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Basic Terrain Generation

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PA199 Advanced Game Design

Lecture 7 Terrain Generation

> Dr. Fotis Liarokapis 09th April 2018



Terrain Data

- Terrain data relates to the 3D configuration of the surface of the Earth
- Map data refers to data located on the surface of the Earth (2D)
- The geometry of a terrain is modeled as a 2 ½-dimensional surface



Terrain Models

- Global terrain model
 Defined by a single function interpolating all data
- Local terrain models
 - Defined on a partition of the domain into patches
 - They represent the terrain by means of a different function on each of the regions in which the domain is subdivided
- In general it is very difficult to find a single function that interpolates all available data

 Usually local models are used

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Mathematical Terrain Models

- A topographic surface or terrain can be mathematically modeled by the image of a real bi-variate function: z = \$\phi\$ (x, y)
- Defined over a domain D such that $\mathsf{D} \, \underline{\subset} \, \Re^2$
- The pair T=(D, ϕ) is called a mathematical terrain model









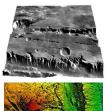
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Digital Elevation Models (DEMs)

- DEM is set of regularly or irregularly spaced height values
 - Terrain elevation data
- No other information



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DEM Video





Elevation Data Acquisition

- Elevation data can be acquired through:
 - Sampling technologies
 - i.e. on-site measurements or remote sensing techniques
 - Digitisation of existing contour maps
- Elevation data can be scattered (irregularly distributed) or form a regular grid
- The set of non-crossing lines can form a collection of polygonal chains



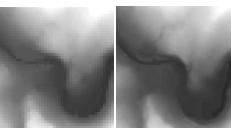
UK DEM Data Sources

http://www.ordnancesurvey.co.uk/

- Ordnance Survey:
 - Landform Panorama
 - Source scale: 1:50,000
 - Resolution: 50m
 - Vertical accuracy: ±3m
 - Landform Profile
 - Source scale: 1:10,000
 - Resolution: 10m
 - Vertical accuracy: ±0.3m



Comparison

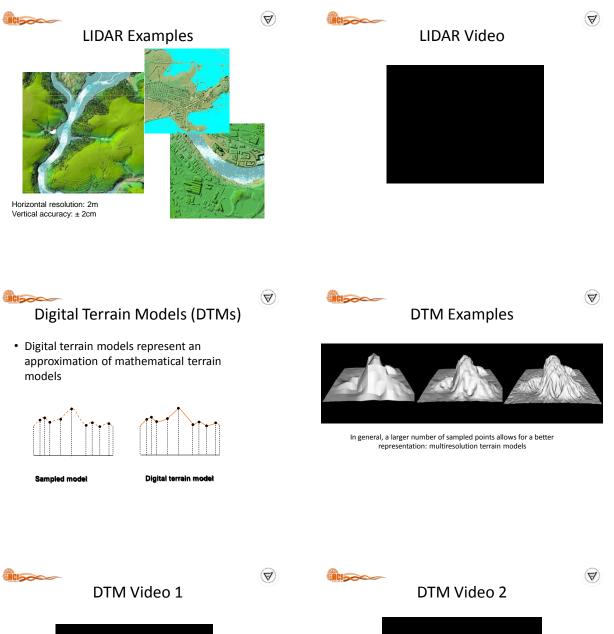


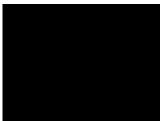
Landform Panorama

Landform Profile

Light Detection And Ranging (LIDAR)

- LIDAR is a remote sensing technology that measures distance by illuminating a target with a laser and analyzing the reflected light
 - Uses ultraviolet, visible or near infrared light to image objects
 - Can target a wide range of materials
 - i.e. non-metallic objects, rocks, rain, chemical compounds, aerosols, clouds, single molecules







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DTM Types

- Polyhedral terrain models
- Gridded elevation models
- Contour maps

Polyhedral Terrain Models (PTM)

- A PTM for a set of sampled points V can be defined on the basis of:
 - A partition of the domain D into polygonal regions having their vertices at points in V
 - A function f that is linear over each region of the partition
 - The image of f over each polygonal region is a planar patch to guarantee continuity of the surface along the common edges

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PTM Properties

- Can be used for any type of sampled pointset
 - Regularly and irregularly distributed
- Can adapt to the irregularity of terrains
- Represent continuous surfaces

