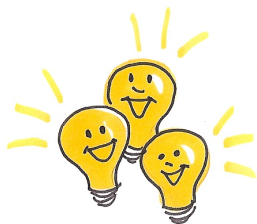


# Cartel and asymmetric information

Varian: Intermediate Microeconomics,  
chapters 27.10–11, 28.4–6, 37.1–6

## In this lecture you will learn

- what cartels do, when they are stable and when not
- what moral hazard and adverse selection are
- how signalization can solve the problem of adverse selection
- what function might have a school not teaching anything useful
- how incentives under complete and asymmetric information work
- what incentives have real-estate agents









# Cartel

**Cartel** – firms are trying to maximize the sum of their profits.  
The cartel behaves as a monopoly with more production plants.

Cartel is illegal.

In the US – personal responsibility of managers.

## Corporate Penalties

|   | Fine  | Damages  | Total   |
|---|---|--|---|
|  | 0   | \$256,000,000  | \$256,000,000   |
|  | \$45,000,000  | \$256,000,000  | \$301,000,000   |
| Sotheby's   | Sotheby's   | Christie's   | Christie's  |
| CEO   | Chairman  | CEO  | Chairman  |
| Dede Brooks   | Alfred Taubman  | Christopher Davidge  | Anthony Tenant  |
|  |  |  |  |
| Pled guilty   | Convicted   | Received leniency  | Indicted  |
| 1000 hours of service   | 9 months in prison  | \$8,000,000 severance  | Not extradicted   |
| \$350,000 fine  | \$7,500,000 fine  |  |   |

## Profit maximization of a cartel with two firms

Inverse market demand:  $p(y)$ , where  $y = y_1 + y_2$  (identical product)

Total revenue of cartel:  $r(y) = p(y)y$

Cost functions of firms:  $c_1(y_1)$  and  $c_2(y_2)$

Cartel chooses quantity  $y_1$  and  $y_2$  in order to maximize profit:

$$\max_{y_1, y_2} \pi(y_1, y_2) = r(y) - c_1(y_1) - c_2(y_2)$$

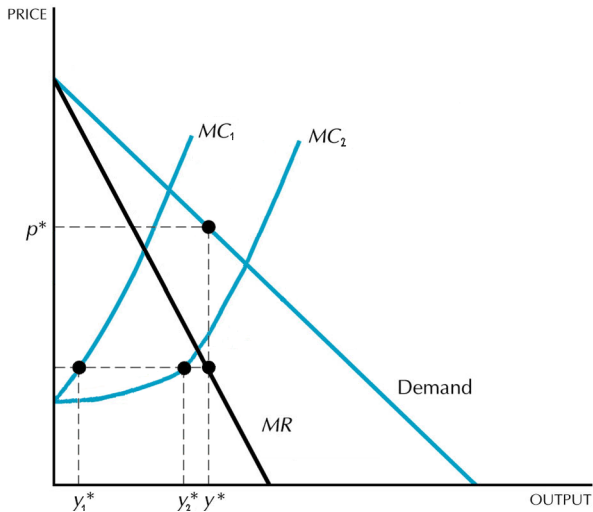
First-order conditions:

$$\frac{\partial \pi(y_1, y_2)}{\partial y_1} = \frac{dr(y)}{dy} \frac{dy}{dy_1} - \frac{dc_1(y_1)}{dy_1} = MR(y) - MC_1(y_1) = 0$$

$$\frac{\partial \pi(y_1, y_2)}{\partial y_2} = \frac{dr(y)}{dy} \frac{dy}{dy_2} - \frac{dc_2(y_2)}{dy_2} = MR(y) - MC_2(y_2) = 0$$

## Profit maximization of a cartel with two firms (graph)

First-order conditions:  $MR(y^*) = MC_1(y_1^*)$  and  $MR(y^*) = MC_2(y_2^*)$



## Cartel is unstable in an one-shot game – example

Inverse demand:  $p = 11 - y$

Costs:  $c_1(y_1) = 3y_1$ ;  $c_2(y_2) = 3y_2$ ;  $MC_1 = MC_2 = 3$

Cartel's quantities, price and profit, if each firm produces half the output?

