

IA165

# Combinatory Logic for Computational Semantics

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# PART I

- General Information about the course on "CL for CS"

- 12 lectures + 1 revision session from 24.02.2012 to 18.05.2012

- Class composition: lecture (1h) + classwork (45h)

- Friday from 12h to 1:50p.m

- Evaluation:

Homework (30%) + Final exam. (50%) + Attendance (10%)  
+ Participation (10%)

- Contact teacher: [qkang@fi.muni.cz](mailto:qkang@fi.muni.cz) office: B206

- Course web page:

<https://is.muni.cz/auth/course/fi/spring2012/IA165>

## Objectives

- Introduce the Combinatory Logic and its application to Computational Semantics  
: How the CL can be applied to semantic analysis of natural language
- Be familiar with a practical technique of constructing semantic representations of natural language and discover the properties of natural language

## Main readings

- H. Curry and R. Feys, *Combinatory Logic*, Vol1&2, 1958.
- P. Blackburn and Johan Bos, *Representation and Inference for Natural Languages: A First Course in Computational Semantics*, CSLI Publications, 2005.
- J.R. Hindley and J.P. Seldin,  *$\lambda$ -calculus and Combinators: An introduction*. Cambridge Univ. Press.

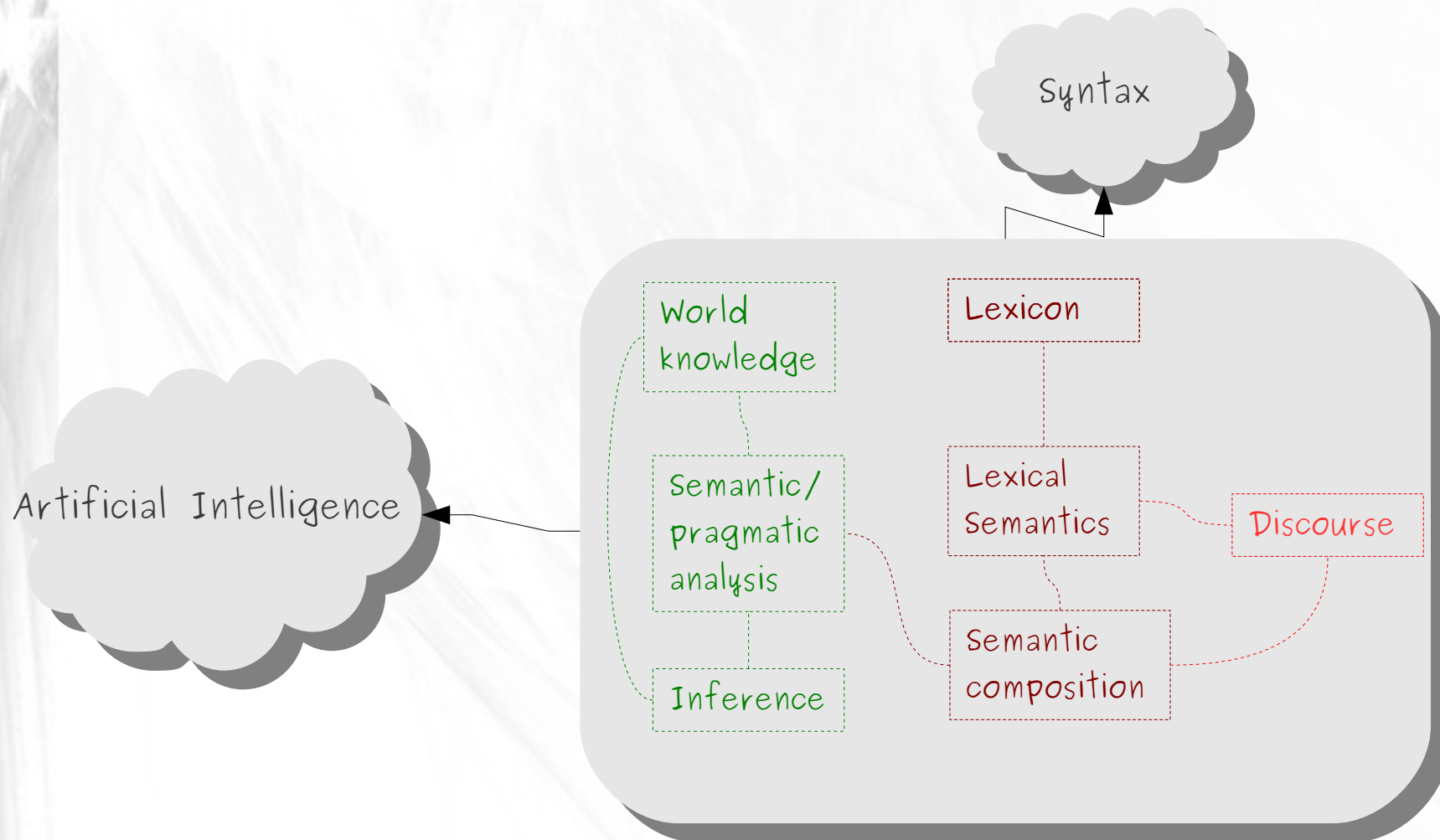
# PART II

## Background on Computational Semantics

# Why the Computational Semantics?

- Promising approach for many domain-embedded applications is to use the benefits of statistical models for disambiguation at a lexical/syntactic level, and then to use logical semantic representations for detailed interpretations