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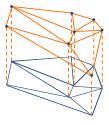
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Triangulated Irregular Networks (TINs)

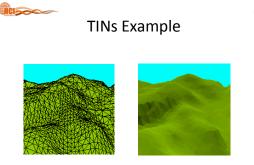
- TINs are the most commonly used PTMs

 Each polygon of the
 - domain partition is a triangle



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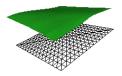


Example of a TIN based on irregularly distributed data



TINs for Regular Data

 Regular sampling is enough in areas where the terrain elevation is more or less constant





TINs Properties

- They guarantee the existence of a planar patch for each region (triangle) of the domain subdivision (three points define a plane)
 - The resulting surface interpolates all elevation data
- The most commonly used triangulations are **Delaunay triangulations**



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TIN Video





Why Delaunay Triangulations

- They generate the most equiangular triangles in the domain subdivision
 - Thus minimising numerical problems • e.g. Point location
- Their Dual is a Voronoi diagram
- Therefore, some proximity queries can be solved efficiently

Why Delaunay Triangulations.

- It has been proven that they generate the best surface approximation independently of the z values
 - -In terms of roughness
- Several efficient algorithms to calculate them exist!



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Delaunay Triangulations

- Intuitively: given a set V of points, among all the triangulations that can be generated with the points of V, the Delaunay triangulation is the one in which triangles are as much equiangular as possible
 - Delaunay triangulations tend to avoid long and thin triangles

Does P lie inside t or t Ρ on its boundary?

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Voronoi Diagrams

· Given a set V of points in the plane, the Voronoi Diagram for V is the partition of the plane into polygons such that each polygon contains one point p of V and is composed of all points in the plane that are closer to **p** than to any other point of V





Voronoi Diagrams.

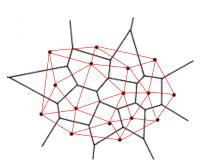
- Property
 - The straight-line dual of the Voronoi diagram of V is a Delaunay triangulation of V
- Dual
 - Obtained by replacing each polygon with a point and each point with a polygon
- Connect all pairs of points contained in Voronoi cells that share an edge

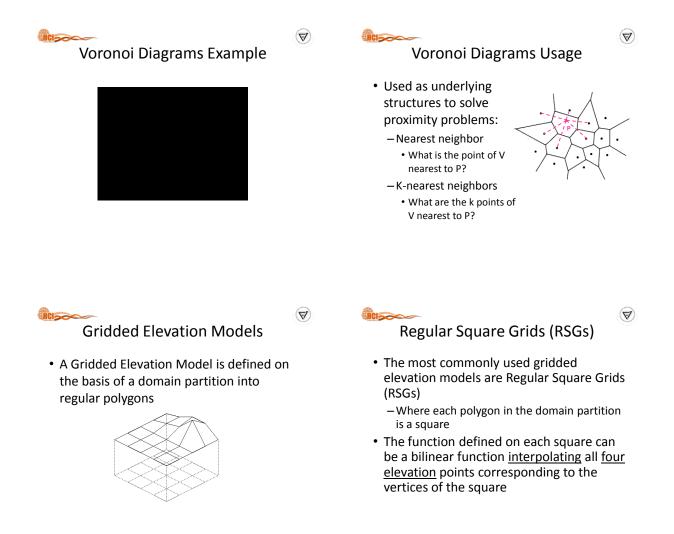
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Voronoi Diagrams Example

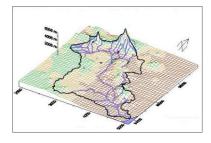




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RSG Example



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RSG Stepped Model

- Alternatively, a constant function can be associated with each square (i.e., a constant elevation value)
- This is called a stepped model

 It presents discontinuity steps along the edges of the squares





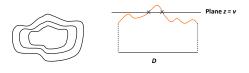
TINs vs RSGs

- Both models support automated terrain analysis operations
 - RSGs are based on regular data distribution
 - TINs can be based both on regular and irregular data distribution
- Irregular data distribution allows to adapt to the "variability" of the terrain relief
 - More appropriate and flexible representation of the topographic surface

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Digital Contours

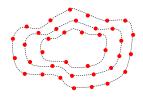
- Given a sequence { v0 , ..., vn } of real values, a digital contour map of a mathematical terrain model (D, ϕ) is an approximation of the set of contour lines
- { (x,y) \in D, $\varphi(x,y) = vi$ } i = 0, ..., n





Digital Contour Maps

 Contours are usually available as sequences of points



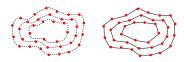


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Digital Contour Maps .

