

$x_{n+1} = F(n, x_n)$ ← differenzialrechnung
1. Ordnung

$x_{n+1} - x_n = ?$

$y(x)$ $y'(x) = F(x, y(x))$

$(e^x)' = e^x$

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$y' = r \cdot y + f(x)$

1. Ordnung + separable Lösung

$(y')^2 - y^2 = 0$

$y' = y$ oder $y' = -y$

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$y(x)$

$y'(x) = f(x, y(x))$

$(x'(t), y'(t)) = (t', y'(t)) = (1, f(x, y(t)))$

$(f'(t), g'(t)) + (x_0, y_0)$

$x'(t) = f(x, y(t))$

$y'(t) = g(x, y(t))$

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$y \xrightarrow{L} L(y)$

{ diff. n. u. f. c. } \xrightarrow{L} { dif. f. c. }

$y(x) = y_0 + \int_{x_0}^x g(x) dx \Leftrightarrow g(x) = y'(x)$

$y(x_1) - y(x_0) = \left| \int_{x_0}^{x_1} f(x, y(x)) dx - \int_{x_0}^{x_1} f(x, z(x)) dx \right|$

$\leq \int_{x_0}^{x_1} |f(x, y(x)) - f(x, z(x))| dx \leq C \int_{x_0}^{x_1} |y(x) - z(x)| dx$

$\leq D |x - x_0|$ per Definition des Mittelwerts

\Rightarrow für $|L(y_1) - L(y_2)| < L_p |y_1 - y_2|$

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$dy = f(x) \cdot g(y) dx$ $y' = \frac{dy}{dx}$

$\frac{1}{g(y)} dy = f(x) dx$ $dy = f(x, y(x)) dx$

$\int \frac{1}{y} dy = L |g(x)| = \frac{1}{2} x^2 + C$

$\Rightarrow |y(x)| = e^{\frac{1}{2} x^2 + C} = e^{\frac{1}{2} x^2} \cdot e^C$

$y(x) = D \cdot e^{\frac{1}{2} x^2} \quad D \in \mathbb{R}$

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$\frac{df}{dt} = \frac{\partial f}{\partial x} \frac{dx}{dt} + \frac{\partial f}{\partial y} \frac{dy}{dt} + \frac{\partial f}{\partial z} \frac{dz}{dt}$

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$$y^{(k)}(x) = F(x, y, y', \dots, y^{(k-1)})$$

$$z_1 = y, z_2 = y', \dots, z_{k-1} = y^{(k-2)}$$

$$\begin{cases} z_1' = z_2 \\ z_2' = z_3 \\ \vdots \\ z_{k-1}' = F(x, z_1, z_2, \dots, z_{k-1}) \end{cases}$$

$y'' = -y$

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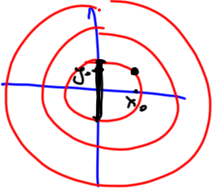
$$y^{(4)} = -y(x)$$

$$y' = x$$

$$x' = y'' = -y$$

$$y'' + y = 0 \quad \leftarrow \lambda x$$

$$(\lambda^2 + 1)e^{\lambda x} = 0 \Rightarrow \lambda^2 = -1, \lambda = \pm i$$

$$\leftarrow \pm i x \quad \lambda^2 + \alpha \lambda + 1 = 0 \Rightarrow$$


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