

Control Explicit—Data Symbolic Model Checking

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Introduction

to Execution-Based Verification

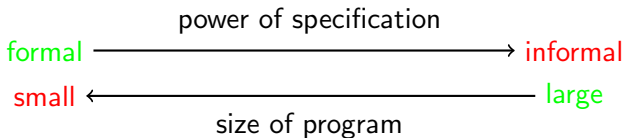
Formal Verification

given a **program**, decide, using rigorous mathematical methods, if the program is **correct** (against behaviour specification)

- undecidable in theory (of computability)

$$\varphi : \mathbb{N} \rightarrow \mathbb{N}, \psi : \mathbb{N} \rightarrow \mathbb{N}; \varphi \stackrel{?}{=} \psi$$

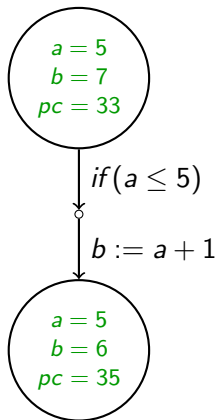
- difficult in practice



Transition System

verifying that a **program** satisfies a **formula** by checking that its **transition system** is a model of the **formula**

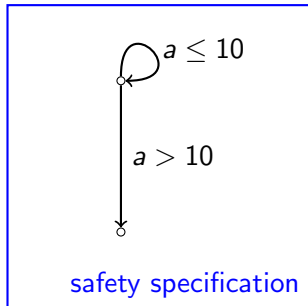
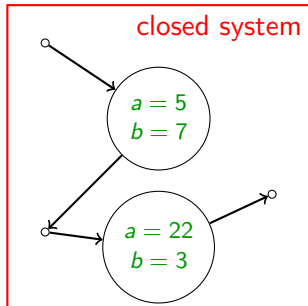
- execution generates a transition system
- **states** are evaluation of variables, program counter(s), heap, stack content
- **transitions** are execution of commands
- **branching** is caused by conditions, cycles, thread interleaving



Execution-Based Verification

execute the **system** while concurrently checking the **specification**

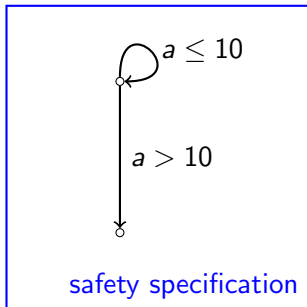
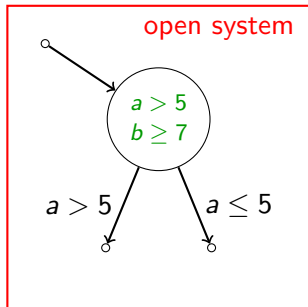
- **Testing** (arbitrary program)



Execution-Based Verification

execute the **system** while concurrently checking the **specification**

- **Symbolic Execution** (no multiplication or cycles)

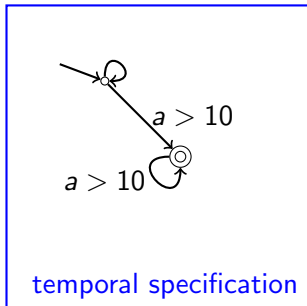
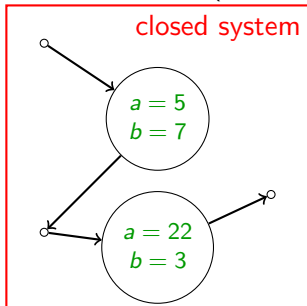


J. King. Symbolic Execution and Program Testing. *Commun. ACM*, 19(7):385–394, 1976.

Execution-Based Verification

execute the **system** while concurrently checking the **specification**

- **Model Checking** (small, parallel programs; communication protocols)



M. Vardi and P. Wolper. An Automata-Theoretic Approach to Automatic Program Verification. In *Proc. of LICS*, pages 332–344, 1986.

