The European Digital Mathematical Library: An Overview of Math Specific Technologies

Petr Sojka

Masaryk University, Faculty of Informatics, Brno, Czech Republic
<sojka@fi.muni.cz>

National Institute of Informatics, Tokyo
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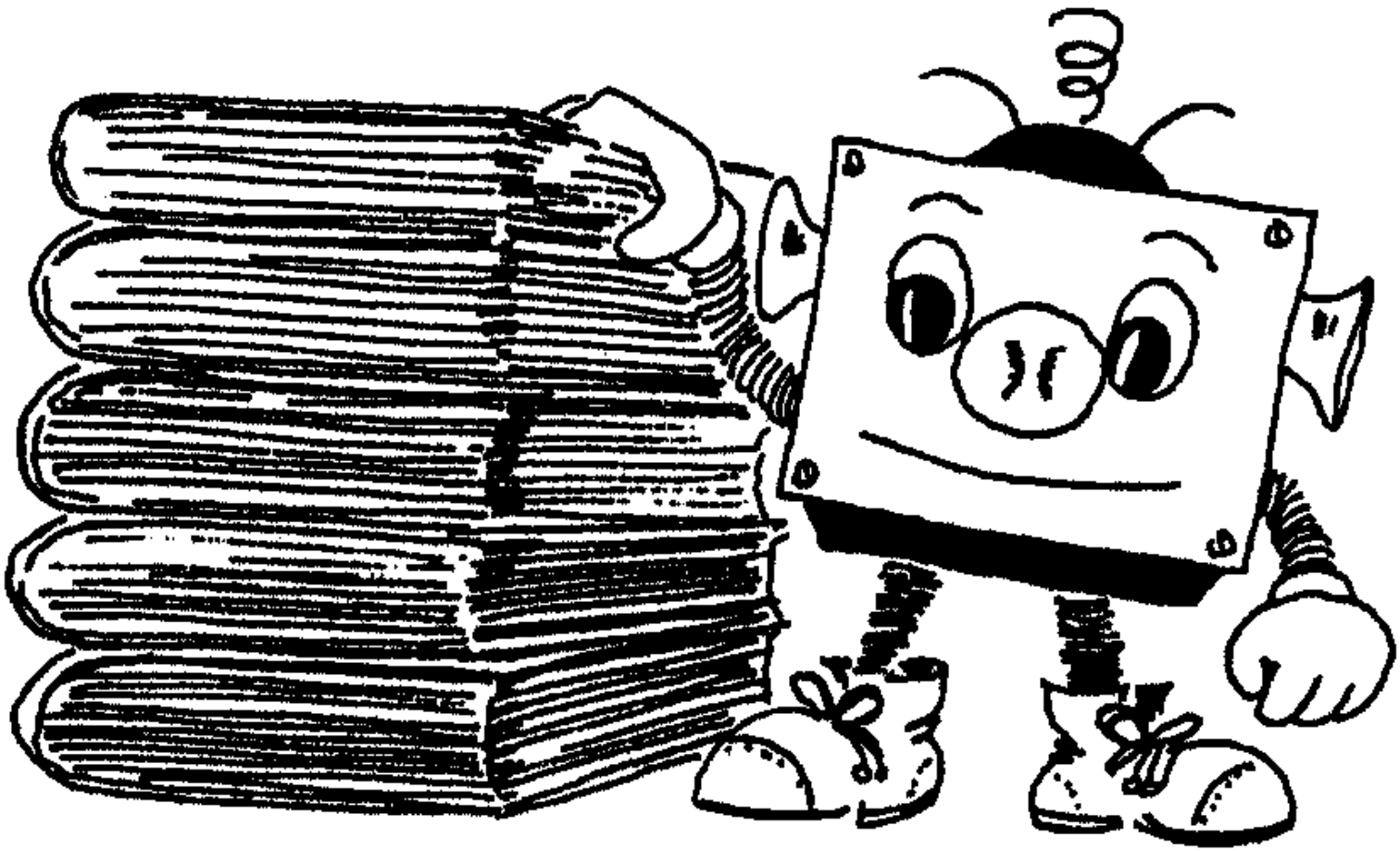
EuDML
The EUROPEAN DIGITAL MATHEMATICS LIBRARY

Outline and take-home message

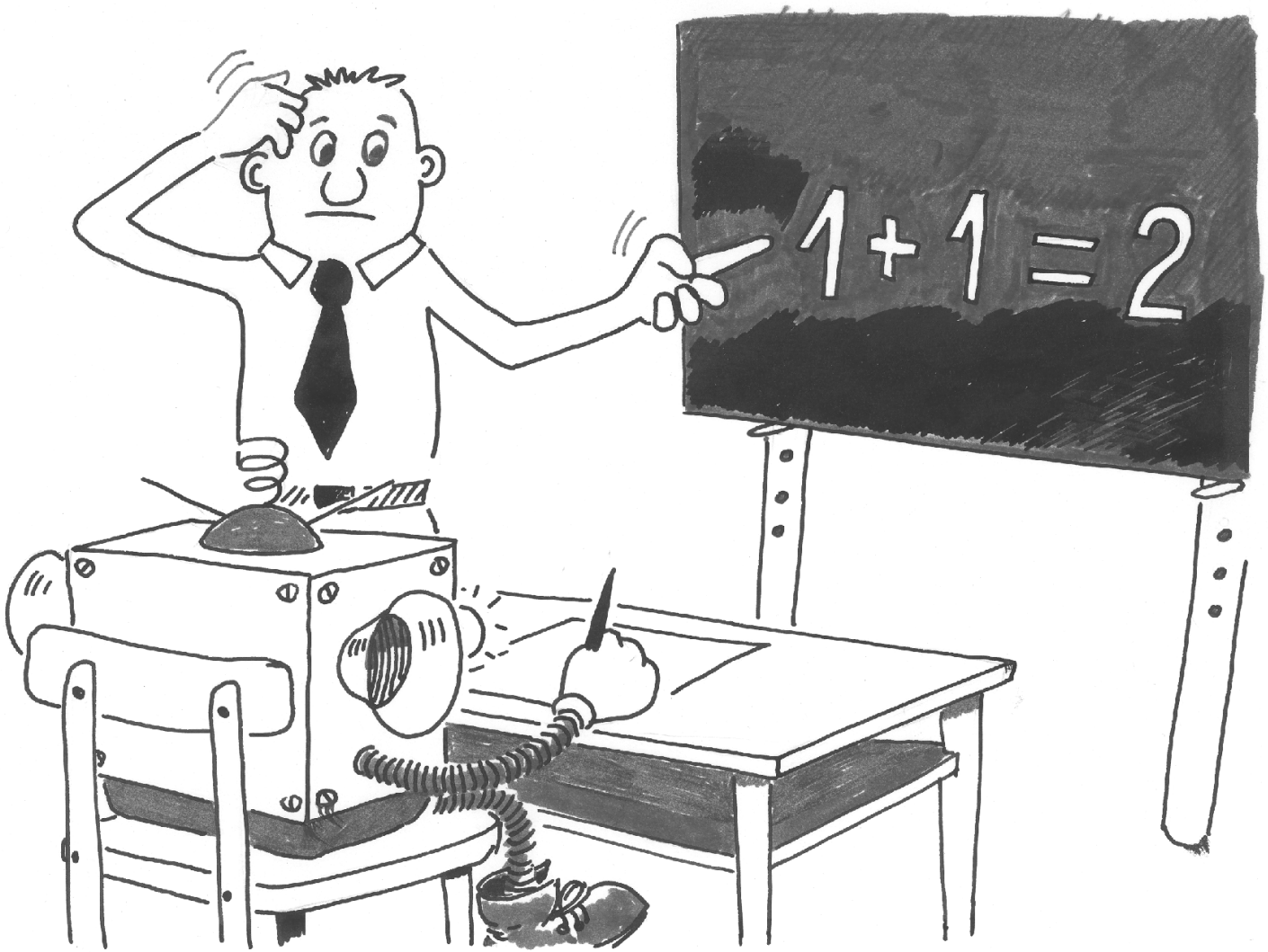
1. Pictorial overview
2. Motivation, vision of WDML, PubMed Central for Mathematics
3. Data aggregation from local DMLs
4. Conversions
5. Search
6. Similarity
7. Conclusions

Towards the dream of *math-aware* WDML: EuDML

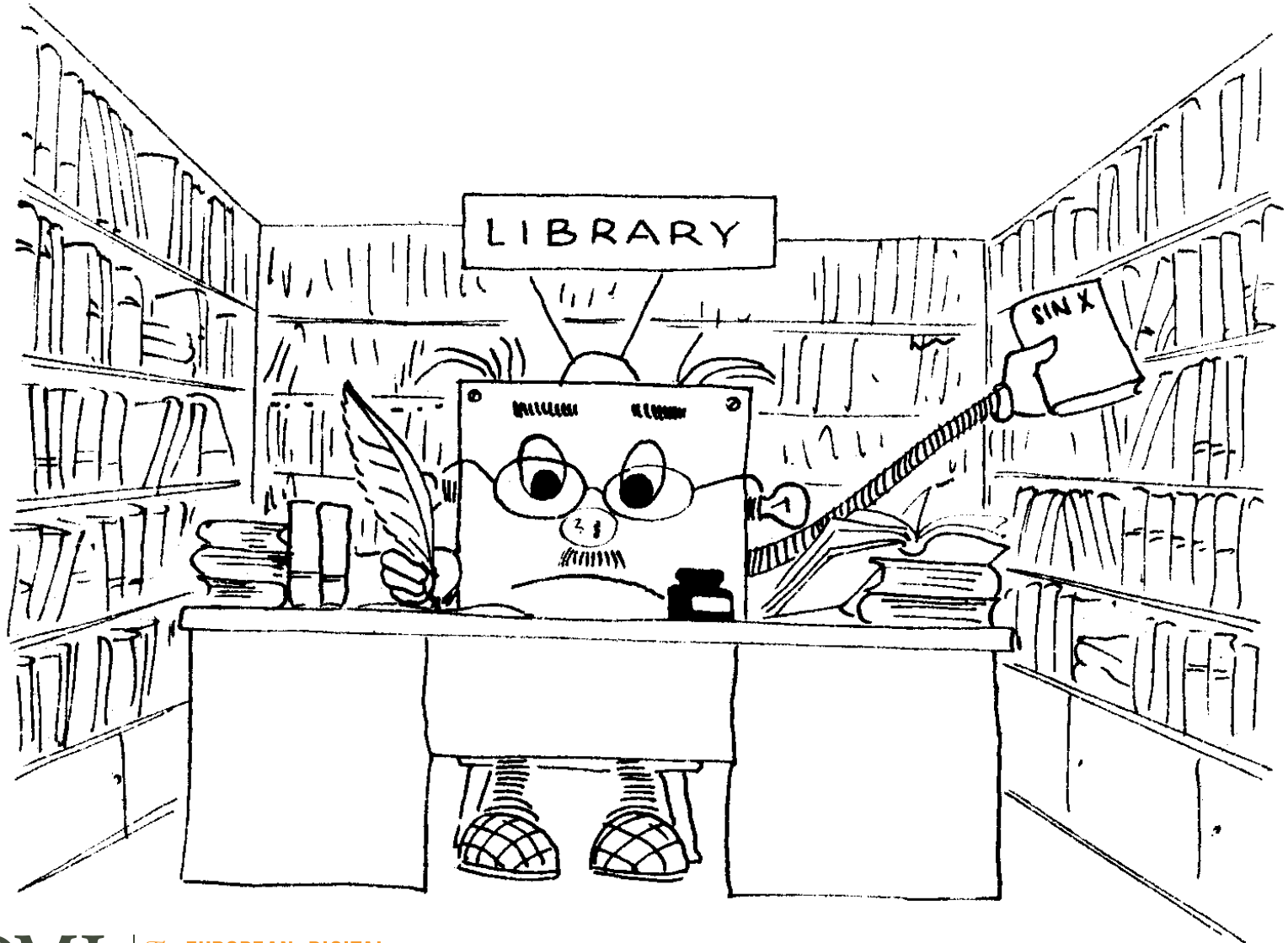


Information overload in globalized *scientific* world

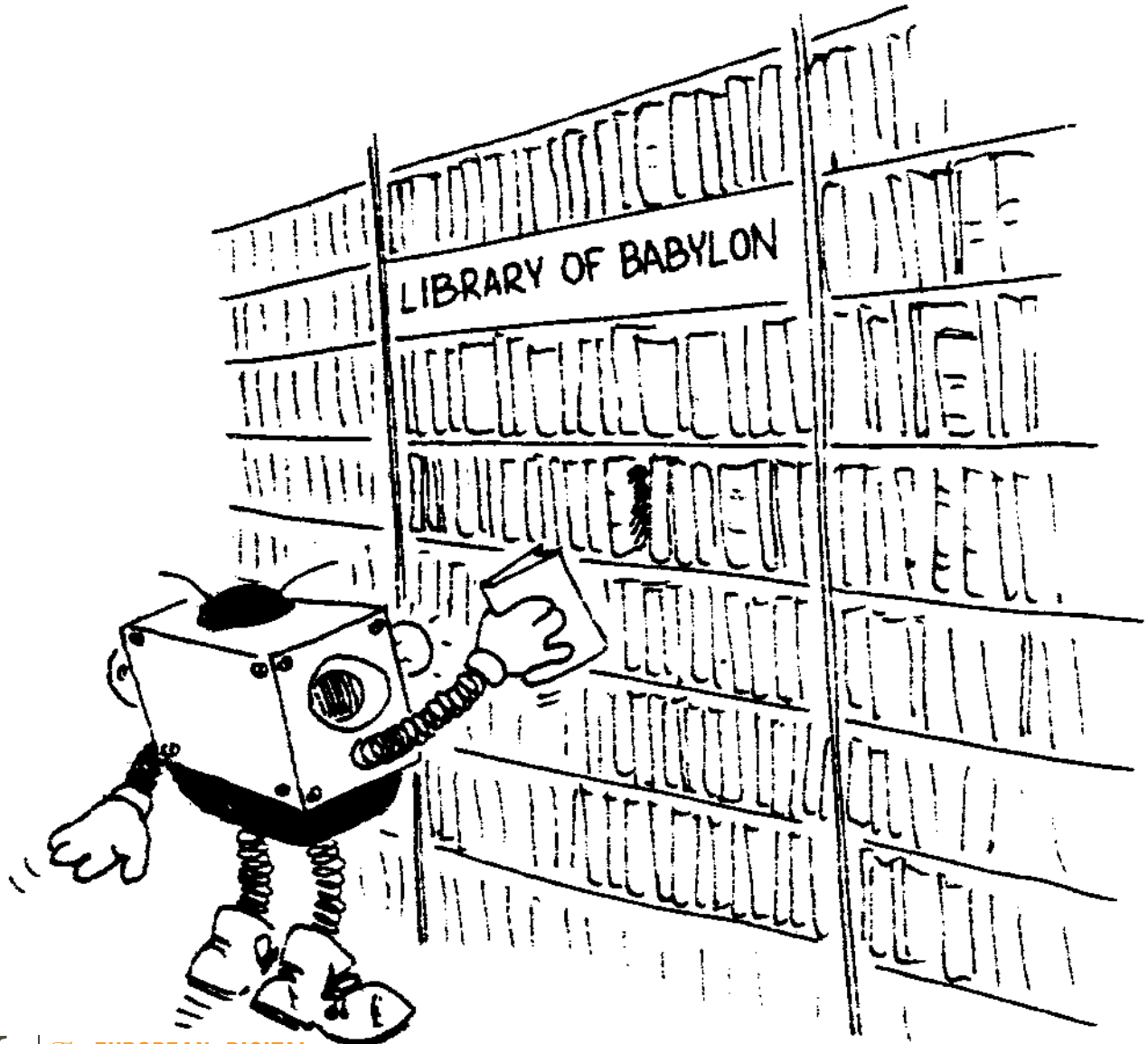
Mathematics should follow other sciences (HEP, PMC,…)



