

# IA169: Model Checking

## Seminar 5

**Exercise 1** Recall the definition of simulation between two Kripke structures  $M = (S^M, \rightarrow^M, S_0^M, L^M)$  and  $N = (S^N, \rightarrow^N, S_0^N, L^N)$ .

**Exercise 2** Given the following Kripke structures  $M_i$ , decide for each pair  $(M_i, M_j)$  such that  $i \neq j$  whether  $M_i \leq M_j$  holds. If it does, find the simulation relation. If not, explain why.

Simulation relation between  $M$  and  $N$  is written as  $M \leq N$  and is read "N simulates M"

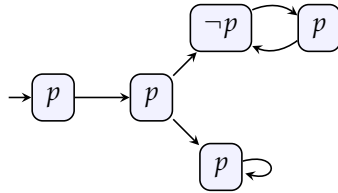


Figure 1:  $M_1$

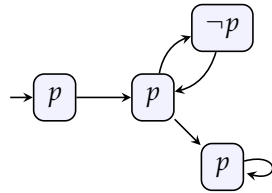


Figure 2:  $M_2$

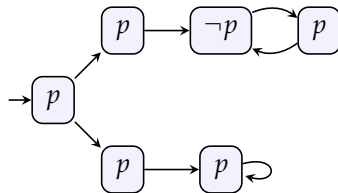


Figure 3:  $M_3$

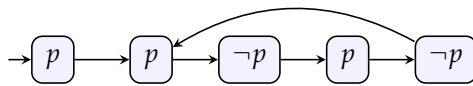


Figure 4:  $M_4$

**Exercise 3** Briefly explain what is a predicate abstraction  $M_{may}$  of a labeled transition system  $M$  given a set of predicates  $\mathbb{P}$ .

**Exercise 4** Consider the labeled transition system  $M$  defined by the following description in guarded command language

$$\begin{aligned}
 V &= \{x, y\}, \\
 E &= \{(a, x = 0, x := x + 1), \\
 &\quad (b, y = 0, y := y + 1), \\
 &\quad (c, x > 0, (x := x + 3, y := y + 3))\}
 \end{aligned}$$

and a set of predicates

$$\mathbb{P} = \{x > 0, x = y, y > 2\}.$$

Compute the system  $M_{may}$  that is the result of predicate abstraction of the system  $M$ .

**Exercise 5** Consider the labeled transition system  $M$  and the set of predicates  $\mathbb{P}$  from Exercise 4. The system satisfies the property  $G(|x - y| \leq 1)$  but the abstract system  $M_{may}$  does not. Find a spurious counterexample.

Try to find a refinement of  $\mathbb{P}$  that blocks the spurious counterexample.

**Exercise 6** Consider the labeled transition system  $M$  defined by the following description in guarded command language

$$\begin{aligned} V &= \{x, y\}, \\ E &= \{(a, \top, y := y + 10), \\ &\quad (b, x \bmod 3 = 0, (x := x + 1, y := y + 3)), \\ &\quad (c, x \bmod 3 = 1, (x := x + 1, y := y + 4)), \\ &\quad (d, x \bmod 3 = 2, (x := x + 1, y := y - 6))\}. \end{aligned}$$

The system satisfies the property  $G(y \geq 0)$ . Find a finite set of predicates  $\mathbb{P}$  that reduces the system  $M$  to a finite-state system  $M_{may}$  that also satisfies the property.

Try to find as small  $\mathbb{P}$  as possible.