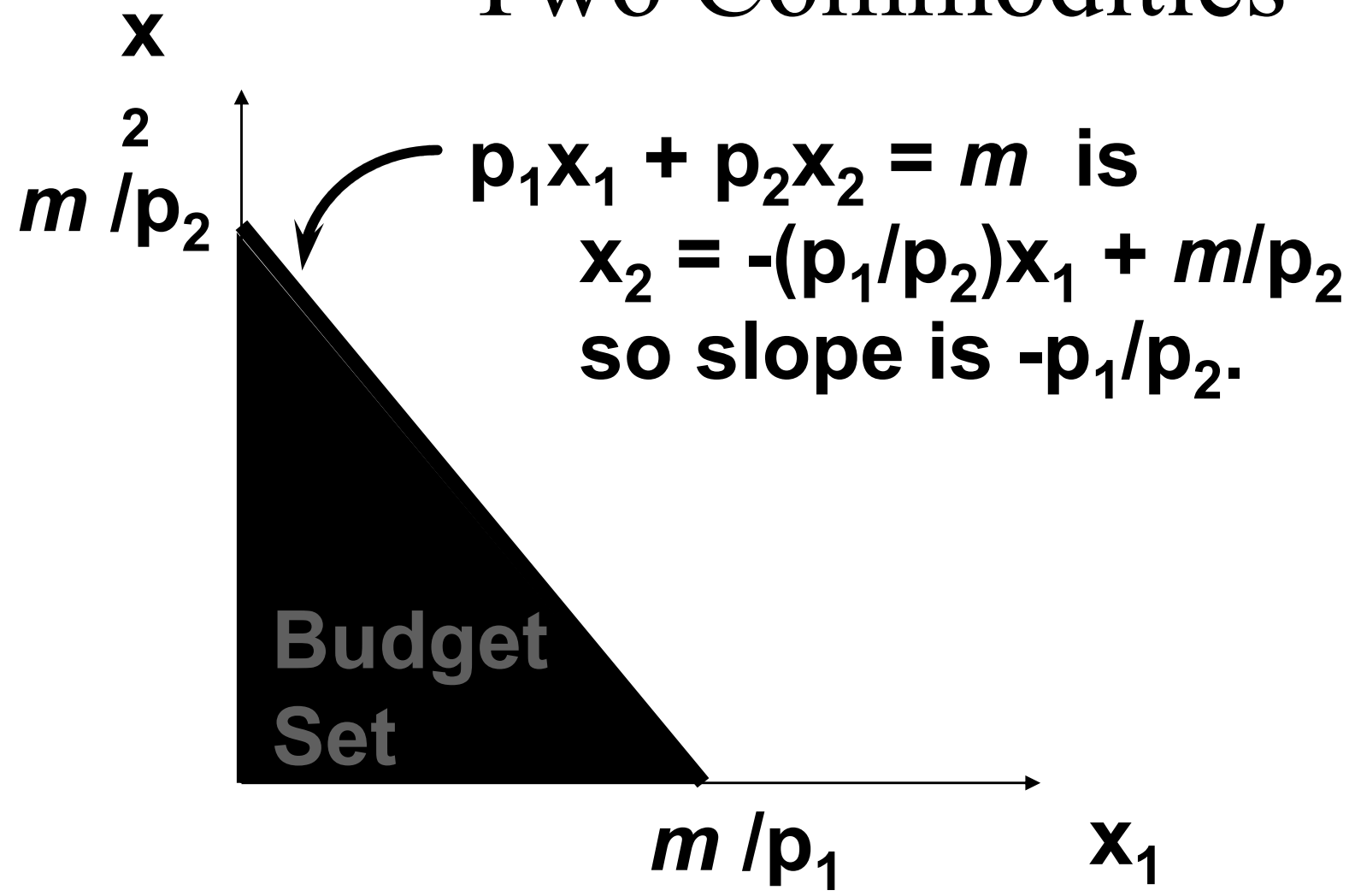
# Budget Set and Constraint for Two Commodities



# Budget Set and Constraint for Two Commodities



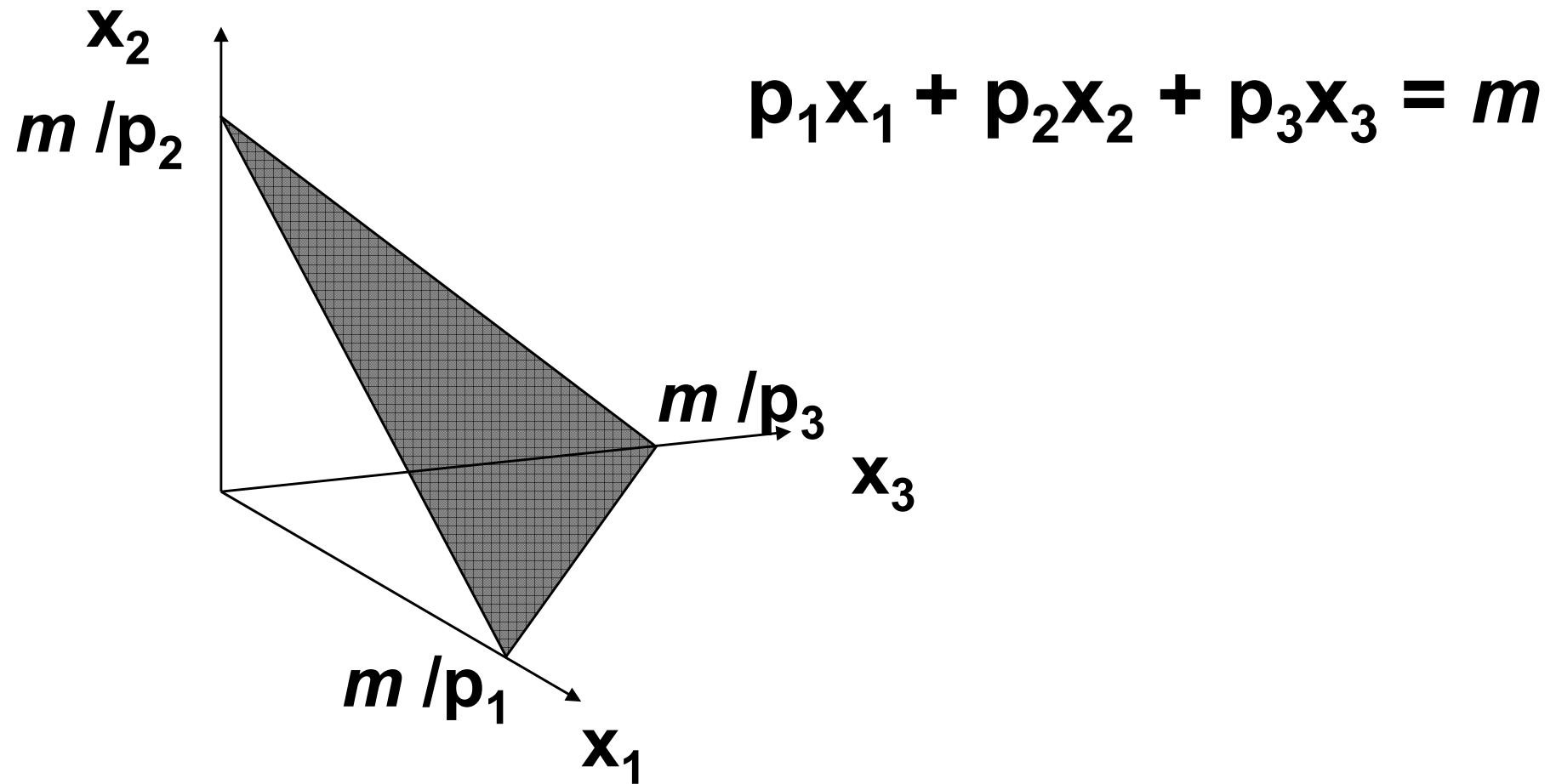
# Budget Set and Constraint for Two Commodities



# Budget Constraints

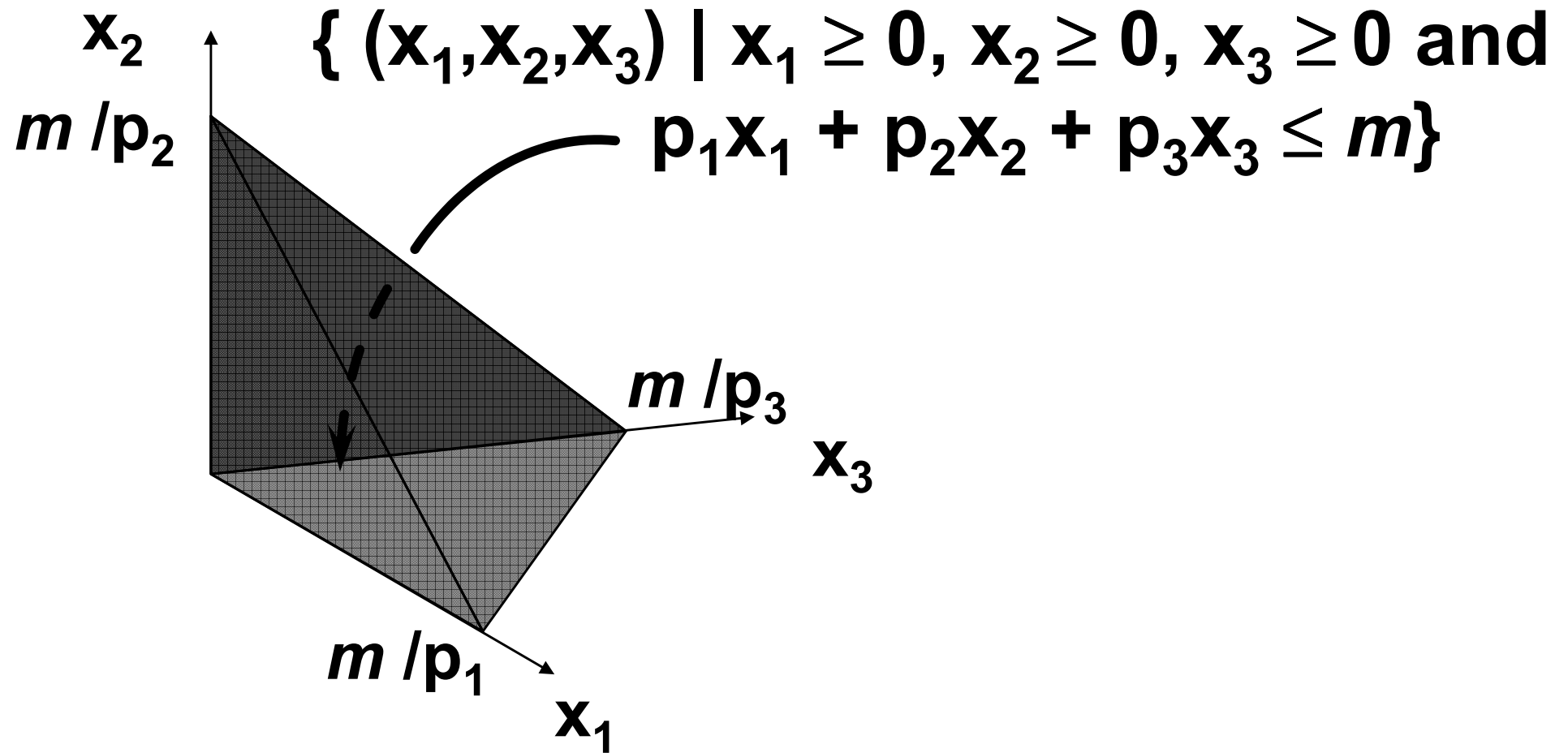
- ◆ **If  $n = 3$  what do the budget constraint and the budget set look like?**

# Budget Constraint for Three Commodities





# Budget Set for Three Commodities



# Budget Constraints

- ◆ For  $n = 2$  and  $x_1$  on the horizontal axis, the constraint's slope is  $-p_1/p_2$ .  
What does it mean?

\_\_\_\_\_

\_\_\_\_\_

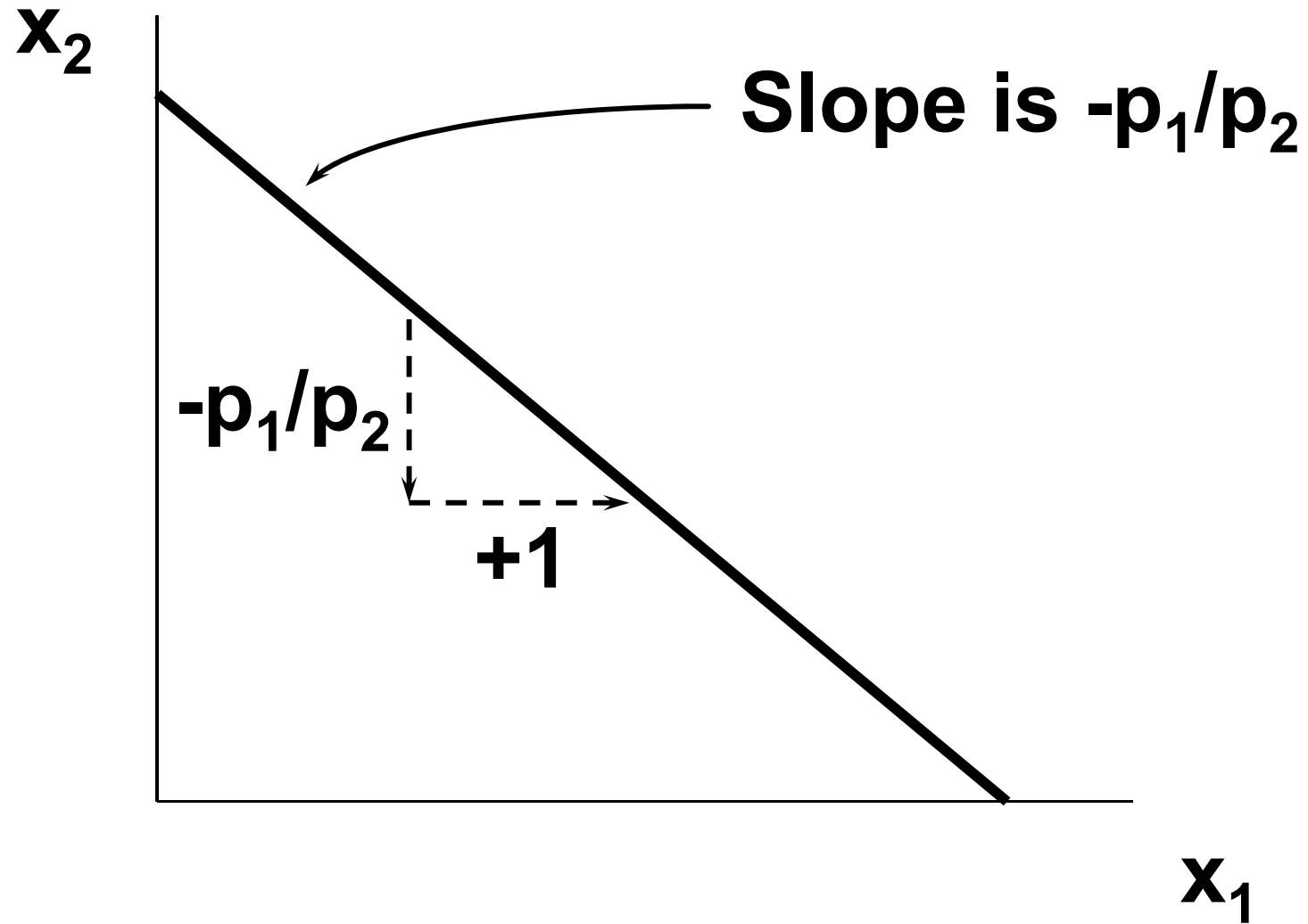
# Budget Constraints

- ◆ For  $n = 2$  and  $x_1$  on the horizontal axis, the constraint's slope is  $-p_1/p_2$ .  
What does it mean?

