

## Chapter 6: Integrity Constraints

- Domain Constraints
- Referential Integrity
- Assertions
- Triggers
- Functional Dependencies

## Domain Constraints

- Integrity constraints guard against accidental damage to the database, by ensuring that authorized changes to the database do not result in a loss of data consistency.
- Domain constraints are the most elementary form of integrity constraint.
- They test values inserted in the database, and test queries to ensure that the comparisons make sense.

## Domain Constraints (Cont.)

- The **check** clause in SQL-92 permits domains to be restricted:
  - Use **check** clause to ensure that an hourly-wage domain allows only values greater than a specified value.

```
create domain hourly-wage numeric(5,2)  
                  constraint value-test check(value >= 4.00)
```

- The domain *hourly-wage* is declared to be a decimal number with 5 digits, 2 of which are after the decimal point
- The domain has a constraint that ensures that the hourly-wage is greater than 4.00.
- The clause **constraint** *value-test* is optional; useful to indicate which constraint an update violated.

## Referential Integrity

- Ensures that a value that appears in one relation for a given set of attributes also appears for a certain set of attributes in another relation.
  - Example: if “Perryridge” is a branch name appearing in one of the tuples in the *account* relation, then there exists a tuple in the *branch* relation for branch “Perryridge”.
- Formal Definition
  - Let  $r_1(R_1)$  and  $r_2(R_2)$  be relations with primary keys  $K_1$  and  $K_2$  respectively.
  - The subset  $\alpha$  of  $R_2$  is a *foreign key* referencing  $K_1$  in relation  $r_1$ , if for every  $t_2$  in  $r_2$  there must be a tuple  $t_1$  in  $r_1$  such that  $t_1[K_1] = t_2[\alpha]$ .
  - Referential integrity constraint:  $\Pi_{\alpha}(r_2) \subseteq \Pi_{K_1}(r_1)$

## Referential Integrity in the E-R Model

- Consider relationship set  $R$  between entity sets  $E_1$  and  $E_2$ .  
The relational schema for  $R$  includes the primary keys  $K_1$  of  $E_1$  and  $K_2$  of  $E_2$ .  
Then  $K_1$  and  $K_2$  form foreign keys on the relational schemas for  $E_1$  and  $E_2$  respectively.
- Weak entity sets are also a source of referential integrity constraints. For, the relation schema for a weak entity set must include the primary key of the entity set on which it depends.

## Database Modification

- The following tests must be made in order to preserve the following referential integrity constraint:

$$\Pi_{\alpha} (r_2) \subseteq \Pi_K (r_1)$$

- **Insert.** If a tuple  $t_2$  is inserted into  $r_2$ , the system must ensure that there is a tuple  $t_1$  in  $r_1$  such that  $t_1[K] = t_2[\alpha]$ . That is

$$t_2[\alpha] \in \Pi_K (r_1)$$

- **Delete.** If a tuple  $t_1$  is deleted from  $r_1$ , the system must compute the set of tuples in  $r_2$  that reference  $t_1$ :

$$\sigma_{\alpha = t_1[K]} (r_2)$$

If this set is not empty, either the delete command is rejected as an error, or the tuples that reference  $t_1$  must themselves be deleted (cascading deletions are possible).

## Database Modification (Cont.)

- **Update.** There are two cases:
  - If a tuple  $t_2$  is updated in relation  $r_2$  and the update modifies values for the foreign key  $\alpha$ , then a test similar to the insert case is made. Let  $t_2'$  denote the new value of tuple  $t_2$ . The system must ensure that

$$t_2'[\alpha] \in \Pi_K (r_1)$$

- If a tuple  $t_1$  is updated in  $r_1$ , and the update modifies values for the primary key ( $K$ ), then a test similar to the delete case is made. The system must compute

$$\sigma_{\alpha = t_1[K]} (r_2)$$

using the old value of  $t_1$  (the value before the update is applied). If this set is not empty, the update may be rejected as an error, or the update may be cascaded to the tuples in the set, or the tuples in the set may be deleted.