# Overview on Formal semantics





# Traditional Topics of CS

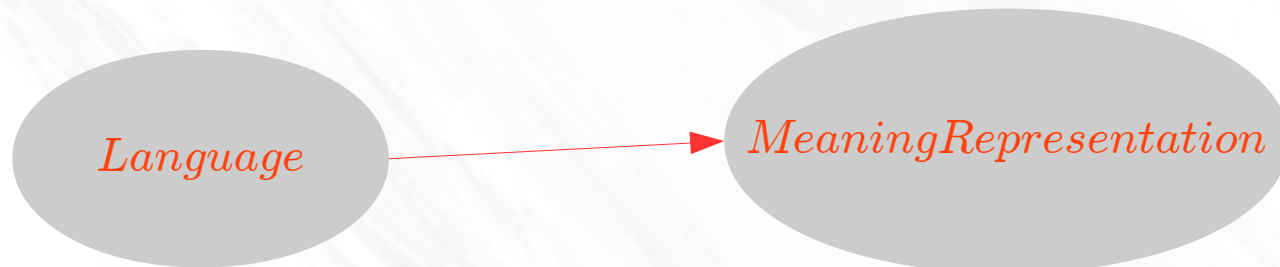
- Construction of meaning representation
- Semantic underspecification
- Anaphora resolution
- Presupposition projection
- quantifier scope resolution—formal semantics
- Statistical semantics

→ point of contact with lexical semantics

word sense disambiguation, semantic role labeling

# What to do

- How can we automate the process of associating semantic representations with expressions of natural language?



# Logical tools used in building meaning representation

- Use of First-Order Logic
- Use of Lambda-Calculus
- Use of Combinatory Logic
- Use of Type Theory
- Use of Propositional Logic
- Use of Modal Logic
- Various dynamic approaches (DRT, DPL...)

→ translating such simple sentences as "John loves Mary" and "A woman<sup>11</sup> walks" into formal semantic representations → being systematic

# Building a Semantic representation

- We need to complete the next three steps:
  - step 1: specify the reasonable syntax for the natural language fragment of interest
  - step 2 specify semantic representations for the lexical items.
  - step 3 specify the translation of constituents compositionally.

$\forall x(\text{MAN}(x) \rightarrow \text{WALK}(x))$  in first-order formula

$(\lambda x.\text{love}(x, \text{mary}))(\text{john}) \Rightarrow \text{love}(\text{john}, \text{mary})$  in lambda term

# What we mean by "systematic"

- In First-Order Logic,

*John loves Mary*

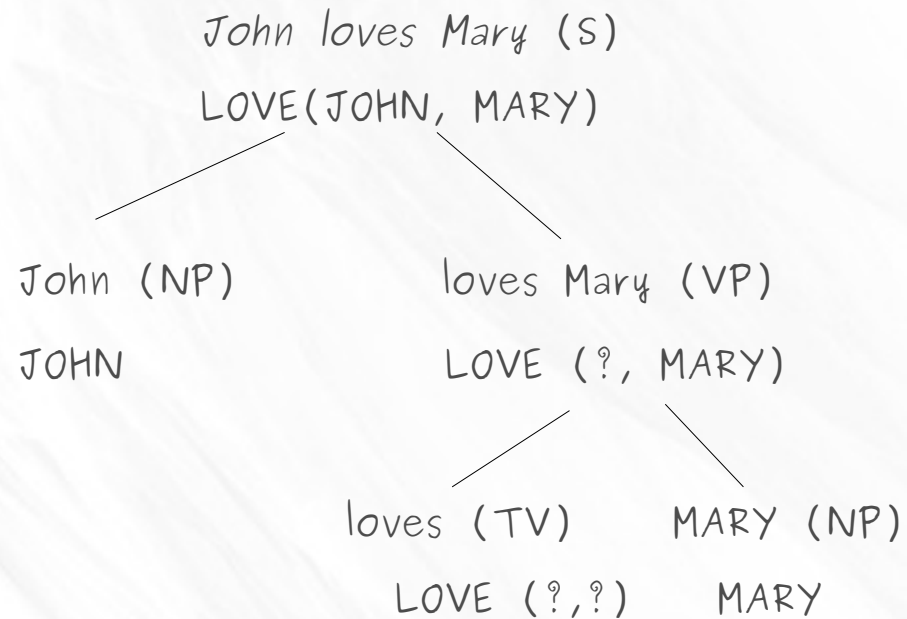
Semantic content is captured by the first-order formula :

