

Machine Translation

Machine Translation (MT) is the task of translating a sentence x from one language (the **source language**) to a sentence y in another language (the **target language**).

$x:$ *L'homme est né libre, et partout il est dans les fers*



$y:$ *Man is born free, but everywhere he is in chains*

– Rousseau

The early history of MT: 1950s

- Machine translation research began in the **early 1950s** on machines less powerful than high school calculators (before term “A.I.” coined!)
- Concurrent with foundational work on automata, formal languages, probabilities, and information theory
- MT heavily funded by military, but basically just simple rule-based systems doing word substitution
- Human language is more complicated than that, and varies more across languages!
- Little understanding of natural language syntax, semantics, pragmatics
- Problem soon appeared intractable

1 minute video showing 1954 MT:

<https://youtu.be/K-HfpsHPmvw>

The early history of MT: 1950s



1990s-2010s: Statistical Machine Translation

- Core idea: Learn a **probabilistic model** from **data**
- Suppose we're translating French \rightarrow English.
- We want to find **best English sentence** y , given **French sentence** x

$$\operatorname{argmax}_y P(y|x)$$

- Use Bayes Rule to break this down into **two components** to be learned separately:

$$= \operatorname{argmax}_y \underbrace{P(x|y)} \underbrace{P(y)}$$

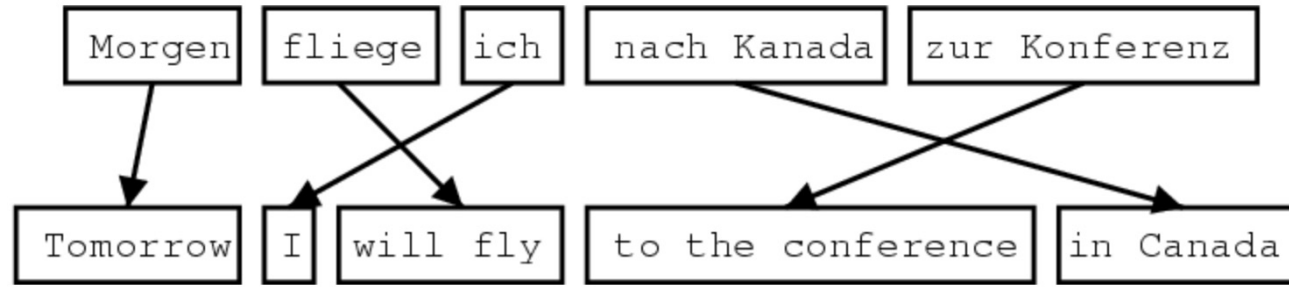
Translation Model

Models how words and phrases should be translated (*fidelity*).
Learned from parallel data.

Language Model

Models how to write good English (*fluency*).
Learned from monolingual data.

What happens in translation isn't trivial to model!



1519年600名西班牙人在墨西哥登陆，去征服**几百万人口**的**阿兹特克帝国**，初次交锋他们损兵**三分之二**。

In 1519, six hundred Spaniards landed in Mexico to conquer **the Aztec Empire** **with a population of a few million**. They lost two thirds of their soldiers in the first clash.

translate.google.com (2009): 1519 600 Spaniards landed in Mexico, **millions of people to conquer the Aztec empire**, the first two-thirds of soldiers against their loss.

translate.google.com (2013): 1519 600 Spaniards landed in Mexico **to conquer the Aztec empire, hundreds of millions of people**, the initial confrontation loss of soldiers two-thirds.

translate.google.com (2015): 1519 600 Spaniards landed in Mexico, **millions of people to conquer the Aztec empire**, the first two-thirds of the loss of soldiers they clash.

