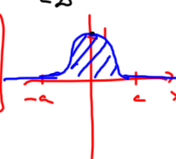


$L(af+bg) = (af+bg)(x_0) = a f(x_0) + b g(x_0)$   
 $\in \mathbb{R} \quad \in \mathbb{R} \quad \Rightarrow aL(f) + bL(g)$

$L(f) = \int_a^b f(x) g(x) dx$

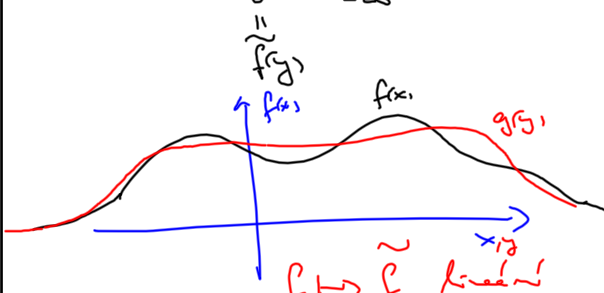
$L(f+g) = \int_a^b (f+g)(x) g(x) dx$   
 $= \int_a^b f(x) g(x) dx + \int_a^b g(x) g(x) dx = L(f) + L(g)$



5 9-14:06

$\mathcal{G} = \{ \text{integrable } f: I \rightarrow \mathbb{R} \}$   
 $\mathcal{G} \ni f \mapsto L_g(f) = \int_{-\infty}^{\infty} f(x) g(x-x) dx$

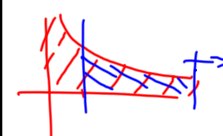
$f \mapsto \tilde{f}$  kernel



5 9-14:28

$\int_1^b \frac{1}{x^2} dx = \lim_{t \rightarrow \infty} \int_1^t \frac{1}{x^2} dx = \left[ -\frac{1}{x} \right]_1^t$   
 $= +1 - \frac{1}{t}$   
 $\rightarrow 1$

$f, g \mapsto f * g = \int_{-\infty}^{\infty} f(x) g(y-x) dx$   
 $t = y-x \quad dt = -dx$   
 $= \int_{-\infty}^{\infty} f(y-t) g(t) dt = \int_{-\infty}^{\infty} g(t) f(y-t) dt = g * f$



5 9-14:36

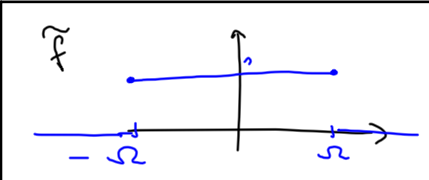
$F(f)(\omega) = \tilde{f}(\omega) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} f(t) e^{-i\omega t} dt$

Fourier transform  
 $a_n = \frac{1}{2\pi} \int_{-\infty}^{\infty} f(x) \cos nx dx$   
 $b_n = \frac{1}{2\pi} \int_{-\infty}^{\infty} f(x) \sin nx dx$

$C_n = \frac{1}{T} \int_{-T/2}^{T/2} f(t) e^{-i\omega t} dt$   
 $f(t) = \sum_{n=-\infty}^{\infty} C_n e^{i\omega t}$

5 9-14:46

$\tilde{f}$



$e \quad \xi \cdot l$

$e^{-i\omega(u+x)} = e^{-i\omega u} \cdot e^{-i\omega x}$

5 9-15:20