Formal Biochemical Space with Semantics in Kappa and BNGL

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Background and Motivation

Comprehensive Modelling Platform (CMP)



Background and Motivation

Biochemical Space in the context of CMP



- need for easy-to-understand but yet formal description of biological processes
- tackle the complexity combinatorial explosion

Annotation Standards

Connection to Bioinformatics



Biochemical Space

Eliminating the Gap Between Biology and Math



- biophysics employs a lot of indirect approximation in models
- combining rule-based approach with reaction-based approach allows compact mechanistic description
- mapping the models to such a description allows better and faster understanding



Abstraction from structural details



- Threonine residue phosphorylated protein
- Both residues phosphorylated protein

BCS abstraction

mixture → order not important
 84 different deviations





Biochemical Space Language

Key Features

- \bullet stoichiometry \rightarrow enumerated shortened forms
- $\bullet~\text{states} \rightarrow \text{encoding different forms of an entity}$
- composition
 - $\bullet~$ full \rightarrow complexation, coexistence in a solution
 - $\bullet \ \ \mathbf{partial} \rightarrow \mathsf{inner} \ \mathsf{structure} \ \mathsf{of} \ \mathsf{interest}$
- locations \rightarrow spatial organisation
- variables \rightarrow wildcards in definitions



Differences from Other Formalisms

Bio**C**hemical **S**pace **L**anguage is a rule-based language which has:

- no binding sites \rightarrow details of complexes formation abstracted out
 - abstract from bonds
- annotation purpose → specify what interacts with what without details of the interaction
- no quantitative data → only qualitative dynamics



Entity Declaration by Example

ENTITY ID. KaiC ENTITY NAME: circadian clock protein kinase KaiC STATES: LOCATIONS: cyt **CLASSIFICATION:** enzyme **DESCRIPTION**: Monomer component representing a core component of the circadian clock system LINKS: uniprot::Q79PF4, kegg::K08482, ncbi::AAM82686 **ORGANISM**: SYNPCC7942{Synpcc7942_1216} NOTES: COMPOSITION: S | T



Abstract Entity Specification

Class

KaiC.KaiC::cyt

Specialized class

Object

$\mathsf{KaiC}(\mathsf{S}\{\mathsf{u}\}|\mathsf{T}\{\mathsf{u}\}).\mathsf{KaiC}(\mathsf{S}\{\mathsf{u}\}|\mathsf{T}\{\mathsf{p}\})){::}\mathsf{cyt}$



Entity Identifier





Composition

Full composition \rightarrow structure of a complex

- KaiBC == KaiC.KaiB
- KaiC6 == KaiC.KaiC.KaiC.KaiC.KaiC.KaiC

 $\label{eq:partial composition} \textbf{Partial composition} \rightarrow \textsf{inner structure of an} \\ \textsf{entity} \\$

- KaiC(S{u}|T{p})
- cytb6f(f{-}|bl{n}|bhc{2-})
- $ps2(qb{2-}|qa{n}|chl{*}|p680{+}|pheo{-}|oec{4+}|yz{n})$

Nested Entity Identifier

• another way to specify a class entity



*compartment specification is obligatory

Examples of Entity Identifiers

- KaiC6::cyt
- KaiA.KaiA::cyt
- ATP::cyt
- CO3{2-}::liq
- KaiC(S{u}|T{p})::cyt
- CO_2 ::**?X** ; **X** = {lum, cell, liq, bub, pps, cyt}

Reaction

 $\begin{array}{rl} \mathsf{KaiC}(\mathsf{S}\{\mathsf{u}\}|\mathsf{T}\{\mathsf{u}\})::\mathsf{cyt} + \mathsf{KaiC}(\mathsf{S}\{\mathsf{p}\}|\mathsf{T}\{\mathsf{p}\})::\mathsf{cyt} \Rightarrow \mathsf{KaiC}(\mathsf{S}\{\mathsf{u}\}|\mathsf{T}\{\mathsf{u}\}).\mathsf{KaiC}(\mathsf{S}\{\mathsf{p}\}|\mathsf{T}\{\mathsf{p}\})::\mathsf{cyt} \\ & \text{object} & + & \text{object} \Rightarrow & \text{object} \end{array}$