1990s–2010s: Statistical Machine Translation

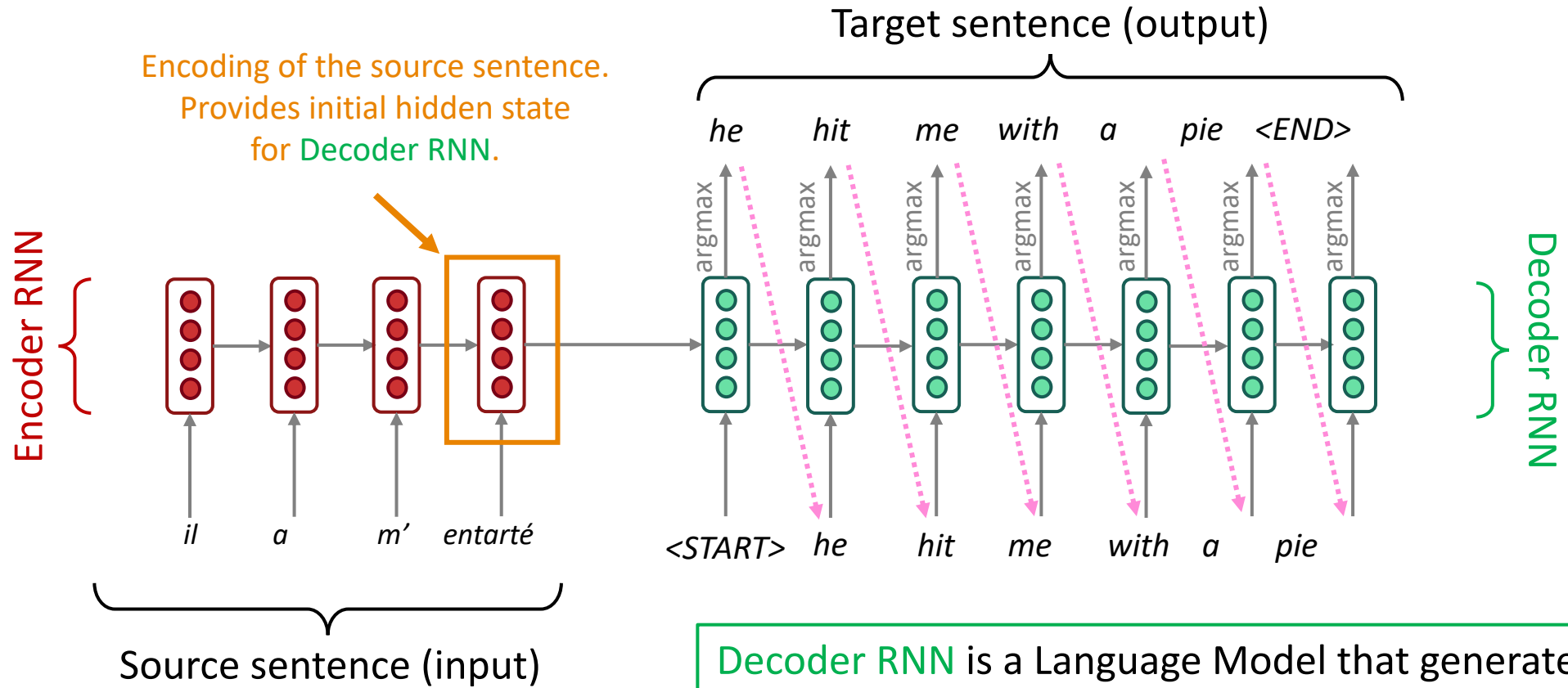
- SMT was a **huge research field**
- The best systems were **extremely complex**
 - Hundreds of important details
- Systems had many **separately-designed subcomponents**
 - Lots of **feature engineering**
 - Need to design features to capture particular language phenomena
 - Required compiling and maintaining **extra resources**
 - Like tables of equivalent phrases
 - Lots of **human effort** to maintain
 - Repeated effort for each language pair!

What is Neural Machine Translation?

- **Neural Machine Translation (NMT)** is a way to do Machine Translation with a *single end-to-end neural network*
- The neural network architecture is called a **sequence-to-sequence** model (aka **seq2seq**) and it involves *two RNNs*

Neural Machine Translation (NMT)

The sequence-to-sequence model



Encoder RNN produces an **encoding** of the source sentence.

Decoder RNN is a Language Model that generates target sentence, *conditioned on encoding*.

Note: This diagram shows **test time** behavior: decoder output is fed in as next step's input

Sequence-to-sequence is versatile!

