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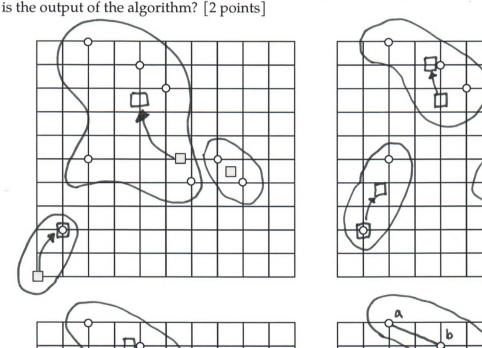
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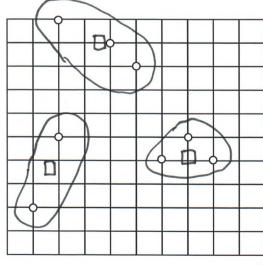
Explain the following aspects of the *K*-means flat clustering algorithm [2 points]:

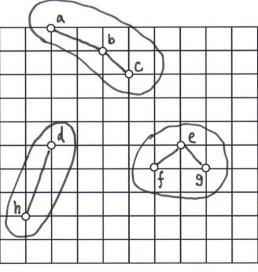
- 1. What do we need to know about our dataset before using the algorithm?
- 2. What is the input and the output of the algorithm?
- 3. What are the two steps that take place in every epoch?
- 4. How do we decide in which epoch to stop the algorithm?
- 1. The number of classes K and initial mean estimates (seeds).
- 2. I: unclassified points and K seeds. O: K groups (clusters) of points.
- 3. Reassigning points, recomputing centroids.

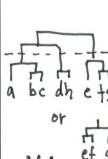
4. Centroids converged.

Given the points O, and the seeds \square , run the K-means algorithm for three epochs. Draw the state of the algorithm at the beginning and after every epoch; no computation should be necessary. What









Perform a hierarchical clustering of the above dataset into three classes using the single-link hierarchical agglomerative clustering algorithm, and draw the resulting dendrogram. [1 point] Is the output the same as the output of the K-means flat hierarchical clustering algorithm above? [1 point]

Yes, it is.

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Consider the following collection of four documents d_i :

- d_1 : Breakthrough drug for hiv
- d_2 : NEW HIV DRUG
- d_3 : NEW APPROACH FOR TREATMENT OF HIV
- d_4 : New hopes for hiv patients

Produce a list of (term, document ID) tuples [1 point], sort this list in lexicographical order [1 point], and use the sorted list to construct an inverted index [1 point]. Write down each step. Describe how you would produce this index using the MapReduce distributed framework [2 points].

(approach, 3), (breakthrough, 1), (drug, 1), (drug, 2), (for, 1), (for, 3), (for, 4), (HIV, 1), (HIV, 2), (HIV, 3), (HIV, 4), (hopes, 4), (new, 2), (new, 3), (new, 4), (of, 3), (patients, 4), (treatment, 3)

approach -> 3 breakthrough -> 1 drug -> 1 -> 2 for > 1 -> 3 -> 4 HIV -> 1 -> 2 -> 3 -> 4 hopes -> 4 new -> 2 -> 3 -> 4 patients -> 4 treatment -> 3

Each parser would process a limited number of documents and produce a sorted (term, document ID) list. Each inverter would take all sublists in a certain alphabetical range of terms and produce postings for that alphabetical range.

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Compute an unbiased estimate of a text retrieval system's precision, recall, and the F_1 measure on the first five esults [2 points], and the *precision at 40% recall* [2 points] given the following lists of results for queries q_1 , and q_2 , where R is a relevant result, and N is a non-relevant result:

- Results for q_1 : RNNRRNR (10 relevant results for q_1 exist in the collection.)
- Results for q_2 : NRNRRRRN (5 relevant results for q_2 exist in the collection.)

The first five results for query q1: RNNRR 92: NRNRR

$$P_1 = \frac{3}{5}$$

$$R_1 = \frac{3}{10}$$

$$F_{191} = \frac{2 \cdot 3|5 \cdot 3|10}{3|5 + 3|10} = \frac{9|25}{9|10} = \frac{10}{25} = \frac{2}{5}$$

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$$P_2 = \frac{3}{5}$$

$$R_2 = \frac{3}{5}$$

$$F_{192} = \frac{2.3|5.3|5}{3|5+3|5} = \frac{3}{5}$$

$$P@5 = \frac{3}{5}$$

$$R@5 = \frac{9}{20}$$

$$F_1@5 = \frac{1}{2}$$

in your computations

The results with 40% recall for query 91: RNNRRNR

92: NRNR

$$R_{q_1} @ 7 = \frac{4}{10}$$
 $P_{q_1} @ 7 = \frac{4}{7}$

$$R_{92}@4 = \frac{2}{5}$$

$$P_{qz}@4 = \frac{2}{4} = \frac{1}{2}$$

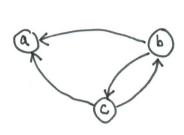
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Given a directed graph G that represents three Web pages $V(G) = \{a,b,c\}$, and the links $E(G) = \{(b,a),(c,a),(c,b),(b,c)\}$ between these three pages, draw G [1 point] and produce the adjacency matrix (also known as the link matrix) A [1 point], and the Markov transition matrix P [2 points].