## Referential Integrity in SQL

- Primary and candidate keys and foreign keys can be specified as part of the SQL **create table** statement:
  - The **primary key** clause of the **create table** statement includes a list of the attributes that comprise the primary key.
  - The **unique key** clause of the **create table** statement includes a list of the attributes that comprise a candidate key.
  - The **foreign key** clause of the **create table** statement includes both a list of the attributes that comprise the foreign key and the name of the relation referenced by the foreign key.



## Referential Integrity in SQL - Example

```
create table customer  
  (customer-name char(20) not null,  
   customer-street char(30),  
   customer-city char(30),  
   primary key (customer-name))
```

```
create table branch  
  (branch-name char(15) not null,  
   branch-city char(30),  
   assets integer,  
   primary key (branch-name))
```

## Referential Integrity in SQL - Example (Cont.)

**create table** *account*

(*branch-name* char(15),  
*account-number* char(10) **not null**,  
*balance* integer,  
**primary key** (*account-number*),  
**foreign key** (*branch-name*) **references** *branch*)

**create table** *depositor*

(*customer-name* char(20) **not null**,  
*account-number* char(10) **not null**,  
**primary key** (*customer-name*, *account-number*),  
**foreign key** (*account-number*) **references** *account*,  
**foreign key** (*customer-name*) **references** *customer*)

## Cascading Actions in SQL

**create table** *account*

...

**foreign key** (*branch-name*) **references** *branch*  
**on delete cascade**  
**on update cascade,**

... )

- Due to the **on delete cascade** clauses, if a delete of a tuple in *branch* results in referential-integrity constraint violation, the delete “cascades” to the *account* relation, deleting the tuple that refers to the branch that was deleted.
- Cascading updates are similar.

## Cascading Actions in SQL (Cont.)

- If there is a chain of foreign-key dependencies across multiple relations, with **on delete cascade** specified for each dependency, a deletion or update at one end of the chain can propagate across the entire chain.
- If a cascading update or delete causes a constraint violation that cannot be handled by a further cascading operation, the system aborts the transaction. As a result, all the changes caused by the transaction and its cascading actions are undone.

## Assertions

- An *assertion* is a predicate expressing a condition that we wish the database always to satisfy.
- An assertion in SQL-92 takes the form

**create assertion** <assertion-name> **check** <predicate>

- When an assertion is made, the system tests it for validity. This testing may introduce a significant amount of overhead; hence assertions should be used with great care.

## Assertion Example

- The sum of all loan amounts for each branch must be less than the sum of all account balances at the branch.

**create assertion *sum-constraint* check**

**(not exists (select \* from *branch***

**where (select sum(*amount*) from *loan***

**where *loan.branch-name* = *branch.branch-name*)**

**>= (select sum(*amount*) from *account***

**where *loan.branch-name* = *branch.branch-name*)))**

## Assertion Example

- Every loan has at least one borrower who maintains an account with a minimum balance of \$1000.00.

**create assertion *balance-constraint* check**

```
(not exists (select * from loan  
  where not exists ( select *  
    from borrower, depositor, account  
  where loan.loan-number = borrower.loan-number  
    and borrower.customer-name = depositor.customer-name  
    and depositor.account-number = account.account-number  
    and account.balance >= 1000)))
```

# Triggers

- A *trigger* is a statement that is executed automatically by the system as a side effect of a modification to the database.
- To design a trigger mechanism, we must:
  - Specify the conditions under which the trigger is to be executed.
  - Specify the actions to be taken when the trigger executes.
- The SQL-92 standard does not include triggers, but many implementations support triggers.



## Trigger Example

- Suppose that instead of allowing negative account balances, the bank deals with overdrafts by
  - setting the account balance to zero
  - creating a loan in the amount of the overdraft
  - giving this loan a loan number identical to the account number of the overdrawn account
- The condition for executing the trigger is an update to the *account* relation that results in a negative *balance* value.