- The general notion here is an **encoder-decoder** model
 - One neural network takes input and produces a neural representation
 - Another network produces output based on that neural representation
 - If the input and output are sequences, we call it a seq2seq model
- Sequence-to-sequence is useful for *more than just MT*
- Many NLP tasks can be phrased as sequence-to-sequence:
 - **Summarization** (long text → short text)
 - **Dialogue** (previous utterances → next utterance)
 - **Parsing** (input text → output parse as sequence)
 - **Code generation** (natural language → Python code)

Neural Machine Translation (NMT)

- The **sequence-to-sequence** model is an example of a **Conditional Language Model**
 - **Language Model** because the decoder is predicting the next word of the target sentence y
 - **Conditional** because its predictions are *also* conditioned on the source sentence x

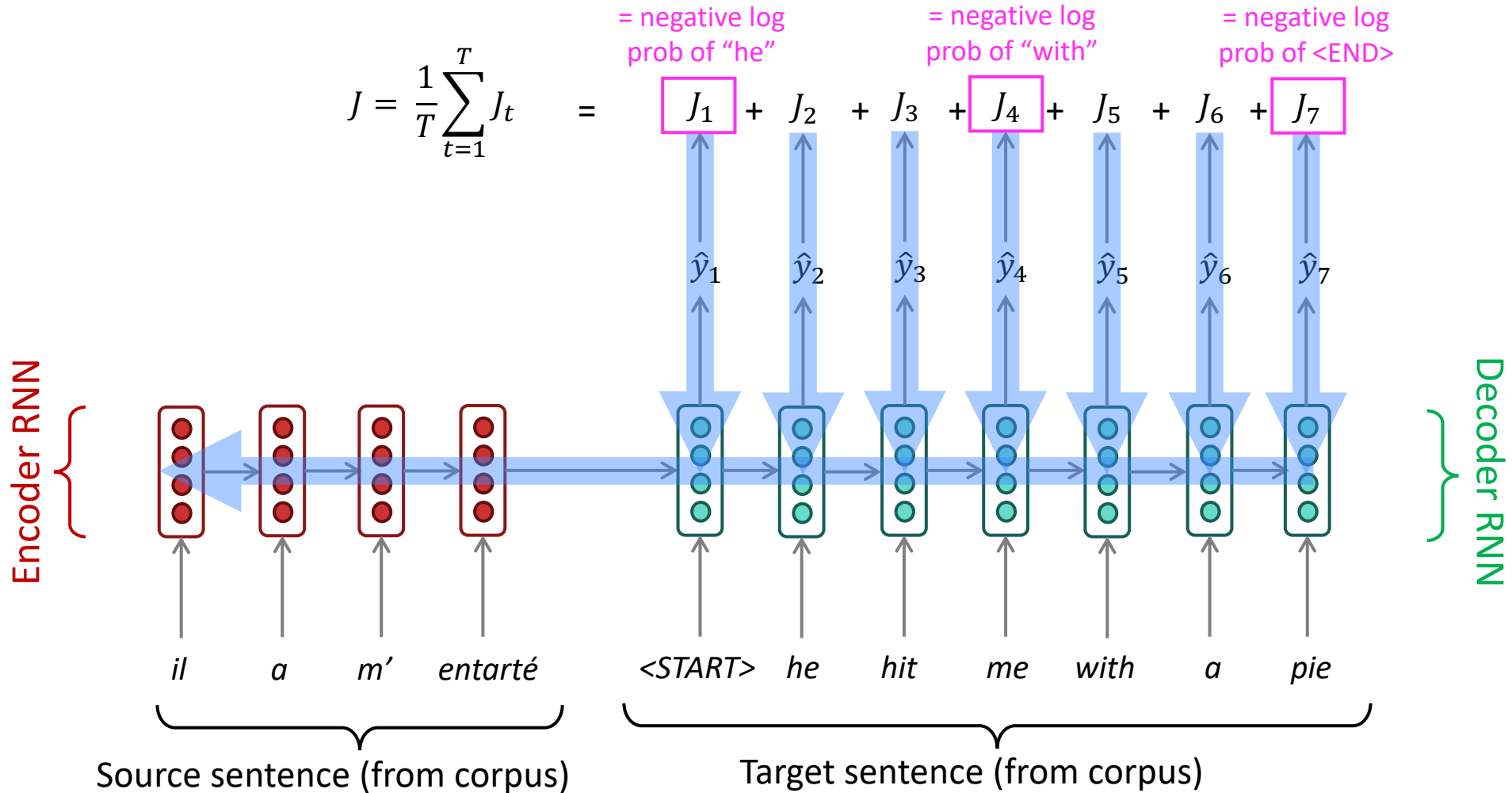
- NMT directly calculates $P(y|x)$:

$$P(y|x) = P(y_1|x) P(y_2|y_1, x) P(y_3|y_1, y_2, x) \dots P(y_T|y_1, \dots, y_{T-1}, x)$$

Probability of next target word, given
target words so far and source sentence x

- **Question:** How to train an NMT system?
- **(Easy) Answer:** Get a big parallel corpus...
 - But there is now exciting work on “unsupervised NMT”, data augmentation, etc.