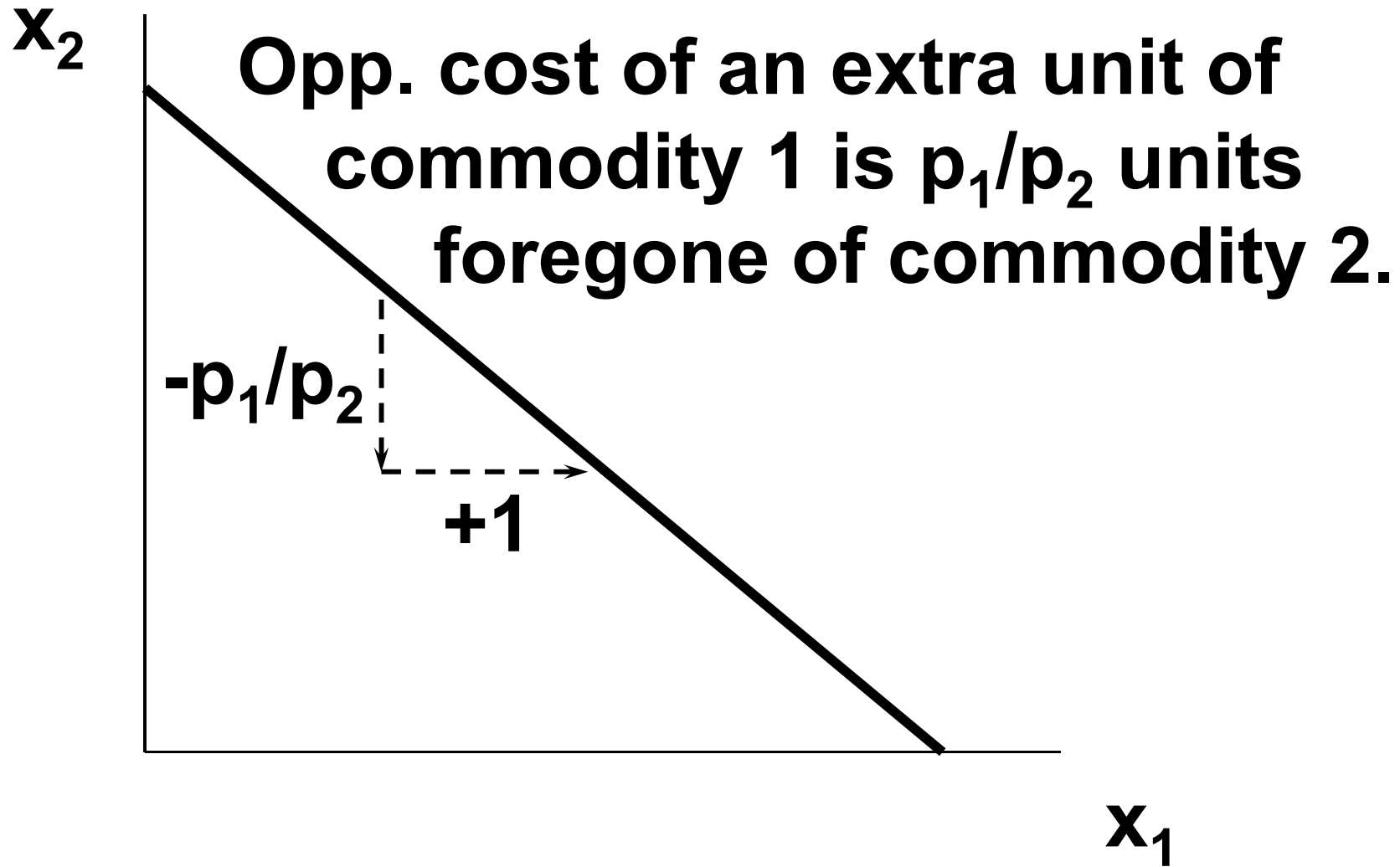
\_\_\_\_\_

- ◆ Increasing  $x_1$  by 1 must reduce  $x_2$  by  $p_1/p_2$ .

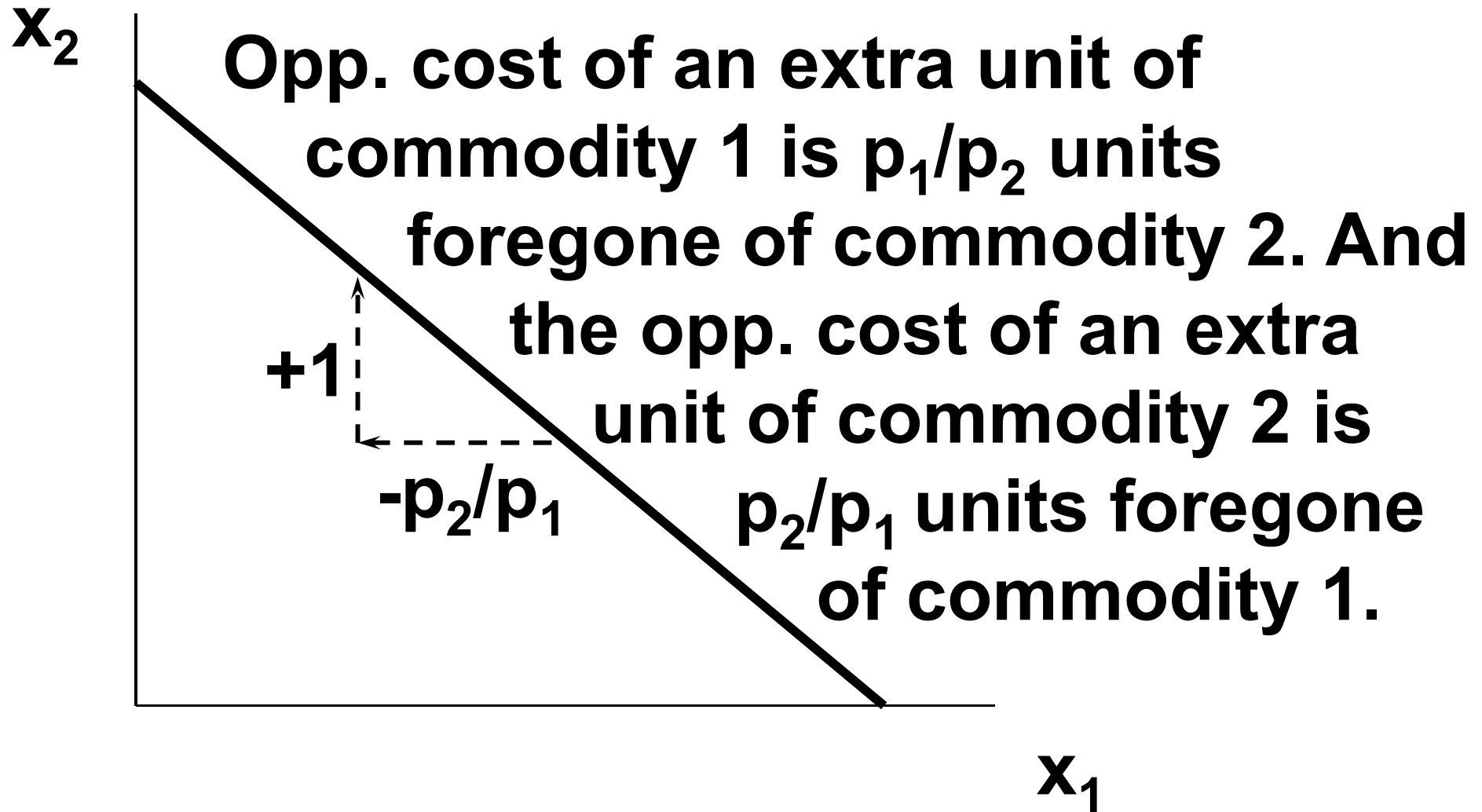
# Budget Constraints



# Budget Constraints



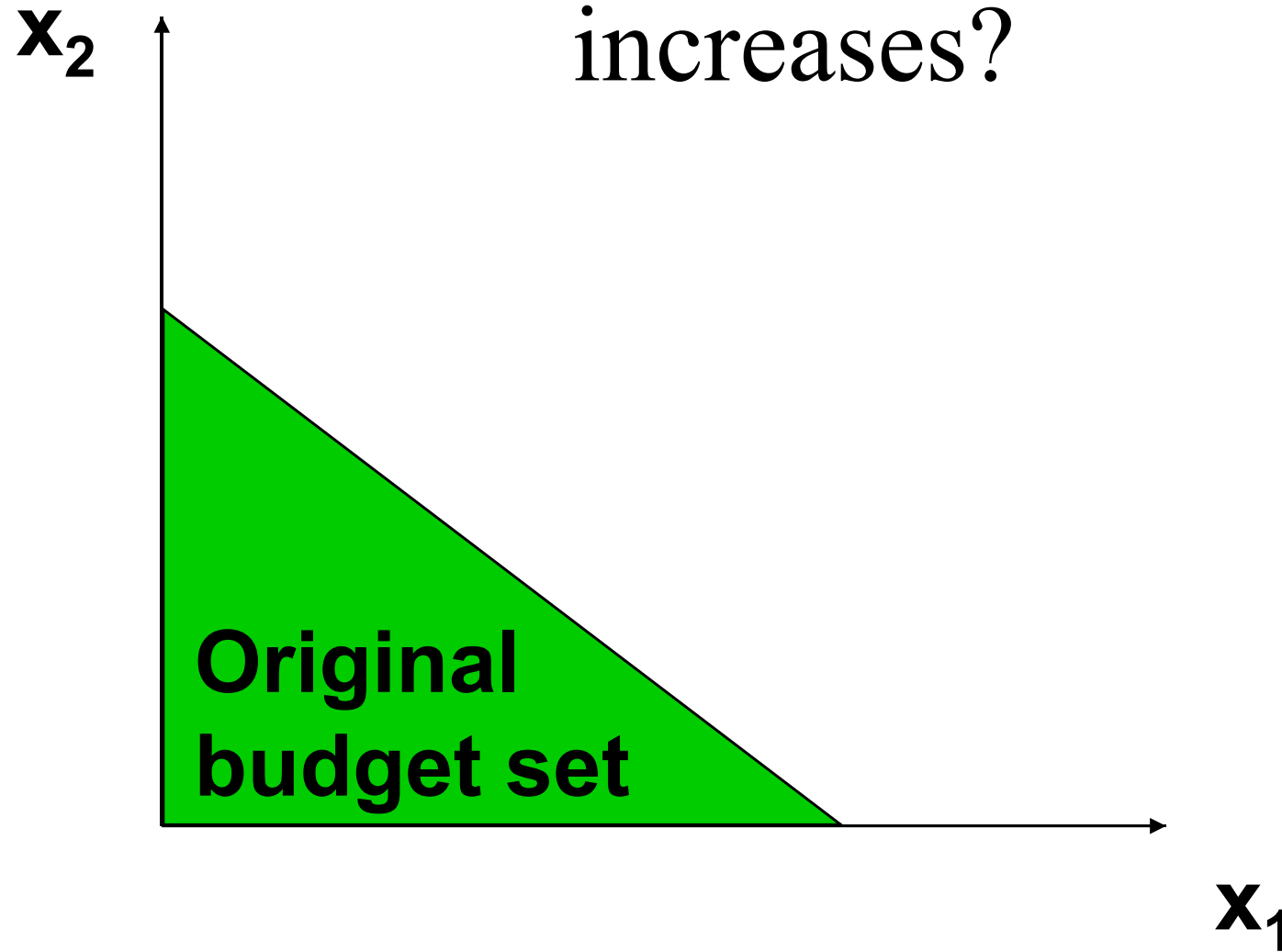
# Budget Constraints



# Budget Sets & Constraints; Income and Price Changes

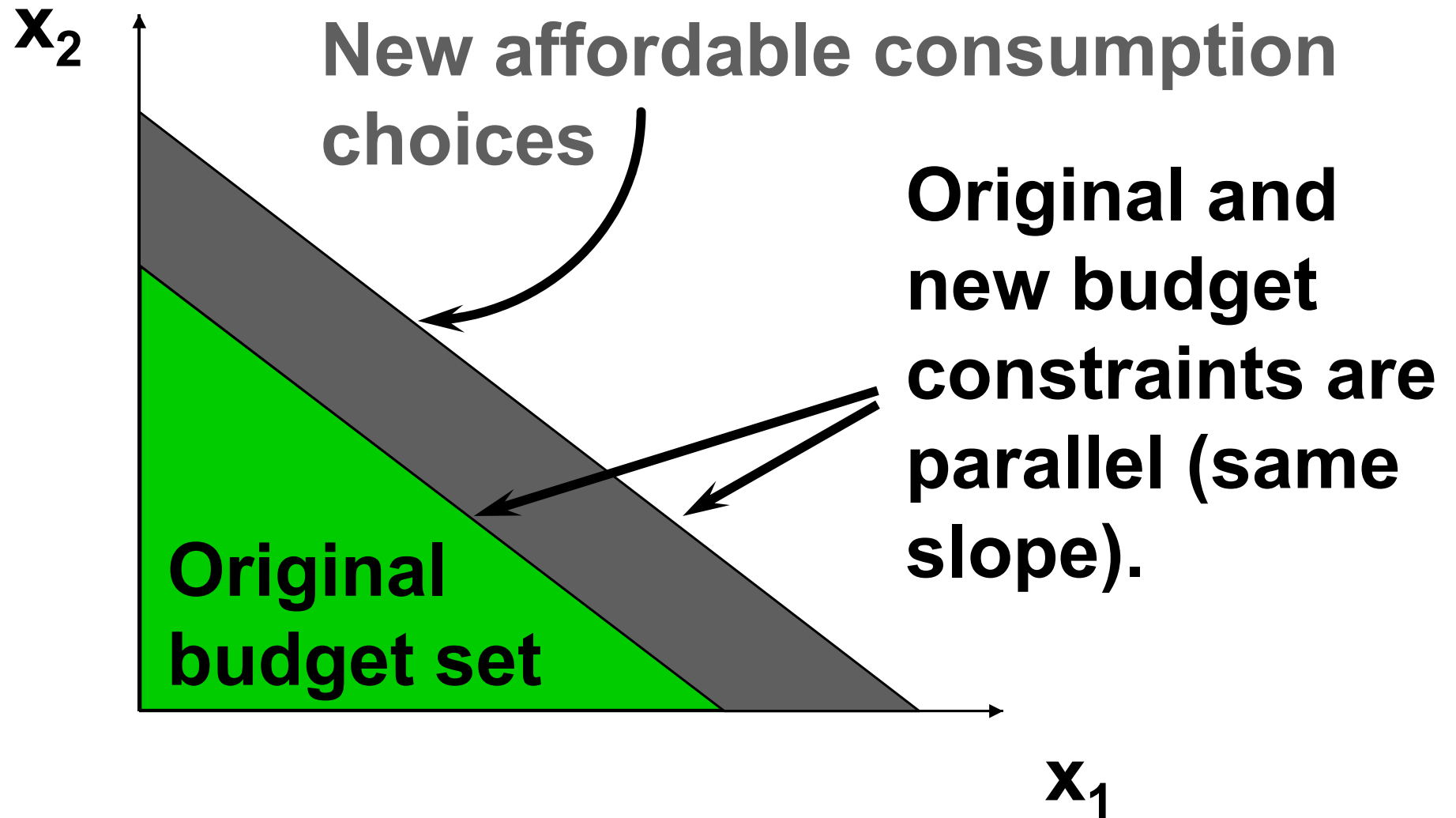
- ◆ **The budget constraint and budget set depend upon prices and income. What happens as prices or income change?**

How do the budget set and budget constraint change as income  $m$  increases?