**LOVE(JOHN, MARY)**

abstract denotation

# How to be systematic

- Notion of syntactic structure



# Summing up

- Building meaning representation

- 1) lexical items

- 2) syntactic structure

- 3) from syntax to semantics

→ tell us how the semantic constructions of the parts of a sentence are to be joined together.

# Syntax-semantic interface

- How to build a complete first-order formula?
  - The mechanism we're can mention is  $\lambda$ -calculus.

That is, lambda calculus is viewed as a notational extension of first-order logic : new operator for binding variables  $\rightarrow \lambda$

ex: simple  $\lambda$ -expression

$\lambda x.woman(x)$



# Function -argument structure

« A function is a rule of correspondence by which when anything is given (as argument) another thing (the value of the function for that argument) may be obtained. That is, a function is an operation which may be applied on one thing (the argument) to yield another thing (the value of the function)... »

—A.Church (1941)

# Concepts for Functional application

- operator
- Function
- Syncategoreme
- Incomplete expression

vs.

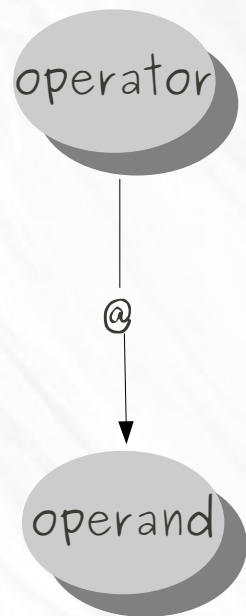
- operand
- Argument
- Categoreme
- Complete expression

#Non chronological order

- Incomplete expression theory of Frege (1879)
- "Logische Untersuchungen" (the distinction between dependent expression and independent expression) of Husserl (1900)

- All linguistic expressions are viewed as **operators** or **operands**.

Conventional notation: (operator(operand))

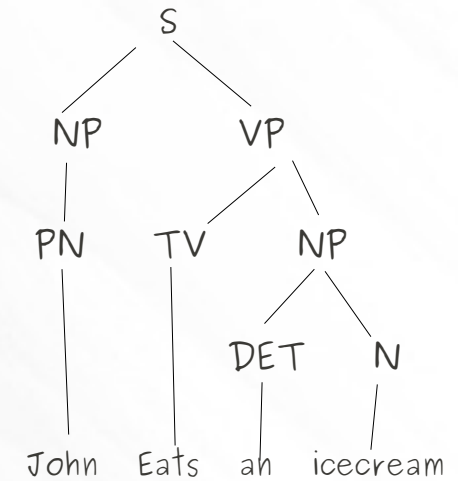
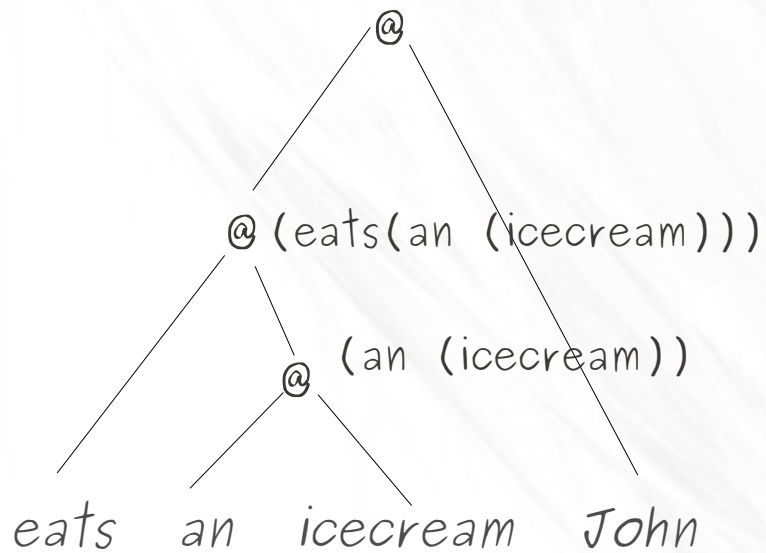


Verbs, adverbs,  
prepositions, conjunctions,  
negation, punctuation...