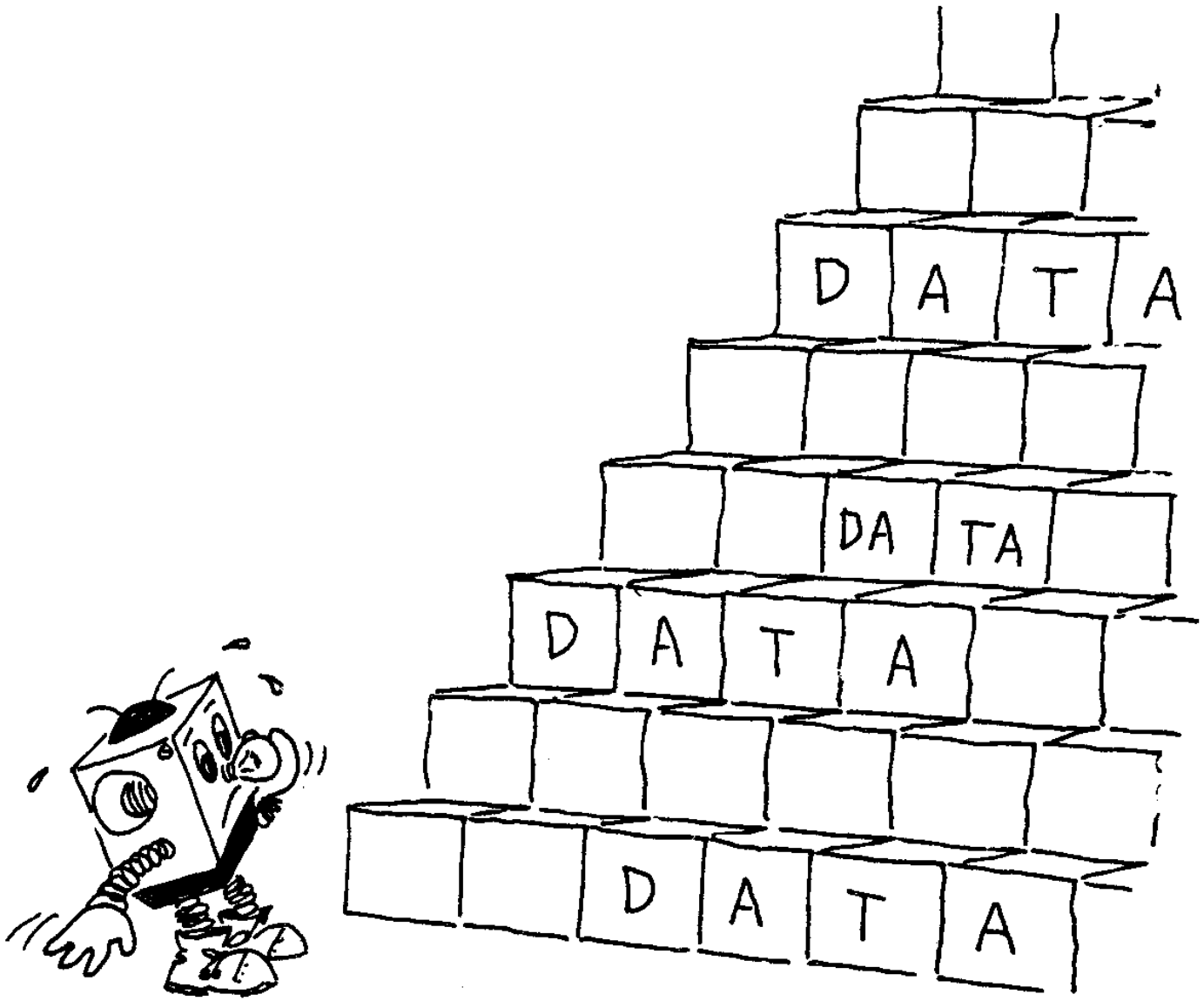
The European Digital Mathematics Library: *EuDML*



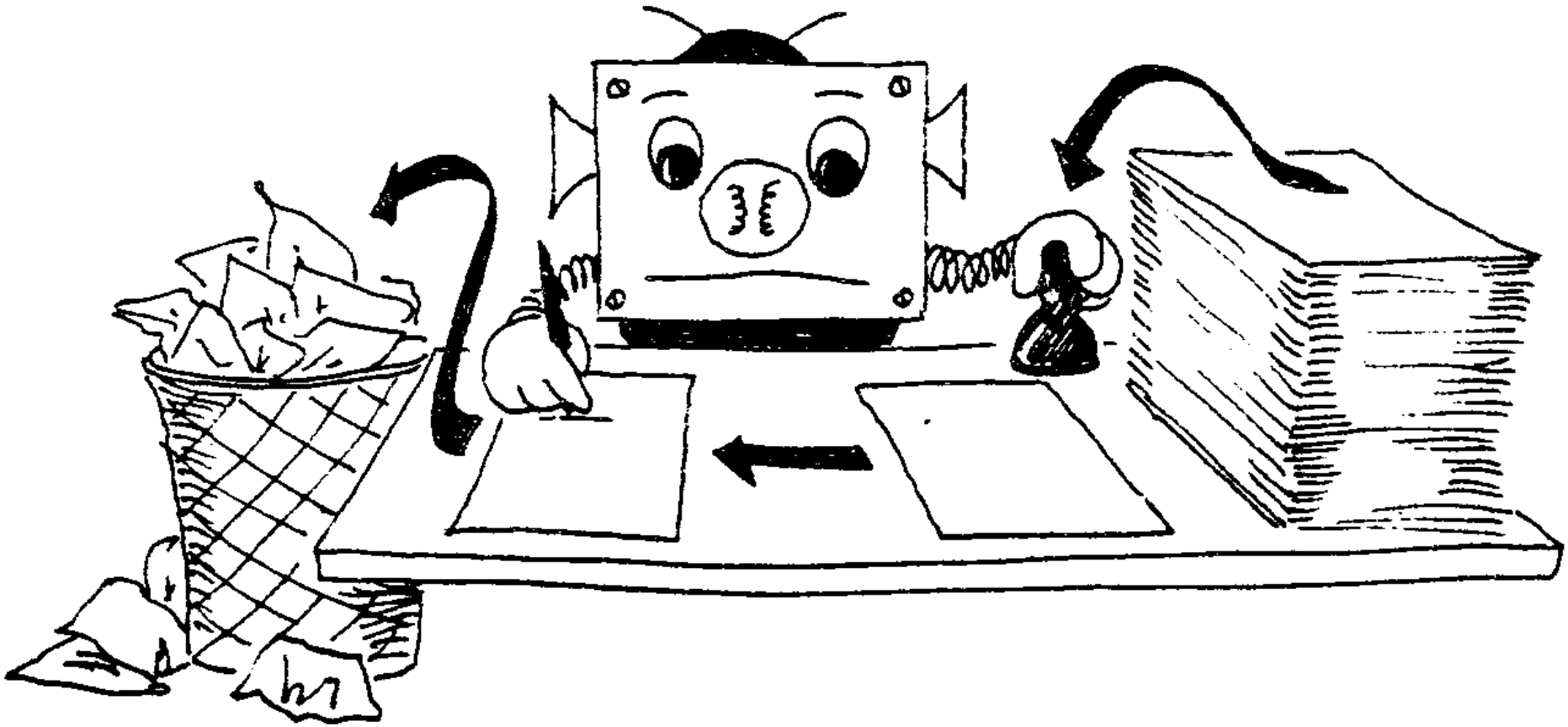
‘Bottom up’ deployment towards EU or *worldwide scale*