Describe the intuition behind *the PageRank algorithm* [1 point]. Compute the *PageRank* of the pages *a*, *b*, and *c* using a single iteration of the PageRank algorithm [2 points].

Describe what we mean, when we call a page a hub, or an authority [1 point]. Compute the hub, and authority scores of the pages a, b, and c [2 points].



Graph 6:

$$A = \begin{bmatrix} 0 & 0 & 0 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{bmatrix}$$

$$P = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{bmatrix} \circ \begin{bmatrix} 1 & 3 & 1 & 1 & 3 \\ 1 & 1 & 2 & 1 & 1 \\ 1 & 1 & 2 & 1 & 2 \end{bmatrix} \cdot (1 - 1) + \frac{1}{3}$$

where 0 is the Hadamard product.

The PageRank algorithm computes the probability that a hypothetical random surfer will end up at a given web page.

$$\overrightarrow{X}_0 = (1 \ 0 \ 0)$$

$$\vec{x}_1 = \vec{x}_0 \cdot P = [100] \begin{bmatrix} 113 & 113 & 113 \\ & & & \\ \end{bmatrix} = \begin{bmatrix} \frac{1}{3} & \frac{1}{3} & \frac{1}{3} \end{bmatrix}$$

A hub is a web page pointing to many anthorities.

An authority is a web page that many hubs point to.

$$\overrightarrow{h}_0 = [111]^T$$

$$\vec{a}_0 = [1111]^T$$

$$A \cdot A^{T} = \begin{bmatrix} 0 & 0 & 0 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{bmatrix} \cdot \begin{bmatrix} 0 & 1 & 1 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 2 & 1 \\ 0 & 1 & 2 \end{bmatrix}$$

$$A^{T} \cdot A = \begin{bmatrix} 0 & 1 & 1 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix} \cdot \begin{bmatrix} 0 & 0 & 0 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 2 & 1 & 1 \\ 1 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix}$$

$$\overrightarrow{h}_{a} = A \cdot A^{T} \cdot \overrightarrow{h}_{o} = \begin{bmatrix} 0 & 3 & 3 \end{bmatrix}^{T} \approx \begin{bmatrix} 0 & 1 & 1 \end{bmatrix}^{T}$$

$$\vec{a}_1 = \vec{A} \cdot \vec{A} \cdot \vec{a}_0 = [422]^T \approx [1\frac{1}{2}\frac{1}{2}]^T$$

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You maintain a text retrieval system. Let E_1 denote the complete set of documents in the index of your system and let E_2 denote the complete set of documents in the index of a competing system. Suppose the indices of both systems are independent uniform random samples without replacement from the World Wide Web N. The size of E_1 is $|E_1|=110$ trillion $(110\cdot 10^{12})$ documents. You take a uniform random subsample of documents without replacement from E_1 and you submit each document to the competing system. This gives you an estimate x=0.2 of the conditional probability $P(d \in E_2 \mid d \in E_1), d \in N$. You repeat the same procedure with E_2 , obtaining an estimate y=0.4 of the conditional probability $P(d \in E_1 \mid d \in E_2), d \in N$. Assume the estimates x, y are the true probabilities. What is the size $|E_2|$ of the competing system's index? [3 points]

The grey parrot, native to equatorial Africa, is categorized as an endangered species by the International Union for Conservation of Nature (IUCN). Suppose you take a uniform random sample M without replacement of size $|M|=8\,000$ from the grey parrot population N and mark the sampled animals. After returning the marked animals back into the population, you take a second independent uniform random sample T without replacement of the same size $|T|=8\,000$ from the population. The number of marked animals $R=M\cap T$ in the second sample is |R|=10. What is the most likely size |N| of the grey parrot population? [2 points]

$$\forall d \in N : P(d \in E_z | d \in E_1) = x = 0.2$$

$$P(d \in E_1 | d \in E_2) = y = 0.4$$

$$P(d \in E_1) = |E_1| / |N|$$

$$P(d \in E_2) = |E_2| / |N|$$

$$x \cdot \frac{|E_1|}{|N|} = y \cdot \frac{|E_2|}{|N|}$$
 $\longrightarrow |E_2| = \frac{x}{y} \cdot |E_1| = \frac{0.2}{0.4} \cdot 110 \cdot 10^2 = 55 \cdot 10^{12}$

The Mark and Recapture Technique:

$$|N| = \frac{|M| \cdot |T|}{|R|} = \frac{8000 \cdot 8000}{10} = 64 \cdot 10^{5}$$