Noun phrase, Sentence

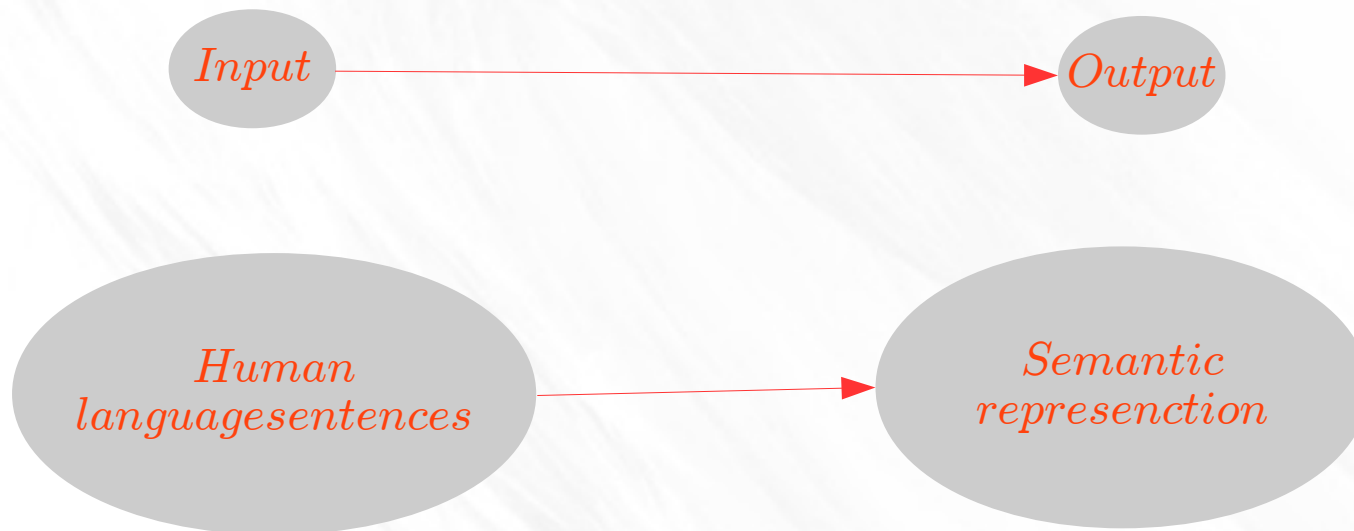
- One example: *John eats an icecream*

((eats(an (icecream))))John)



# Computing semantic representation

- How do we automate the process of assigning semantic representations to sentences of human language?



- Two main approaches

- 1) use of the unification

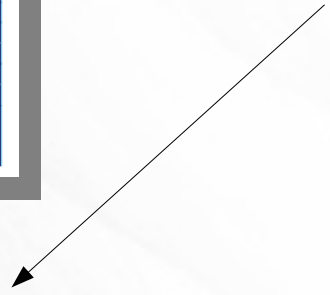
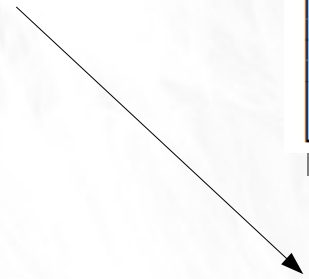
- 2) use of the lambda calculus

→ They both requires a grammar describing the syntactic structure of the fragment of language of interest.

$\left[ \begin{array}{l} \textit{phon: woman} \\ \textit{syn: noun} \\ \textit{sem: } \left[ \begin{array}{l} \textit{index: } \boxed{1} \\ \textit{content: WOMAN}(\boxed{1}) \end{array} \right] \end{array} \right]$

$\left[ \begin{array}{l} \textit{phon: walks} \\ \textit{syn: iv} \\ \textit{sem: } \left[ \begin{array}{l} \textit{index: } \boxed{1} \\ \textit{content: WALK}(\boxed{1}) \end{array} \right] \end{array} \right]$

$\left[ \begin{array}{l} \textit{phon: a} \\ \textit{syn: det} \\ \textit{sem: } \left[ \begin{array}{l} \textit{index: } \boxed{3} \\ \textit{restr: } \boxed{1} \\ \textit{scope: } \boxed{2} \\ \textit{content: } \exists \boxed{3}(\boxed{1} \wedge \boxed{2}) \end{array} \right] \end{array} \right]$