Training a Neural Machine Translation system

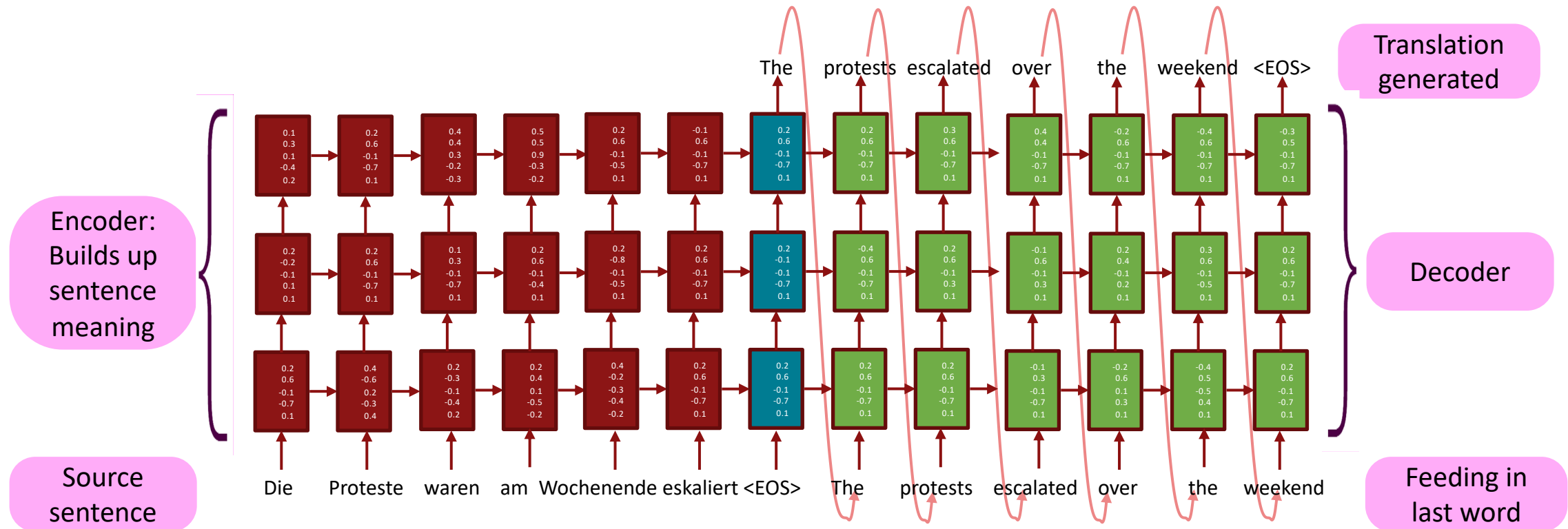


Seq2seq is optimized as a **single system**. Backpropagation operates "end-to-end".

Multi-layer deep encoder-decoder machine translation net

[Sutskever et al. 2014; Luong et al. 2015]