- A line interportating points of a contour can be obtained in different ways
- Typical examples
 - Polygonal chains
 - -Lines described by higher order equations



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Digital Contour Maps Properties

- They are easily drawn on paper
- They are very intuitive for humans
- They are not good for complex automated terrain analysis

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Problems with DEMs

- Issues worth considering when creating/using DTMs
 - -Quality of data used to generate DEM
 - -Interpolation technique
 - -Give rise to errors in surface such as:
 - -Sloping lakes and rivers flowing uphill
 - Local minima
 - -Stepped appearance
 - -etc

Example Applications

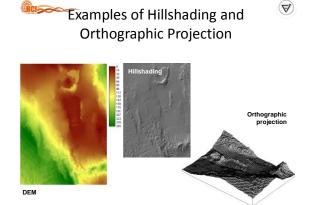
- Visualisation
 - Terrain and other 3D surfaces
- Visibility analysis
 - Intervisibility matrices and viewsheds
- Hydrological modeling

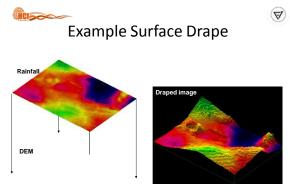
 Catchment modeling and flow models
- Engineering
 - -Cut & fill, profiles, etc

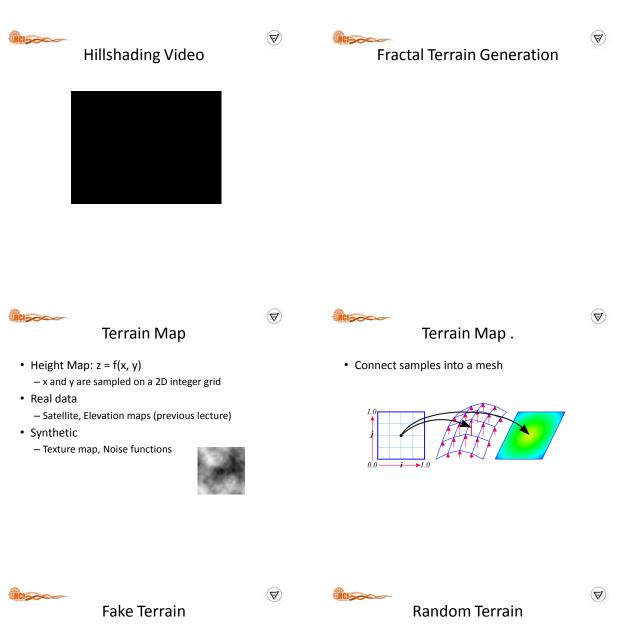


Terrain Visualisation

- Analytical hillshading
- Orthographic views
 - Any azimuth, altitude, view distance/point
 Surface drapes (point, line and area data)
- Animated 'fly-through'
- What if? modeling
 - Photorealism
 - Photomontage
 - CAD







- Generate the height-field
- Random process
 - This can be controlled
- Reflects 'realistic' terrain in some way



Terrain (x,y) = rand (MAX_HEIGHT)Results in random noise

- Next step:
 - $-\operatorname{Smooth}$ the terrain generated above
 - Finite Impulse Response (FIR) filter:

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Procedural Modeling With Fractals

- Procedural Modeling
 - Compute geometry "on-the-fly"
- Fractals
 - Model Natural Phenomena Self Similarity
 Mountains, fire, clouds, etc
 - Scales to infinity
 - Add or "make up" natural looking details with mathematical tools

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Fractals - A Definition

 A geometrically complex object, the complexity of which arises through the repetition of some shape over a range of scales



 Sufficient definition for describing terrains





Fractals in Nature

- Fractals are common in:
 - Mountains, clouds, trees, turbulence, circulatory systems in plants and animals
- Wide variety of other phenomena such as:
 - Noise in transistors
 - Fluctuations in river fluxes





