

Index Compression + Vector Space Model (Chapter 5+6)

Exercise 6/1

Consider the frequency table of the words of three documents.
Calculate the **tf-idf** weight of the terms **car**, **auto**, **insurance**, and **best** for each document.
idf values of terms are in the table.

| | doc ₁ | doc ₂ | doc ₃ | idf |
|-----------|------------------|------------------|------------------|------|
| car | 27 | 4 | 24 | 1.65 |
| auto | 3 | 33 | 0 | 2.08 |
| insurance | 0 | 33 | 29 | 1.62 |
| best | 14 | 0 | 17 | 1.5 |

term frequency x idf

| | doc ₁ | doc ₂ | doc ₃ |
|-----------|------------------|------------------|------------------|
| car | 14.55 | 6.6 | 39.6 |
| auto | 6.24 | 68.64 | 0 |
| insurance | 0 | 53.46 | 46.98 |
| best | 21 | 0 | 25.5 |

Definition 6 (Inverse document frequency)

Inverse document frequency of a term t is defined as

$$idf_t = \log \left(\frac{N}{df_t} \right)$$

where N is the number of all documents and df_t (the document frequency of t) is the number of documents that contain t .

Definition 7 (tf-idf weighting scheme)

In the tf-idf weighting scheme, a term t in a document d has weight

$$tf \cdot idf_{d,t} = t_{f,d} \cdot idf_t$$

where $t_{f,d}$ is the number of tokens t (the term frequency of t) in a document d .

Exercise 6/2

Count document representations as normalized Euclidean weight vectors for each document from the previous exercise. Each vector has four components, one for each term.

Represent the documents
and the query as vectors:

```
doc_1 = [0, 1, 0, 1]
doc_2 = [0, 1, 0, 0]
doc_3 = [0, 0, 0, 1]
q = "car insurance"
q = [0, 0, 0, 0]
```

Different approaches/views:

a) Boolean retr. results: } OR operator
(doc1, doc2, doc3)

b) Ranked retr. results: } dot/scale product
query + doc

```
doc_1 = 1+1+0+1+1+0+0+1 = 1
doc_2 = 1+1 = 2
doc_3 = 1+1 = 2
```

c) using TF (term frequency):

```
doc_2 = 4 + 33 = 37
doc_3 = 24 + 29 = 53 BEST HIT ?
```

d) using IDF (inverse document frequency):

TF-IDF + Euclidean normalization

Exercise 6/3

Based on the weights from the last exercise, compute the **similarity scores** (scalar products) of the three documents for the query Q: "car insurance".

Use each of the two weighting schemes:

- Term weight is 1 if the query contains the word and 0 otherwise.
- Euclidean normalized tf-idf.

```
doc_2 = [0, 1, 0, 0]
doc_3 = [0, 0, 0, 1]
```

Exercise 6/4

Compute the Levenshtein distance between **paris** and **alice**.

Write down the matrix of distances between all prefixes as computed by Algorithm 2.

| | e | p | a | r | i | s |
|---|---|---|---|---|---|---|
| e | 0 | 1 | 2 | 3 | 4 | 5 |
| a | 1 | 1 | 1 | 1 | 1 | 1 |
| i | 2 | 2 | 2 | 2 | 2 | 2 |
| r | 3 | 3 | 3 | 3 | 3 | 3 |
| s | 4 | 4 | 4 | 4 | 4 | 4 |
| e | 5 | 5 | 5 | 5 | 5 | 5 |

Table 4: Initialization of the matrix.