How does the result change if firm 1 maximizes its own profit?

- Cartel:

$$\max_{y_1, y_2} \pi(y_1, y_2) = (11 - y)y - 3y_1 - 3y_2$$

The same first order conditions for both firms:  $11 - 2y = 3$

Result:  $y = 4$ ,  $y_1 = y_2 = 2$ ,  $p = 7$ ,  $\pi_1 = \pi_2 = 8$

- Firm 1:

$$\max_{y_1} \pi(y_1, 2) = (9 - y_1)y_1 - 3y_1$$

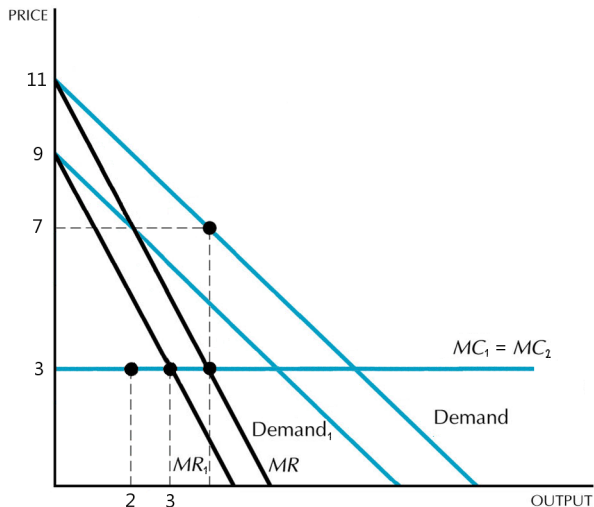
First-order condition:  $9 - 2\hat{y}_1 = 3$

Result:  $\hat{y}_1 = 3$ ,  $y_2 = 2$ ,  $y = 5$ ,  $p = 6$ ,  $\pi_1 = 9$ ,  $\pi_2 = 6$

## Cartel is unstable in an one-shot game (graph)

Result cartel:  $y = 4$ ,  $y_1 = y_2 = 2$ ,  $p = 7$ ,  $\pi_1 = \pi_2 = 8$

Result firm 1:  $D_1 : p = 9 - y_1$ ,  $MR_1 = 9 - 2y_1$ ,  $\hat{y}_1 = 3$



## Prisoner's dilemma

The situation of a cartel corresponds to a game **prisoner's dilemma** = a simultaneous game in which

- there are 2 players – player A and B,
- each player has 2 actions – confess *C* and deny *D*,
- preferences of both payers are  $CD \succ DD \succ CC \succ DC$ .

|          |         | Player B |        |
|----------|---------|----------|--------|
|          |         | Confess  | Deny   |
| Player A | Confess | -3, -3   | 0, -6  |
|          | Deny    | -6, 0    | -1, -1 |

Nash equilibrium and equilibrium in dominant strategies is *CC*.

Is this equilibrium Pareto efficient? No. Both players are better off in *DD*.



## Prisoner's dilemma – a cartel with two firms

Simultaneous game:

- two firms 1 and 2
- each firm has two actions:
  - cartel quantity  $q_i^m$
  - competitive (Cournot) quantity  $q_i^c$
- preferences given by profits of firms:  
 $\pi_i^d$  (**default**)  $>$   $\pi_i^m$  (**monopoly**)  $>$   $\pi_i^c$  (**competition**)  $>$   $\pi_i^s$  (**sucker**)

Payoff matrix of the game – the same structure as prisoner's dilemma:

|        |         | firm 2             |                    |
|--------|---------|--------------------|--------------------|
|        |         | $q_2^c$            | $q_2^m$            |
| firm 1 | $q_1^c$ | $\pi_1^c; \pi_2^c$ | $\pi_1^d; \pi_2^s$ |
|        | $q_1^m$ | $\pi_1^s; \pi_2^d$ | $\pi_1^m; \pi_2^m$ |

Nash equilibrium and equilibrium in dominant strategies  $(q_1^c, q_2^c)$  is not Pareto efficient – both firms better off in  $(q_1^m, q_2^m)$ .