The hidden states from RNN layer i are the inputs to RNN layer $i+1$



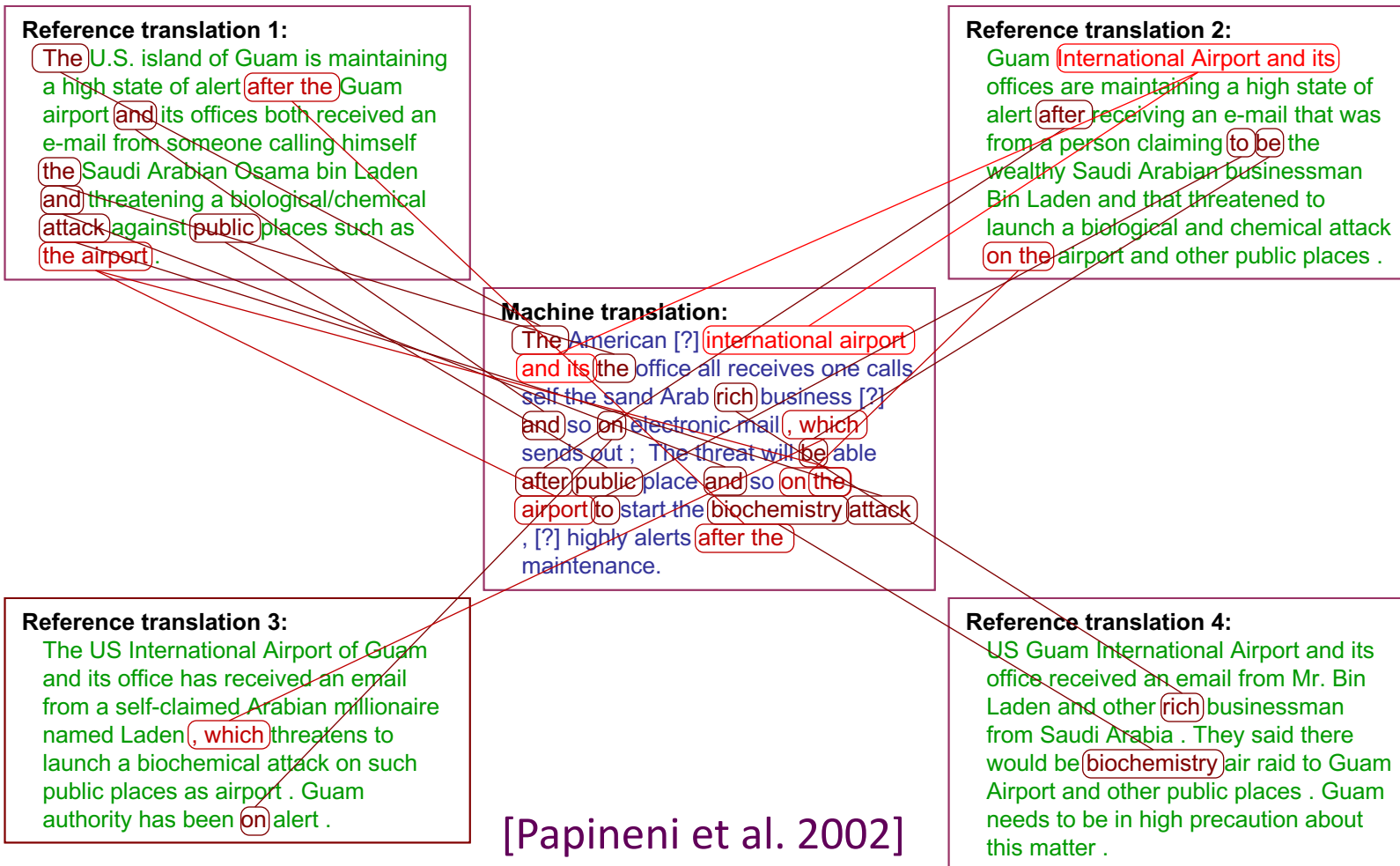
How do we evaluate Machine Translation?

BLEU (Bilingual Evaluation Understudy)

You'll see BLEU in detail
in Assignment 4!

