Name: University number (UČO):

Problem 1: Simplyfy and find conditions for:

$$\left(\frac{2x}{x+y} + \frac{y}{x-y} + \frac{y^2}{y^2 - x^2}\right) : \left(\frac{1}{x+y} + \frac{x}{x^2 - y^2}\right).$$

Problem 2: Solve the equation $4 + 2\sqrt{x - 4} = x$.

Problem 3: Solve the inequality $\frac{x}{x-5} > \frac{1}{2}$.

Problem 4: Solve the equation $4^{x+3} \cdot 8^{x-3} = 128$.

Problem 5: Solve the inequality $\log_5(3x-1) < 1$.

Problem 6: Solve the inequality $x^2 - 4x - 12 > 0$.

Problem 7: Solve the equation |x| - |x - 2| = 2.

Problem 8: Find the inverse of a function $y = \sqrt{x-1}$.

Problem 9: Find the intersections of the graphs of functions f and g, where $f(x) = x^2 - 11x + 20$, $g(x) = 6 - x^2$.

Problem 10: Sketch a graphs of functions $h(x) = 2^x$, $f(x) = 2^{-x}$ and $g(x) = -2^x$ into one picture.