## Repeated prisoner's dilemma

In the repeated prisoner's dilemma, the players may keep  $(q_1^m, q_2^m)$ , because it is possible to punish the player who chooses  $q^c$  in future rounds.

Example of a punishment strategy = **grim trigger** if one of the firm defaults, the other firm chooses  $q_i^c$  for the rest of the game  
Cartel in a finitely repeated game is not stable.

Why? Let us assume that the cartel game has 10 rounds:

- Both firms choose  $q_i^c$  in the 10th round (the dominant strategy).
- Firms' actions in the 9th round cannot be punished.  
     $\implies$  Both firms choose  $q_i^c$  in the 9th round.
- ...
- Firms' actions in the 1st round cannot be punished.  
     $\implies$  Both firms choose  $q_i^c$  in the first round.

In an infinitely repeated game, the punishment strategy can be successful.

## Cartel stability in an infinitely repeated game

Under what conditions does *grim trigger* make the cartel stable?

Firm  $i$  chooses:

- ① stay in cartel – net present value of profits:

$$\pi_i^m + \frac{\pi_i^m}{r}$$

- $\pi_i^m$  = cartel profit in this round
- $\pi_i^m/r$  = discounted future cartel profit ( $r$  = interest rate)

- ② default – net present value:

$$\pi_i^d + \frac{\pi_i^c}{r}$$

- $\pi_i^d$  = a higher profit from defaulting in this round
- $\pi_i^c/r$  = a lower discounted future competitive profit

## Cartel stability in an infinitely repeated game (cont'd)

The cartel will be stable if

$$\pi_i^m + \frac{\pi_i^m}{r} > \pi_i^d + \frac{\pi_i^c}{r}$$

$$r < \frac{\pi_i^m - \pi_i^c}{\pi_i^d - \pi_i^m}$$

Because  $\pi_i^d > \pi_i^m$  and  $\pi_i^m > \pi_i^c$ ,

$$\frac{\pi_i^m - \pi_i^c}{\pi_i^d - \pi_i^m} > 0.$$

### Conclusion:

The cartel is stable if the firms are sufficiently patient ( $r$  is low).

If  $r$  is low, the loss of future profits  $\pi_i^m/r - \pi_i^c/r$  outweighs the increase of current profits  $\pi_i^d - \pi_i^m$ .

## Example – cartel stability in an infinitely repeated game

The same instructions as in the previous example:

Cartel profit  $\pi_i^m = 8$

Cournot profit  $\pi_i^{c(C)} = 64/9 = 7,\bar{1}$

Profit from default:  $\pi_i^d = 9$

What is the threshold interest rate that makes the cartel stable?

Cournot:

$$r < \frac{\pi_i^m - \pi_i^c}{\pi_i^d - \pi_i^m} = \frac{8 - 7,\bar{1}}{1} = 0,\bar{8}$$

Cartel is stable if the interest rate is below 89%.

## CASE: Indianapolis concrete cartel

2006 and 2007: the DOJ busted up a long-lived cartel with concrete.

How did the cartel work?

- regular meetings at local hotels – agreement on prices
- monitoring – directors anonymously gathered price quotes
- threats or an emergency meeting when the agreement was violated

Cartel had a lot of problems, but occasionally increased prices by 17%.

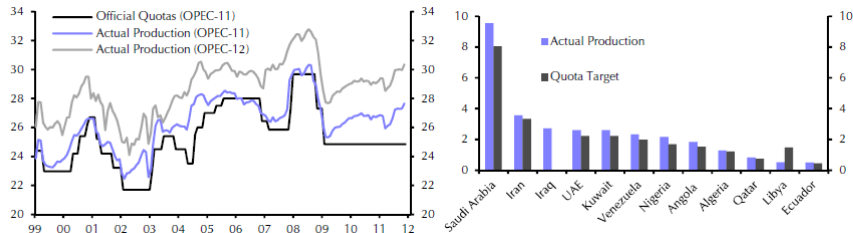
Why did the cartel fall apart?

