Logical analysis of natural language

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PA153 Natural Language Processing

Outline

Logical analysis of natural language

- Sentence → logical formula
    - formal reasoning
    - interlingua for machine translation
    - precise expressions

- Which formalism?
    - (first order) predicate logic
    - modal logics
    - intensional logics (IL, Richard Montague)
    - transparent intensional logic (TIL)

Natural language $\rightarrow$ predicate logic

- What are formulas for
  - „Some prime numbers are even"
  - „Some odd numbers are even"
  - „Some smart people are lazy"
  - „No bachelor is married"
  - „No bachelor is rich"
  - „Miloš Zeman is the president of CR."
  - „Karel counts $5 + 7$"

- What is wrong?

Natural language $\rightarrow$ predicate logic

- What are formulas for

  - „Some prime numbers are even"
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- What is wrong?

  - different types of truth
  - granularity of the description is insufficient

Natural language $\rightarrow$ predicate logic

Karel counts $5 + 7$
$5 + 7 = 12$

Karel counts 12

Miloš Zeman is the president of CR.
Karel Schwarzenberg wanted to become the president of CR.

Karel Schwarzenberg wanted to become Miloš Zeman.

It is not true that the king of France is bald-headed

The king of France has some hair on his head.

Natural language → predicate logic

- Predicate logic can be used for natural language analysis
    - some applications are doing it
    - but not in all cases
    - we need to be aware of the limits
    - work-arounds are possible but may be complicated

- Advantages of predicate logic
    - it is simple
    - it is well explored
    - inference machine exists

What is the meaning of an expression?

Frege's model of semantics
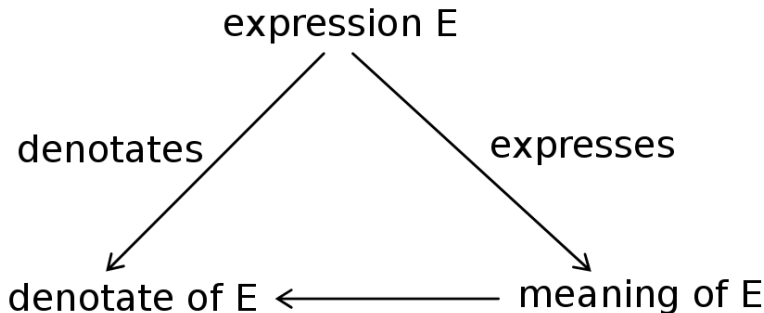
Conception of possible worlds

- A possible world
    - a set of non-contradictory formulas about the universe
    - the current world is one of the possible worlds

- Empirical truth
    - the truth of a formula depends on the particular world
    - meaning is always world-independent

- Intensional logics
    - intensions (world-independent)
    - extensions (denotates, objects in a particular world)

Transparent intensional logic

- Pavel Tichý, Pavel Materna
- Procedural logic
    - possible worlds + possible times
    - meaning is a emphconstruction, i.e. abstact procedure (algorithm) which takes the current world and time and outputs the denotate (the particular object)
    - coded as lambda function
- Typed logic
    - o – true, false
    - ι – set of individuums
    - τ – set of real numbers (or time moments)
    - ω – set of possible worlds
    - $((o\tau)\omega)$ – proposition
    - $(((o\iota)\tau)\omega)$ – property $((o\iota)_{\tau\omega})$

Transparent intensional logic – examples

Miloš Zeman je prezidentem CR.

$\lambda w \lambda t [= \text{Miloš\_Zeman President\_CR}_{wt}]$

type $o_{\tau\omega}$ Miloš_Zeman$/\iota$ President_CR$/\iota_{\tau\omega}$ $=/(o\iota\iota)$

Schwarzenberg wanted to become CR.

$\lambda w \lambda t [\text{want\_to\_become}_{wt} \text{ Schwarzenberg President\_CR}]$

$o_{\tau\omega}$ Schwarzenberg$/\iota$ President_CR$/\iota_{\tau\omega}$ want_to_become$/(o\iota\iota_{\tau\omega})$

Transparent intensional logic – examples

5 + 7

$[+ 5\ 7\ ]$

type τ $5, 7/\tau$ $+/(\tau\tau\tau)$

Karel counts 5 + 7.

$\lambda w \lambda t [\ \text{count}_{wt}\quad \text{Karel}\quad {}^0[+ 5\ 7\ ]\ ]$

type $o_{\tau\omega}$ ${}^0[+\ 5\ 7]/{}^*1$ $\text{count}/(o\iota*_1)_{wt}$ $Karel/\iota$

Normal translation algorithm

- Automatic conversion of sentences into TIL constructions
    - doc. Aleš Horák
    - morphological analysis
    - syntactic analysis
    - conversion from tree to TIL formula
    - type check
    - output of all the layers is ambiguous
    - implementation within the Synt parser, currently experiments with other parsers (SET)

- Further requirements
    - lexicon of types ("snow" vs. "give" – exploitation of valency lexicons)
    - rules for type control

Transparent intensional logic – pros and cons

- Advantages
    - correct and very precise analysis
    - makes general correct reasoning possible

- Disadvantages
    - very abstract and complex
    - not really wide-spread
    - experts often do not agree on correct analysis

Transparentní intenzionální logika na FI

- doc. Aleš Horák
- prof. Marie Duží

    - subjects Introduction to Transparent Intensional Logic

- Small corpus of correct constructions for Czech

    - https://corpora.fi.muni.cz/til

- Semantic network of constructions

    - as a knowledge base for automatic reasoning