EuDML: from local data collections to the virtual DL

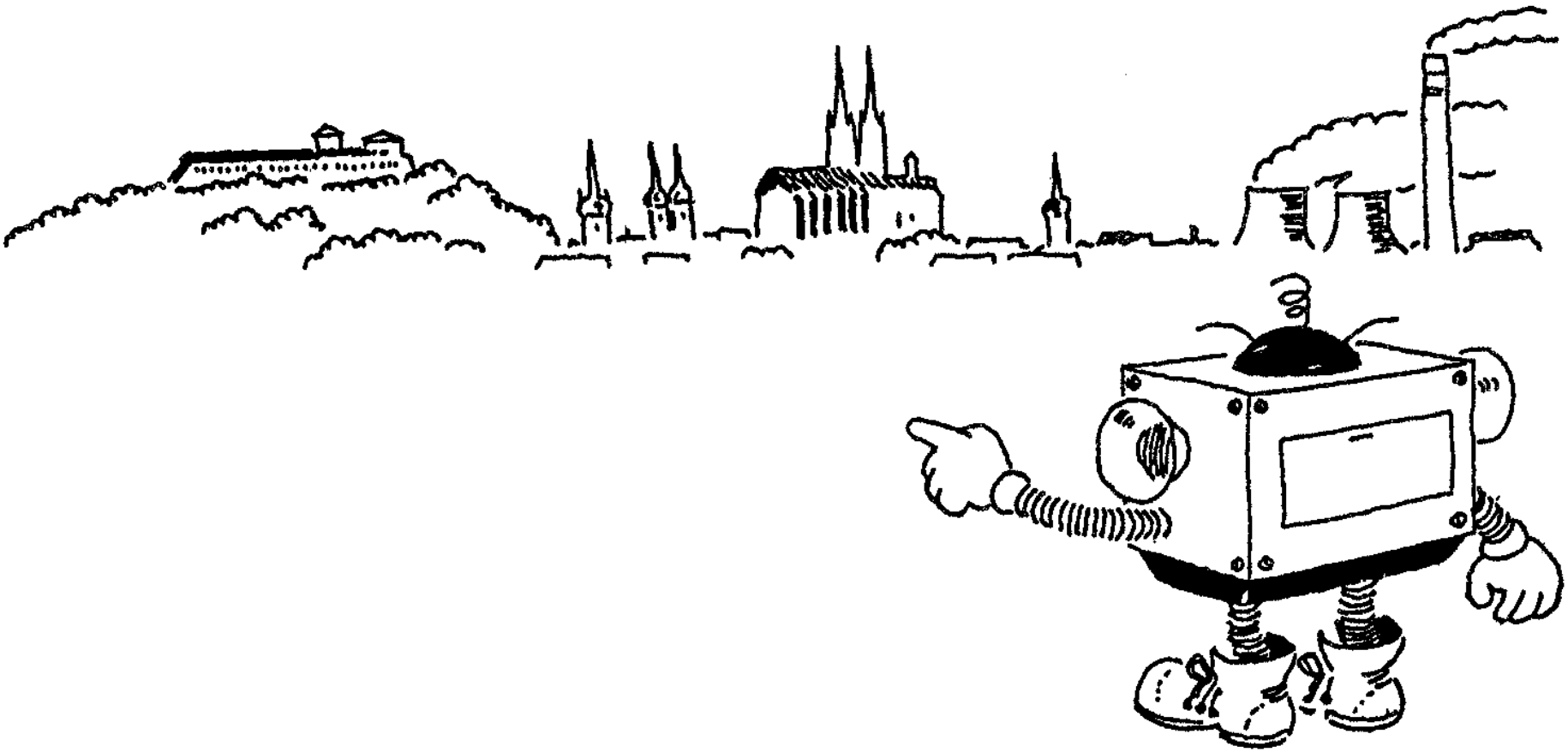


From paper to digital *workflow*

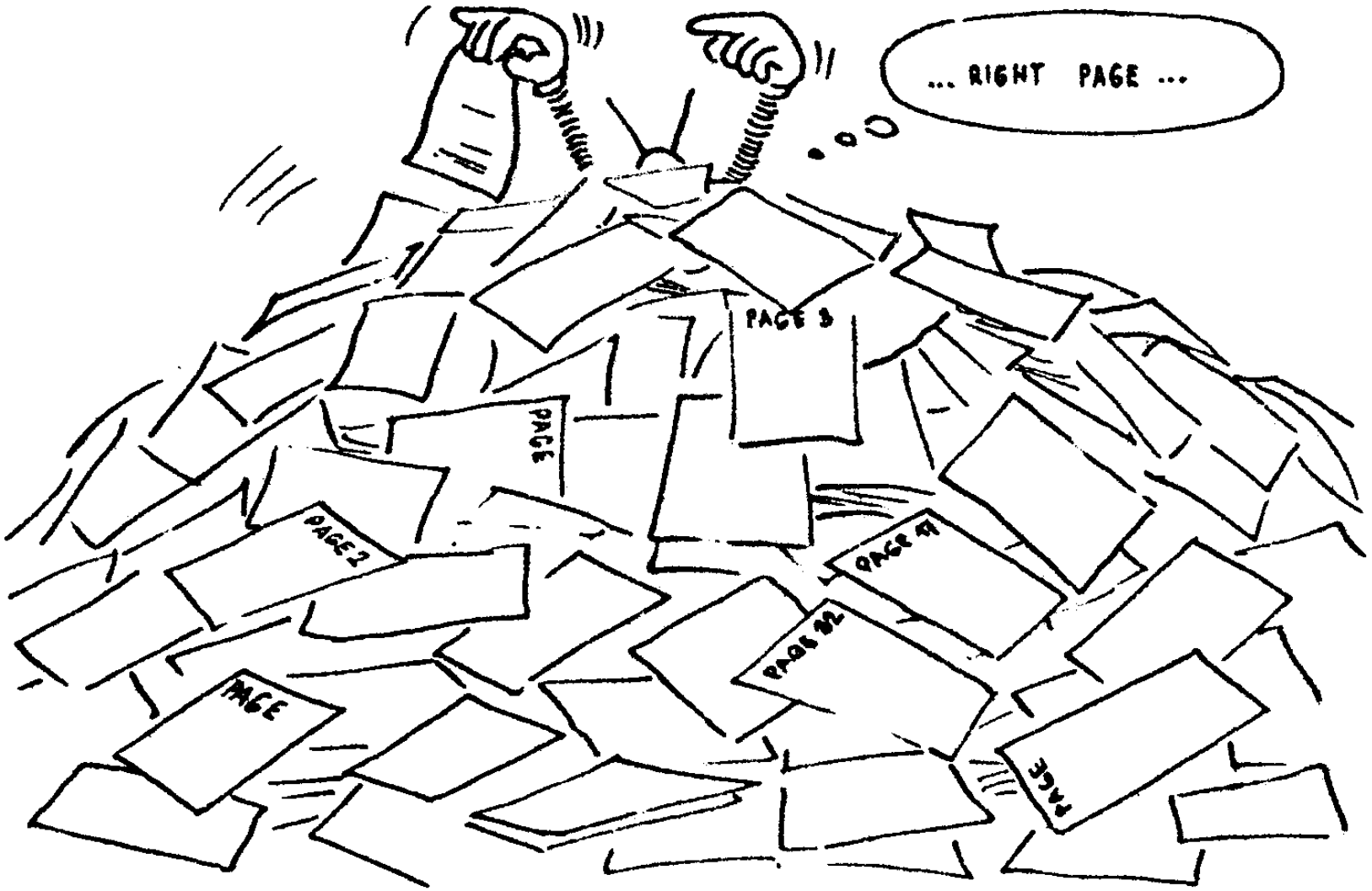


Retro-digitization, *accessible* digital library development

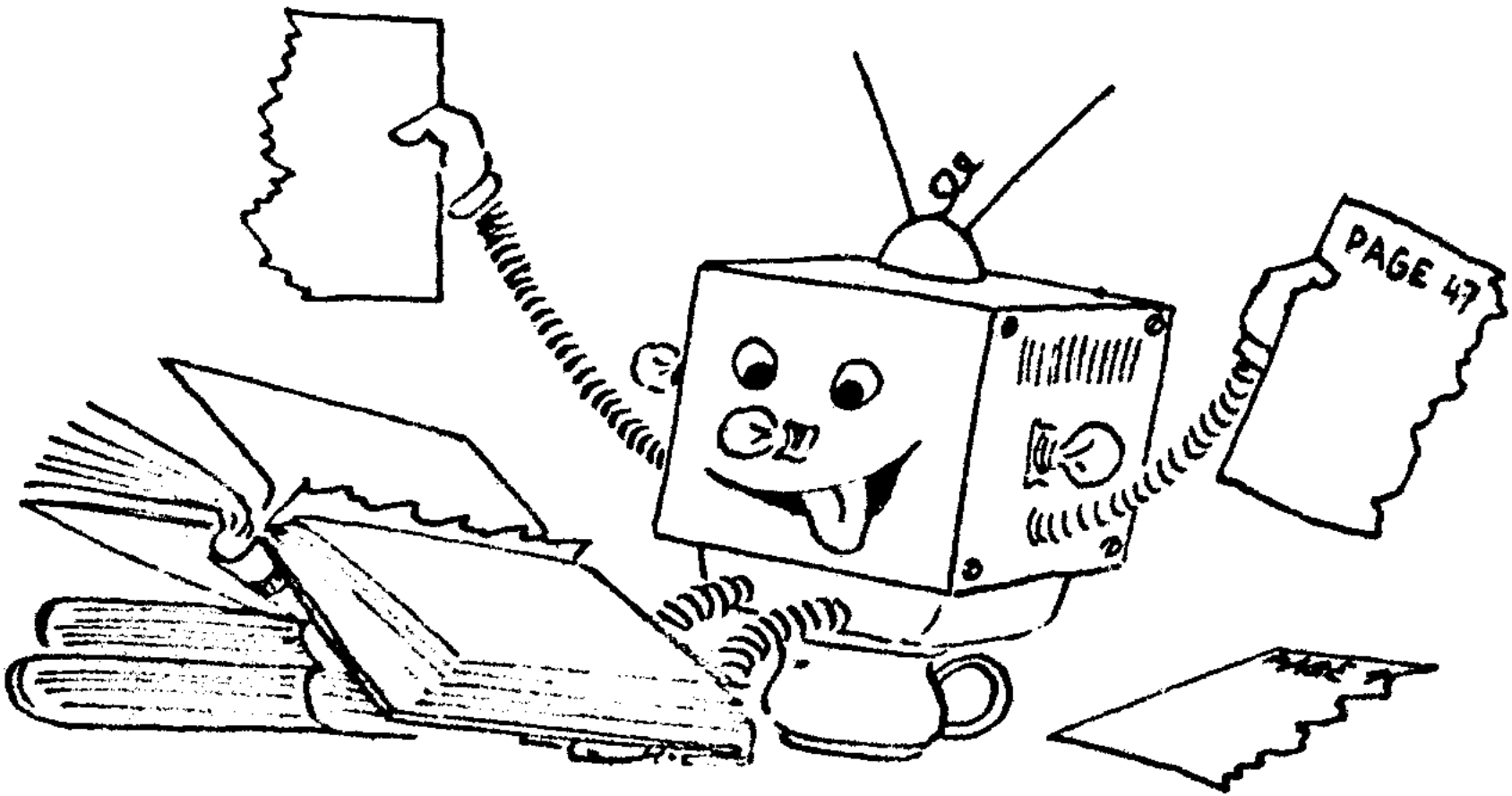
Experiences from project *DML-CZ* for EuDML (Brno, CZ)



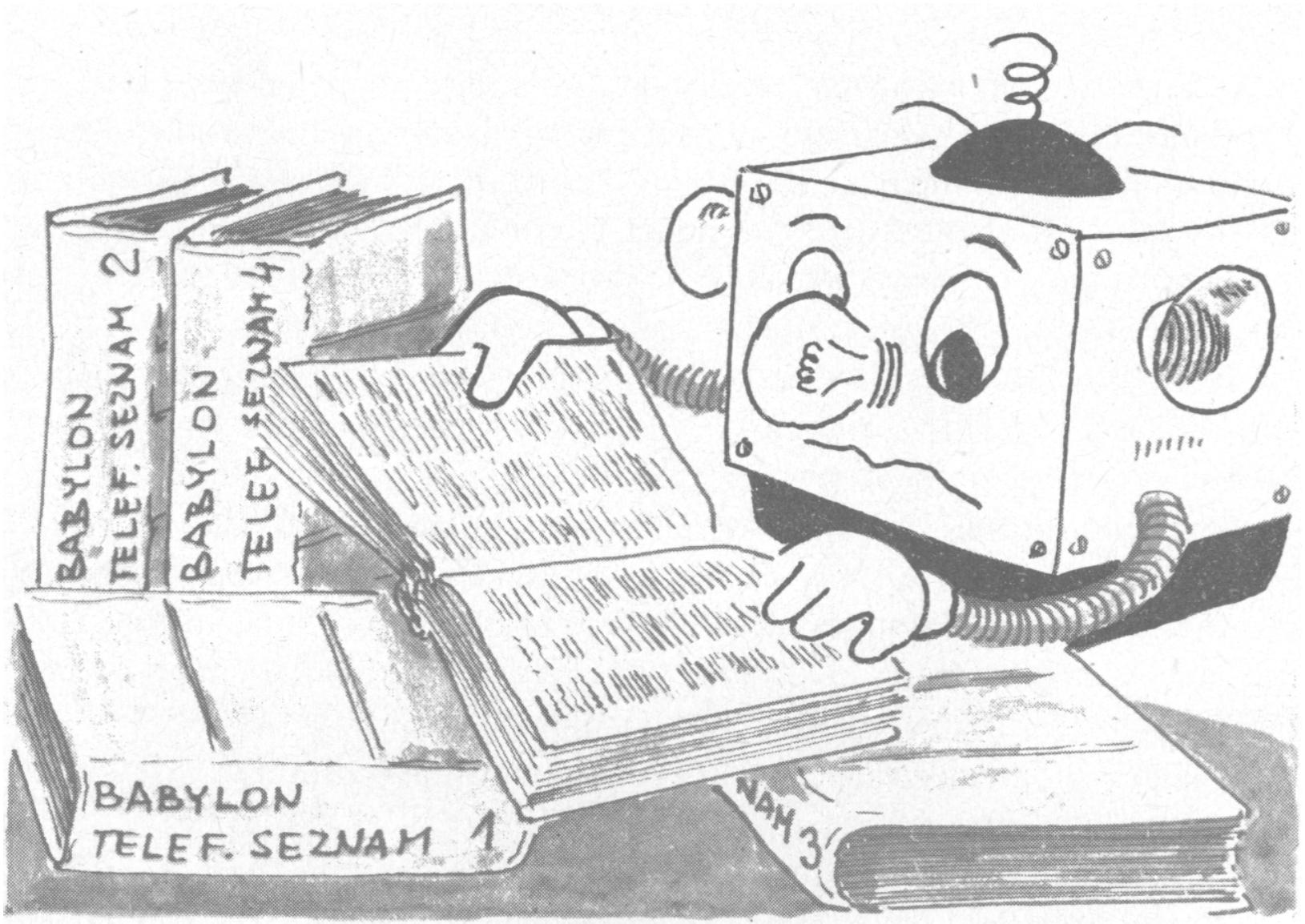
EuDML: new approaches to *math document retrieval*



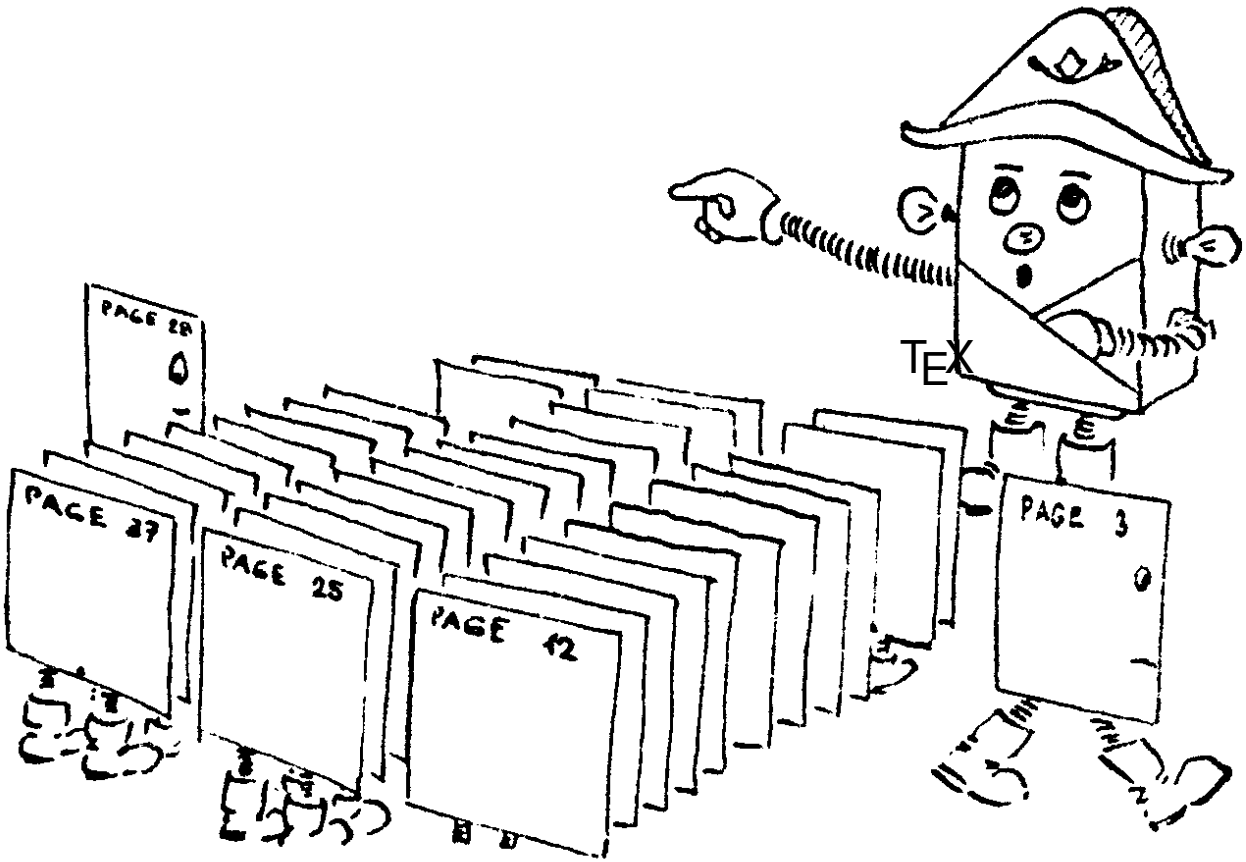
New approaches to *math-aware similarity, clustering and accessibility*