- ① problem: a noncooperative manager from a firm outside of the cartel
- ② repeated attempts to persuade the manager to join the scheme
- ③ complaints about his performance to his corporate boss
- ④ manager went to the FBI and informed them of the cartel's operations

## EXAMPLE: OPEC

- legal cartel
- 12 members
- is not a monopoly – half of production from non-OPEC countries

Problems with overproduction – example (2011):



OPEC-11 = OPEC without Iraq that did not have a quota (transition phase)

Libya – not reaching its quota for technical reasons (Arab spring)

Source: <http://seekingalpha.com/article/314086-who-is-cheating-on-their-opec-production-quota>

## Asymmetric information

Up to now we assumed **complete information** = consumers and firms know quality of goods sold and purchased.

**Market with asymmetric information** = one side of the market has better information than the other side of the market.

Examples:

- health sector – the MD is better informed than the patient
- insurance – the client has better information than the insurer
- used cars – the seller has better information than the buyer

Asymmetric information  $\implies$  quantity traded can be inefficiently low.

There are private solutions of the problem of asymmetric information.



## Asymmetric information (cont'd)

We will deal with 2 types of asymmetric information...

- **adverse selection** – a situation, in which one side of the market does not observe the type/quality of the good on the other side
- **moral hazard** – a situation, in which one side of the market does not observe the behavior of the other side of the market

a 2 possible solutions of asymmetric-information problems.

- **signalization** – agents might want to invest in signals that will differentiate them from other agents
- **incentives** – using contract conditions to solve moral hazard in labor markets

## Example of adverse selection – the market for “lemons”

Market for used cars: good cars  $G$  and bad cars  $B$

Supply:

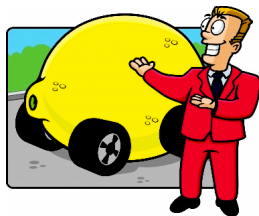
- 100 sellers offering 50  $G$  and 50  $B$
- willingness to sell  $G$  for \$2,000 and  $B$  for \$1,000

Demand:

- a large quantity of risk-neutral buyers
- each knows that 50 cars are  $G$  and 50 cars are  $B$
- willingness to purchase  $G$  for \$2,400 and  $B$  for \$1,200

If the buyers *can tell*  $G$  from  $B$ ,  
all good cars  $G$  sell for \$2,400  
and all bad cars  $B$  sell for \$1,200.

The market for used cars is efficient.



## Example of adverse selection – the market for “lemons”

What cars sell and for what price if the buyers can't tell  $G$  from  $B$ ?

If buyers can't tell  $G$  from  $B$ , their willingness to pay is

$$1/2 \times 1,200 + 1/2 \times 2,400 = \$1,800.$$

Who is willing to sell at the price? Only the owners  $B$ .

The buyer is willing to pay only

$$1 \times 1,200 = \$1,200.$$

Result: Only  $B$  will be traded in equilibrium for \$1,200.

Conclusion: The quantity sold in the market is inefficiently low.

Reason: The presence of  $B$  reduces the willingness to pay for  $G$   
(externality due to adverse selection)

## Example of signalization – the market for “lemons”

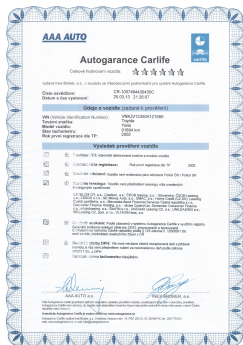
Sellers of  $G$  can signal that they have good cars.

E.g. they can spend \$100 for a certificate of quality.

If sellers of  $B$  can't get the certificate, customers can use the certificate to tell  $G$  from  $B$  – the certificate signals quality.

Certificates solve the adverse-selection problem:

- The market is efficient. Cars  $B$  and  $G$  are sold.
- The welfare in the market increases by  $50 \times (2,400 - 2,000 - 100) = \$15,000$ .