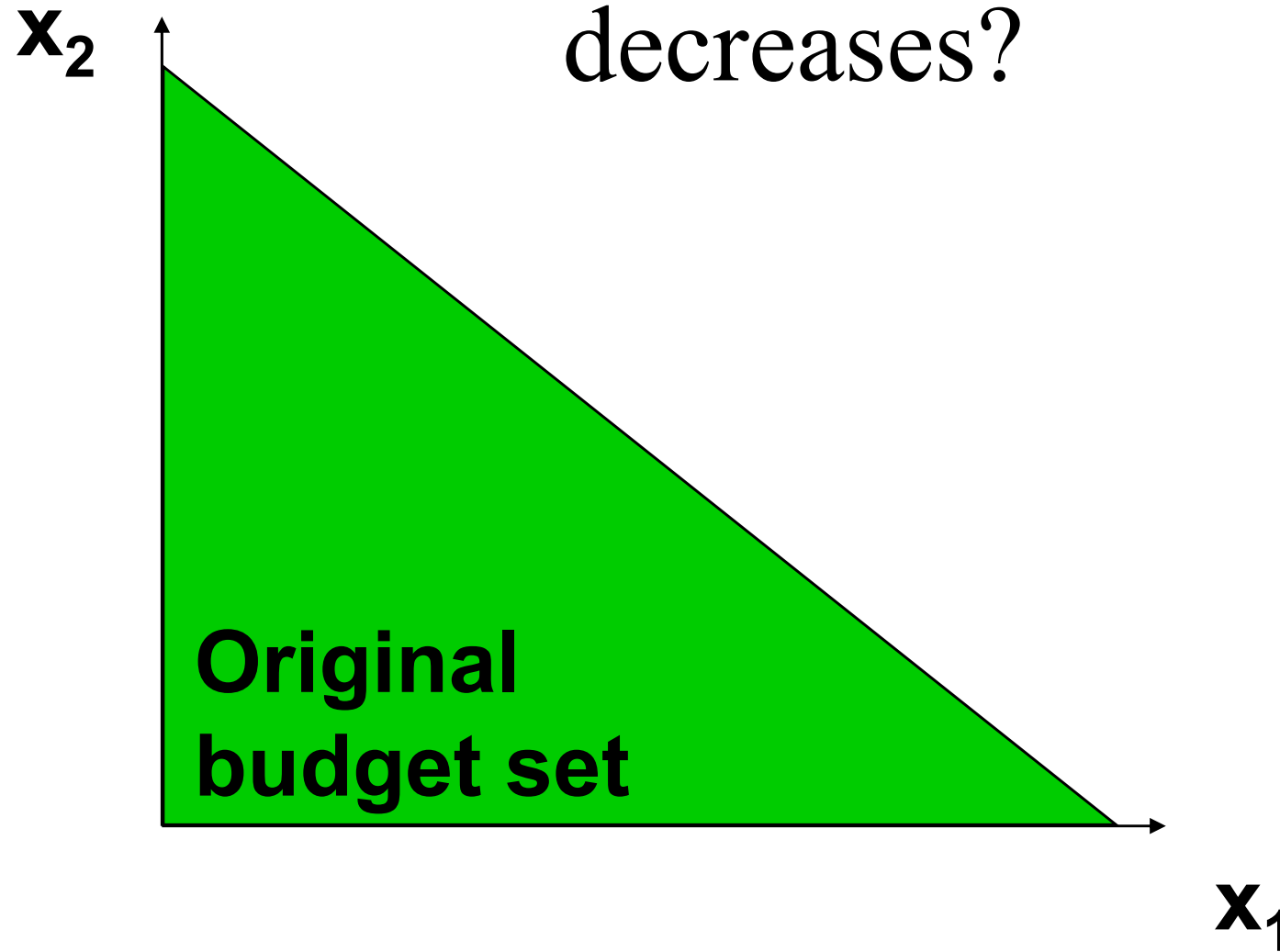




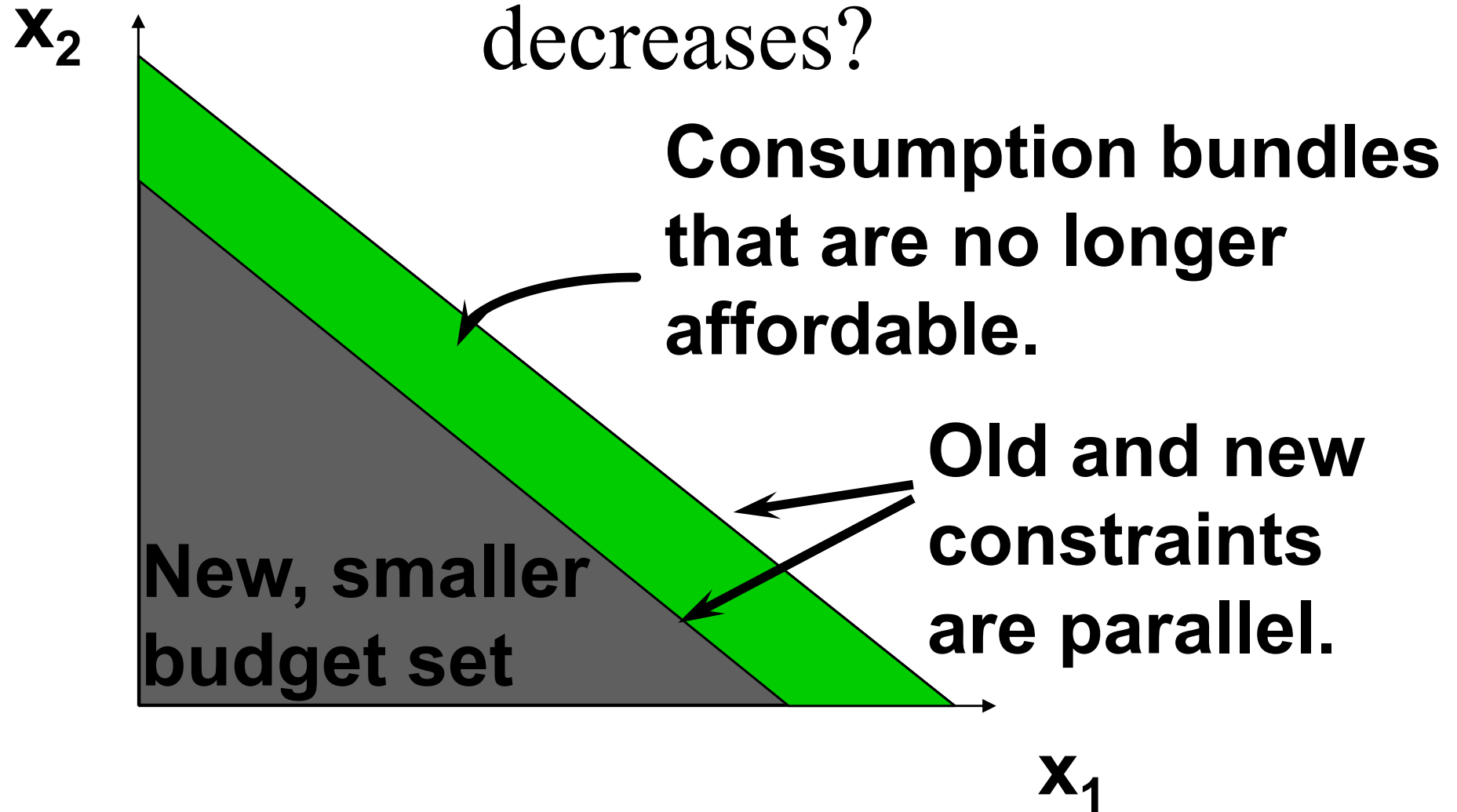
# Higher income gives more choice



How do the budget set and budget constraint change as income  $m$  decreases?



How do the budget set and budget constraint change as income  $m$  decreases?



# Budget Constraints - Income Changes

- ◆ **Increases in income  $m$  shift the constraint outward in a parallel manner, thereby enlarging the budget set and improving choice.**

# Budget Constraints - Income Changes

- ◆ **Increases in income  $m$  shift the constraint outward in a parallel manner, thereby enlarging the budget set and improving choice.**
- ◆ **Decreases in income  $m$  shift the constraint inward in a parallel manner, thereby shrinking the budget set and reducing choice.**

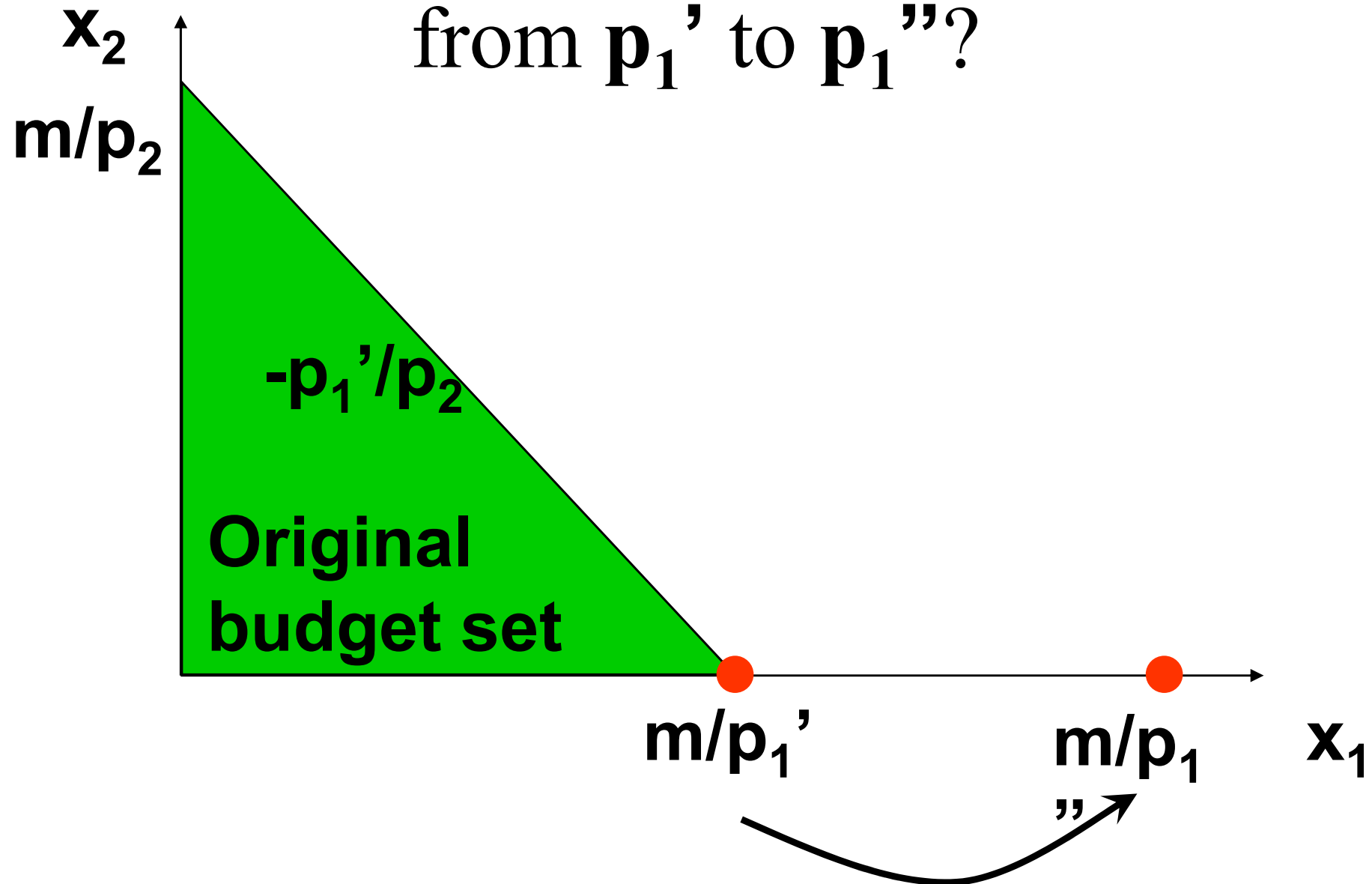
# Budget Constraints - Income Changes

- ◆ **No original choice is lost and new choices are added when income increases, so higher income cannot make a consumer worse off.**
- ◆ **An income decrease may (typically will) make the consumer worse off.**

# Budget Constraints - Price Changes

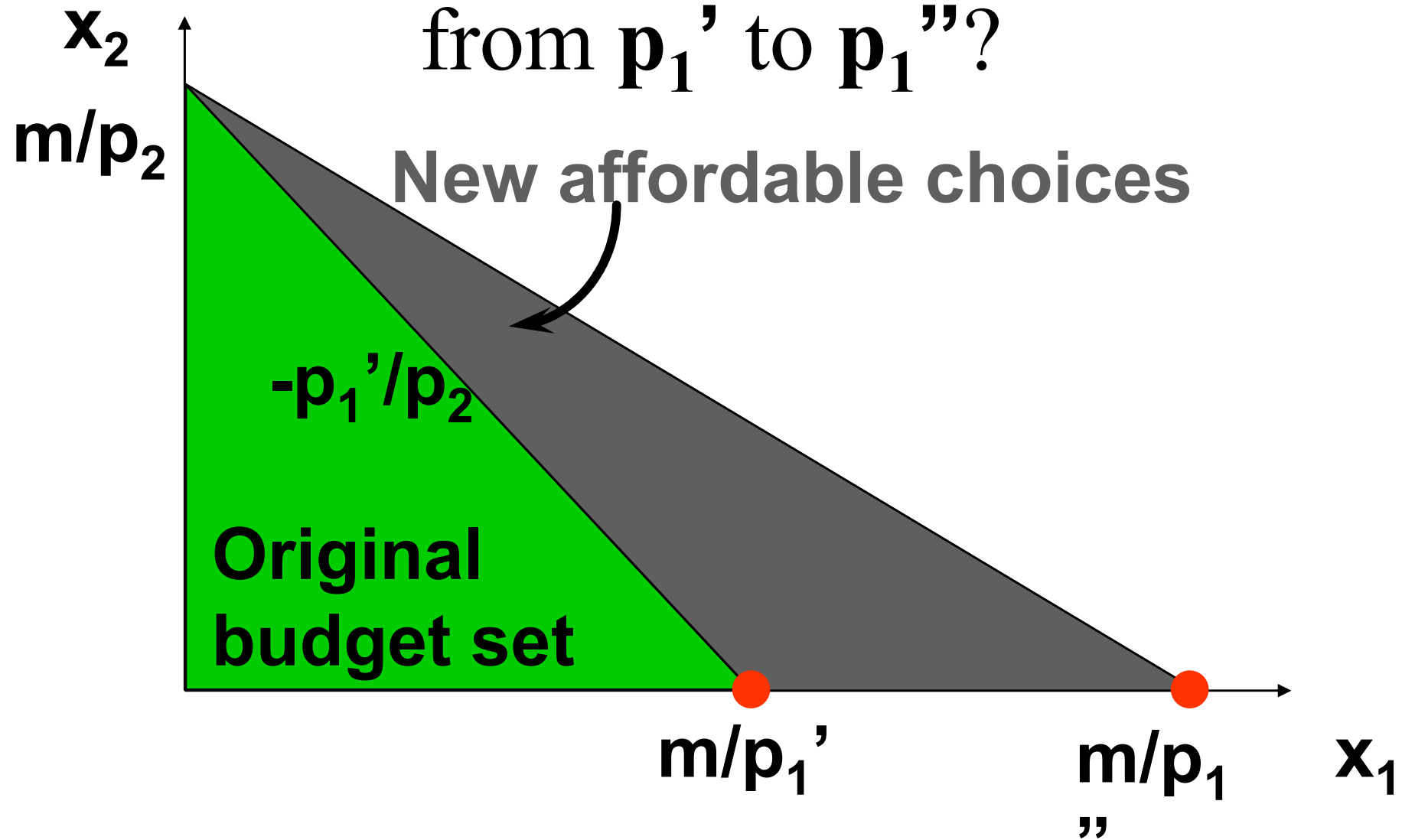
- ◆ **What happens if just one price decreases?**
- ◆ **Suppose  $p_1$  decreases.**

How do the budget set and budget constraint change as  $p_1$  decreases from  $p_1'$  to  $p_1''$ ?

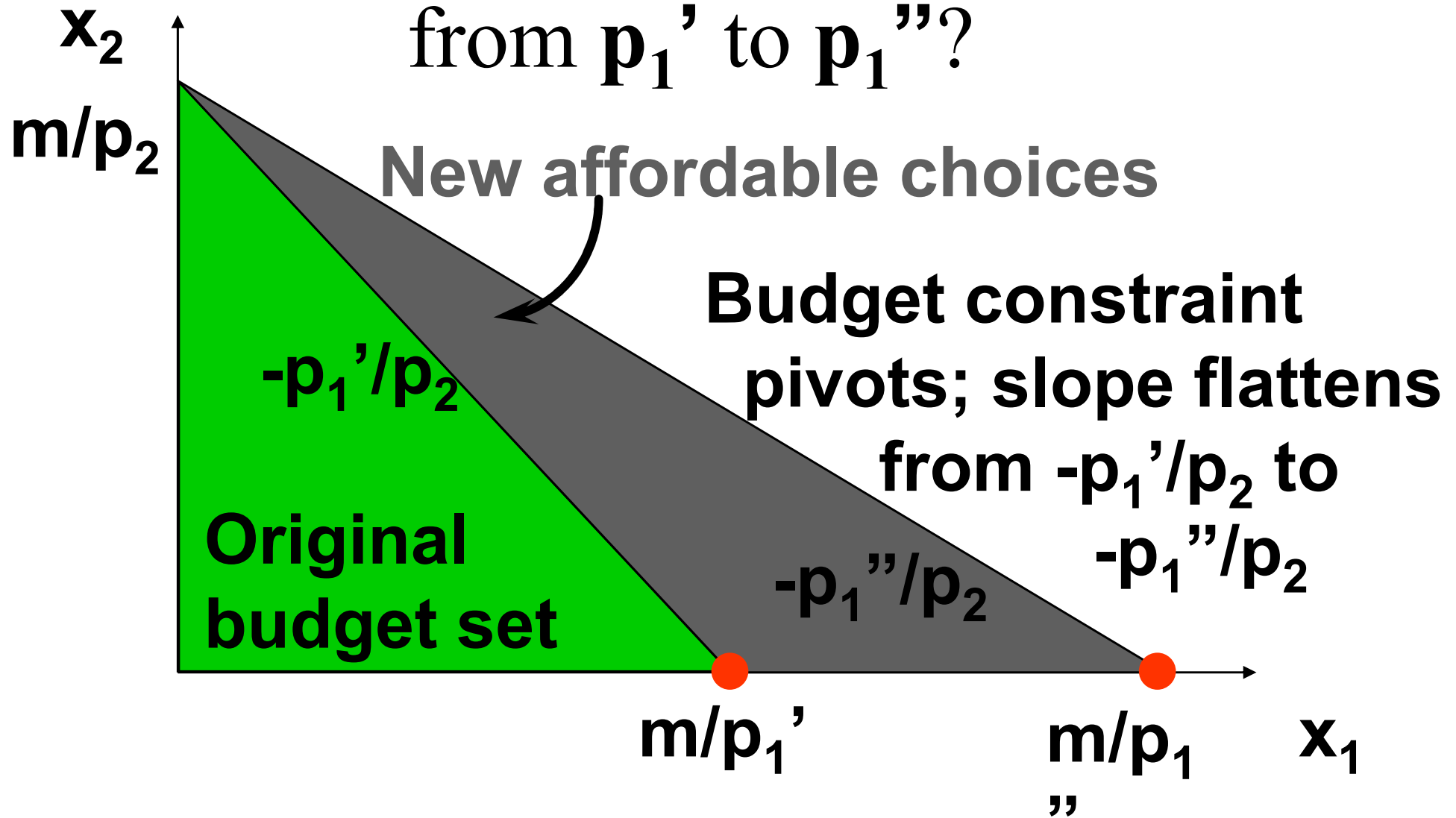




How do the budget set and budget constraint change as  $p_1$  decreases from  $p_1'$  to  $p_1''$ ?



