

Vzorce pro integrování

$$\int 0 \, dx = c,$$

$$\int 1 \, dx = x + c,$$

$$\int x^a \, dx = \frac{x^{a+1}}{a+1} + c \quad \text{pro } a \neq -1$$

$$\int \frac{1}{x} \, dx = \ln |x| + c,$$

$$\int e^x \, dx = e^x + c,$$

$$\int a^x \, dx = \frac{a^x}{\ln a} + c,$$

$$\int \cos x \, dx = \sin x + c,$$

$$\int \sin x \, dx = -\cos x + c,$$

$$\int \frac{1}{\cos^2 x} \, dx = \operatorname{tg} x + c,$$

$$\int \frac{1}{\sin^2 x} \, dx = -\operatorname{cotg} x + c,$$

$$\int \frac{1}{x^2 + 1} \, dx = \operatorname{arctg} x + c,$$

$$\int \frac{1}{\sqrt{1-x^2}} \, dx = \operatorname{arcsin} x + c,$$

linearita integrálu: $\int (f \pm g) = \int f \pm \int g$, $\int k \cdot f = k \int f$ pro $k \in \mathbb{R}$

per partes: $\int f \cdot g' = f \cdot g - \int f' \cdot g$

substituce: $\int f(g(x)) \cdot g'(x) \, dx = \int f(y) \, dy = F(y) + c = F(g(x)) + c$,
kde F je primitivní funkce k funkci f

integrály funkcí ve speciálním tvaru:

$$\int f(ax + b) \, dx = \frac{1}{a} F(ax + b) + c,$$

$$\int \frac{f'(x)}{f(x)} \, dx = \ln |f(x)| + c,$$

$$\int f(x) \cdot f'(x) \, dx = \frac{1}{2} f^2(x) + c,$$

$$\int \frac{1}{x^2 + a} \, dx = \frac{1}{\sqrt{a}} \operatorname{arctg} \frac{x}{\sqrt{a}} + c \quad \text{pro } a > 0$$