Fractal Geometry

- Fractal geometry is very powerful!
 - But not sufficient for describing the complex forms found in Nature
- Mathematics are simple
 - Based on the Euclidean geometry of lines, planes, spheres and cones
- Fractal geometry has very little use in describing man-made objects

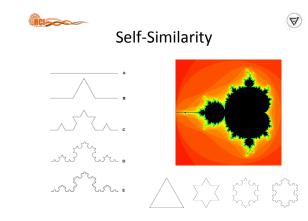


Fractal Properties

- Two properties:
 - Self-similarity

- Fractal Dimension





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Fractal Dimension

- Euclidean dimensions
- 1, 2, 3, 4, ...
- Fractal

 1.2342, 2.7656
- Measure of detail or roughness of a fractal — D = (In N)/(In 1/s)

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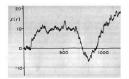
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Brownian Motion

- One of the most realistic ways of representing natural objects is the Brownian motion method because of the ability of creating peculiar curves
- Brownian method has been used to describe the chaotic and random manner in which a particle moves in a fluid
 - -Application in terrains

Brownian Motion Examples





```
Graph of a Brownian Sample Function
```

A simulation of a Brownian Path in 2-Dimensions

Fractional Brownian motion (fBm)

- fBm consists of steps in a random direction and with a step-length that has some characteristic value
 - Also known as the Random Walk Process
 Hence the random walk process
- A key feature to fBm is that if you zoom in on any part of the function you will produce a similar random walk in the zoomed in part



Differences

- The main difference between fBm and regular Brownian motion is that while the increments in Brownian Motion are independent they are dependent in fBm
 - This dependence means that if there is an increasing pattern in the previous steps, then it is likely that the current step will be increasing as well

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Code Example of fBm



total = 0.0f; //for each pixel, get the value

frequency = 1.0f/(float)hgrid; amplitude = gain;

```
for (i = 0; i < octaves; ++i)
```

map[x][y]=total; //now that we have the value, put it in



Terrain using fBm Noise

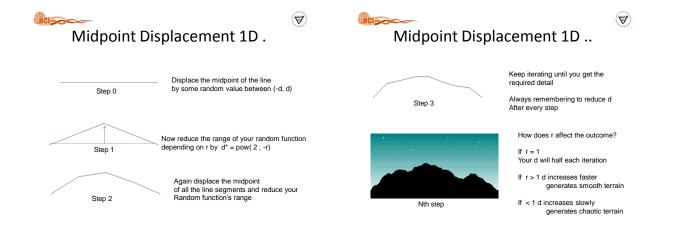
- A simple approach is to generate a heightmap using fBm noise
 - Results look ok but not very realistic
 - Since fBm is homogeneous and isotropic



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Midpoint Displacement 1D

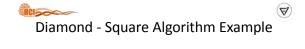
- Type of polygon subdivision algorithm, also a fractal function
- Created to simulate tectonic uplift of mountain ranges
- One of its main input parameters is the roughness constant r

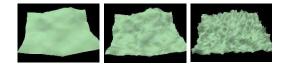


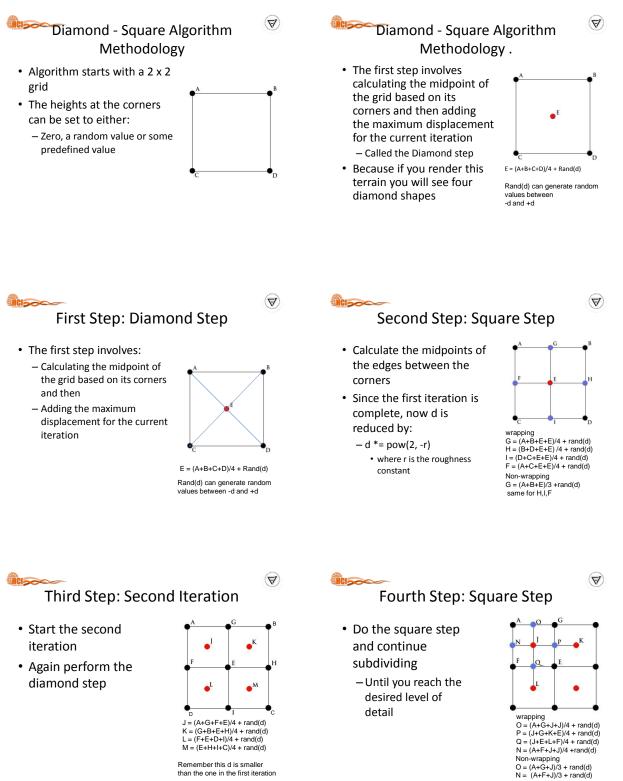
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Diamond - Square Algorithm