How do the budget set and budget constraint change as  $p_1$  decreases from  $p_1'$  to  $p_1''$ ?



# Budget Constraints - Price Changes

- ◆ **Reducing the price of one commodity pivots the constraint outward. No old choice is lost and new choices are added, so reducing one price cannot make the consumer worse off.**

# Budget Constraints - Price Changes

- ◆ **Similarly, increasing one price pivots the constraint inwards, reduces choice and may (typically will) make the consumer worse off.**

# Uniform *Ad Valorem* Sales Taxes

- ◆ An *ad valorem* sales tax levied at a rate of 5% increases all prices by 5%, from  $p$  to  $(1+0.05)p = 1.05p$ .
- ◆ An *ad valorem* sales tax levied at a rate of  $t$  increases all prices by  $tp$  from  $p$  to  $(1+t)p$ .
- ◆ A uniform sales tax is applied uniformly to all commodities.

# Uniform *Ad Valorem* Sales Taxes

- ◆ A uniform sales tax levied at rate  $t$  changes the constraint from

$$p_1x_1 + p_2x_2 = m$$

to

$$(1+t)p_1x_1 + (1+t)p_2x_2 = m$$

# Uniform *Ad Valorem* Sales Taxes

- ◆ A uniform sales tax levied at rate  $t$  changes the constraint from

$$p_1x_1 + p_2x_2 = m$$

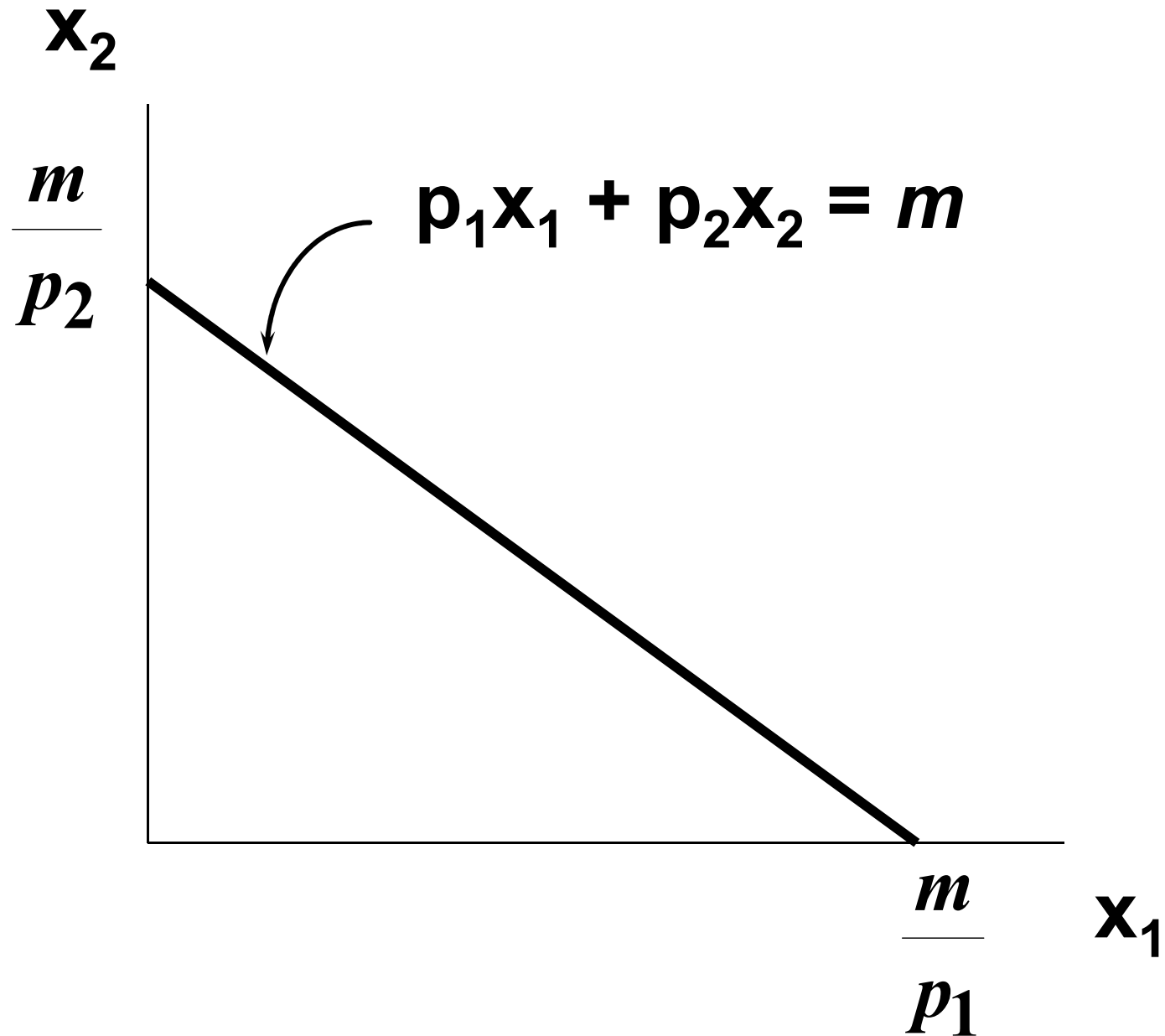
to

$$(1+t)p_1x_1 + (1+t)p_2x_2 = m$$

i.e.

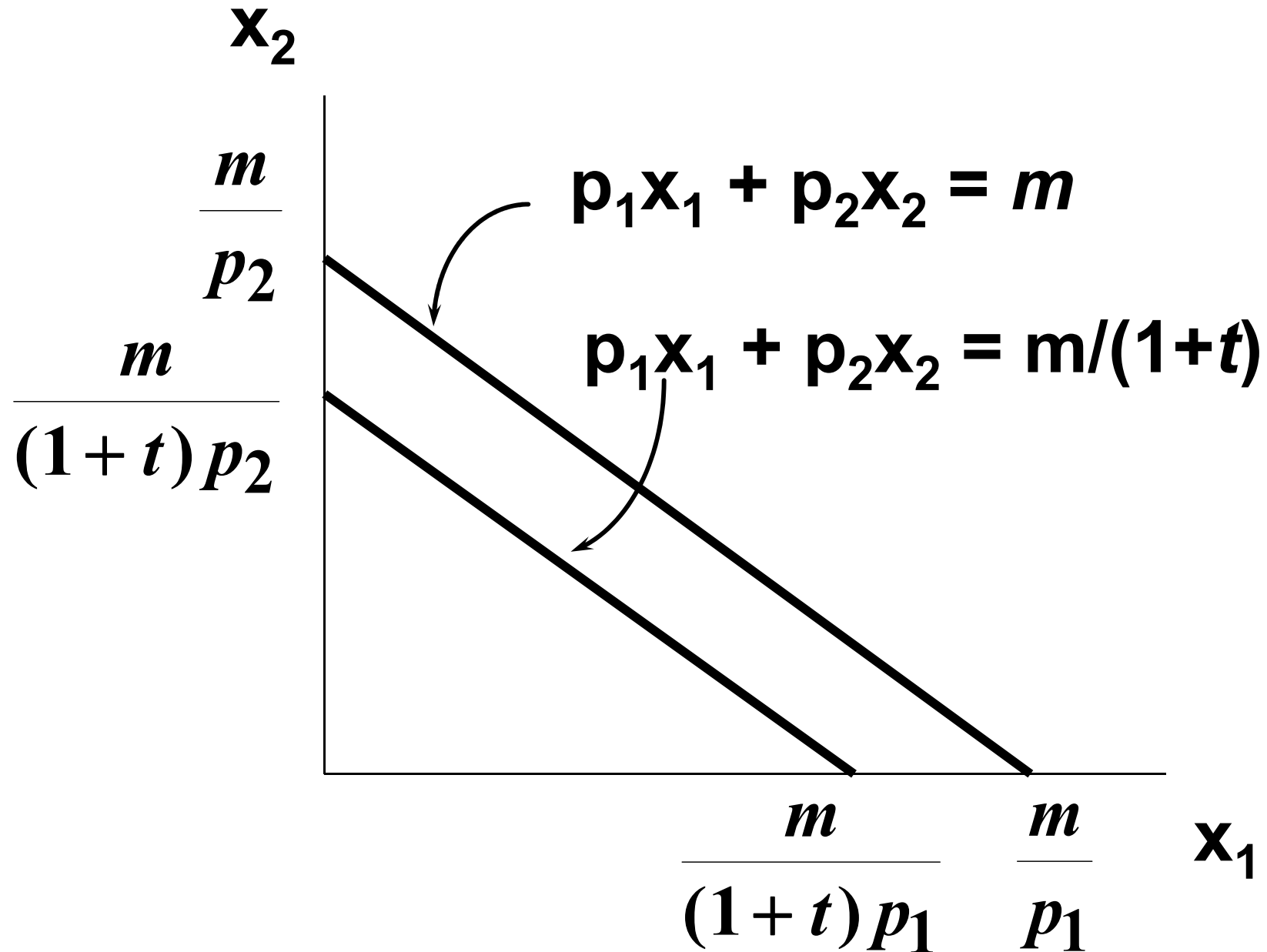
$$p_1x_1 + p_2x_2 = m/(1+t).$$

# Uniform *Ad Valorem* Sales Taxes

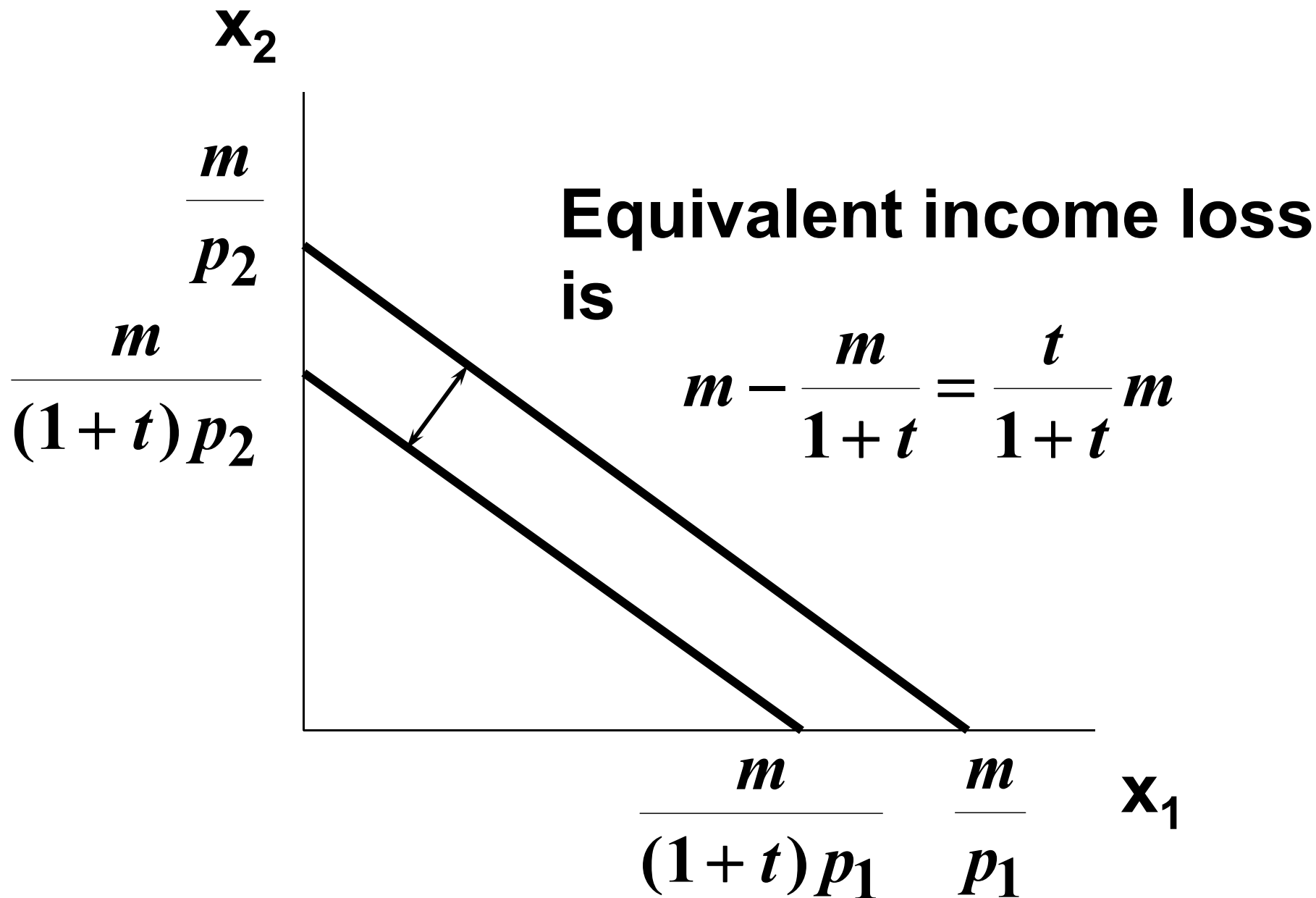




# Uniform *Ad Valorem* Sales Taxes

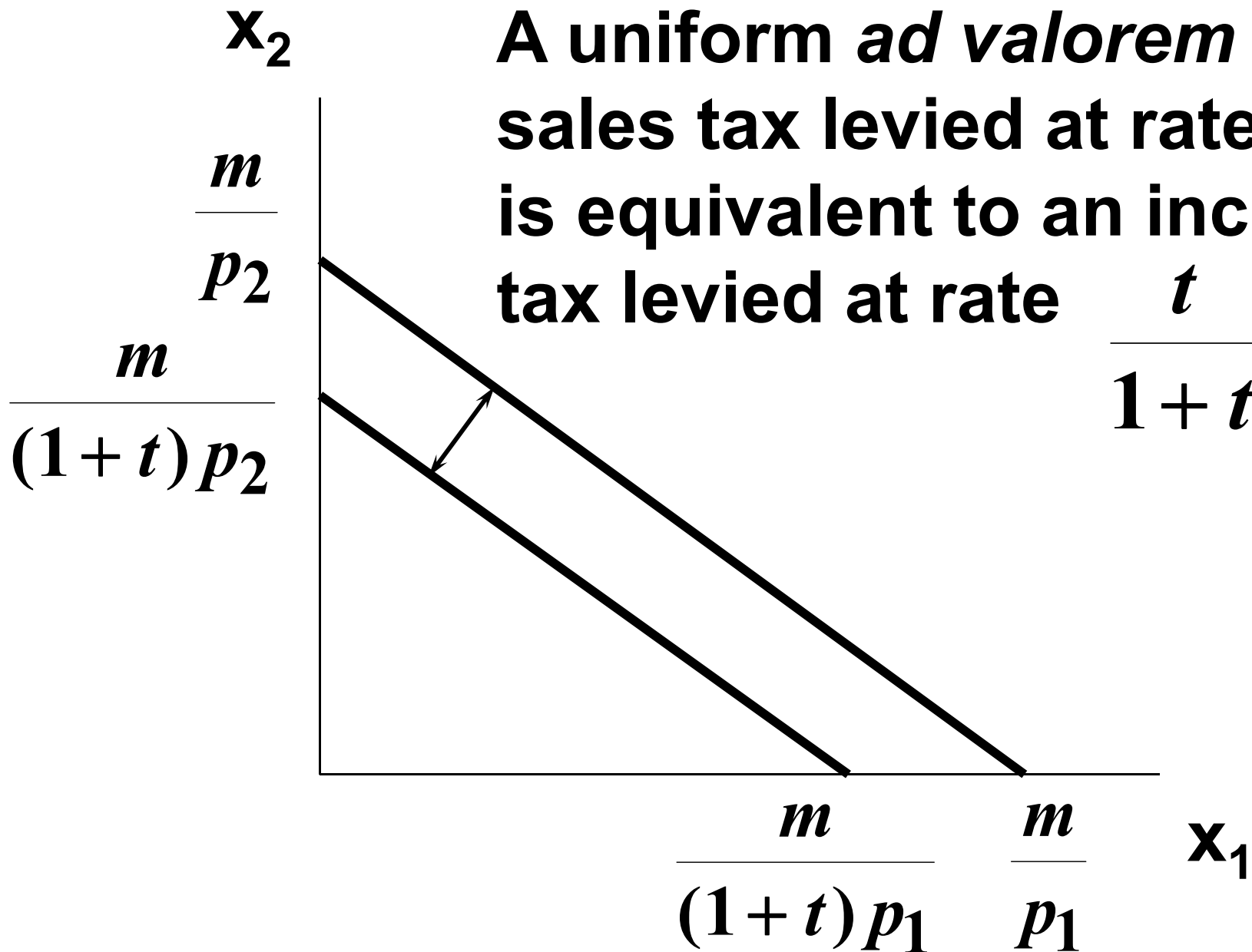


# Uniform *Ad Valorem* Sales Taxes



# Uniform *Ad Valorem* Sales Taxes

A uniform *ad valorem* sales tax levied at rate  $t$  is equivalent to an income tax levied at rate  $\frac{t}{1+t}$ .