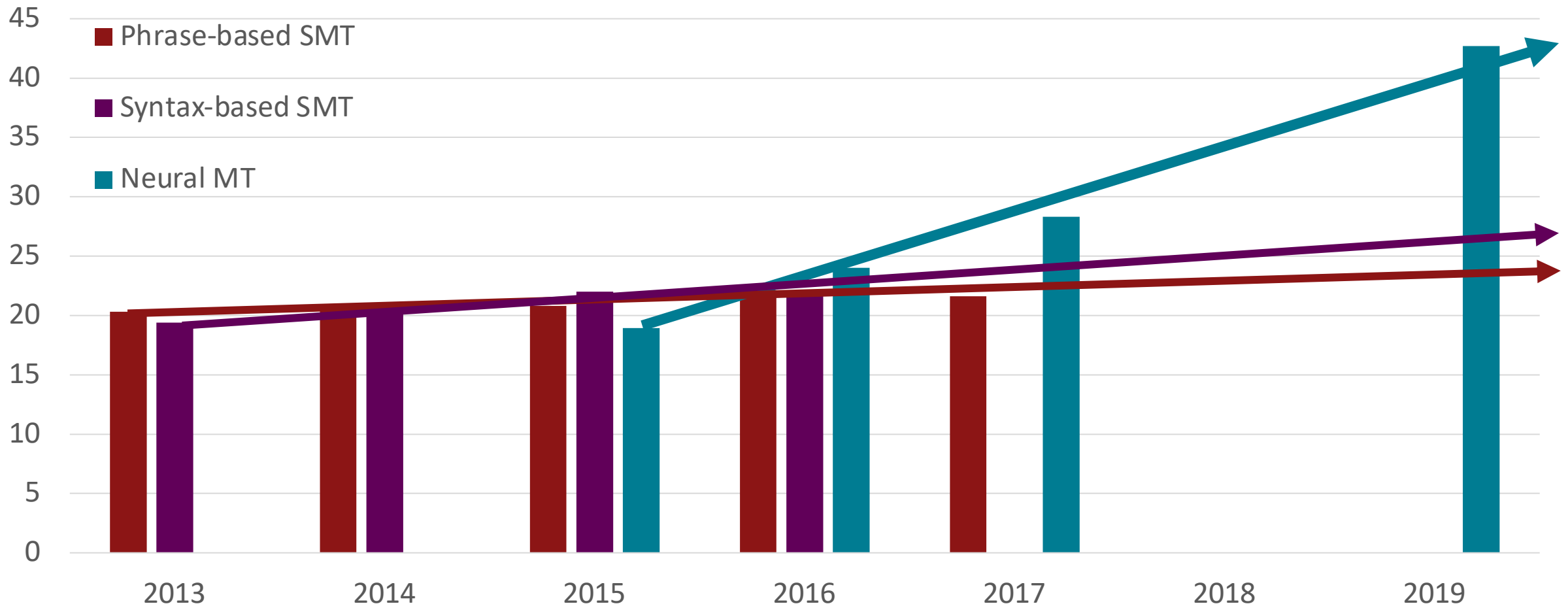
- BLEU compares the machine-written translation to one or several human-written translation(s), and computes a **similarity score** based on:
 - ***n*-gram precision** (usually for 1, 2, 3 and 4-grams)
 - Plus a penalty for too-short system translations
- BLEU is **useful** but **imperfect**
 - There are many valid ways to translate a sentence
 - So a **good** translation can get a **poor** BLEU score because it has low *n*-gram overlap with the human translation 😞

BLEU score against 4 reference translations



MT progress over time

[Edinburgh En-De WMT newstest2013 Cased BLEU; NMT 2015 from U. Montréal; NMT 2019 FAIR on newstest2019]



Sources: http://www.meta-net.eu/events/meta-forum-2016/slides/09_sennrich.pdf & <http://matrix.statmt.org/>

Advantages of NMT

Compared to SMT, NMT has many advantages:

- Better performance
 - More fluent
 - Better use of context
 - Better use of phrase similarities
- A single neural network to be optimized end-to-end
 - No subcomponents to be individually optimized
- Requires much less human engineering effort
 - No feature engineering
 - Same method for all language pairs

Disadvantages of NMT?

Compared to SMT:

- NMT is **less interpretable**
 - Hard to debug
- NMT is **difficult to control**
 - For example, can't easily specify rules or guidelines for translation
 - Safety concerns!

NMT: the first big success story of NLP Deep Learning

Neural Machine Translation went from a **fringe research attempt** in **2014** to the **leading standard method** in **2016**

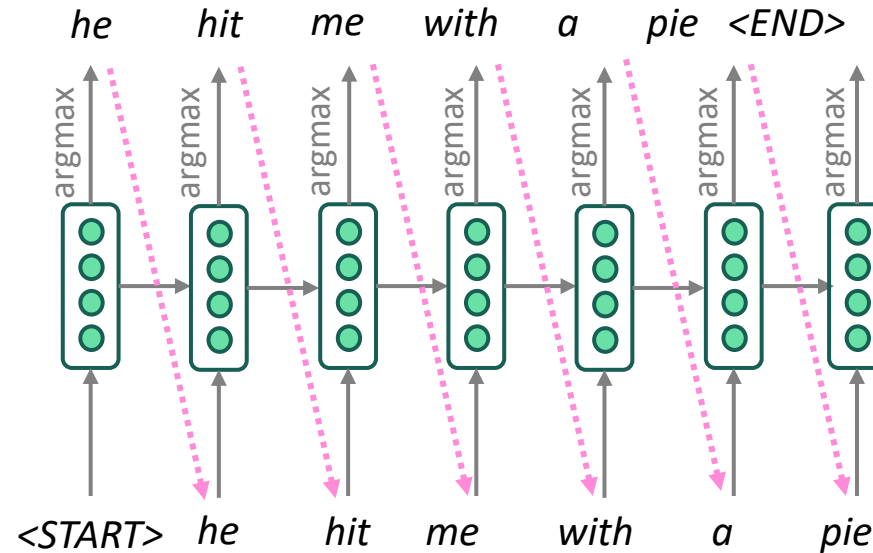
- **2014**: First seq2seq paper published
- **2016**: Google Translate switches from SMT to NMT – and by 2018 everyone has