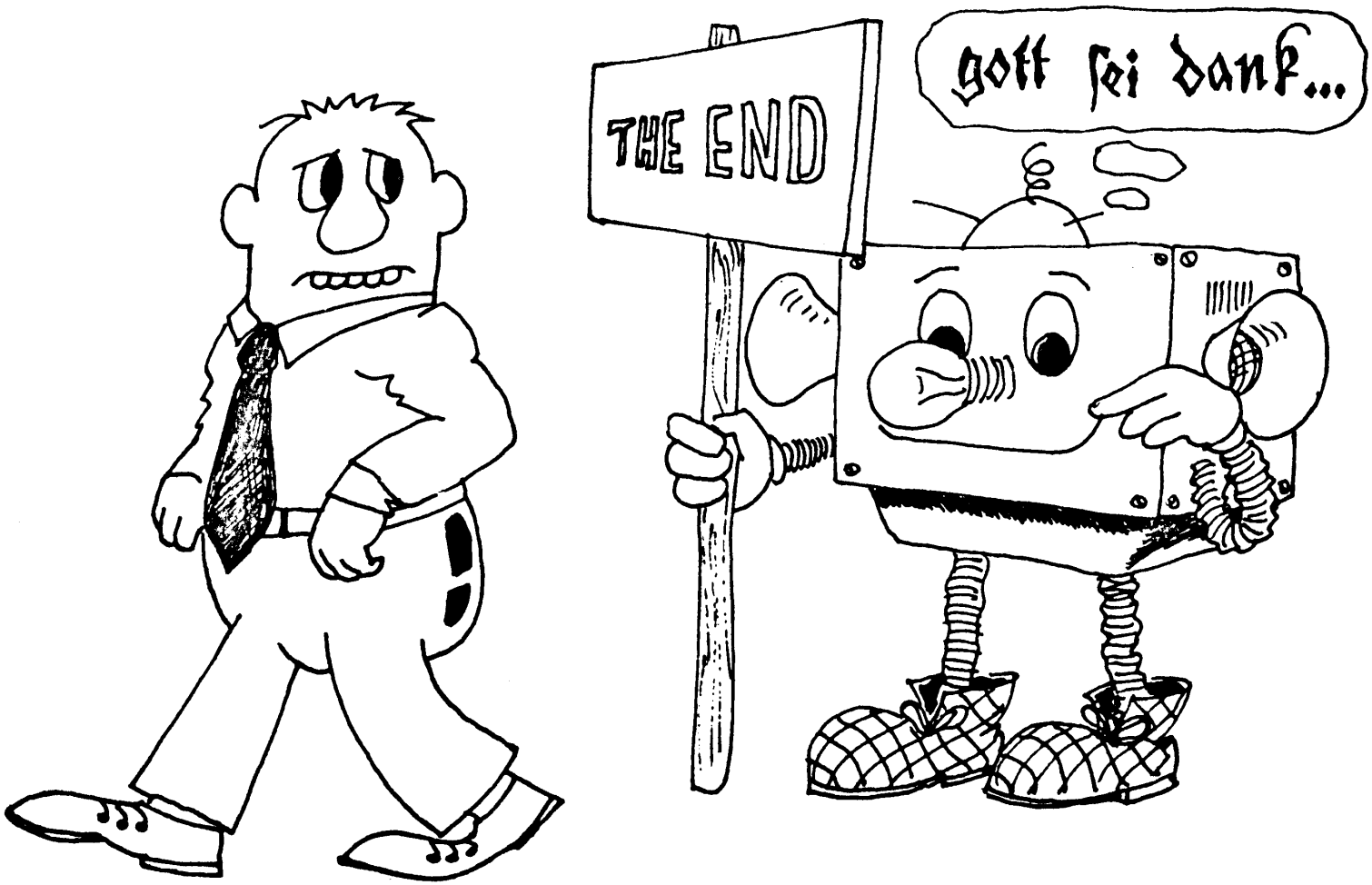
Tools for *automated math extraction* from PDF



Yes, you can! <http://eudml.org>: accessible math, search, visibility, scalability,…



End of talk overview



History of the dream: vision of WDML as PubMed 4 Math

In the beginning was vision of all mathematical knowledge, *peer reviewed, verified* (100,000,000 pages) and engineered into one-stop e-shop/DL.

AMS supported NSF preparation grant (in 2003) for WDML—Worldwide digital mathematics library, planned to be funded by de Moore foundation ($100,000,000 requested). Application was *not* successful.

Publishers started massive digitization themselves.

Even other attempts on the European level (FP5, FP6) were not successful.

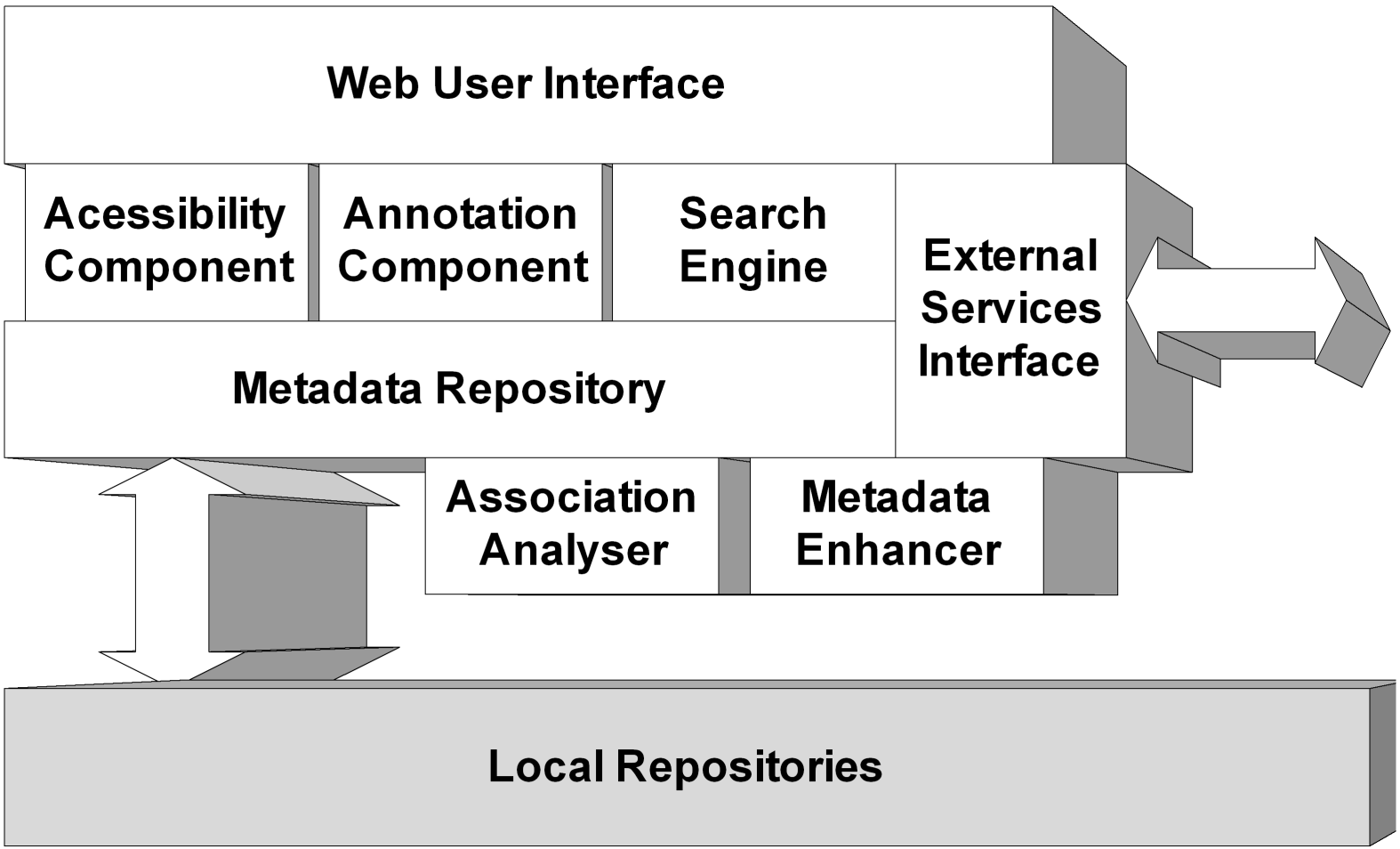
Vision of European Digital Mathematics Library

Finally three year project or *European Digital Mathematics Library, EuDML* (programme EU CIP-ICT-PSP, type Pilot B, EU contribution *(1.6 MEur, 50% of total budget only)* February 2010–January 2013. The strategy of EuDML The EUROPEAN DIGITAL MATHEMATICS LIBRARY was:

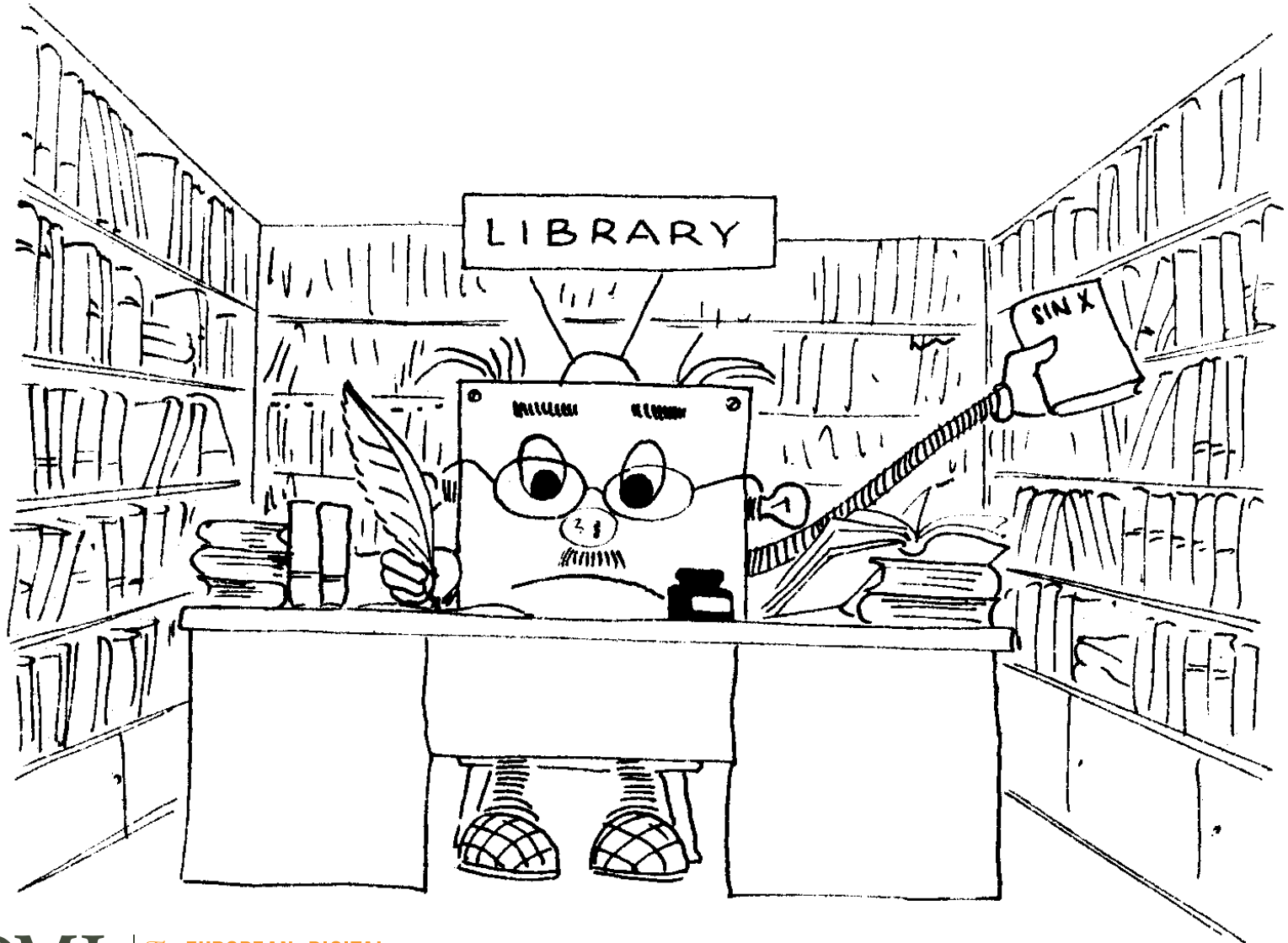
- to master the technology, develop tools and offer them;
- concept of *moving wall* to motivate and engage commercial publishers without Open Access bussiness model;
- to collect data (from existing local or publisher's) *digital libraries* into 'one-stop shop' and achieve critical mass in the domain $\rightarrow$ 'a must/me too' effect then as with PubMed Central.

EuDML as a virtual library portal

EuDML provides a *virtual* library based on data from smaller data providers, DLs and publishers:



One portal: European Digital Mathematics Library



Aggregation of data from building bricks of regional repositories

14 data and technology providers plus associated partners as ZMath, Göttingen library,…

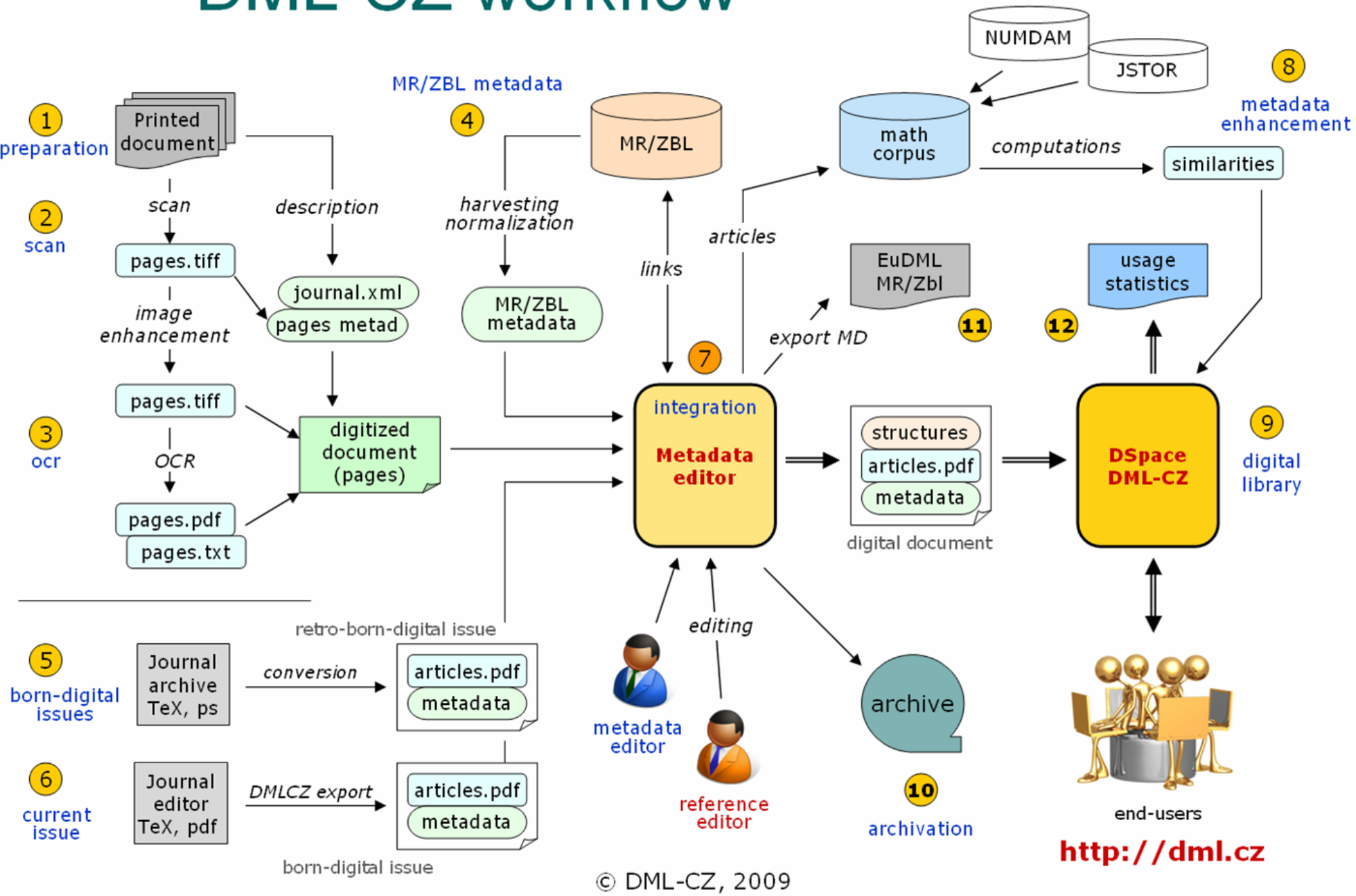
DML content providers serve mostly publisher's or regional more or less established DML repositories: The Czech Digital Mathematics Library DML-CZ, NUMDAM, DML-PL, DML-PT, DML-GR, DML-BG, DML-ES,…

Aggregation via standard OAI-PMH protocol (OAI servers run by data providers).