# The Food Stamp Program

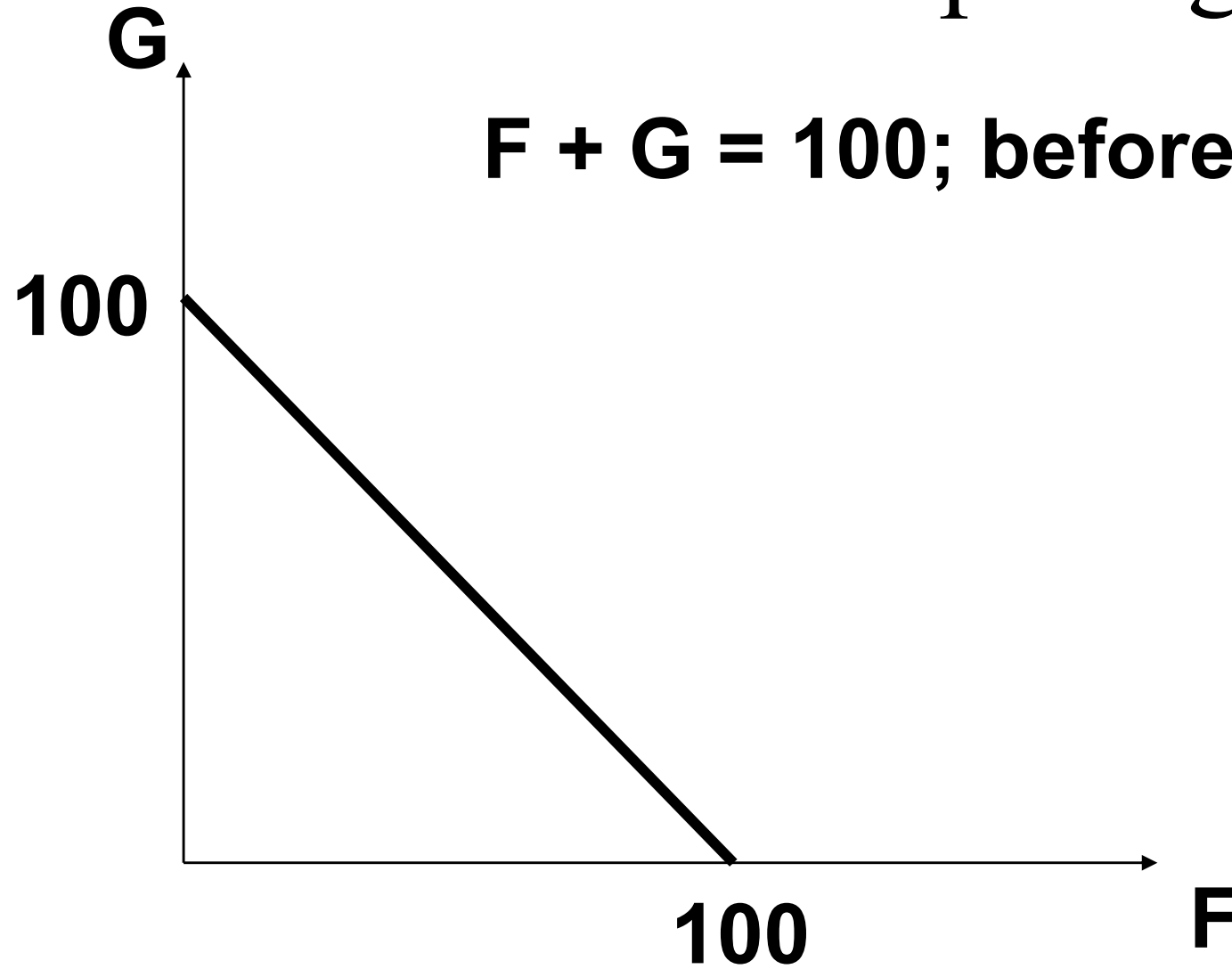
- ◆ **Food stamps are coupons that can be legally exchanged only for food.**
- ◆ **How does a commodity-specific gift such as a food stamp alter a family's budget constraint?**

# The Food Stamp Program

- ◆ **Suppose  $m = \$100$ ,  $p_F = \$1$  and the price of “other goods” is  $p_G = \$1$ .**
- ◆ **The budget constraint is then**  
 **$F + G = 100$ .**