- **This is amazing!**
 - **SMT** systems, built by **hundreds** of engineers over many **years**, outperformed by NMT systems trained by a **small group** of engineers in a few **months**

Decoding: Greedy decoding

- We saw how to generate (or “decode”) the target sentence by taking argmax on each step of the decoder



- This is **greedy decoding** (take most probable word on each step)

Problems with greedy decoding

- Greedy decoding has no way to undo decisions!
 - Input: *il a m'entarté* *(he hit me with a pie)*
 - → *he* _____
 - → *he hit* _____
 - → *he hit a* _____ *(whoops! no going back now...)*
- How to fix this?

Exhaustive search decoding

- Ideally, we want to find a (length T) translation y that maximizes

$$\begin{aligned} P(y|x) &= P(y_1|x) P(y_2|y_1, x) P(y_3|y_1, y_2, x) \dots, P(y_T|y_1, \dots, y_{T-1}, x) \\ &= \prod_{t=1}^T P(y_t|y_1, \dots, y_{t-1}, x) \end{aligned}$$

- We could try computing **all possible sequences** y
 - This means that on each step t of the decoder, we're tracking V^t possible partial translations, where V is vocab size
 - This $O(V^T)$ complexity is **far too expensive!**

Beam search decoding

- Core idea: On each step of decoder, keep track of the k most probable partial translations (which we call *hypotheses*)
 - k is the *beam size* (in practice around 5 to 10, in NMT)

- A hypothesis y_1, \dots, y_t has a *score* which is its log probability:

$$\text{score}(y_1, \dots, y_t) = \log P_{\text{LM}}(y_1, \dots, y_t | x) = \sum_{i=1}^t \log P_{\text{LM}}(y_i | y_1, \dots, y_{i-1}, x)$$

- Scores are all negative, and higher score is better
 - We search for high-scoring hypotheses, tracking top k on each step
- Beam search is *not guaranteed* to find optimal solution
- But *much more efficient* than exhaustive search!

Beam search decoding: example

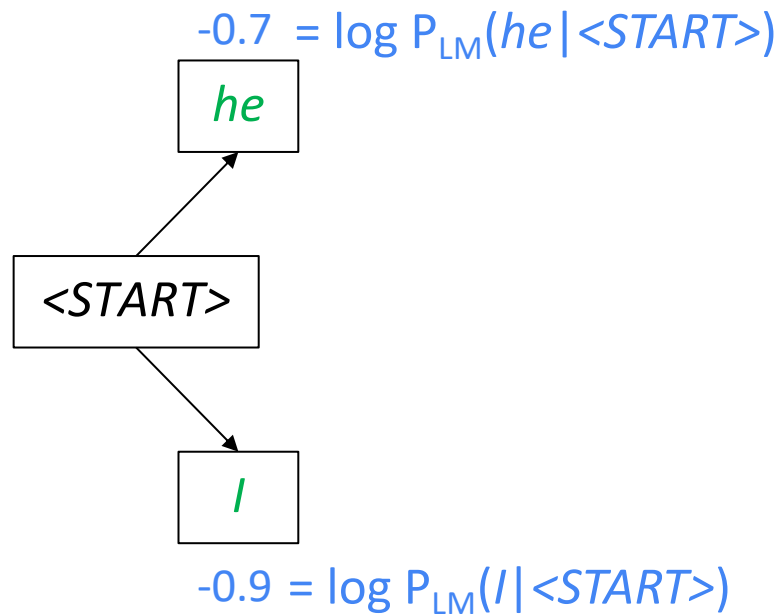
Beam size = $k = 2$. Blue numbers = $\text{score}(y_1, \dots, y_t) = \sum_{i=1}^t \log P_{\text{LM}}(y_i | y_1, \dots, y_{i-1}, x)$