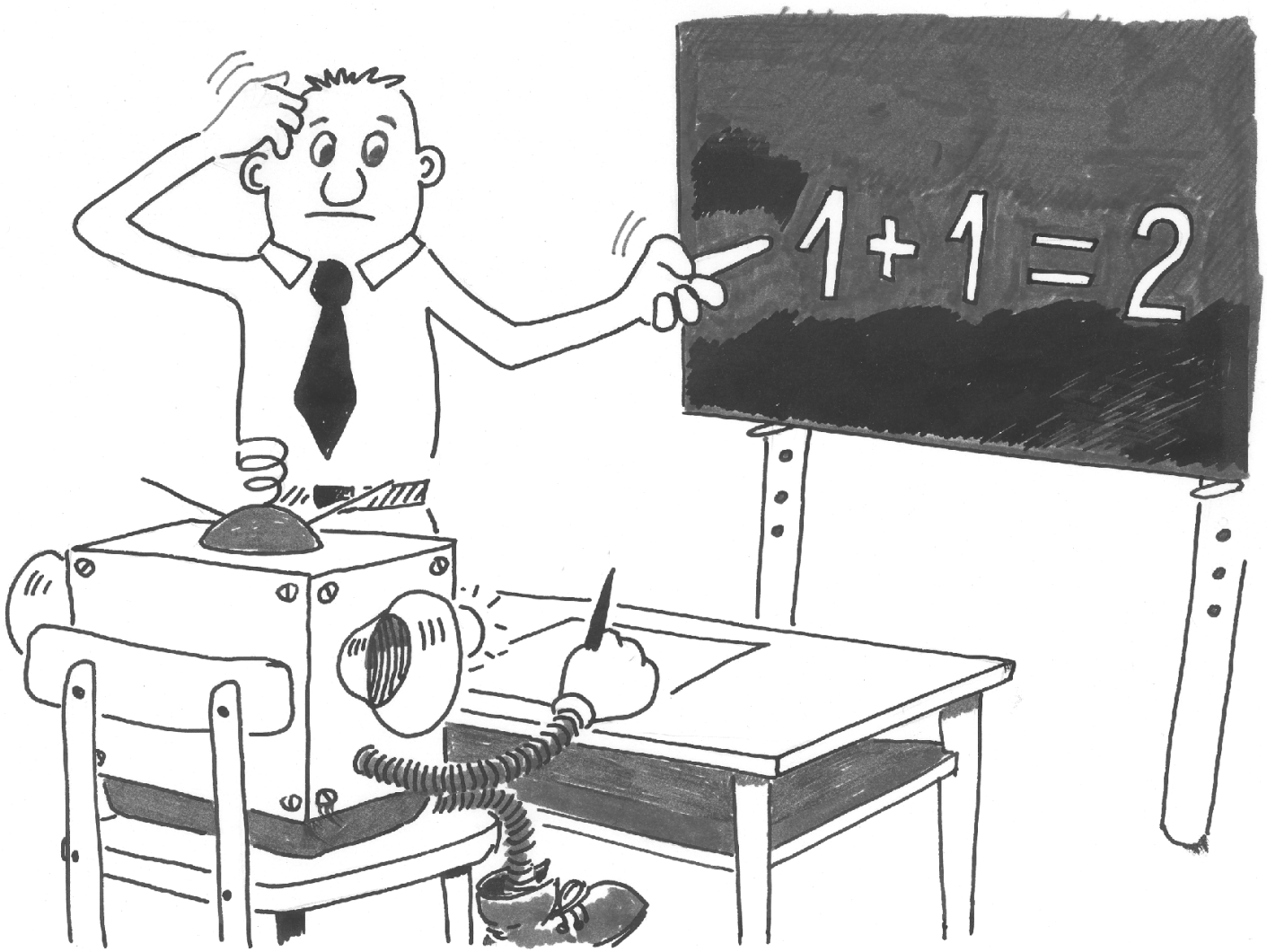
EuDML metadata schema(s) was borrowed from NLM (heavily funded by US NiH), as it allows also math-awareness (e.g. math stored both in TEX and MathML), and fully fledged reference lists.

Inovation, rather than research. Example of DML-CZ: <http://dml.cz> with 30,000+ papers (300,000+ pages). For more, see (who, what, browse, browse similar, how to search).

DML-CZ workflow



Challenges of Math handling: OCR, indexing, search…



Take care! “God is in the details.” (Mies van der Rohe)

Data heterogenity, specificity: no free lunch to unify

Proof. Let $\hat{K}$ be a cube, $\hat{K} \subset \hat{G}$; put $K = \varphi^{-1}(\hat{K})$. According to theorem 50 we have $K \in \mathfrak{A}$ and it follows from theorem 24 that

$$P(K, v) = \int_K f(x)\,\mathrm{d}x\,. \tag{89}$$

The functional determinant T of the mapping $\psi = \varphi^{-1}$ fulfils the relation $T(\varphi(x)) \,.\, \det M(x) = 1$, so that

$$\int_K f(x)\,\mathrm{d}x = \int_{\hat{K}} f(\psi(y)) \,.\, |T(y)|\,\mathrm{d}y = \int_{\hat{K}} \hat{f}(y)\,\mathrm{d}y\,. \tag{90}$$

From theorem 50 (and relation (86)) we see that $P(K, v) = P(\hat{K}, \hat{v})$; relations (89), (90) show therefore that $P(\hat{K}, \hat{v}) = \int_{\hat{K}} \hat{f}(y)\,\mathrm{d}y$, which completes the proof.

Remark. The reader may compare this paper with [6].

REFERENCES

[1] *V. Jarník:* Diferenciální počet, Praha 1953.
[2] *V. Jarník:* Integrální počet II, Praha 1955.
[3] *J. Mařík:* Vrcholy jednotkové koule v prostoru funkcionál na daném polouspořádaném prostoru, Časopis pro pěst. mat., *79* (1954), 3—40.
[4] *Ян Маржик* (Jan Mařík): Представление функционала в виде интеграла, Чехословацкий мат. журнал, *5* (80), 1955, 467—487.
[5] *J. Mařík:* Plošný integrál, Časopis pro pěst. mat., *81* (1956), 79—82.
[6] *Ян Маржик* (Jan Mařík): Заметка к теории поверхностного интеграла, Чехословацкий мат. журнал, *6* (81), 1956, 387—400.
[7] *S. Saks:* Theory of the integral, New York.

Резюме

ПОВЕРХНОСТНЫЙ ИНТЕГРАЛ

ЯН МАРЖИК (Jan Mařík), Прага.

(Поступило в редакцию 10/X 1955 г.)

Пусть m — натуральное число; пусть E_m — m-мерное евклидово пространство. Для всякого ограниченного измеримого множества $A \subset E_m$ положим $\|A\| = \sup \int_A \sum_{i=1}^{m} \frac{\partial v_i(x)}{\partial x_i}\,\mathrm{d}x$, где $v_1, \ldots, v_m$ — многочлены такие, что $\sum_{i=1}^{m} v_i^2(x) \leqq 1$ для всех $x \in A$. Пусть $\mathfrak{A}$ — система всех ограниченных измеримых множеств A, для которых $\|A\| < \infty$. Теорема 18 тогда утверждает: *Пусть $A \in \mathfrak{A}$; пусть D — граница множества A. Тогда на системе $\mathfrak{B}$ всех борелевских подмножеств множества D существует мера p и на*

ИОСИФ ВИССАРИОНОВИЧ СТАЛИН
1879—1953

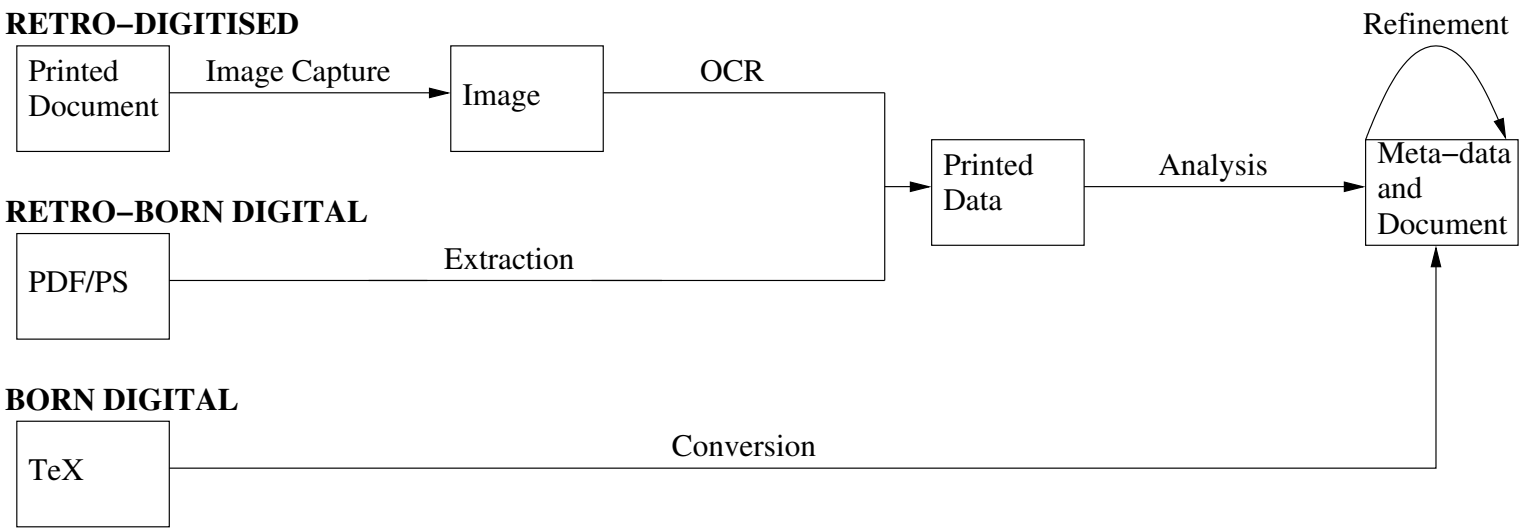
Document accessibility 4 DML processing challenges

Conversions (inversion of authoring+typesetting) needed from:

born-digital period: typesetting by TEX with export of [meta]data into digital library: maxTract

retro-digital period: scanning, geometrical transformations (BookRestorer), OCR (FineReader, InftyReader), *two-layer PDF*

retro-born-digital period: not complete .tex or .dvi data, bad formats, bitmap fonts of low resolution: finally Tesseract



From PDF to MathML (via LaTeX)

Most fulltext available as PDF only, often as low quality scanned volume pages. Aggregation via IP protected OAI-PMH, including the PDFs behing moving wall.

Workflow based in the case of:

born-digital PDFs: on maxTract, otherwise on PDFBox (plain text);

bitmap PDFs: on Infty, otherwise on Tesseract (no math).

Infty from Fukuoka

Run in parallel in Brno, Grenoble and Lisbon to speed up. Almost 200K papers (more than 1M pages and still running).

Working with prof. Suzuki to improve further (automation, support for Russian, LaTeX driver,...).

Automated only, no time (and money) to fix OCR errors.

MathML output used for [internal] indexing and similarity computations only, not for metadata or export.

maxTract from Birmingham

```
\left(
\sum ^{ m }_{ i = 0 } a _{ i } x ^{ i }
\right)
```

$$r(x) = \sum_{i=0}^{p} c_i x^i.$$

$$[p(x)q(x)]r(x) = \left[\left(\sum_{i=0}^{m} a_i x^i\right)\left(\sum_{i=0}^{n} b_i x^i\right)\right]\left(\sum_{i=0}^{p} c_i x^i\right)$$

$$= \left[\sum_{i=0}^{m+n}\left(\sum_{j=0}^{i} a_j b_{i-j}\right) x^i\right]\left(\sum_{i=0}^{p} c_i x^i\right)$$

```
open parenthesis
sum from i = zero to m of
a sub i x to the power of i
closing parenthesis
```

```
<math
  xmlns='http://www.w3.org/1998/Math/MathML'
  <mo>(</mo>
  <munderover>
    <mo>&Sum;</mo>
    <mrow>
      <mi>i</mi>
      <mo>=</mo>
      <mn>0</mn>
    </mrow>
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  </munderover>
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    <mi>i</mi>
  </msub>
  <msup>
    <mi>x</mi>
    <mi>i</mi>
  </msup>
  <mo>)</mo>
</math>
```

maxTract from Birmingham II: adding accessibility

Adding accessibility to mathematical documents on multiple levels:

- access to content for print impaired users, such as those with visual impairments, dyslexia or dyspraxia
- output compatible with web browsers, screen readers and tools such as copy and paste, which is achieved by enriching the regular text with mathematical markup. The output can also be used directly, within the limits of the presentation MathML produced, as machine readable mathematical input to software systems such as Mathematica or Maple.