## Trigger Example (Cont.)

```
define trigger overdraft on update of account T  
  (if new T.balance < 0  
    then (insert into loan values  
      (T.branch-name, T.account-number, - new T.balance)  
    insert into borrower  
      (select customer-name, account-number  
        from depositor  
        where T.account-number = depositor.account-number)  
    update account S  
      set S.balance = 0  
      where S.account-number = T.account-number))
```

The keyword **new** used before *T.balance* indicates that the value of *T.balance* after the update should be used; if it is omitted, the value before the update is used.

## Functional Dependencies

- Constraints on the set of legal relations.
- Require that the value for a certain set of attributes determines uniquely the value for another set of attributes.
- A functional dependency is a generalization of the notion of a *key*.

## Functional Dependencies (Cont.)

- Let  $R$  be a relation schema

$$\alpha \subseteq R, \beta \subseteq R$$

- The functional dependency

$$\alpha \rightarrow \beta$$

holds on  $R$  if and only if for any legal relations  $r(R)$ , whenever any two tuples  $t_1$  and  $t_2$  of  $r$  agree on the attributes  $\alpha$ , they also agree on the attributes  $\beta$ . That is,

$$t_1[\alpha] = t_2[\alpha] \Rightarrow t_1[\beta] = t_2[\beta]$$

- $K$  is a superkey for relation schema  $R$  if and only if  $K \rightarrow R$
- $K$  is a candidate key for  $R$  if and only if
  - $K \rightarrow R$ , and
  - for no  $\alpha \subset K$ ,  $\alpha \rightarrow R$

## Functional Dependencies (Cont.)

- Functional dependencies allow us to express constraints that cannot be expressed using superkeys. Consider the schema:

*Loan-info-schema = (branch-name, loan-number, customer-name, amount).*

We expect this set of functional dependencies to hold:

*loan-number* → *amount*

*loan-number* → *branch-name*

but would not expect the following to hold:

*loan-number* → *customer-name*

## Use of Functional Dependencies

- We use functional dependencies to:
  - test relations to see if they are legal under a given set of functional dependencies. If a relation  $r$  is legal under a set  $F$  of functional dependencies, we say that  $r$  *satisfies*  $F$ .
  - specify constraints on the set of legal relations; we say that  $F$  *holds* on  $R$  if all legal relations on  $R$  satisfy the set of functional dependencies  $F$ .
- Note: A specific instance of a relation schema may satisfy a functional dependency even if the functional dependency does not hold on all legal instances. For example, a specific instance of *Loan-schema* may, by chance, satisfy *loan-number*  $\rightarrow$  *customer-name*.

## Closure of a Set of Functional Dependencies

- Given a set  $F$  set of functional dependencies, there are certain other functional dependencies that are logically implied by  $F$ .
- The set of all functional dependencies logically implied by  $F$  is the *closure* of  $F$ .
- We denote the *closure* of  $F$  by  $F^+$ .
- We can find all of  $F^+$  by applying Armstrong's Axioms:
  - if  $\beta \subseteq \alpha$ , then  $\alpha \rightarrow \beta$  (**reflexivity**)
  - if  $\alpha \rightarrow \beta$ , then  $\gamma\alpha \rightarrow \gamma\beta$  (**augmentation**)
  - if  $\alpha \rightarrow \beta$  and  $\beta \rightarrow \gamma$ , then  $\alpha \rightarrow \gamma$  (**transitivity**)

These rules are sound and complete.

## Closure (Cont.)

- We can further simplify computation of  $F^+$  by using the following additional rules.
  - If  $\alpha \rightarrow \beta$  holds and  $\alpha \rightarrow \gamma$  holds, then  $\alpha \rightarrow \beta\gamma$  holds (**union**)
  - If  $\alpha \rightarrow \beta\gamma$  holds, then  $\alpha \rightarrow \beta$  holds and  $\alpha \rightarrow \gamma$  holds (**decomposition**)
  - If  $\alpha \rightarrow \beta$  holds and  $\gamma\beta \rightarrow \delta$  holds, then  $\alpha\gamma \rightarrow \delta$  holds (**pseudotransitivity**)

The above rules can be inferred from Armstrong's axioms.