Long-Term Objectives

overcome the limitations of individual methods

- **testing**: more user friendly
 - automatic (Godefroid, et. al., 2008)
 - parallelism (Simsa, et. al., 2010)
- **symbolic execution**: more robust
 - temporal properties (Braione, et. al., 2008)
 - parallelism (Păsăreanu, et. al., 2003)
 - cycles (Trtík, et. al., 2012)
- **model checking**: smaller state space
 - symbolic representation (McMillan, et. al., 1992)
 - bounded approach (Biere, et. al., 1999)
 - parallel approach (Barnat, et. al., 2001)

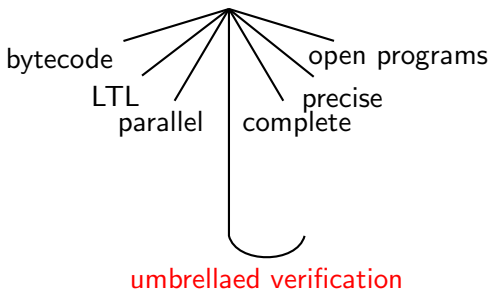
Explicit vs Symbolic Model Checking

- **explicit:**
states forming the transition system are stored **explicitly**
better for asynchronous, **control-flow** nondeterministic systems
allow parallel processing
- **symbolic:**
transition system is encoded into a **logical formula**
better for synchronous, **data-flow** nondeterministic systems
parallelisation is difficult

C. Eisner and D. Peled. Comparing Symbolic and Explicit Model Checking of a Software System. In *SPIN* volume 2318 of *LNCS*, pages 230–239. Springer, 2002.

State of the Art

towards complete and precise verification of parallel software
against temporal specification



Symbolic Execution

- states (path conditions) represented as linear constraints
use state-of-the-art libraries [1], e.g. Omega library [2]
– fast, unbounded variable evaluation, Presburger arithmetic

1. A. Coen-Porisini and G. Denaro and C. Ghezzi and M. Pezzé. Using Symbolic Execution for Verifying Safety-Critical Systems. In *Proc. of ESEC/FSE*, pages 142–151, 2001.

2. W. Pugh. A Practical Algorithm for Exact Array Dependence Analysis. *Communications of the ACM*, 35(8):102–114, 1992.

Symbolic Execution

- handle **nondeterminism**, **parallelism** by generating execution interleavings
- no state equivalence → no accepting cycle detection → no **temporal specification**

S. Khurshid, C. Păsăreanu, and W. Visser. Generalized Symbolic Execution for Model Checking and Testing. In *TACAS*, volume 2619 of *LNCS*, pages 553–568. Springer, 2003.

Symbolic Execution

- handle **loops**: unwind [1], invariants [2], path counters [3]
 1. J. King. Symbolic Execution and Program Testing. *Commun. ACM*, 19(7):385–394, 1976.
 2. S. Khurshid, C. Păsăreanu, and W. Visser. Generalized Symbolic Execution for Model Checking and Testing. In *TACAS*, volume 2619 of *LNCS*, pages 553–568. Springer, 2003.
 3. J. Strejček and M. Trtík. Abstracting Path Conditions. In *Proc. of ISSTA*, pages 155–165, 2012.

Symbolic Execution

- handle **complex operations**: state-of-the-art decision procedures [1], SMT solvers (bit-vectors, arrays), trigonometric functions [2]
 1. S. Anand and C. Păsăreanu and W. Visser. JPF-SE: A Symbolic Execution Extension to Java PathFinder. In *TACAS*, volume 4424 of *LNCS*, pages 134–138. Springer, 2007.
 2. M. Souza and M. Borges and M. d'Amorim and C. Păsăreanu. CORAL: Solving Complex Constraints for Symbolic PathFinder. In *NFM* volume 6617 of *LNCS*, pages 359–374. Springer, 2011.

Symbolic Execution

- handle **bytecode** as input language

C. Pășăreanu and N. Rungta. Symbolic PathFinder: Symbolic Execution of Java Bytecode. In *Proc. of ASE*, pages 170–180, 2010.