Rule

$$\begin{array}{lll} \mathsf{KaiC::cyt} + \mathsf{KaiC::cyt} \Rightarrow \mathsf{KaiC}.\mathsf{KaiC::cyt} \\ \mathsf{class} &+ \mathsf{class} \Rightarrow \mathsf{class} \end{array}$$



Stringency of Entity Identifiers

• consider the rule:

 $\mathsf{S}\{\mathsf{p}\}{::}\mathsf{KaiC}{::}\mathsf{KaiC}\mathsf{6}{::}\mathsf{cyt} \Rightarrow \mathsf{S}\{\mathsf{u}\}{::}\mathsf{KaiC}{::}\mathsf{KaiC}\mathsf{6}{::}\mathsf{cyt}$

- both sides identify the same object in location
 cyt
- it is a complex **KaiC6** (assume it has a given well-defined full composition)
- which contains at least one KaiC protein
- whose partial composition contains **S**{**p**}



Translation of Entities to Kappa

Assume every entity composition is lexicographically ordered.

- **agent** ← entity name
- **agent name** ← entity name suffixed with a location
- interface ← partial composition (at least two internal states are required)
- site \leftarrow each member entity of partial composition
- site name ← name of a member entity
- **internal state** ← state of the entity
- **binding state** ← assign a generic structure, i.e., linear



BCSL Rules Expressed in Kappa

- left/right side S of a BCS rule is set of entities
 ⇒ expressed as a set E of agents in Kappa
- since each entity in S is lexicographically ordered, rules are ensured to be unique (up-to structural equivalence of reaction complexes),
- for full compositions ('.' operator) a labeling by bound sites is created (concretisation)
 ⇒ abstract meaning of coexistence is lost



BCS: 2 KaiC(S{p}) \Rightarrow KaiC(S{p}).KaiC(S{p}) **Kappa :** KaiC(S_p), KaiC(S_p) \rightarrow KaiC(S¹_p), KaiC(S¹_p)

BCS: $S\{p\}$::KaiC::KaiC6::cyt \Rightarrow $S\{u\}$::KaiC::KaiC6::cyt **Kappa :** KaiC(S¹_p), KaiC(S¹,T²), KaiC(S²,T³), KaiC(S³,T⁴), KaiC(S⁴,T⁵), KaiC(S⁵) \rightarrow

 $\rightarrow \mathsf{KaiC}(\mathsf{S}^1_{\mathit{u}}),\,\mathsf{KaiC}(\mathsf{S}^1,\mathsf{T}^2),\,\mathsf{KaiC}(\mathsf{S}^2,\mathsf{T}^3),\,\mathsf{KaiC}(\mathsf{S}^3,\mathsf{T}^4),\,\mathsf{KaiC}(\mathsf{S}^4,\mathsf{T}^5),\,\mathsf{KaiC}(\mathsf{S}^5)$



Case Study: Synechocystis

Metabolism

- over 1000 entities (objects) and over 500 rules
- entities concrete since there is no combinatorial explosion (rules are reactions)
- two mathematical models are mapped

Photosynthesis and Respiration

- over 100 entity classes and over 50 rules
- compaction is significant mainly for reactions
- one (lumped) mathematical model is mapped

Cyanobacterial circadian clock

- 18 class entities interacting in 18 rules
- creates over 500 object entities
- two (lumped) mathematical models are mapped



Cyanobacteria Circadian Clock BCS



Conclusions

- in the paper: formal syntax and semantics of BCS
- implementation: operational semantics in BNGL (then translated to DiVinE)
- currently we work on direct SOS to employ CTL model checking directly on BCS
- it will allow to study equivalences and reduction directly at the syntactic level of BCS





Thank You for your attention.



The Project Team