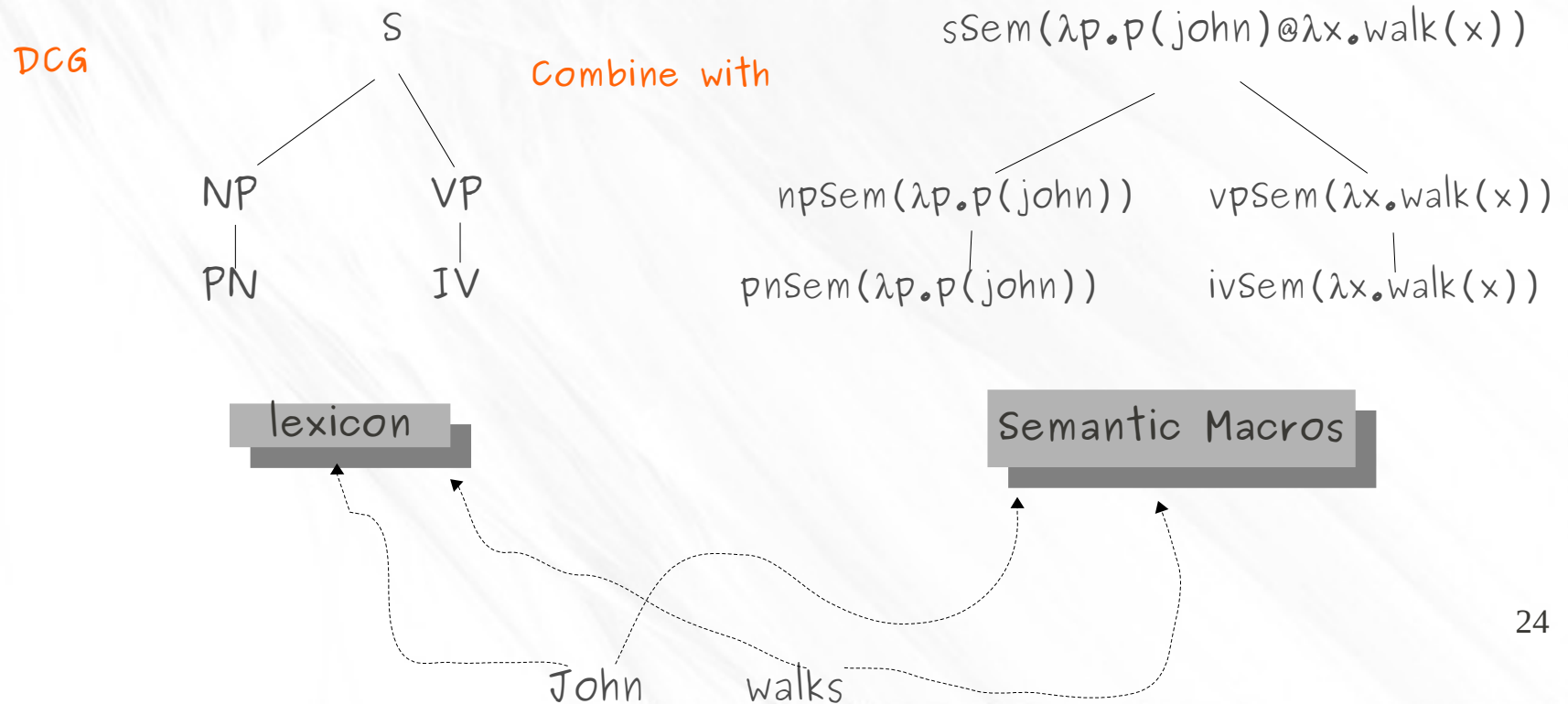


$\left[ \begin{array}{l} \textit{phon: a woman walks} \\ \textit{syn: s} \\ \textit{sem: } \left[ \textit{content: } \exists \boxed{1}(\textit{WOMAN}(\boxed{1}) \wedge \textit{WALK}(\boxed{1})) \right] \end{array} \right]$

$\exists x (\textit{WOMAN} ( x ) \wedge \textit{WALK} ( x ) )$

# Semantic construction system

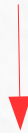
- One example of a modular implementation of a semantic construction system by Burchardt, Koller and Walter





- Various ways to construct logical formulae as meaning representations for sentences

→ How to do useful work with such meaning representation?



Finding out what can be inferred from the formula constructed for a sentence is a very important task in Computation Semantics.

# Next week...

- We will view the **Combinatory Logic** as a logical tool for representing a semantic meaning.