On EuDML 10k+ fulltexts are served, mostly for reading in Chrome (HTML5 output) and/or Adobe Acrobat Reader (as multiple-layer PDFs, [no tagged PDFs yet]).

Metadata and conversions: MathML and LaTeX!

Data heterogenity, plethora of formats, validation and conversions:

world of authors: LaTeX, TeX notation of mathematics

world of applications/data exchange: XML, *MathML*

REPOX engine (by IST Lisbon) to remap different metadata formats to unique representation.

Metadata on the web—W3C standards: MathML, WAI-ARIA (Web Accessibility Initiative—Acessible Rich Internet Applications), WCAG (Web Content Accessibility Guidelines) 2.0.

Big volumes: $\rightarrow$ high *automation* to save costs: converting to MathML (via Tralics) to allow discoverability and indexing (formulae similarity search). 130+K fulltexts with MathML, Infty still running….

Why Search?

Vast amounts of [moving] contents in digital libraries: from browsing to *search*; from static links to indirect search links, or even semantic search.

Searching is crucial part of *accessibility* and *exploration* of the great ideas around, carved into 0s and 1s.

Pragmatic decisions on math indexing level: *presentation* vs. *content* vs. *semantic*. In EuDML first step: scalable presentation (structural), with methods (tree indexing and weighting) extendable for content or semantic.

Why Math Search (MIR)?

A picture is worth thousands words.

“A math formulae is worth of hundreds of words.“ (Ross Moore)

There are papers with more formulae than plain text.

Precision vs. Recall optimisation: optimizing recall is better for exploratory searching (we have not opted for precision as holy grail at the moment).

Motivation for MSE (including formulae) – cont.

prof. James Davenport, CEIC member, MKM2011 PC chair, on panel at EuDML workshop in Bertinoro as a reply to the question "what functionality and incentives would made a working mathematician to login and use a modern DML as EuDML?":

"Math formulae search."

Why math *search* is more relevant now than ever?

- Allowing formulas in queries helps to *disambiguate and narrow* search. Sometimes the only difference among set of notions/key words would be in a math formula.
- Example 1: knowing the solution of partial differential equation in $L^1(\mathbb{C}^3)$, is there one in $L^2(\mathbb{C}^5)$?
- Example 2: historians may want to follow the history of a (class of) formula(s) across languages and vocabularies (e.g. same objects studied/used by physicists and mathematicians under different names).
- Imagine your favourite ebook math textbook being [TEX]-search aware—e.g. your search app supports math formulae search.

We did not start from scratch

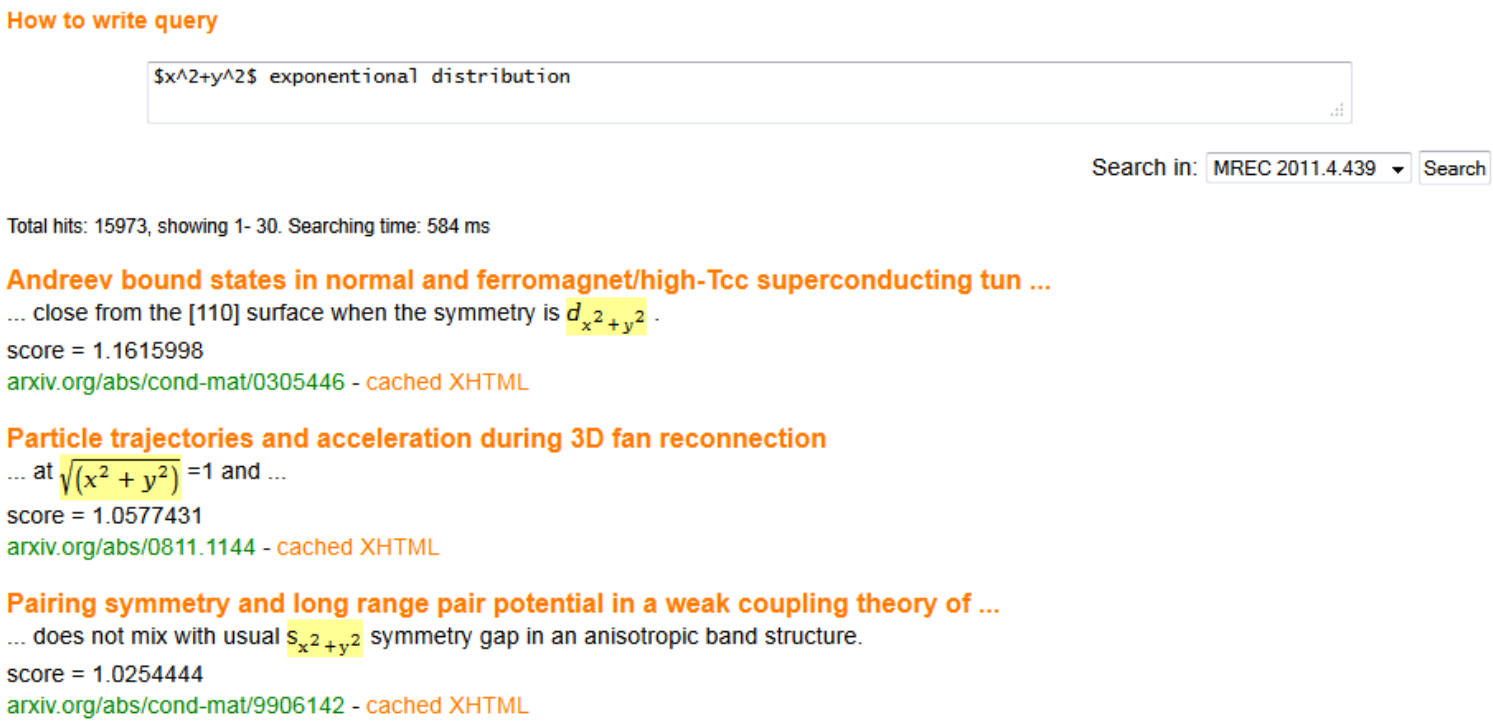
Compare `google.com/search?q=Einstein` with math-aware search of `Einstein+$E=mc^2$` over arXiv.

Existing systems – pros and cons

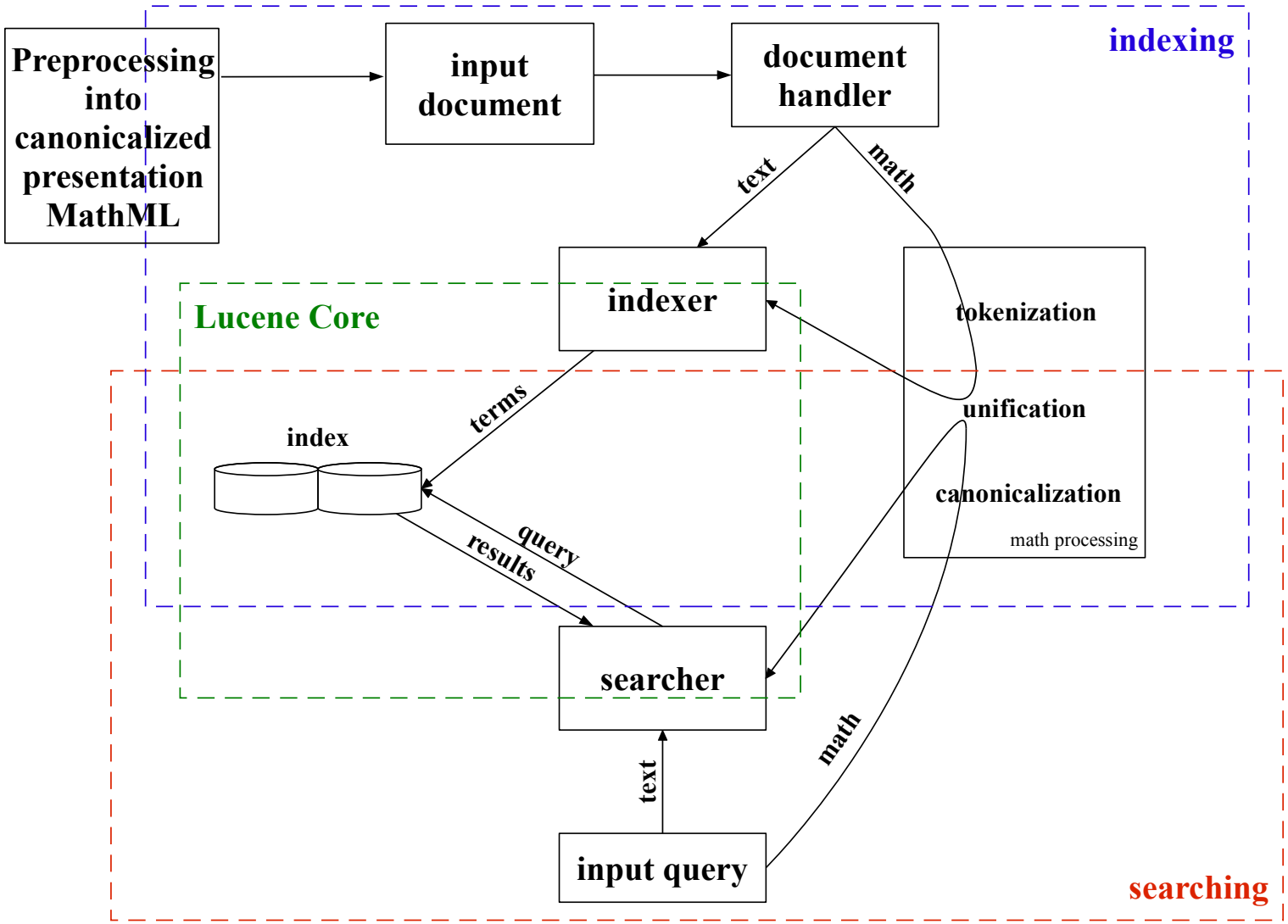
- **MathDex**: formerly MathFind * seven digit figure NSF grant by Design Science (Robert Miner) * Lucene based, indexing n-grams of presentation MathML * pioneering conversion effort
- **EgoMath and EgoMath2**: based on full text web search system Egothor * presentation MathML for indexing * idea of formulae augmentation, α-equivalence algorithms and relevance calculation
- **LaTeXSearch**: MSE offered by Springer * closed source * only for LaTeX math string approximate match based on strings * no formulae structure matching * small database: 3 million formulae from 'random' sources
- **LeActiveMath**: indexing string tokens from OMDoc with OpenMath semantic notation * *only* for documents authored for LeActiveMath learning environment
- **DLMF**: *only* for documents authored for DLMF in special markup * equation search
- **MathWeb Search**: semantic approach – uses substitution trees – not based on full text searching * supports Content MathML and OpenMath * problem with acquiring semantic data

MIaS — Math Indexer and Searcher

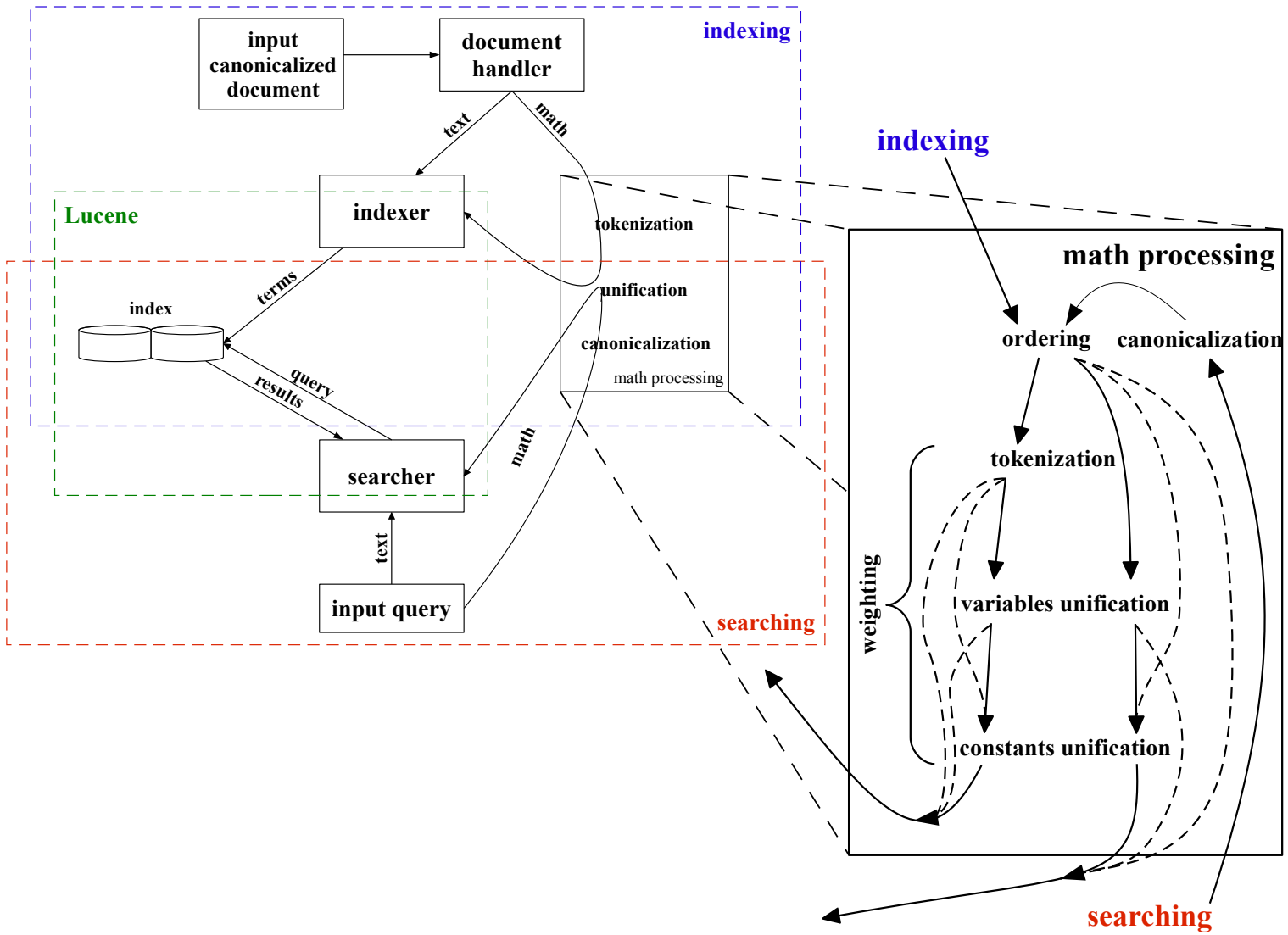
- math-aware, full-text based search engine
- joins textual and mathematical querying
- MathML *or* TEX input