Algorithm 2 (Levenshtein distance – imperative approach)

```
1 function levenshteinDistance(a, b)
2   for i ← 0 to |a| do
3     m[i, 0] ← i
4   end for
5   for j ← 0 to |b| do
6     m[0, j] ← j
7   end for
8   for i ← 1 to |a| do
9     for j ← 1 to |b| do
10      if a[i] = b[j] then
11        m[i, j] ← min(m[i-1, j], m[i, j-1], m[i-1, j-1])
12      else
13        m[i, j] ← min(m[i-1, j], m[i, j-1], m[i-1, j-1]) + 1
14      end if
15    end for
16  end for
17  return m[|a|, |b|]
18 end function
```

Table 5: First two iterations of the main dynamic programming step.

| | e | p | a | r | i | s |
|---|---|---|---|---|---|---|
| e | 0 | 1 | 2 | 3 | 4 | 5 |
| a | 1 | 1 | 1 | 1 | 1 | 1 |
| i | 2 | 2 | 2 | 2 | 2 | 2 |
| r | 3 | 3 | 3 | 3 | 3 | 3 |
| s | 4 | 4 | 4 | 4 | 4 | 4 |
| e | 5 | 5 | 5 | 5 | 5 | 5 |

Algorithm 3 (Levenshtein Distance – declarative approach)

```
1 function levenshteinDistance(a, b)
2   return min(|a|, |b|)
3 end function
4
5 let m[i, j] ← min(
6   if a[i] = b[j] then 1 else 0,
7   min(
8     m[i-1, j],
9     m[i, j-1],
10    m[i-1, j-1]
11   )
12 ) + 1
13
14 where m[i, j] is the indicator function equal to 1 when a[i] ≠ b[j], and 0 otherwise.
15 m[i, j] is the distance between the first i characters of string a and the first j characters of string b.
```

Table 6: The final matrix with the Levenshtein distance in bold.

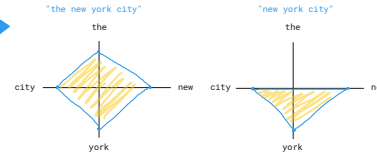
| | e | p | a | r | i | s |
|---|---|---|---|---|---|---|
| e | 0 | 1 | 2 | 3 | 4 | 5 |
| a | 1 | 1 | 1 | 1 | 1 | 1 |
| i | 2 | 2 | 2 | 2 | 2 | 2 |
| r | 3 | 3 | 3 | 3 | 3 | 3 |
| s | 4 | 4 | 4 | 4 | 4 | 4 |
| e | 5 | 5 | 5 | 5 | 5 | 5 |

movement: operation (price):

- delete (1)
- ← insert (1)
- ↔ replace (1) / move (0)

paris
 aris (1)
 aris (0)
 aris (1)
 aris (1)
 aris (0)
 aris (1)
 aris (1)
 aris (1)

paris
 aris (1)
 aris (0)
 aris (1)
 aris (0)
 aris (1)
 aris (1)
 aris (1)



$$idf = \log \left(\frac{\#documents}{\#documents \text{ with 'the'}} \right) = \log(1) = 0$$



Exercise 5/5

From the following sequence of **γ**-encoded gaps, reconstruct first the gaps list and then the original postings list. Recall that the **γ** code encodes a number n with n 1s followed by one 0.

```
111000111010101111110101111011
  ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓
 100 4 110 11 11011 111 11
  || || || || || || ||
  9 6 3 59 7
```

[9, 15, 18, 79, 84]

Definition 1 (γ code)

γ code, also referred to as a **code**, is a coding type where a number n is represented by a sequence of n 1s (or 0s) and terminated with one 0 (or 1). That is, n is in unary code is 111110 (or 000001). The alternative representation in parentheses is equivalent but for this course we use the default representation.

Definition 2 (γ code)

γ code is a coding type, that consists of an **offset** and its length: $\gamma(n) = \alpha(\text{length of offset}(n)) \text{ offset}(n)$. **Offset** is a binary representation of a number n without the highest bit (1). The length of this offset is the unary (α) code. Then the number n is encoded in γ as 11110,11100.

(binary) } gaps
(decimal) }
(posting list)

Q: how to encode '1' in gamma code?

- ↓ (decimal / unary)
- ↓ (offset of length 0)
- ↓ (zero, γ-code of the offset)
- ↓ (zero, γ-code of '1')

0110111010
 ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓
 1 111 10
 || || || || || || || || || || || || || || || ||
 1 7 2
 [1, 8, 10] (γ-code) Example
 (binary) (add leading '1' to the offset)
 (decimal)
 (posting list)