## Model of signalization – labor market in a town

### Labor supply:

10,000 able workers  $A$ :

- value of product:  $a_A = 16M$
- year of study costs:  $c_A = 0.2M$

10,000 unable workers  $U$ :

- value of product:  $a_U = 14M$
- year of study costs:  $c_U = 1M$

All workers are willing to work for a minimum wage  $w^{min} = 5$

### Demand for labor:

Perfect competition: many risk-neutral firms

Each firm has a production function:  $a_A L_A + a_U L_U$

### Endogenous variables:

- the number of workers:  $L_A$  and  $L_U$
- lifetime wage of workers:  $w_A$  and  $w_U$
- the number of years at the university:  $e_A$  and  $e_U$

## Model of signalization – labor market in a town (cont'd)

The town has no universities – no one has education ( $e_U = e_A = 0$ )

Who works and for what wages? Is the labor market efficient?

The result depends on whether firms can tell  $A$  from  $U$ .

- Complete information – firms can tell  $A$  from  $U$ :

Demand for labor as in perfect competition –  $w = \text{value } MP_L$ :

- $w_A = a_A = 16$
- $w_U = a_U = 14$

Wages higher than  $w^{min} \implies$  everyone works  $\implies$  efficient market

- Asymmetric information – firms cannot tell  $A$  from  $U$ :

Firms willing to pay an average value of  $MP_L$ :

$$w_A = w_U = a_A/2 + a_U/2 = 15$$

Wages higher than  $w^{min} \implies$  everyone works  $\implies$  efficient market

## Model of signalization – labor market in a town (cont'd)

Asymmetric information – firms cannot tell  $A$  from  $U$ .

Workers can study, but education does not increase their productivity.

Sequential game with two steps:

- 1 Workers have 2 choices:
  - study program lasting  $e^*$  years
  - study program lasting 0 years
- 2 Firms choose the wages of workers  $w_A$  and  $w_U$

Two different sequential equilibria:

- **pooling equilibrium** – all workers make the same choice  
⇒ not possible to tell  $A$  from  $U$
  - **separating equilibrium** –  $A$  and  $U$  make a different choices
- 

When does the separating equilibrium arise?

Do education opportunities increase efficiency of markets and welfare?

## Model of signalization – labor market in a town (cont'd)

Looking for separating equilibrium, in which  $A$  study and  $U$  don't.

In this separating equilibrium, firms believe that

- workers with education are  $A \implies$  they pay them  $w_A = a_A = 16$
- workers without education are  $U \implies$  they pay them  $w_U = a_U = 14$

If the duration of education  $e^*$  is in a range

$$\frac{a_A - a_U}{c_U} < e^* < \frac{a_A - a_U}{c_A}$$
$$2 < e^* < 10,$$

the profile  $(e_A, e_U, w_A, w_U) = (e^*, 0, 16, 14)$  is separating equilibrium.

It is an equilibrium – no incentive to change actions:

- firms maximize profit (workers  $A$  get  $a_A$  and  $U$  get  $a_U$ )
- $U$  does not choose  $e_U = e^*$  because the education cost  $1 \times e^* > 2$
- $A$  does not choose  $e_A = 0$  because wage increase  $2 > 0.2e^*$



## Model of signalization – labor market in a town (cont'd)

Do study possibilities increase welfare and efficiency of the market?

No:

- Market efficiency stays the same – efficient even without education.
- Welfare is lower because workers  $A$  spent  $0.2e^*$  for education (assuming that education does not create any value *per se*).

### BONUS QUESTION:

Does the result change if  $A$  can also freelance for  $w_A^f = a_A^f = 15.2$ ?

Yes:

If the education  $e^* < 4$ ,  $A$  are willing to study.

- Efficiency increases because  $A$  are more productive in firms:  $a_A > a_S^Z$
- Welfare is higher because the cost of studying  $0.2e^* < a_A - a_S^Z = 0.8$ . Education signals the quality of the worker.

# APPLICATION: The sheepskin effect

Difficult to measure the effect of diploma on wages – selection bias.

Clark and Martorell (JPE, 2014) – use regression discontinuity design.  
No evidence of a sheepskin effect of a Texan high school diploma.