- Also called the cloud fractal, plasma fractal or random midpoint displacement
- The 2D version of the original Midpoint displacement algorithm
 - Therefore it also has a roughness constant
- The algorithm works best if it is run on square grids of width 2ⁿ
 - This ensures that the rectangle size will have an integer value at each iteration







Remember this d is smaller than the one in the first iteration

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Diamond - Square Algorithm Summary

- While length of square sides > 0
 - Pass through the whole array and apply the diamond step for each square
 - Pass through the whole array and apply the square step for each diamond
 - Reduce the range of the random displacement



Smoothness of Terrain

 Lorentz and Gaussian distributions for the height array can control the smoothness of the terrain

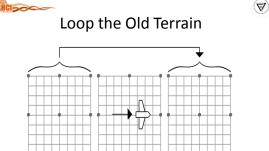
height = y = (random number) × $\frac{D^2 / 8}{(x - x_o)^2 + (z - z_o)^2 + D^2 / 8}$

- where (x_0, z_0) is the position of the peak and D² is the length of the square
- The value of the width affects the smoothness of the terrain
 - By decreasing the width of the bell-shaped distribution the terrain becomes steeper



Outer Boundaries

- Three solutions can be considered:
 - Large terrain
 - The user would never reach the outer boundary
 - -Loop the old terrain
 - When the user reaches a boundary the user reenters the map on the opposite side
 - -Infinite terrain
 - When the user reaches a boundary an extension to the map is added

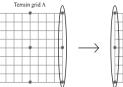


Upon reaching the right side of the landscape, a tile of terrain is mo in front of the player to provide the illusion of endless terrain



Infinite Terrain

Upon reaching the right side of terrain grid A, the values of the far-right points are copied to the far left points of terrain grid B





Terrain grid F

The other points of terrain grid B are then calculated via randomization and mid-point displacement, as done for grid A





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Other Techniques

- Cracked terrains for dry lakes and riverbeds
- Throw random points onto the plane
- Construct the Voronoi diagram and use the graph to etch into the terrain

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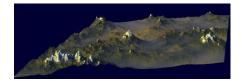
Cracked Terrains

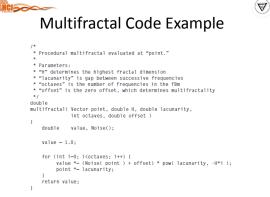


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Multifractals

- A better choice would be to use Multifractals – Proposed by Kenton Musgrave
- These are fractals whose dimension/roughness varies with location



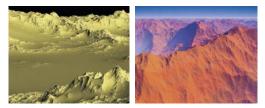




Other Multifractals

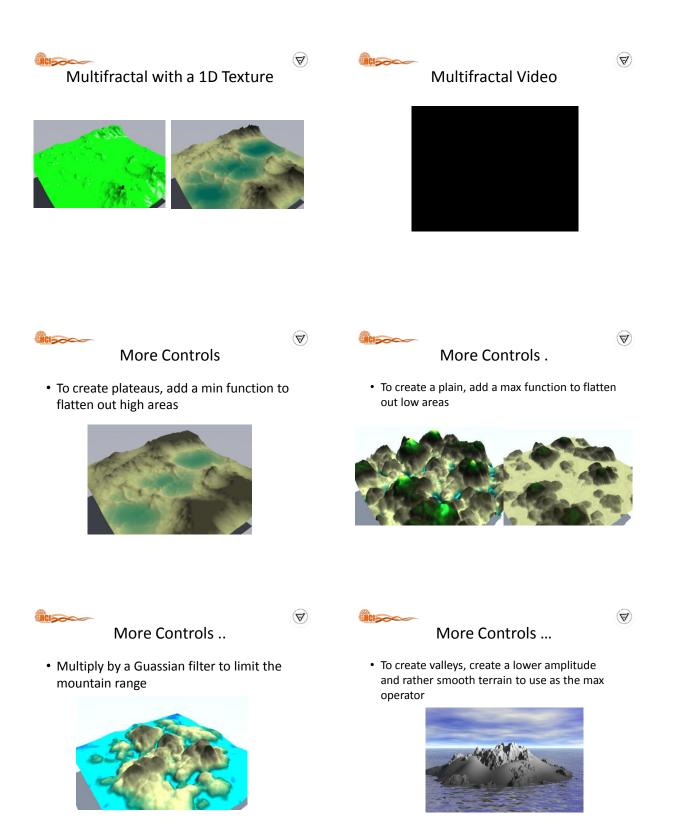
- Hybrid multifractals
 - Called hybrid because they are both additive and multiplicative multifractals
- Ridged multifractals
 - -Similar to Perlin's turbulence noise
 - They calculate 1-abs(noise) so that the resulting "canyons" from abs(noise) become high ridges