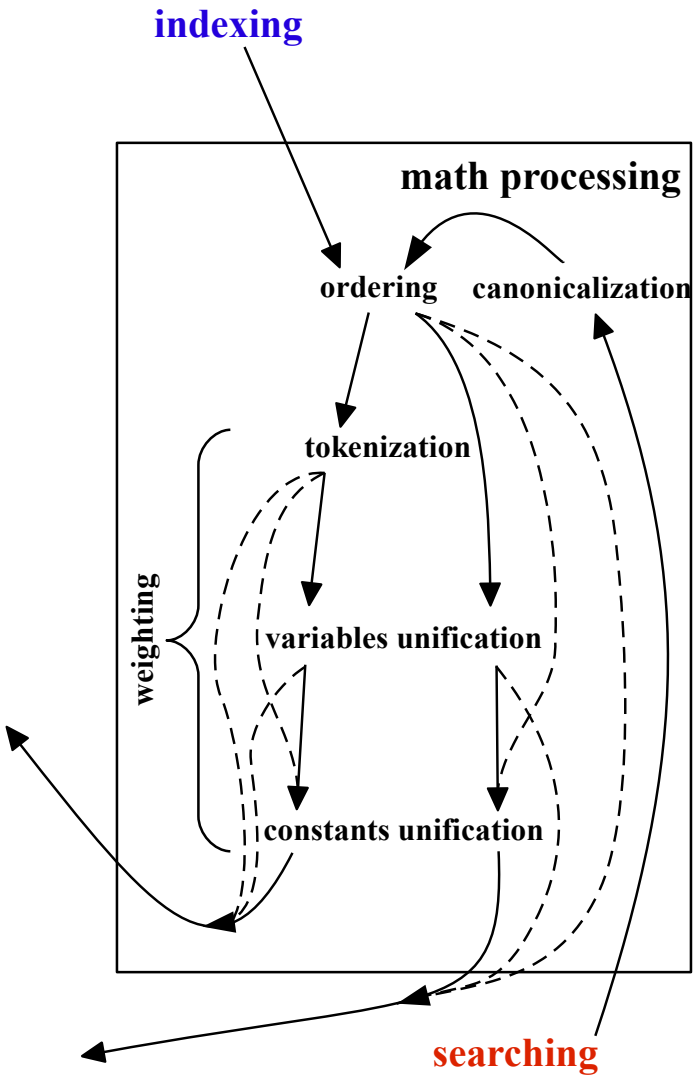
MSE overall design

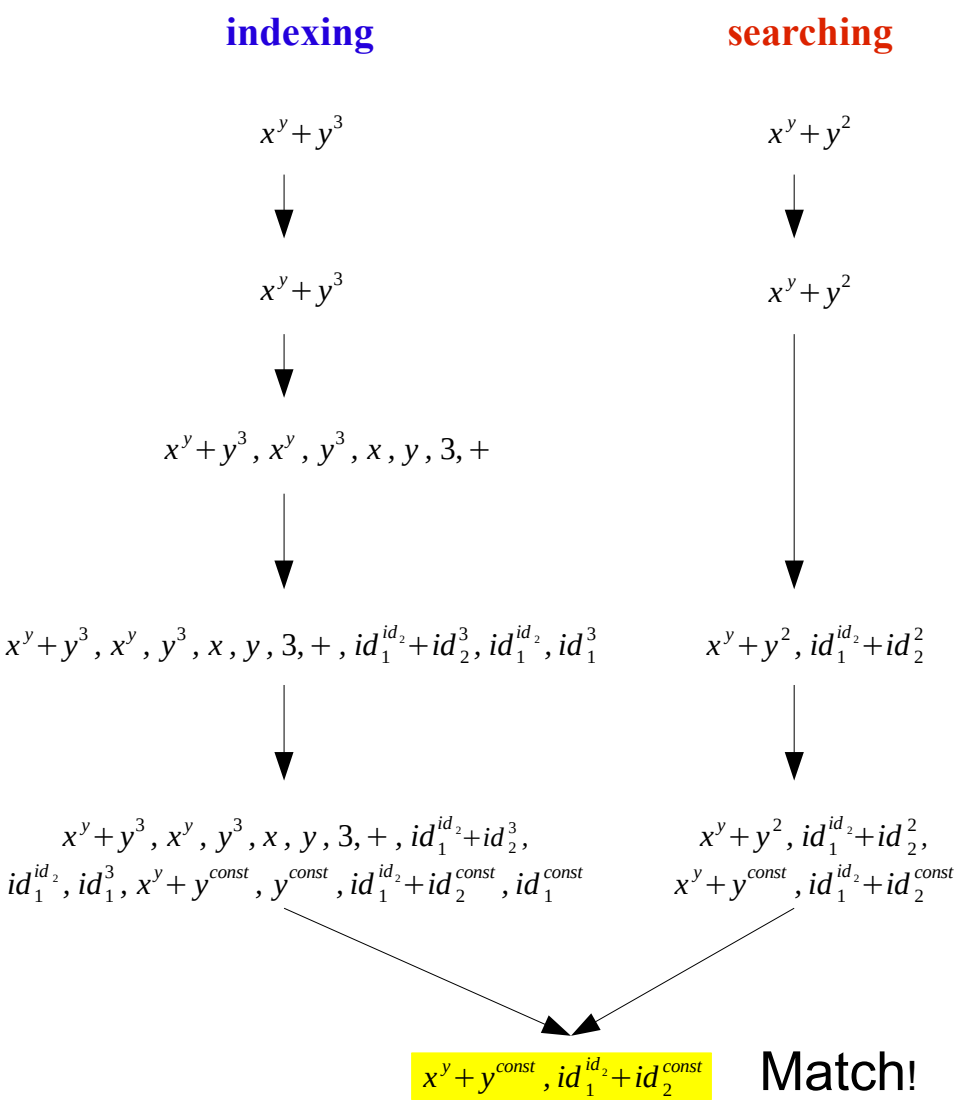


Math indexing design



Example


indexing
math processing
ordering
canonicalization
tokenization
weighting
variables unification
constants unification
searching


indexing
searching
x^y+y^3
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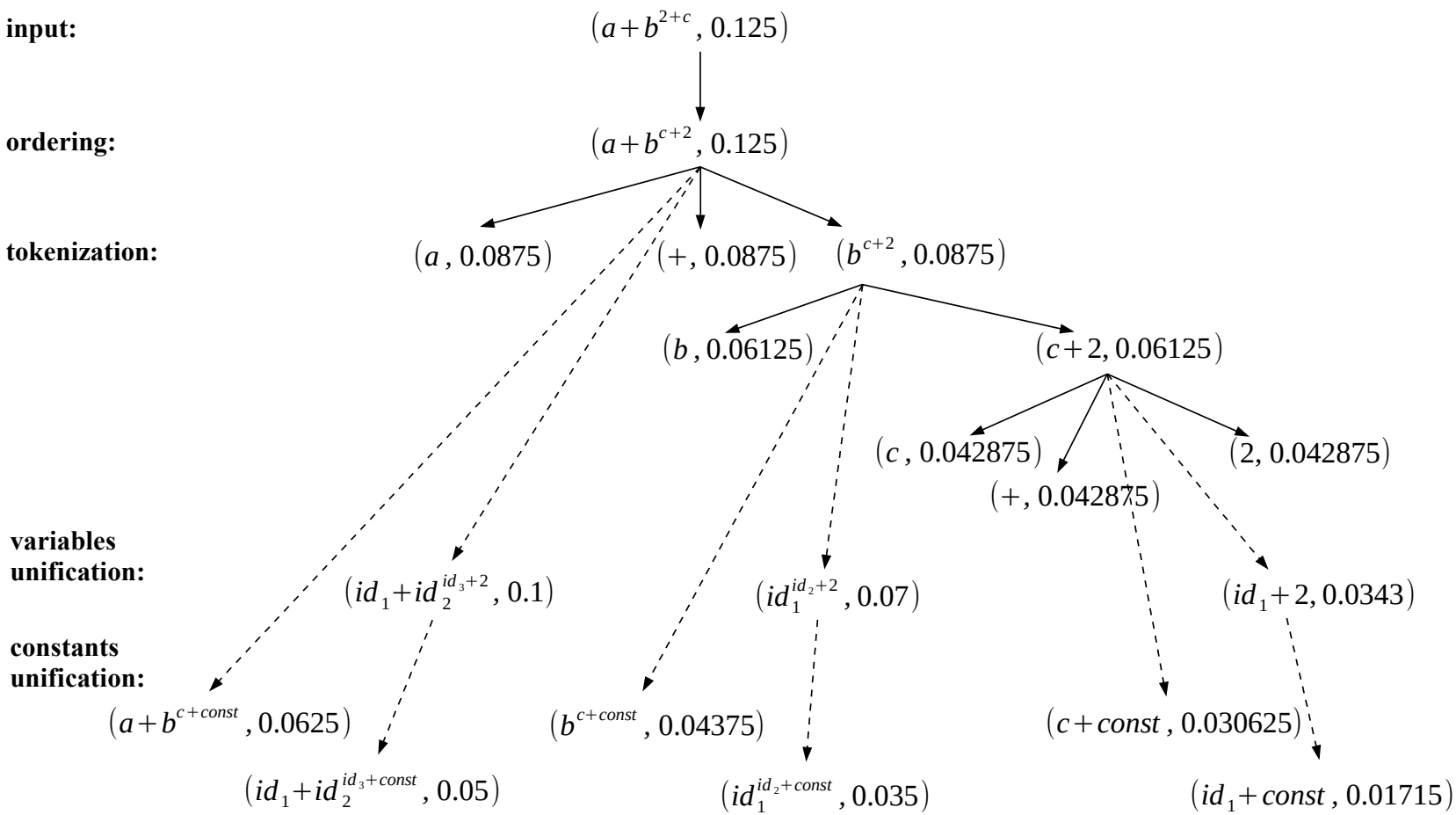
x^y+y^2
$x^y+y^3, x^y, y^3, x, y, 3, +$
$x^y+y^3, x^y, y^3, x, y, 3, +, id_1^{id_2}+id_2^3, id_1^{id_2}, id_1^3$
$x^y+y^2, id_1^{id_2}+id_2^2$
$x^y+y^3, x^y, y^3, x, y, 3, +, id_1^{id_2}+id_2^3, id_1^{id_2}, id_1^3, x^y+y^{const}, y^{const}, id_1^{id_2}+id_2^{const}, id_1^{const}$
$x^y+y^2, id_1^{id_2}+id_2^2, x^y+y^{const}, id_1^{id_2}+id_2^{const}$
$x^y+y^{const}, id_1^{id_2}+id_2^{const}$
Match!

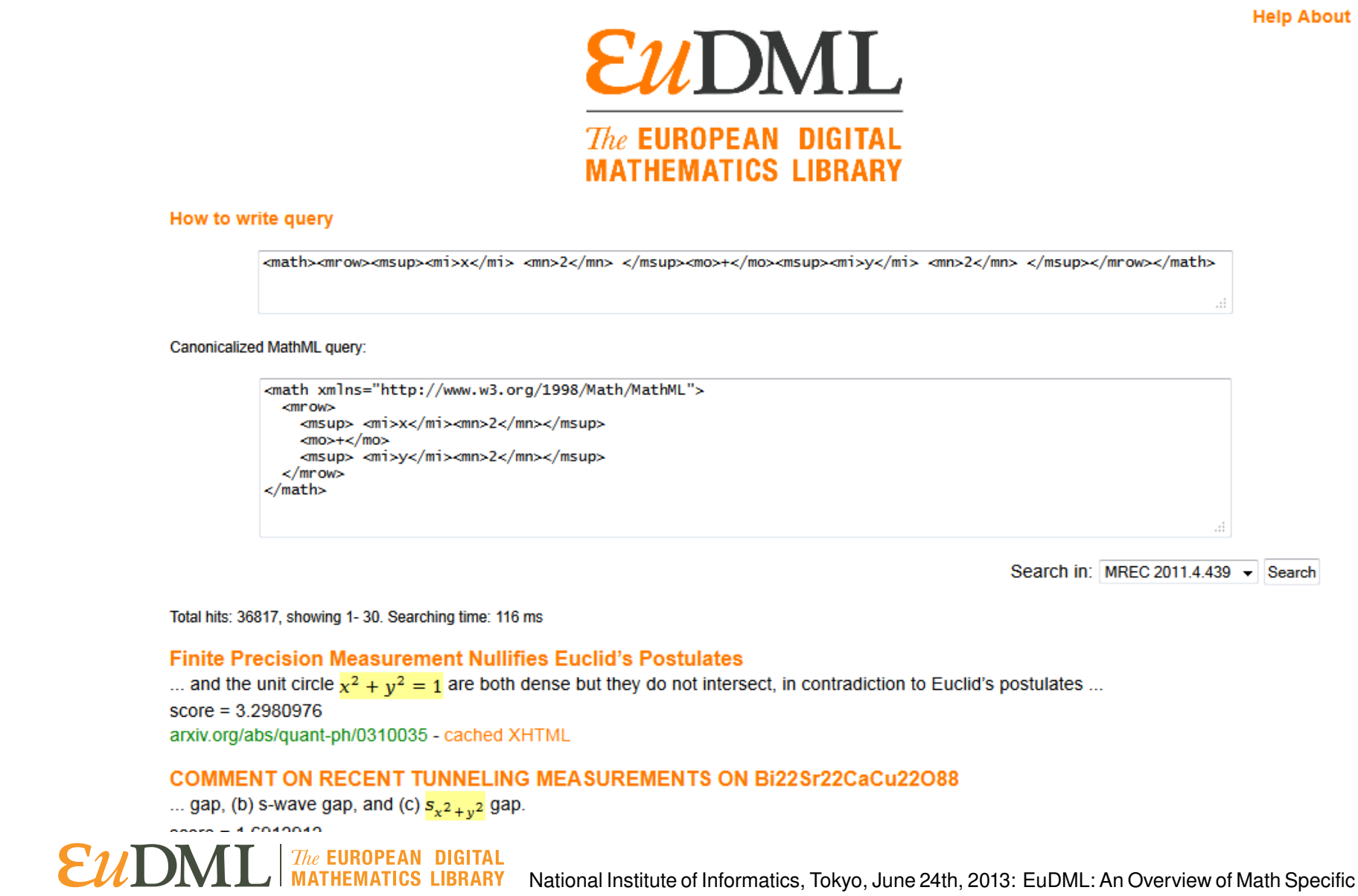
Formula processing example – subformulae weighting



Implementation

- Java
- Lucene 3.1.0, now switching to Lucene/Solr 4
- Mathematical part implements Lucene's interface Tokenizer – able to integrate to any Lucene based system
- MIaS4Solr plugin was created for the use in Solr
- Textual content – processed by StandardAnalyzer
- easily deployable in Java/Lucene based system or as a web service

Search demonstration



Formulae search demonstration comments

Demo web interface: http://aura.fi.muni.cz:8085/webmias/

- MathML/TEX input (Tralics [2] for conversion to MathML [**?**])
- Canonicalization of the query – problems with UMCL library [1]
- Matched document snippet generation
- MathJax for nicer math rendering and better portability
- Snuggle TeX for on-the-fly as-you-type rendering

All up and ready on the EuDML system.