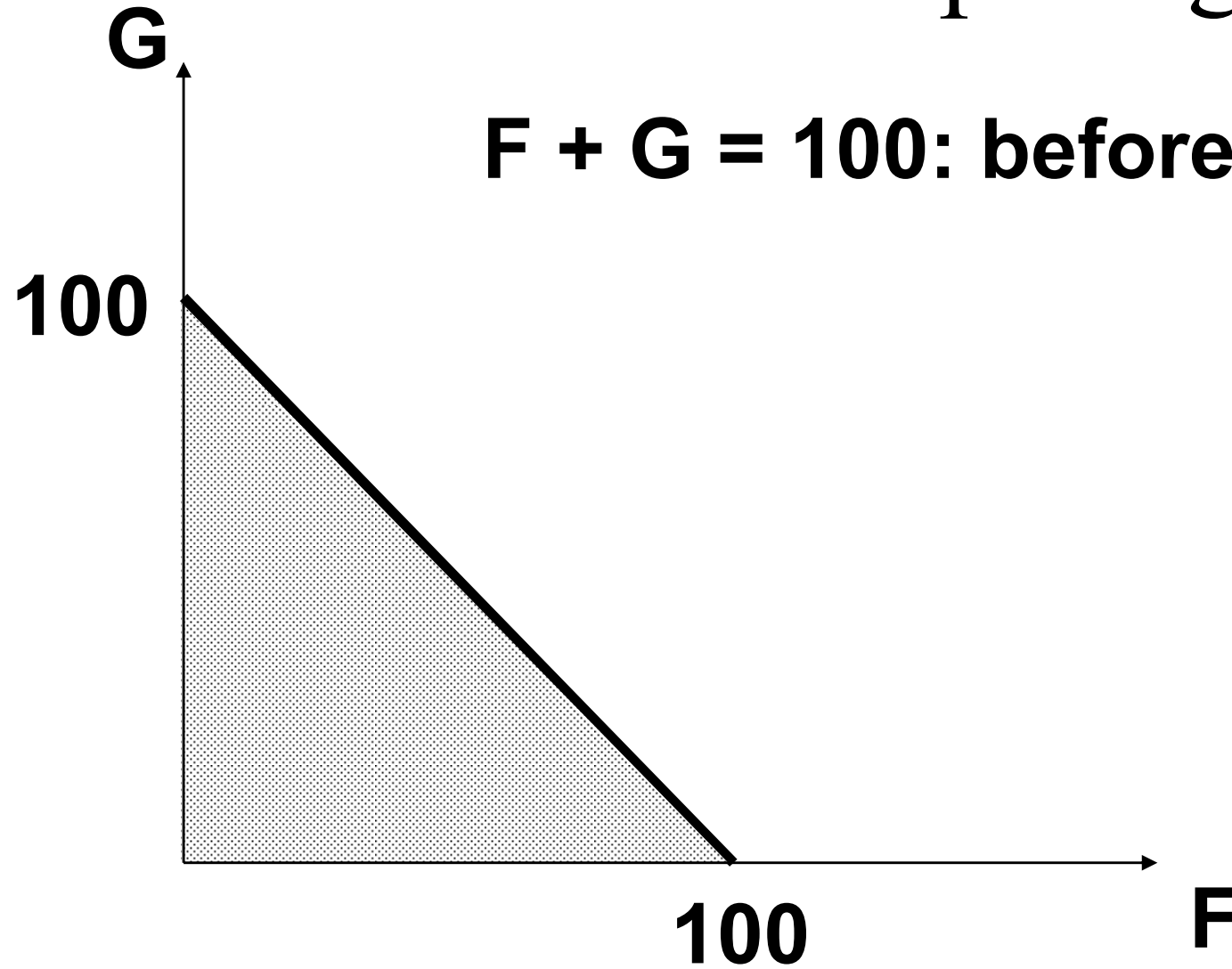
# The Food Stamp Program

**$F + G = 100$ ; before stamps.**

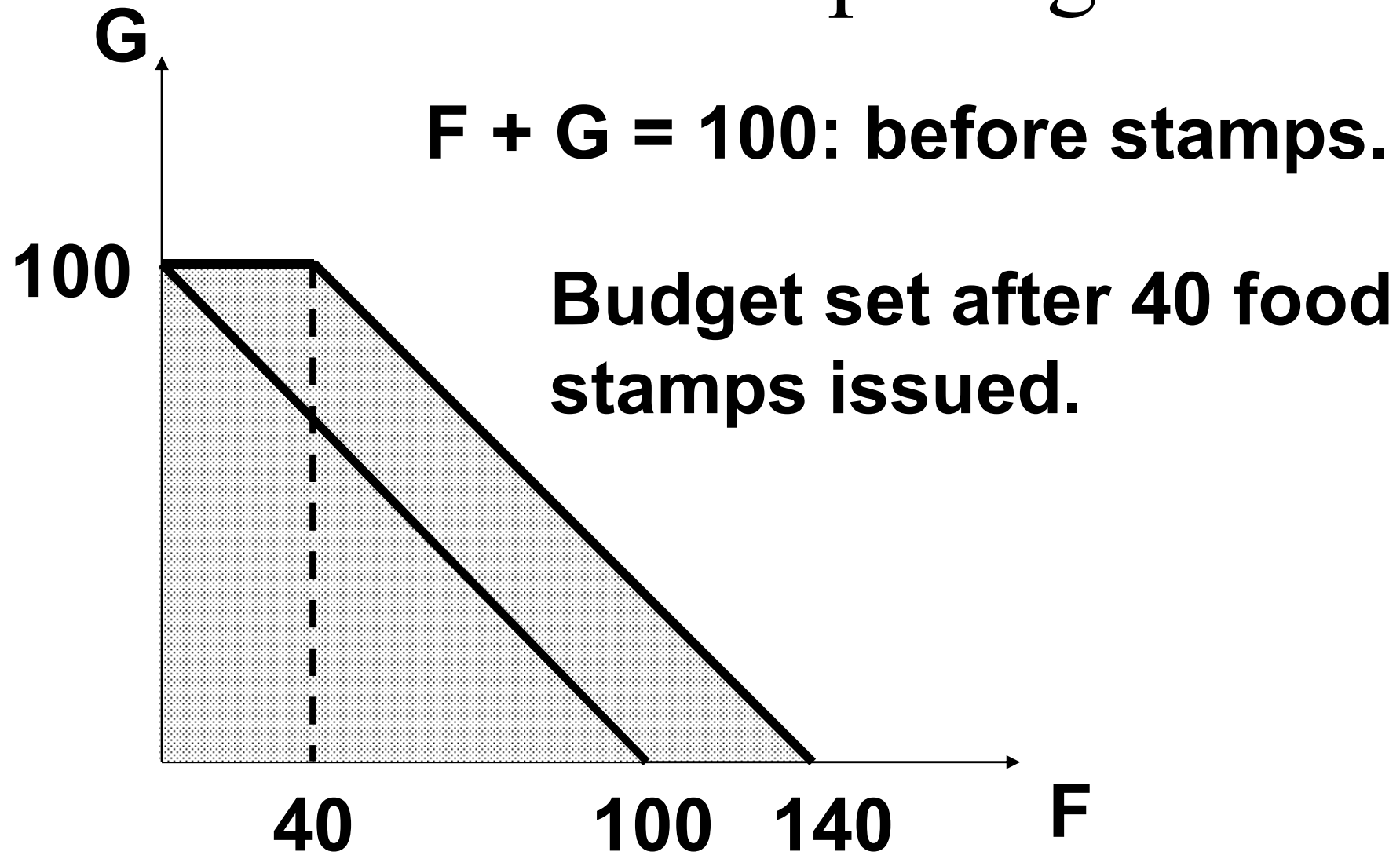


# The Food Stamp Program

**$F + G = 100$ : before stamps.**

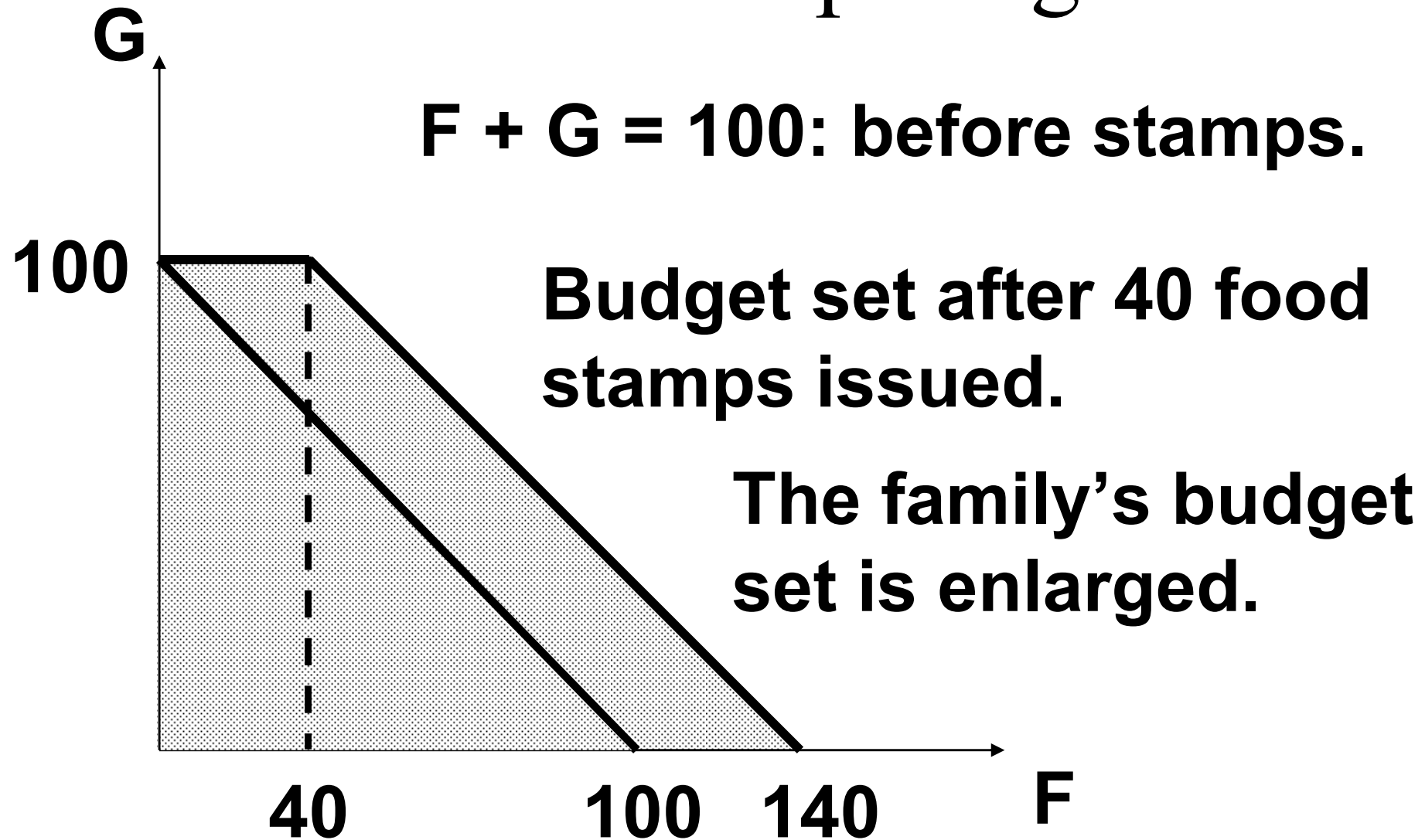


# The Food Stamp Program





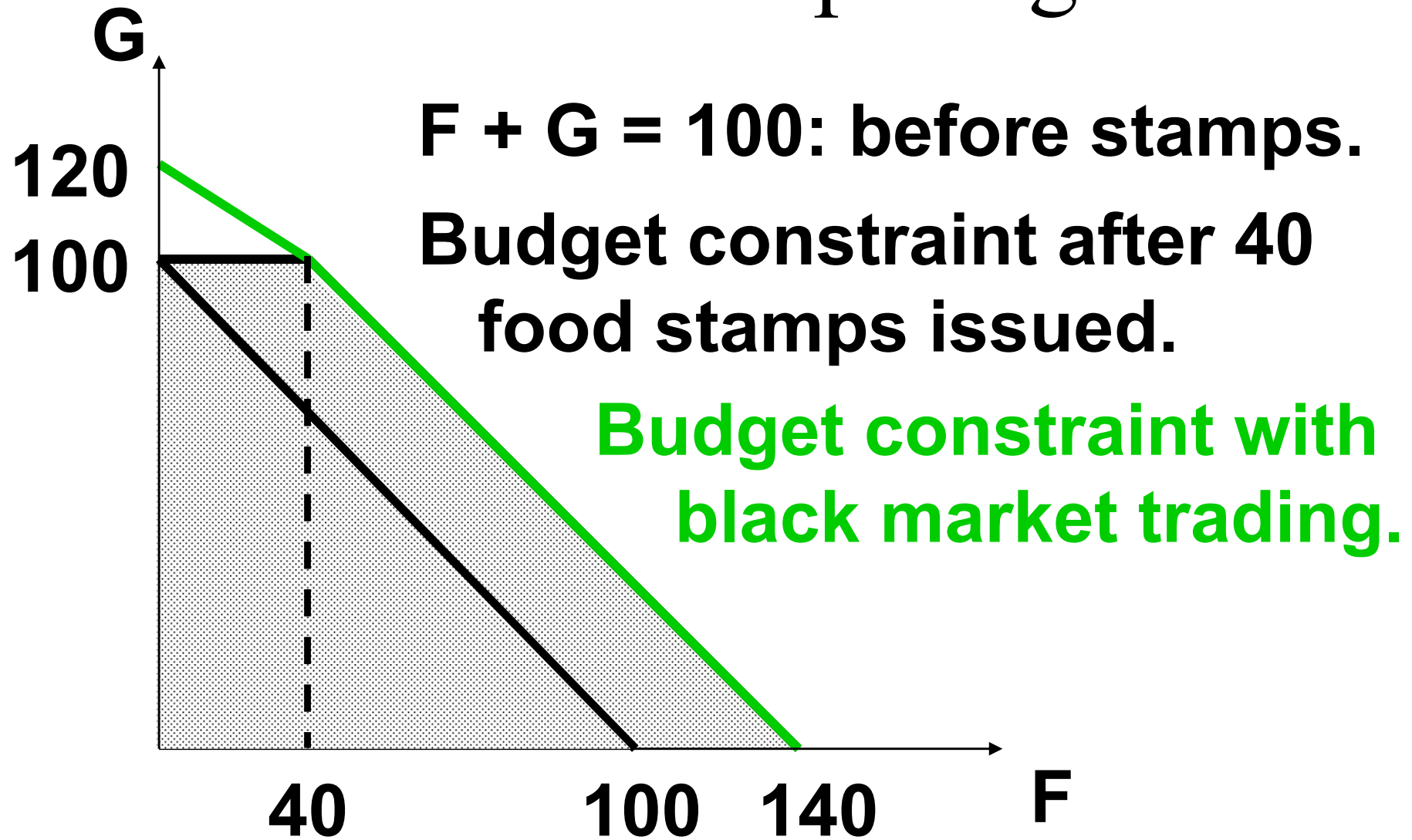
# The Food Stamp Program



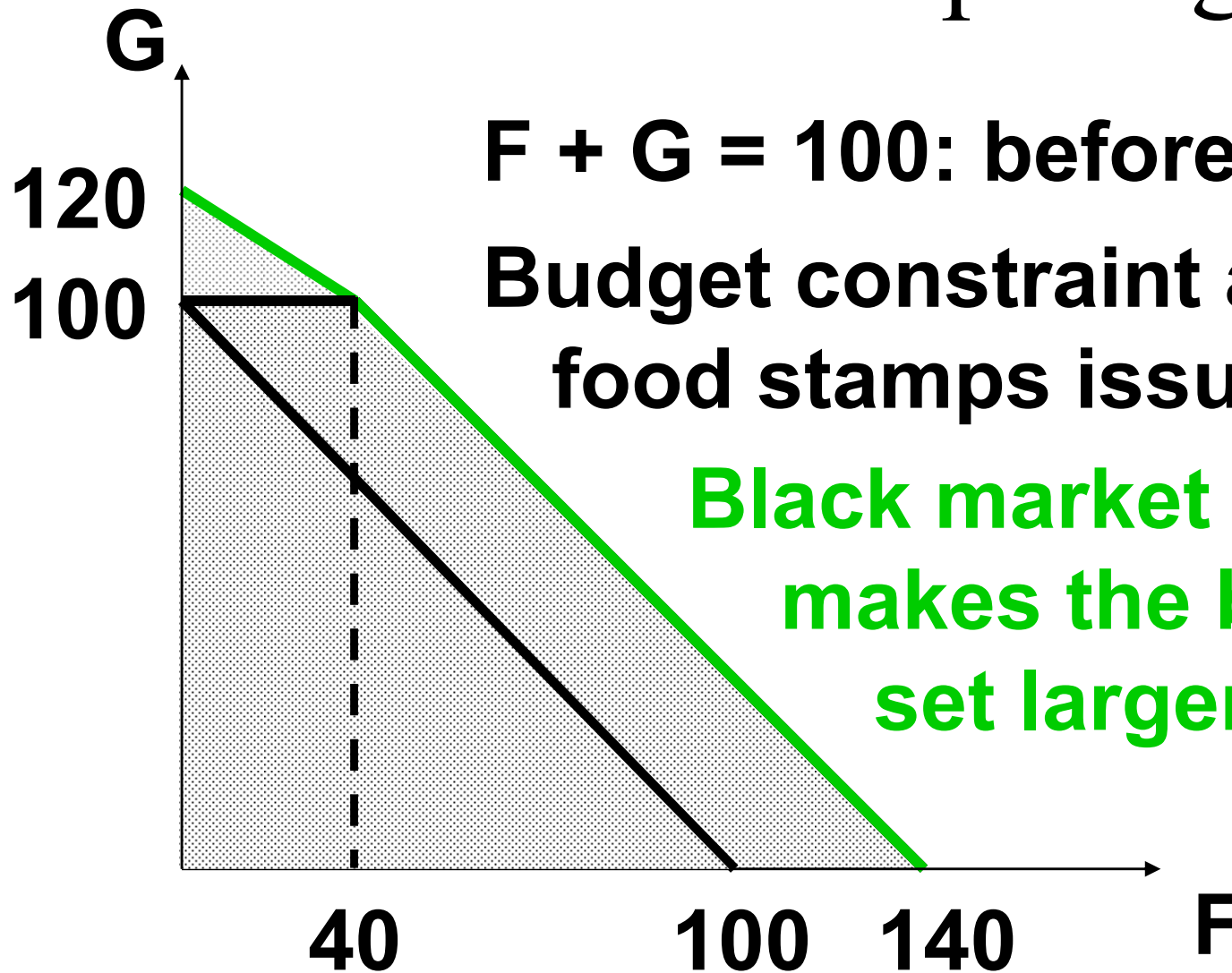
# The Food Stamp Program

- ◆ **What if food stamps can be traded on a black market for \$0.50 each?**

# The Food Stamp Program



# The Food Stamp Program



**$F + G = 100$ : before stamps.**

**Budget constraint after 40  
food stamps issued.**

**Black market trading  
makes the budget  
set larger again.**

# Budget Constraints - Relative Prices

- ◆ **“Numeraire” means “unit of account”.**
- ◆ **Suppose prices and income are measured in dollars. Say  $p_1 = \$2$ ,  $p_2 = \$3$ ,  $m = \$12$ . Then the constraint is**

$$2x_1 + 3x_2 = 12.$$

# Budget Constraints - Relative Prices

- ◆ If prices and income are measured in cents, then  $p_1=200$ ,  $p_2=300$ ,  $m=1200$  and the constraint is

$$200x_1 + 300x_2 = 1200,$$

the same as

$$2x_1 + 3x_2 = 12.$$

- ◆ Changing the numeraire changes neither the budget constraint nor the budget set.

# Budget Constraints - Relative Prices

- ◆ **The constraint for  $p_1=2$ ,  $p_2=3$ ,  $m=12$**

$$2x_1 + 3x_2 = 12$$

**is also  $1 \cdot x_1 + (3/2)x_2 = 6$ ,**

**the constraint for  $p_1=1$ ,  $p_2=3/2$ ,  $m=6$ .**

**Setting  $p_1=1$  makes commodity 1 the numeraire and defines all prices relative to  $p_1$ ; e.g.  $3/2$  is the price of commodity 2 relative to the price of commodity 1.**

# Budget Constraints - Relative Prices

- ◆ **Any commodity can be chosen as the numeraire without changing the budget set or the budget constraint.**



# Budget Constraints - Relative Prices

- ◆  $p_1=2$ ,  $p_2=3$  and  $p_3=6 \Rightarrow$
- ◆ price of commodity 2 relative to commodity 1 is  $3/2$ ,
- ◆ price of commodity 3 relative to commodity 1 is 3.
- ◆ Relative prices are the rates of exchange of commodities 2 and 3 for units of commodity 1.

# Shapes of Budget Constraints

◆ **Q: What makes a budget constraint a straight line?**

◆ **A: A straight line has a constant slope and the constraint is**

$$p_1x_1 + \dots + p_nx_n = m$$

**so if prices are constants then a constraint is a straight line.**

# Shapes of Budget Constraints

- ◆ **But what if prices are not constants?**
- ◆ ***E.g.* bulk buying discounts, or price penalties for buying “too much”.**
- ◆ **Then constraints will be curved.**

# Shapes of Budget Constraints - Quantity Discounts

- ◆ **Suppose  $p_2$  is constant at \$1 but that  $p_1 = \$2$  for  $0 \leq x_1 \leq 20$  and  $p_1 = \$1$  for  $x_1 > 20$ .**

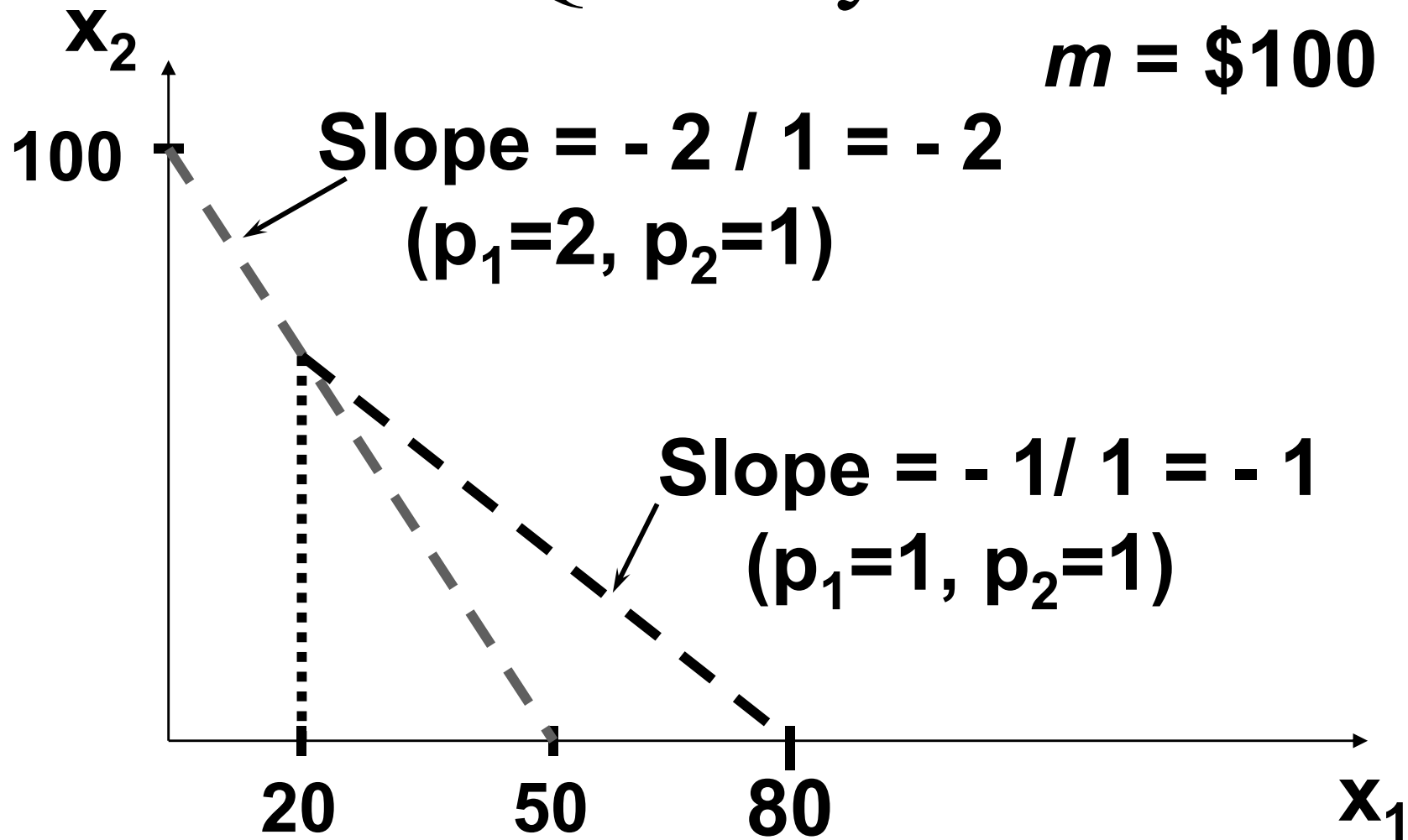
# Shapes of Budget Constraints - Quantity Discounts

- ◆ **Suppose  $p_2$  is constant at \$1 but that  $p_1 = \$2$  for  $0 \leq x_1 \leq 20$  and  $p_1 = \$1$  for  $x_1 > 20$ . Then the constraint's slope is**

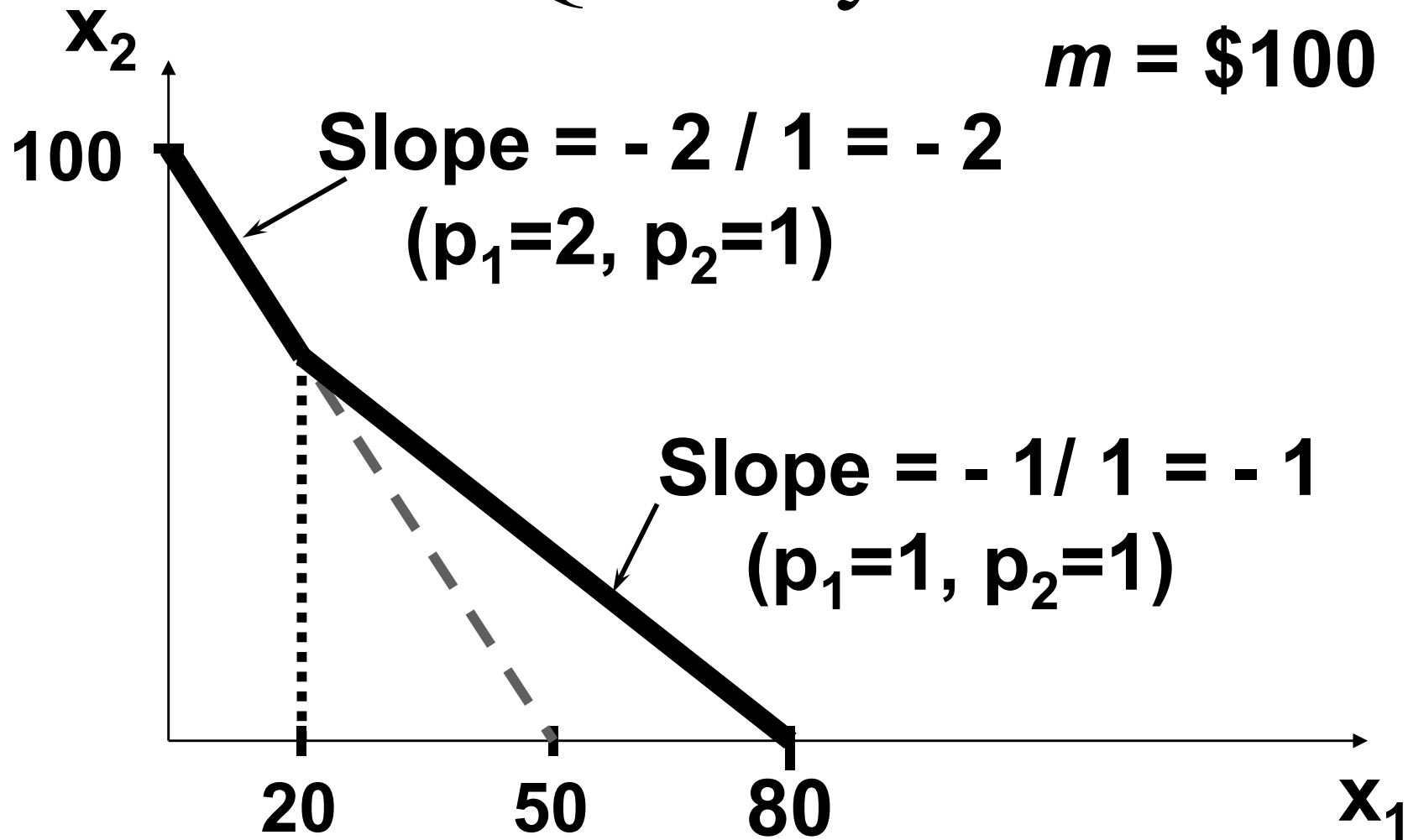
$$-p_1/p_2 = \begin{cases} -2, & \text{for } 0 \leq x_1 \leq 20 \\ -1, & \text{for } x_1 > 20 \end{cases}$$