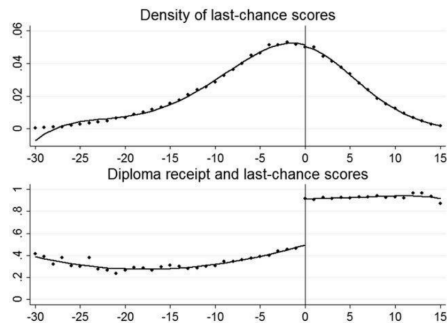


FIG. 1.—Last-chance exam scores and diploma receipt. The graphs are based on the last-chance sample. See table 1 and the text. Dots are test score cell means. The scores on the x-axis are the minimum of the section scores (recentered to be zero at the passing cutoff) that are taken in the last-chance exam. Lines are fourth-order polynomials fitted separately on either side of the passing threshold.

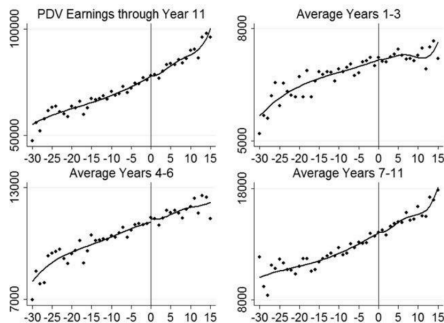


FIG. 2.—Earnings by last-chance exam scores. The graphs are based on the last-chance samples. See table 1 and the text. Dots are test score cell means. The scores on the x-axis are the minimum of the section scores (recentered to be zero at the passing cutoff) that are taken in the last-chance exam. Lines are fourth-order polynomials fitted separately on either side of the passing threshold.

## CASE: Reputations in collectibles sales

List (JPE, 2006) studied the market for sports memorabilia.

Asymmetric information – sellers know the value of the items.

Natural experiment:

- 1 Seller: „I would like to buy a card, which has a value of \$x.“
- 2 The buyers can offer a card of
  - a corresponding value
  - a lower value – but he may damage his reputation
- 3 the card is evaluated by an independent expert

Findings:

- local sellers cheat less (they are more often in the market)
- everyone cheats with items that cannot be evaluated by a third party



## Example of moral hazard – bicycle insurance

Theft probability depends on behavior (e.g. the number of locks).

If the insurance

- observes clients' behavior, it can adjust insurance accordingly
- does not observe the behavior, the insured bikers do not have incentives to take care of their bicycles = **moral hazard**

The insurance is not willing to provide full insurance (“deductible”).

The amount of insurance is inefficiently low due to moral hazard.



## CASE: Vehicle insurance

Probability of accident depends on many factors such as speed.  $\implies$  moral hazard occurs in this situation.

The insurance premium is usually based on driver's history. It is an imperfect solution of moral hazard.

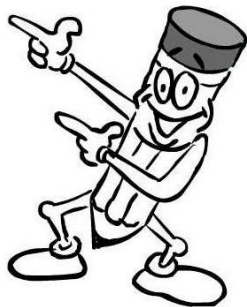
Solution: usage-based insurance (UBI) or pay as you drive (PAYD)

Payment for km may be based on data collected from the vehicle:

- type of driving (speed, braking)
- time-of-day information
- historic riskiness of the road
- distance or time traveled
- time/distance driven without a break

## What should you know?

- The prisoner's dilemma is a particular game in which the Pareto efficient outcome is strategically dominated by an inefficient outcome.
- A cartel is a group of firms that maximize profit of the industry.
- If firms play a one-shot or a finitely repeated game, the cartel is unstable.
- If they play an infinitely repeated game, punishment ensures cartel's stability if firms are sufficiently patient ( $r$  is low).



## What should you know? (cont'd)

- Adverse selection is a situation, in which one side of the market does not observe the type/quality of the good on the other side
- Moral hazard a situation, in which one side of the market does not observe the behavior of the other side of the market.
- Signalization may solve the problem of asymmetric information, but may also be publically wasteful.