Explicit Model Checking

- model checking **real code**: C [1], Microcode [2], Simulink [3], LLVM [4]

1. M. Musuvathi and D. Park and A. Chou and D. Engler and D. Dill. CMC: A Pragmatic Approach to Model Checking Real Code. *OSR*, 36:75–88, 2002.

2. B. Schlich. *Model checking of Software for Microcontrollers*. PhD thesis, Aachen University, 2008.

3. J. Barnat, J. Beran, L. Brim, T. Kratochvíla, and P. Ročkai. Tool Chain to Support Automated Formal Verification of Avionics Simulink Designs. In *FMICS*, volume 7437 of *LNCS*, pages 78–92. Springer, 2012.

4. J. Barnat, L. Brim, and P. Ročkai. Towards LTL Model Checking of Unmodified Thread-Based C&C++ Programs. In *NFM*, volume 7226 of *LNCS*, pages 252–256. Springer, 2012.

Symbolic Model Checking

- standard representation (Binary Decision Diagram) is **exponential for integer multiplication** [1] → model checking with Binary Moment Diagram [2] and Boolean Expression Diagram [3]

1. R. Bryant. On the Complexity of VLSI Implementations and Graph Representations of Boolean Functions with Application to Integer Multiplication. *IEEE Trans. Comput.*, 40(2):205–213, 1991.

2. R. Bryant and Y.-A. Chen. Verification of Arithmetic Circuits with Binary Moment Diagrams. In *Proc. of DAC*, pages 535–541, 1995.

3. P. Williams, A. Biere, E. Clarke, and A. Gupta. Combining Decision Diagrams and SAT Procedures for Efficient Symbolic Model Checking. In *CAV*, volume 1855 of *LNCS*, pages 124–138. Springer, 2000.

Symbolic Model Checking

- smaller state space using **bounded** approach, allows to use state-of-the-art satisfiability procedures, such as SAT [1] or SMT (satisfiability modulo theory) [2]
1. A. Biere, A. Cimatti, E. Clarke, M. Fujita, and Y. Zhu. Symbolic Model Checking Using SAT Procedures instead of BDDs. In *Proc. of DAC*, pages 317–320, 1999.
 2. A. Armando, J. Mantovani, and L. Platania. Bounded Model Checking of Software Using SMT Solvers Instead of SAT Solvers. In *SPIN*, volume 3925 of *LNCS*, pages 146–162. Springer, 2006.

Explicit/Symbolic Combination

handle combination of control and data -flow

- multiple explicit states in one symbolic [1,2]
- explicit property, symbolic system description [3,4]

1. A. Cimatti, M. Roveri, and P. Bertoli. Searching Powerset Automata by Combining Explicit-State and Symbolic Model Checking. In *TACAS*, volume 2031 of *LNCS*, pages 313–327. Springer, 2001.
2. A. Duret-Lutz, K. Klai, D. Poitrenaud, and Y. Thierry-Mieg. Self-Loop Aggregation Product — A New Hybrid Approach to On-the-Fly LTL Model Checking. In *ATVA*, volume 6996 of *LNCS*, pages 336–350. Springer, 2011.
3. A. Biere, E. Clarke, and Y. Zhu. Multiple State and Single State Tableaux for Combining Local and Global Model Checking. In *Correct System Design*, volume 1710 of *LNCS*, pages 163-179. Springer, 1999.
4. R. Sebastiani, S. Tonetta, and M. Vardi. Symbolic Systems, Explicit Properties: On Hybrid Approaches for LTL Symbolic Model Checking. In *CAV*, volume 3576 of *LNCS*, pages 100–246. Springer, 2005.

Research Goals

- combine explicit and symbolic approaches to model checking
- explicit control, symbolic data
- investigate symbolic representation for software model checking
- propose new representation for better performance

the goal is **umbrellaed verification**

Achieved Results

- extended DiVinE with support for symbolic data representation (multi-states)
- proposed requirements on the symbolic representation for use in explicit model checking
- case study experiments: DVE, Simulink
- experiments show potential towards **umbrellaed verification**