**and the constraint is**

# Shapes of Budget Constraints with a Quantity Discount

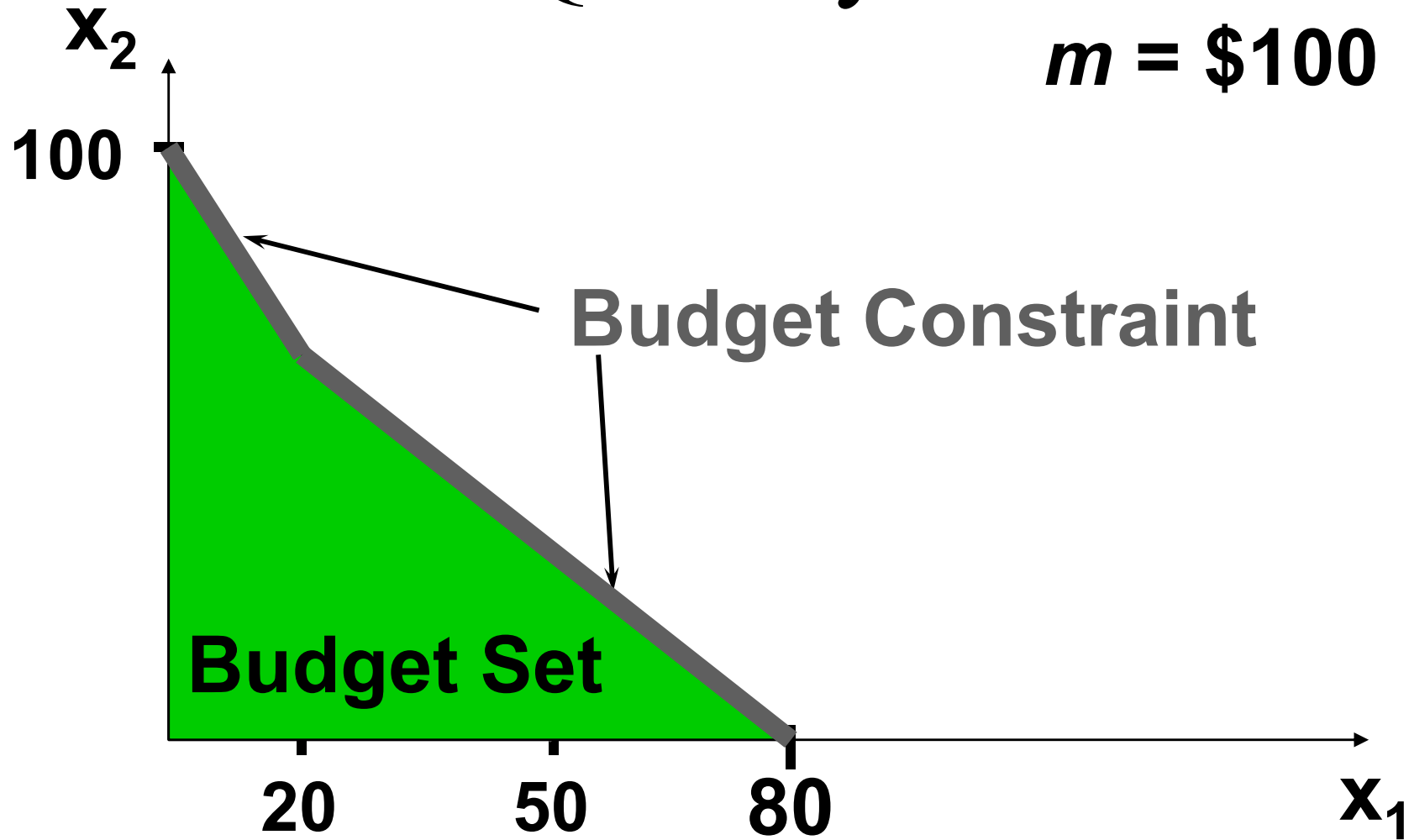


# Shapes of Budget Constraints with a Quantity Discount



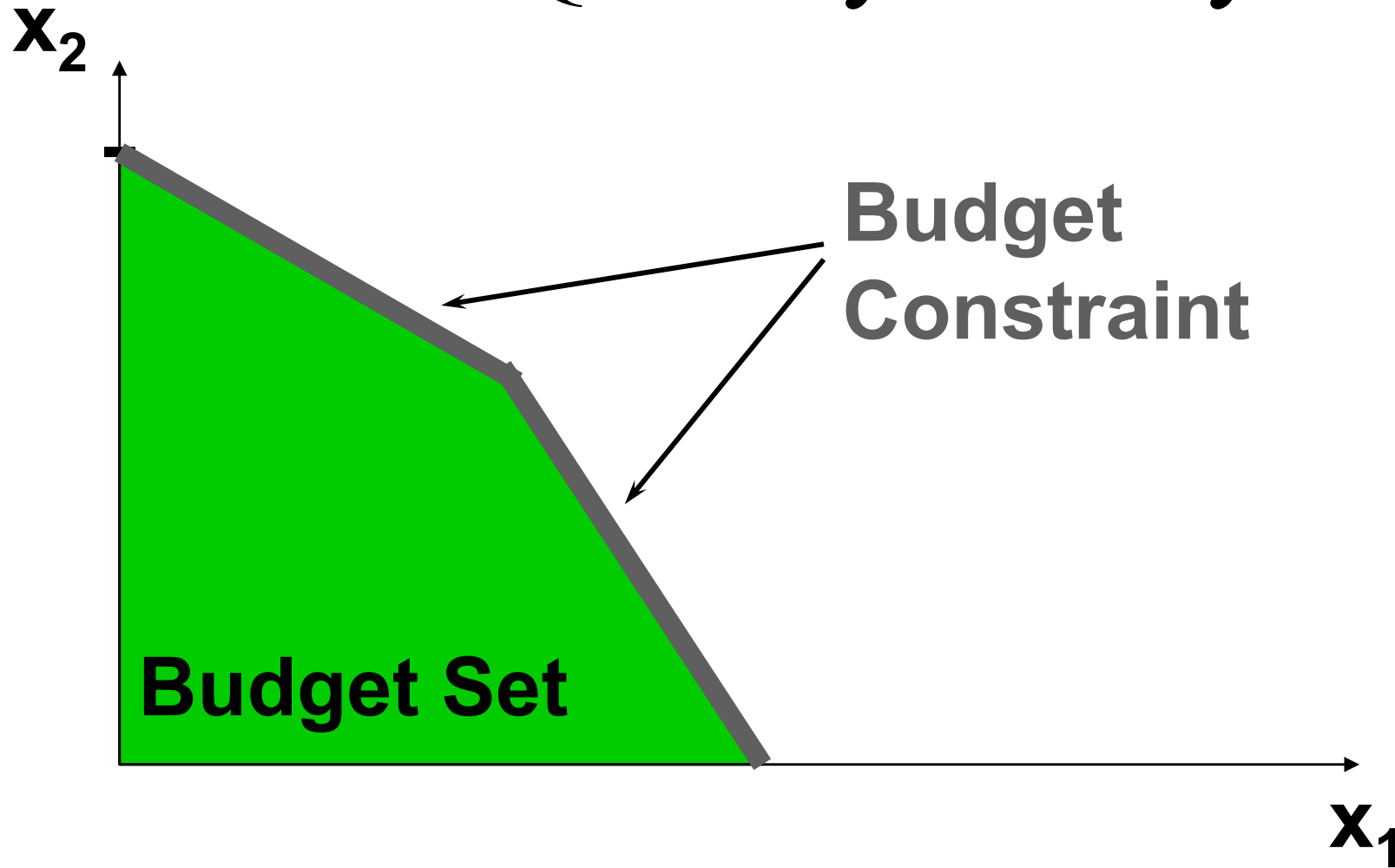
# Shapes of Budget Constraints with a Quantity Discount

$m = \$100$





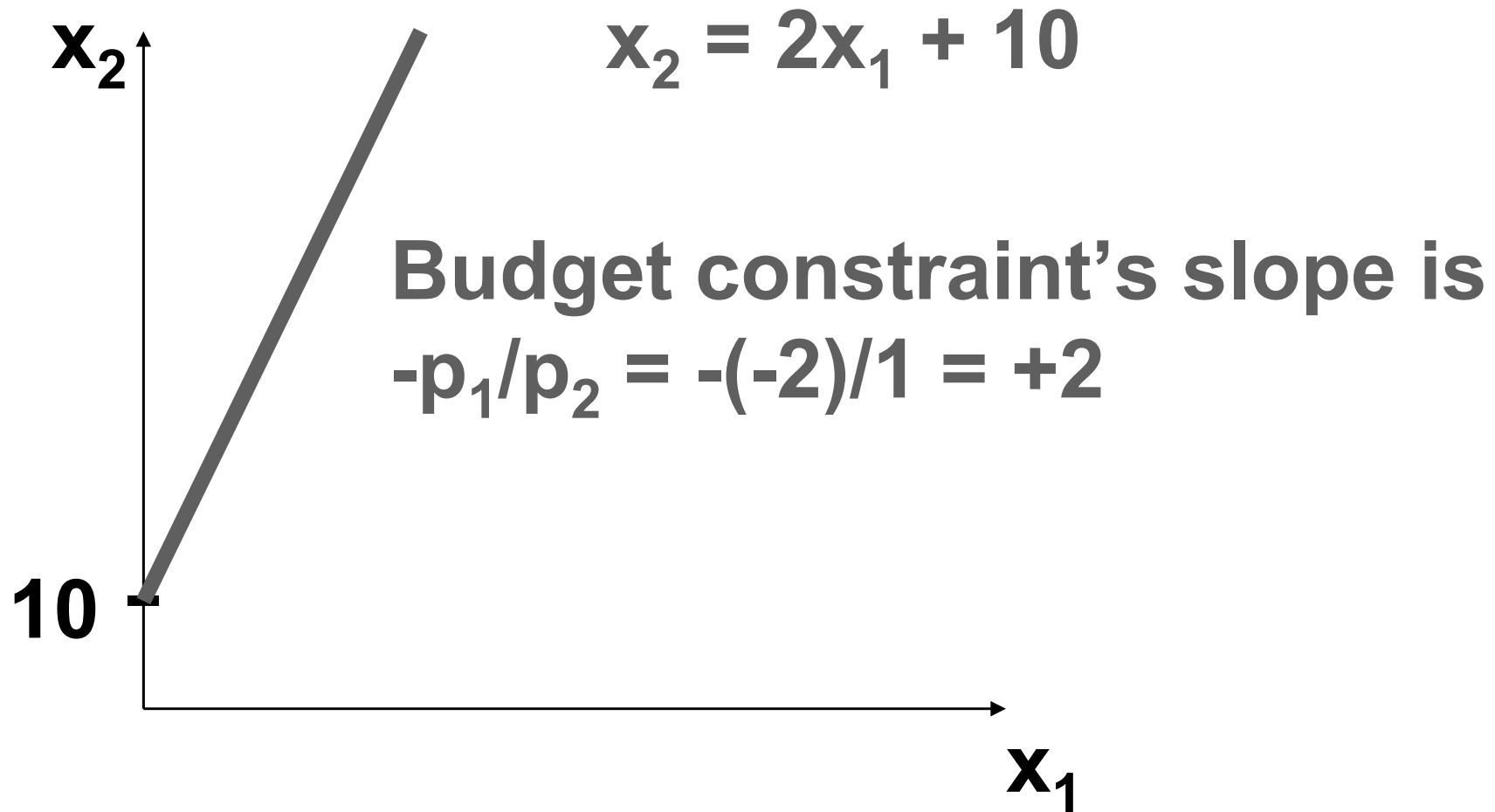
# Shapes of Budget Constraints with a Quantity Penalty



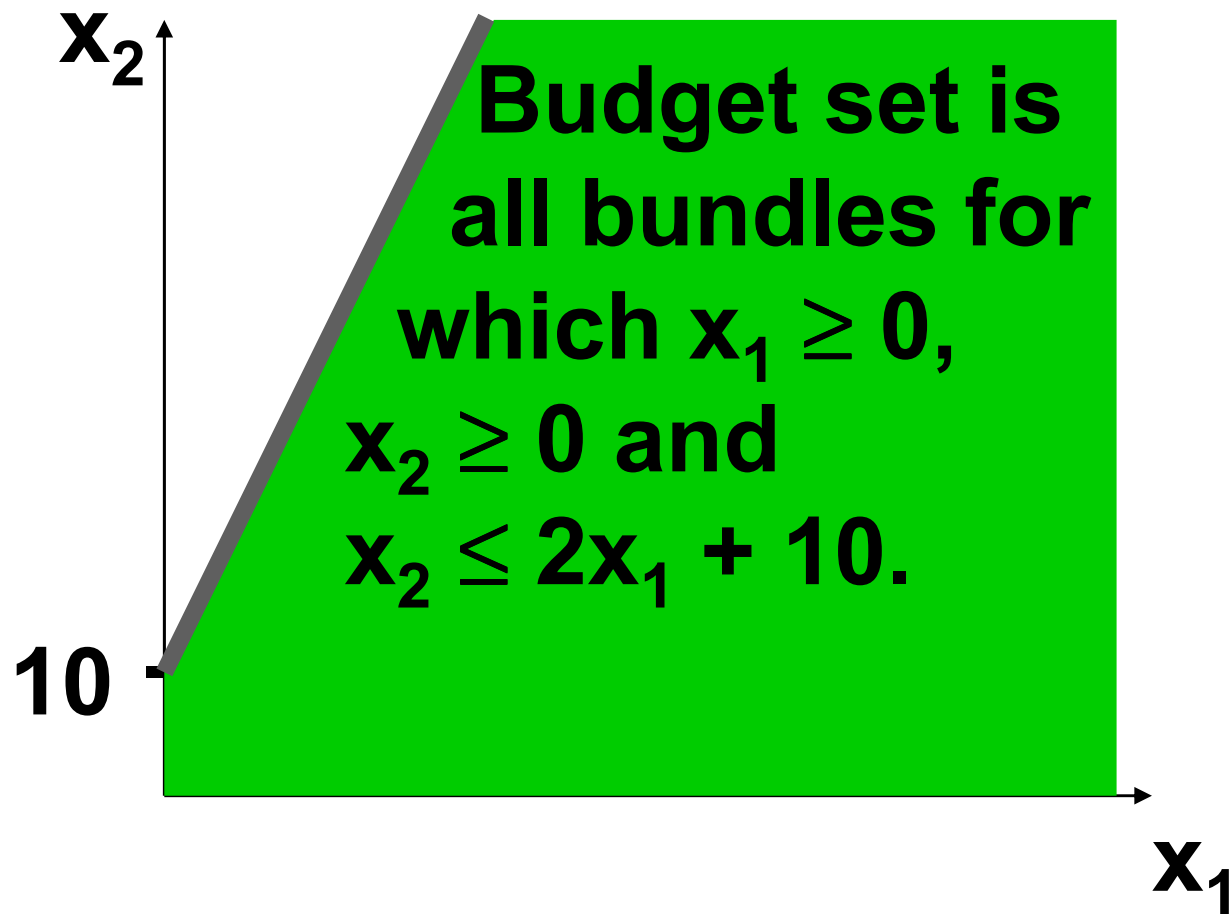
# Shapes of Budget Constraints - One Price Negative

- ◆ **Commodity 1 is stinky garbage. You are paid \$2 per unit to accept it; *i.e.*  $p_1 = - \$2$ .  $p_2 = \$1$ . Income, other than from accepting commodity 1, is  $m = \$10$ .**
- ◆ **Then the constraint is**  
$$- 2x_1 + x_2 = 10 \quad \text{or} \quad x_2 = 2x_1 + 10.$$

# Shapes of Budget Constraints - One Price Negative



# Shapes of Budget Constraints - One Price Negative

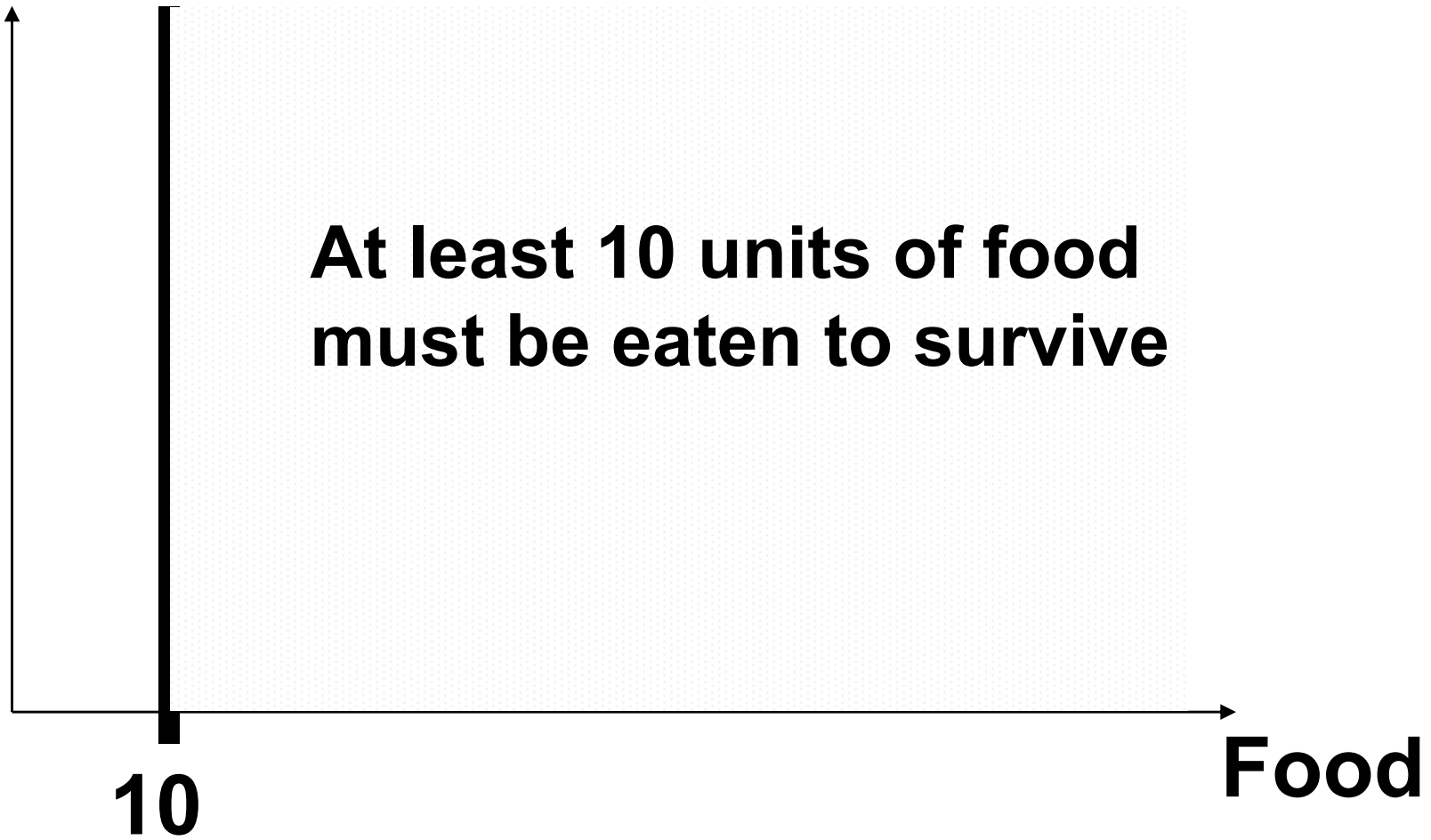


# More General Choice Sets

- ◆ **Choices are usually constrained by more than a budget; e.g. time constraints and other resources constraints.**
- ◆ **A bundle is available only if it meets every constraint.**

