

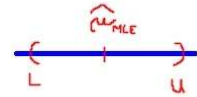
DATA SAMPLE:  $(x_1, \dots, x_n)$   
 MODEL:  $(X_1, \dots, X_n) = (X_1, \dots, X_n)$ ,  $X \sim N(\mu, \sigma^2)$

$(1-\alpha) \cdot 100\%$  CI: 1) 2-sided: (L, U)  
 95%

$$P(L \leq \mu \leq U) = 1 - \alpha$$

$$L = \hat{\mu}_{MLE} - q_{1-\frac{\alpha}{2}} \cdot \frac{\sigma}{\sqrt{n}}$$

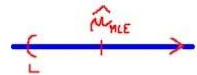
$$U = \hat{\mu}_{MLE} + q_{1-\frac{\alpha}{2}} \cdot \frac{\sigma}{\sqrt{n}}$$



2) LEFT:  $(L, \infty)$

$$P(L \leq \mu) = 1 - \alpha$$

$$L = \hat{\mu}_{MLE} - q_{1-\alpha} \cdot \frac{\sigma}{\sqrt{n}}$$



3) RIGHT:  $(-\infty, U)$

$$P(\mu \leq U) = 1 - \alpha$$

$$U = \hat{\mu}_{MLE} + q_{1-\alpha} \cdot \frac{\sigma}{\sqrt{n}}$$



$q_{1-\frac{\alpha}{2}}$ ,  $q_{1-\alpha}$  are the QUANTILES of: stand. NORMAL dist. ( $\sigma^2$  is known)  
 STUDENT t-distribution (is not)  
 (with  $n - 1$  degrees of freedom)