Other Multifractal Examples



Ridged multifractal terrains : taken from Texturing and Modeling: A Procedural Approach pg 518 (left) pg 480(right)

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• Quantize a terrain to create ridges

- Use directly or as the min function
- Can also be done as a transfer function that maps f(x)->g(x)

Ridges



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Fault Line Algorithm

- This algorithm is a very simple one, yet its results, although not the best, are pretty good
- The technique is not limited to planar height fields, being also applicable to spheres to generate artificial planets
 - Can also approximate real world terrain features such as escarpments, mesas, and seaside cliffs

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Fault Line Algorithm .

- Start with a planar height field

 All points have zero height
- Then select a random line which divides the terrain in two parts
 - The points to one side of the line will have their height displaced upwards
 - The points on the other side will have their heights displaced downwards



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Fault Line Algorithm ..

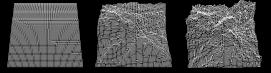
- The red points will have their height decreased, whereas the blue points will have their height increased
 - So the terrain has two distinct heights
- If we keep dividing the terrain can get something that has valleys, mountains and so on



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First step in faulting process





1 iteration

100 iterations

400 iterations

Generating Fault Lines in a Height Field[♥] Grid

- Randomly pick two grid points ${\bf p}_1$ and ${\bf p}_2$
- · Calculate the line between them
- Go through all the points in the height field and add or subtract an offset value depending on what side of the line they are located
- Before the next fault is drawn reduce the range of the offset by some amount



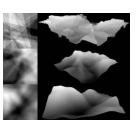
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Filtering Height Fields

- Height fields generated by this algorithm need to be filtered to look more realistic
 - A low pass filter can be used

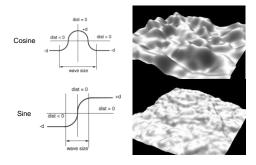


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Variations to the Fault Line Algorithm



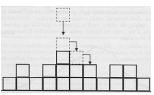
Particle Deposition .

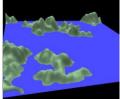


Particle Deposition

- Simulates volcanic mountain ranges and island systems
 - Drop random particles in a blank grid
 - Determine if the particle's neighboring cells are of a lower height
 - If true, increment the height of the lowest cell
 - Keep checking its surrounding cells for a set number of steps or until it is the lowest height among its surrounding cells
 - If not, increment the height of the current cell







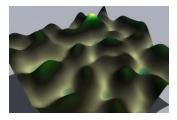
Generated after 5 series of 1000 iterations



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 Using a 1D texture map based on the altitude can provide many useful mapping

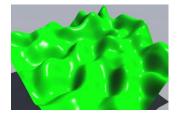
Terrain Coloring





Perlin Noise

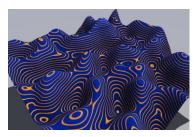
• Using a sampling of 2D Perlin Noise provides smooth hills





Terrain Coloring.

• Striped 1D texture map



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Terrain Coloring ..

• Using a 2D texture map provides richer detail, but is independent of the terrain





Terrain Coloring ...