# More General Choice Sets

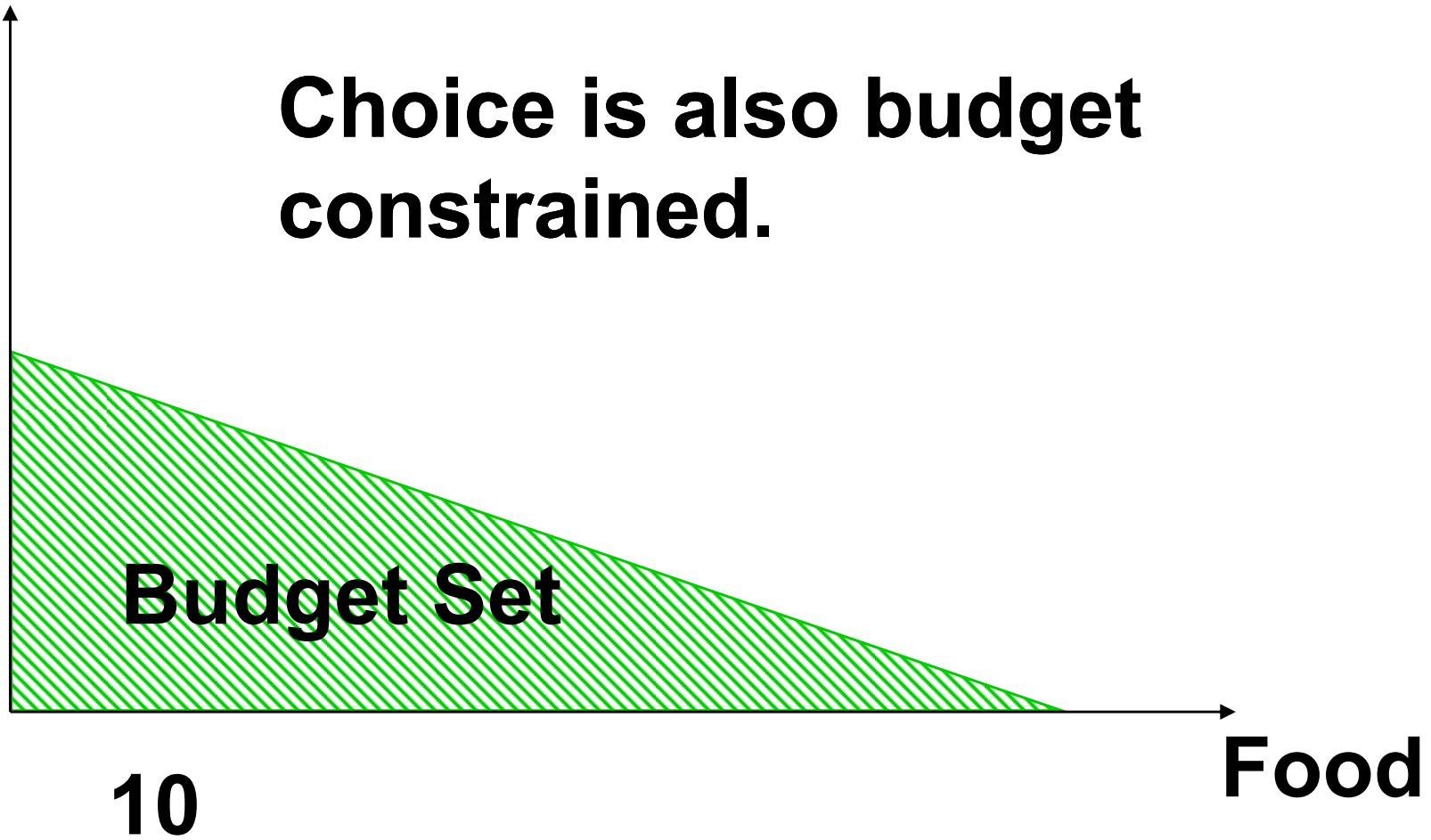
**Other Stuff**



# More General Choice Sets

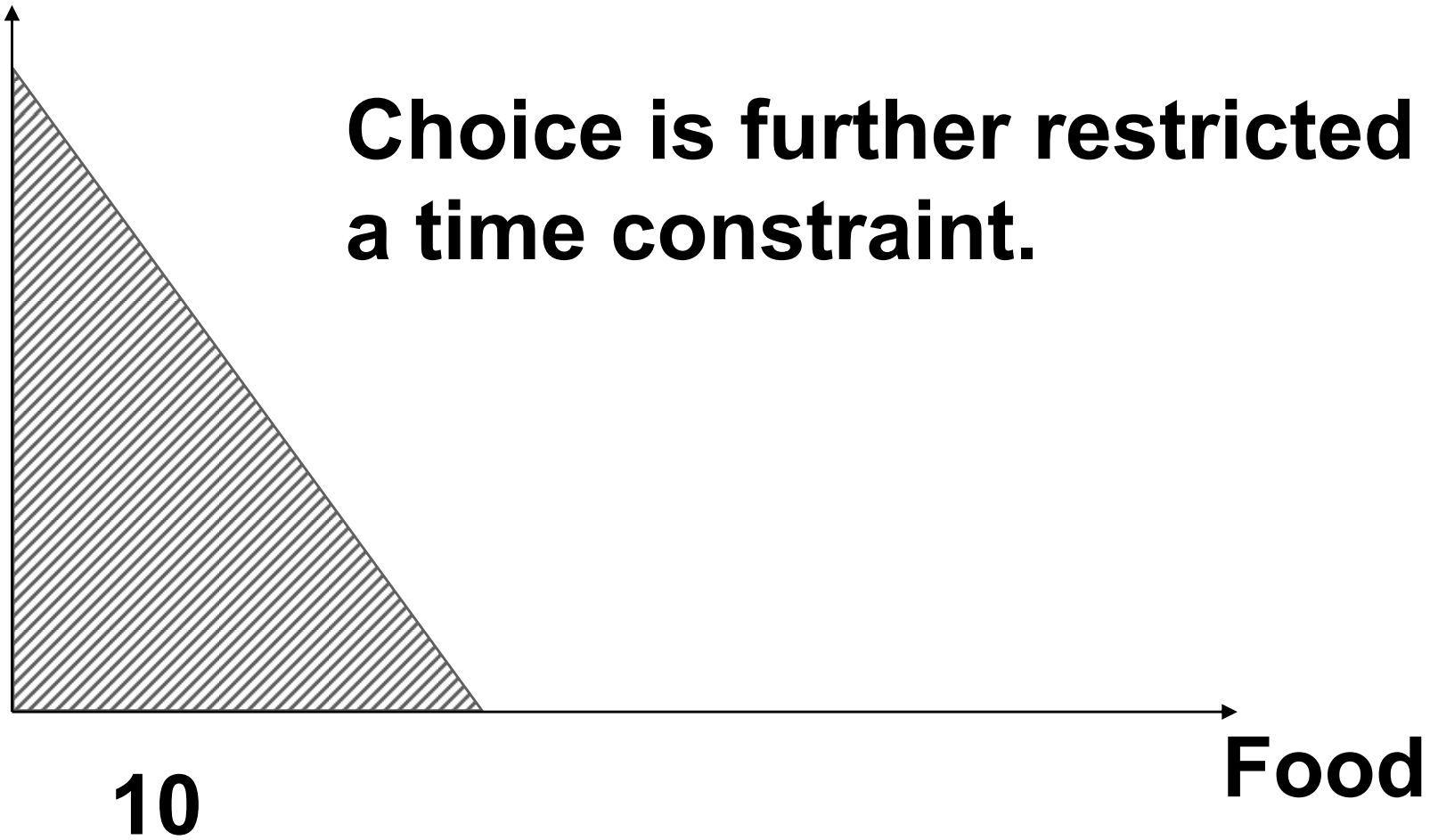
## Other Stuff

**Choice is also budget constrained.**



# More General Choice Sets

**Other Stuff**



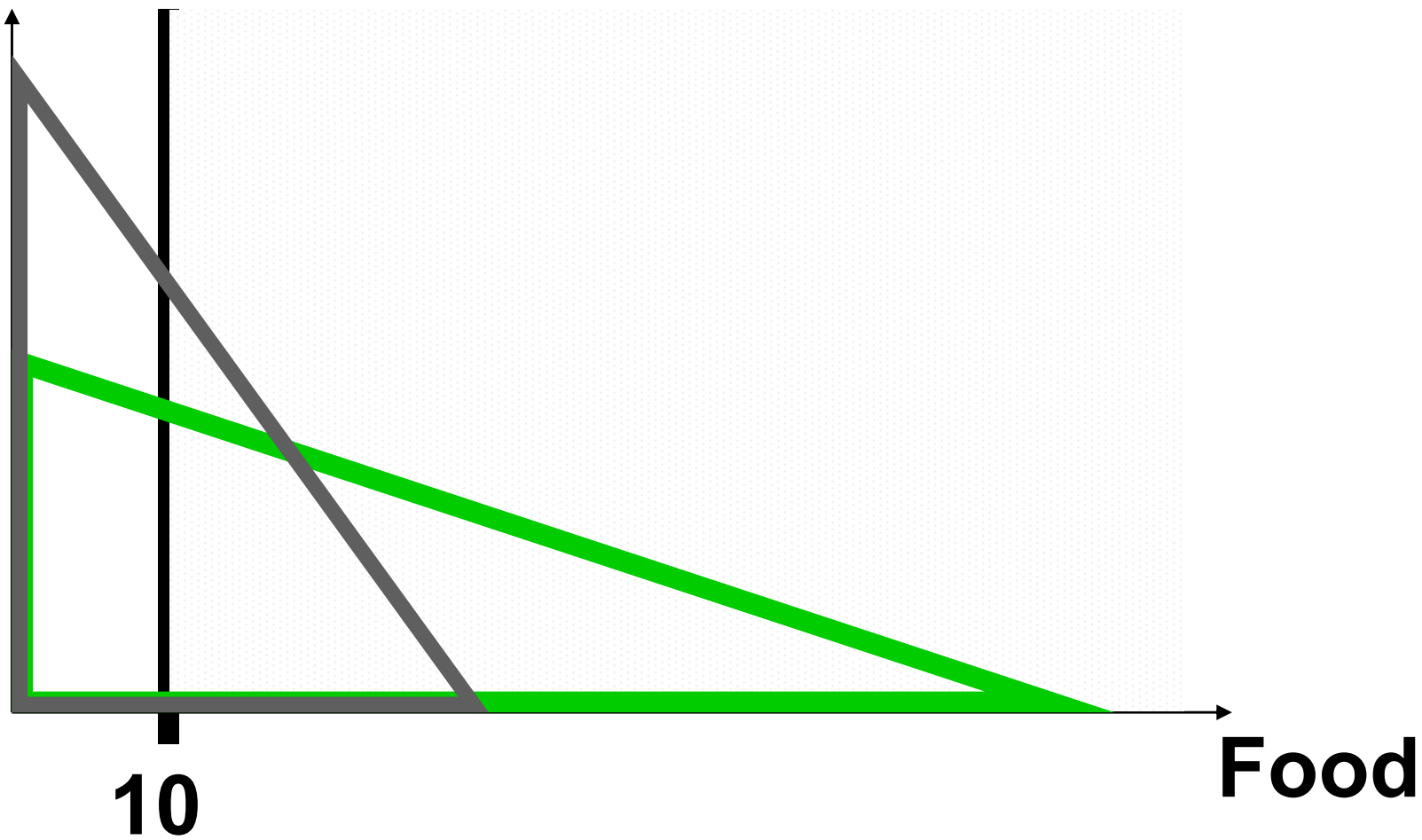


# More General Choice Sets

**So what is the choice set?**

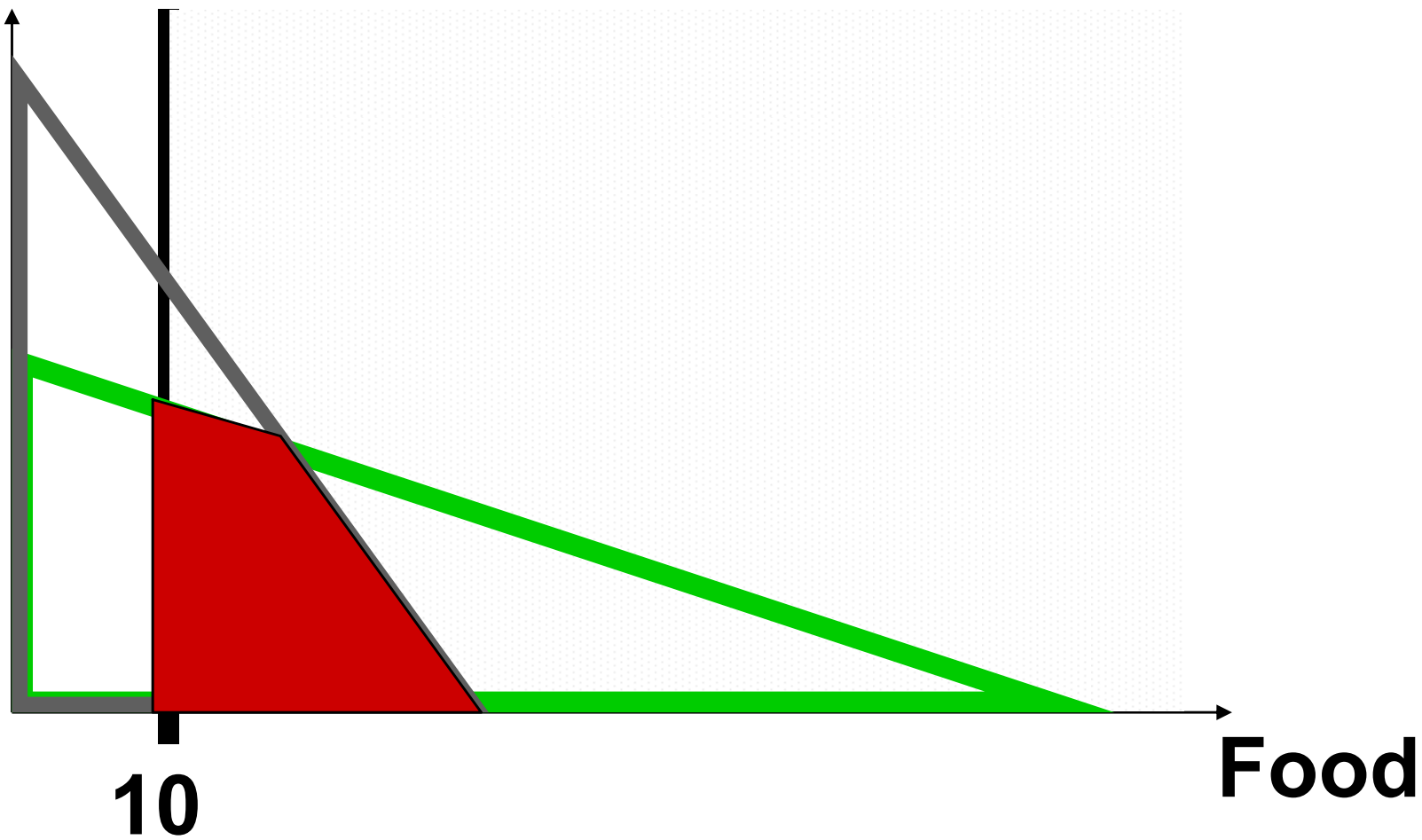
# More General Choice Sets

## Other Stuff



# More General Choice Sets

## Other Stuff



# More General Choice Sets

**Other Stuff**