Searching (semantically) similar papers

Exploration of a DML: browsing (semantically) similar papers

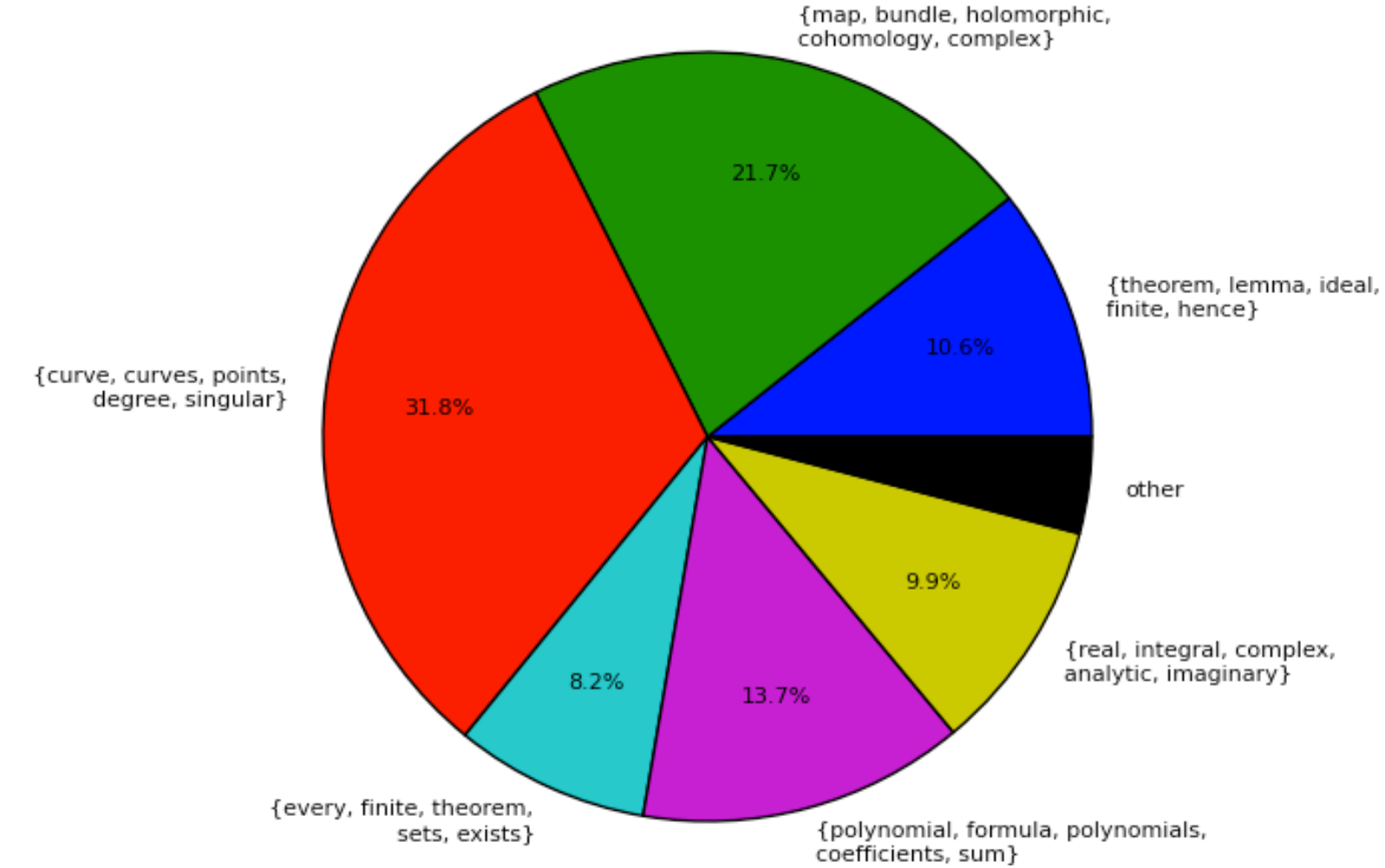
Semantic search via topic modeling: Latent Semantic Indexing, Latent Dirichlet Allocation

Leading Edge Example: Automated Meaning Picking from Texts

LDA Topics Pie Chart for math.0406240:

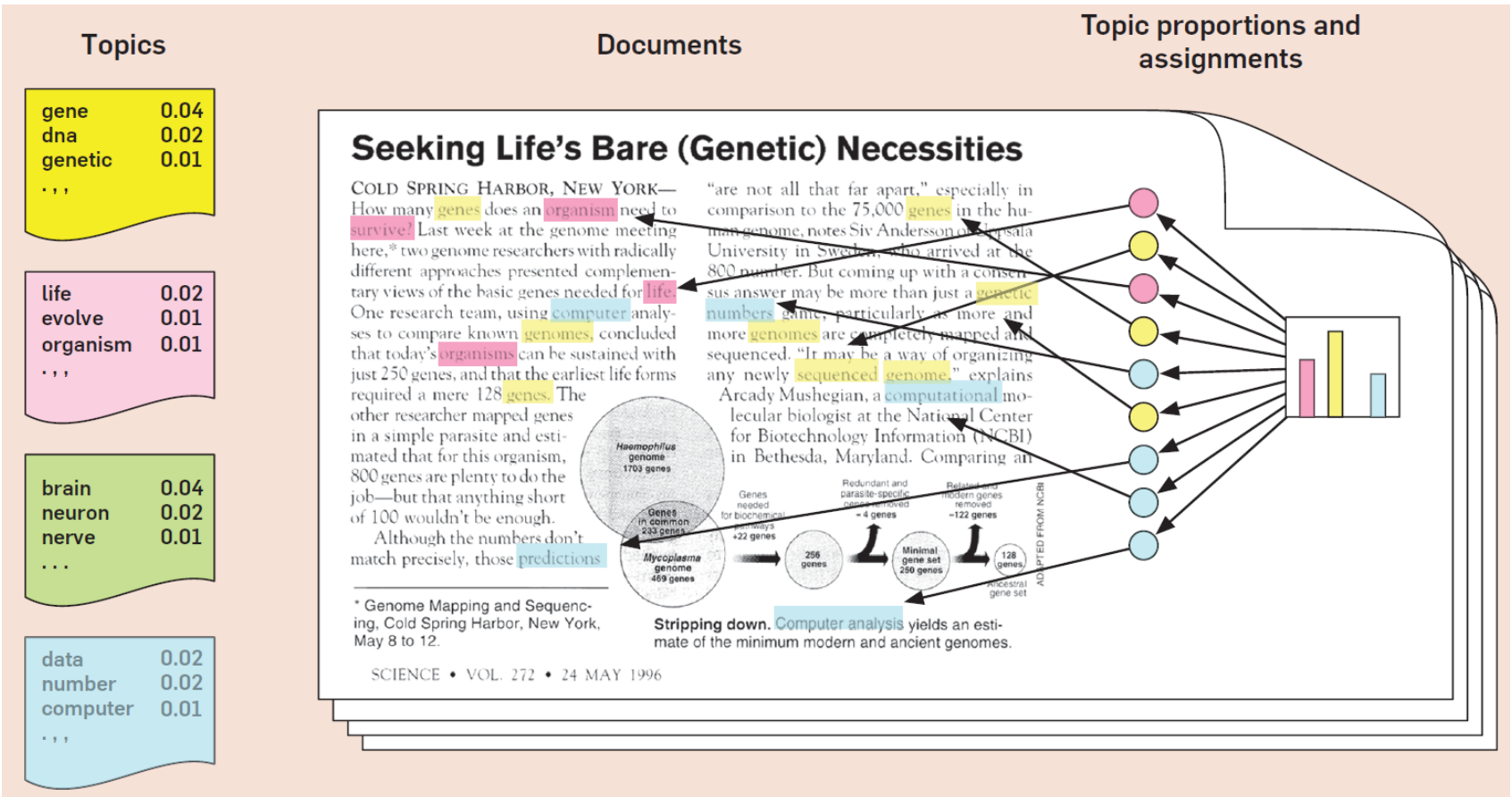
Each slice represents a different topic. The size of the slice corresponds to "how much is the article about this topic?". Topics which contribute <6% to the above document are aggregated under "other".

LDA topics are distributions over words; in the image, each topic is summarized by its five most probable words.



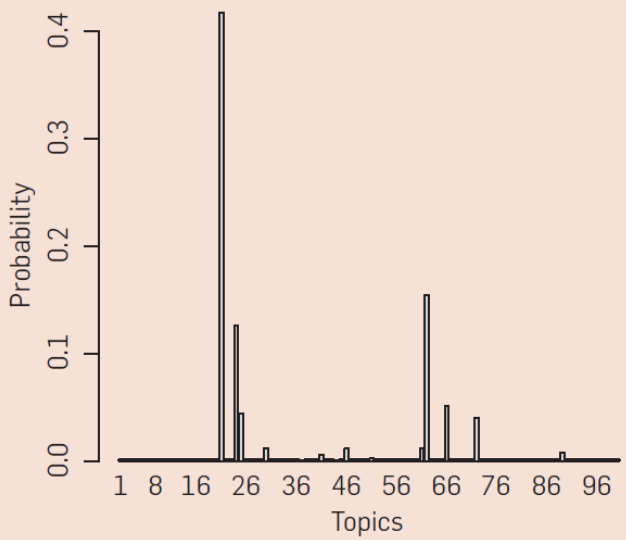
Probabilistic Topical Modeling: Latent Dirichlet Allocation

- topic: weighted list of words
- document: weighted list of topics



Topical Modeling: Latent Dirichlet Allocation II

- all topics computed automatically from document corpora



"Genetics"	"Evolution"	"Disease"	"Computers"
human	evolution	disease	computer
genome	evolutionary	host	models
dna	species	bacteria	information
genetic	organisms	diseases	data
genes	life	resistance	computers
sequence	origin	bacterial	system
gene	biology	new	network
molecular	groups	strains	systems
sequencing	phylogenetic	control	model
map	living	infectious	parallel
information	diversity	malaria	methods
genetics	group	parasite	networks
mapping	new	parasites	software
project	two	united	new
sequences	common	tuberculosis	simulations

Content Similarity Results in <http://eudml.org>

We have developed and delivered technology for *similarity* (gensim), document *conversions* (to Braille or to text: Mathml2text) and math content *normalization*. Different formulae representations for similarity computation.

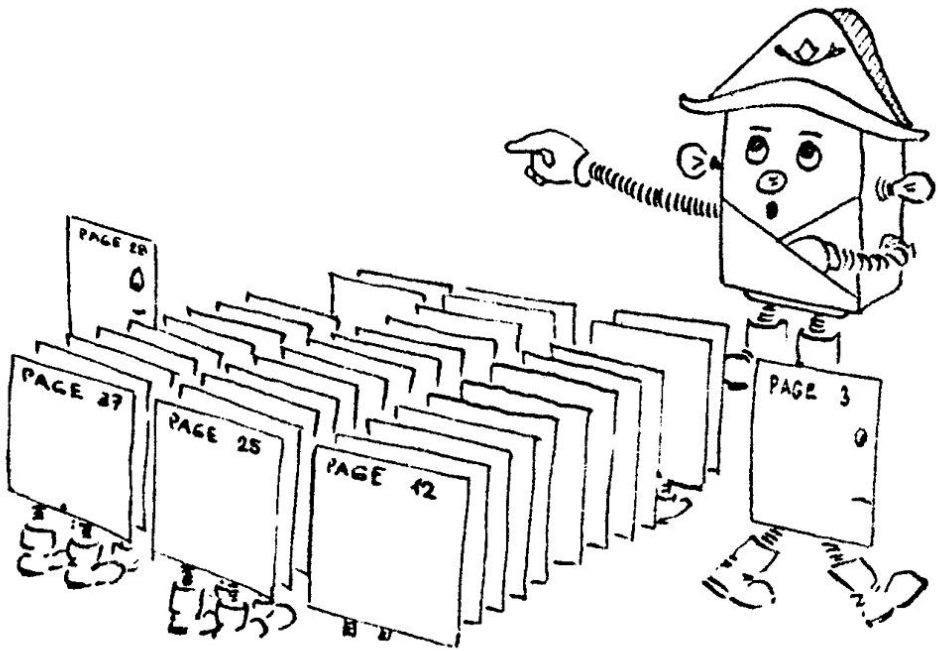
Summary

- EuDML is up and running, with several novel math-aware approaches developed and *in use*
- verified complex workflow and proven technologies and tools for DML
- Scalable solution for math formulae search researched, implemented, tested and integrated into current version of EuDML system!
- MIR/MIaS project pages – https://mir.fi.muni.cz/
- math-aware methods for document similarity (MathML2text, gensim)
- a lot more on <http:/project.eudml.org> (e.g. PDF size reduction of 62% of original already CCITT-G4 compressed PDFs, etc.)

Future work

- DML workshop series, join us at DML 2013 c/o CICM Bath in UK in July 2013
- Activities towards WDML (Sloan funding,…)
- EuDML initiative consortium, further sustainability solutions (grant proposal writing).
- Improved MathML canonicalization and new preprocessing filters, search developed and evaluated with the use of EuDML math query database of intentions.
- Addition of Content MathML tree indexing.
- NCTIR 11!

Acknowledgments and questions?



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