## Example

- $R = (A, B, C, G, H, I)$

- $F = \{A \rightarrow B$   
 $A \rightarrow C$   
 $CG \rightarrow H$   
 $CG \rightarrow I$   
 $B \rightarrow H\}$

- some members of  $F^+$

- $A \rightarrow H$

- $AG \rightarrow I$

- $CG \rightarrow HI$

## Closure of Attribute Sets

- Define the *closure* of  $\alpha$  under  $F$  (denoted by  $\alpha^+$ ) as the set of attributes that are functionally determined by  $\alpha$  under  $F$ :

$$\alpha \rightarrow \beta \text{ is in } F^+ \Leftrightarrow \beta \subseteq \alpha^+$$

- Algorithm to compute  $\alpha^+$ , the closure of  $\alpha$  under  $F$

```
result :=  $\alpha$ ;  
while (changes to result) do  
  for each  $\beta \rightarrow \gamma$  in  $F$  do  
    begin  
      if  $\beta \subseteq \textit{result}$  then result := result  $\cup$   $\gamma$ ;  
    end
```

## Example

- $R = (A, B, C, G, H, I)$

$$F = \{A \rightarrow B \\ A \rightarrow C \\ CG \rightarrow H \\ CG \rightarrow I \\ B \rightarrow H\}$$

- $(AG^+)$

1.  $result = AG$

2.  $result = ABCG$  ( $A \rightarrow C$  and  $A \subseteq AGB$ )

3.  $result = ABCGH$  ( $CG \rightarrow H$  and  $CG \subseteq AGBC$ )

4.  $result = ABCGHI$  ( $CG \rightarrow I$  and  $CG \subseteq AGBCH$ )

- Is  $AG$  a candidate key?

1.  $AG \rightarrow R$

2. does  $A^+ \rightarrow R$ ?

3. does  $G^+ \rightarrow R$ ?

## Canonical Cover

- Consider a set  $F$  of functional dependencies and the functional dependency  $\alpha \rightarrow \beta$  in  $F$ .
  - Attribute  $A$  is extraneous in  $\alpha$  if  $A \in \alpha$  and  $F$  logically implies  $(F - \{\alpha \rightarrow \beta\}) \cup \{(\alpha - A) \rightarrow \beta\}$ .
  - Attribute  $A$  is extraneous in  $\beta$  if  $A \in \beta$  and the set of functional dependencies  $(F - \{\alpha \rightarrow \beta\}) \cup \{\alpha \rightarrow (\beta - A)\}$  logically implies  $F$ .
- A *canonical cover*  $F_c$  for  $F$  is a set of dependencies such that  $F$  logically implies all dependencies in  $F_c$  and  $F_c$  logically implies all dependencies in  $F$ , and further
  - No functional dependency in  $F_c$  contains an extraneous attribute.
  - Each left side of a functional dependency in  $F_c$  is unique.

## Canonical Cover (Cont.)

- Compute a canonical cover for  $F$ :

**repeat**

Use the union rule to replace any dependencies in  $F$

$\alpha_1 \rightarrow \beta_1$  and  $\alpha_1 \rightarrow \beta_2$  with  $\alpha_1 \rightarrow \beta_1 \beta_2$

Find a functional dependency  $\alpha \rightarrow \beta$  with an  
extraneous attribute either in  $\alpha$  or in  $\beta$

If an extraneous attribute is found, delete it from  $\alpha \rightarrow \beta$

**until**  $F$  does not change

## Example of Computing a Canonical Cover

- $R = (A, B, C)$

$$F = \{A \rightarrow BC$$
$$B \rightarrow C$$
$$A \rightarrow B$$
$$AB \rightarrow C\}$$

- Combine  $A \rightarrow BC$  and  $A \rightarrow B$  into  $A \rightarrow BC$

- $A$  is extraneous in  $AB \rightarrow C$  because  $B \rightarrow C$  logically implies  $AB \rightarrow C$ .

- $C$  is extraneous in  $A \rightarrow BC$  since  $A \rightarrow BC$  is logically implied by  $A \rightarrow B$  and  $B \rightarrow C$ .

- The canonical cover is:

$$A \rightarrow B$$
$$B \rightarrow C$$