• More advanced coloring is based on altitude and slope





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Rolling Hills

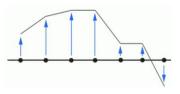
• Scaling in one dimension gives smooth rolling hills





Height Fields Issues

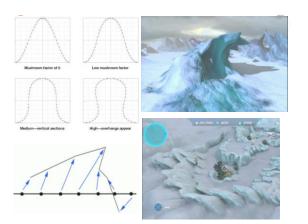
• They cannot generate overhangs or caves





- "Mushrooming" effects that involve the manipulation of vertex normals
 - To render height field textures with overhangs
- The game Halo Wars implemented a new type of height field called a vector height field
 - Stored a vector to displace a vertex instead of a height value

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Realistic Terrain Video 1





Realistic Terrain Video 2





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Erosion

- Hydraulic Erosion
 - Water (rain) depositing to settle in height field
- Thermal Weathering
 - "Any material that knocks material loose, which then falls down to pile up at the bottom of an incline."









Erosion Examples



Erosion by Water

Erosion by Wind and Water



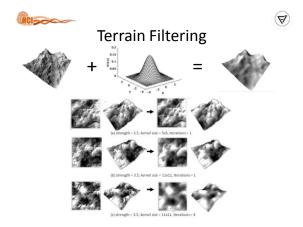
Mesh control menu

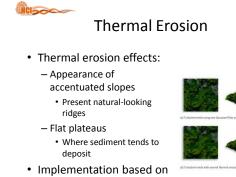
Erosion menu

Filters menu

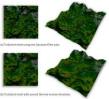
Three gradual values for the 'roughness' parameter and a mesh size of a

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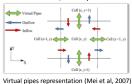
(Musgrave et al., 1989), (Jako and Toth, 2011)





Hydraulic Erosion

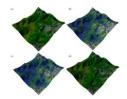
- Hydraulic erosion refers to the natural process in which the motion of fluids (specifically water) produces mechanical weathering over the soil
 - (Mei et al, 2007), (Anh et al., 2007), (Štava et al., 2008), (Jákó and Tóth, 2011)

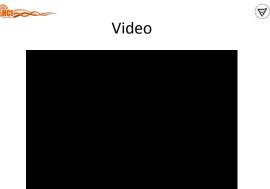




Rain Simulation & Evaporation

- The rainfall causes the water levels to rise up at random positions
- · Water movement by allowing water to escape
 - Approximation of the sediment amount that is to be eroded
- Water evaporation based on environmental heat





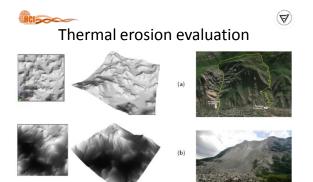
I Conference on Games and Virtual Worlds for Serious Cristea, A., Liarokapis, F. Fractal Nature - Generating Realistic Terrains for Games, Proc. of the 7th Inter Applications (VS-Games 2015), IEEE Computer Society, Skovde, Sweden, 16-18 September, 84-91, 2015.



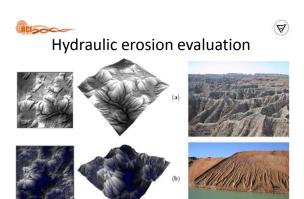
Evaluation

- Qualitative evaluation with 12 expert users
 - 6 academics with computer graphics/virtual reality background
 - 6 industry professionals working in game companies
- Three stage evaluation:
 - GUI exploration
 - Simple flight simulator game
 - Comparison with real landscapes

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(a) Medium temperature values comparison (b) High temperature values comparison



(a) Low density + heavy erosion comparison (b) Low density + high viscosity comparison



Academics Feedback

- · Improve the visual realism of the terrain
 - More accurate algorithms for hydraulic erosion
 - Making the software open-source
 - Compare these methods with Perlin noise generator
 - Port the implementation (or part of it) on GPUs
 - Implement fluid simulation for the representation of sea, rivers and lakes
 - Stochastic smoothing algorithms to make the landscapes look more realistic



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Industry Feedback

- The level of realism quite satisfying and appropriate for the generation of interactive video games Strong similarities with real life landscapes
- All of them stated that the generated terrains cannot be used without manual editing into modern games
 - Larger studios mentioned that they are using similar procedural approaches but then they perform a lot of editing
 - Independent studios stated that they could use the generated terrain as they are
- More procedural elements such as different types of trees and plants
- Better texturing techniques

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Conclusions

- Real terrain data still used in games
 - Very expensive
 - Need a lot of manual editing
- Procedural are getting more and more attention
 - More work is required to make them more realistic





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