<START>

Calculate prob
dist of next word

Beam search decoding: example

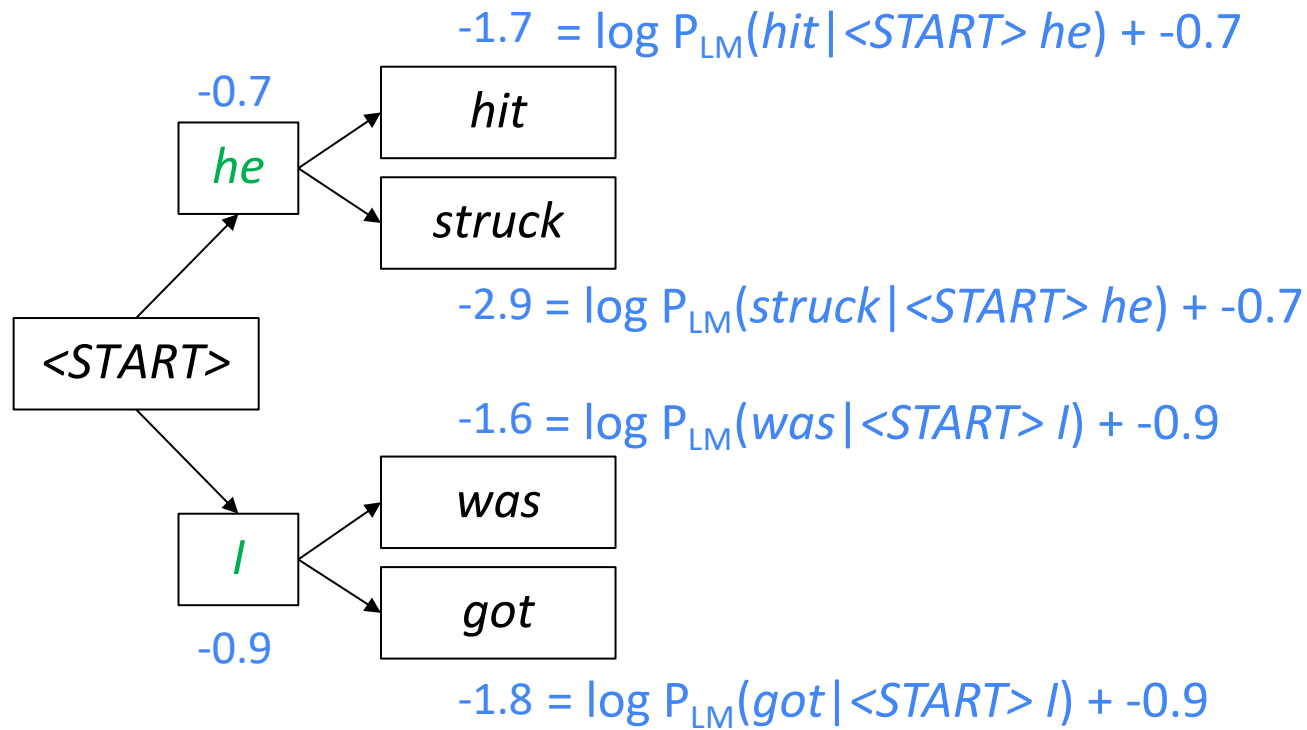
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Take top k words
and compute scores

Beam search decoding: example

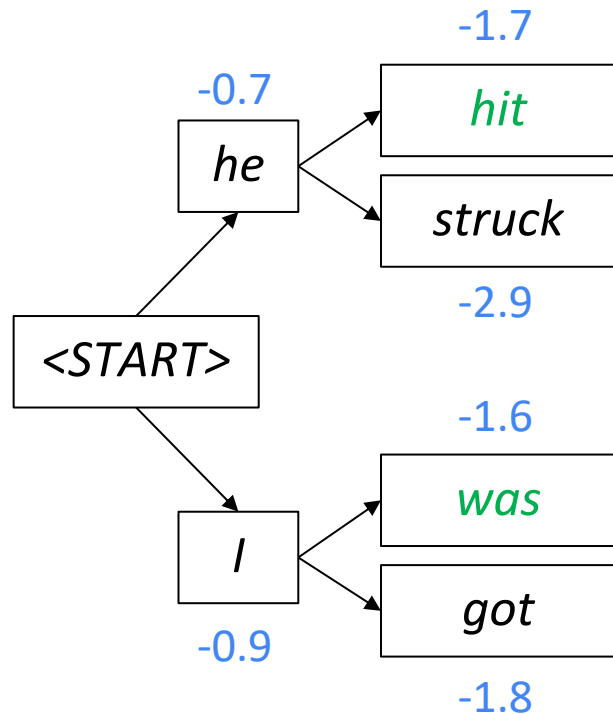
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For each of the k hypotheses, find top k next words and calculate scores

Beam search decoding: example

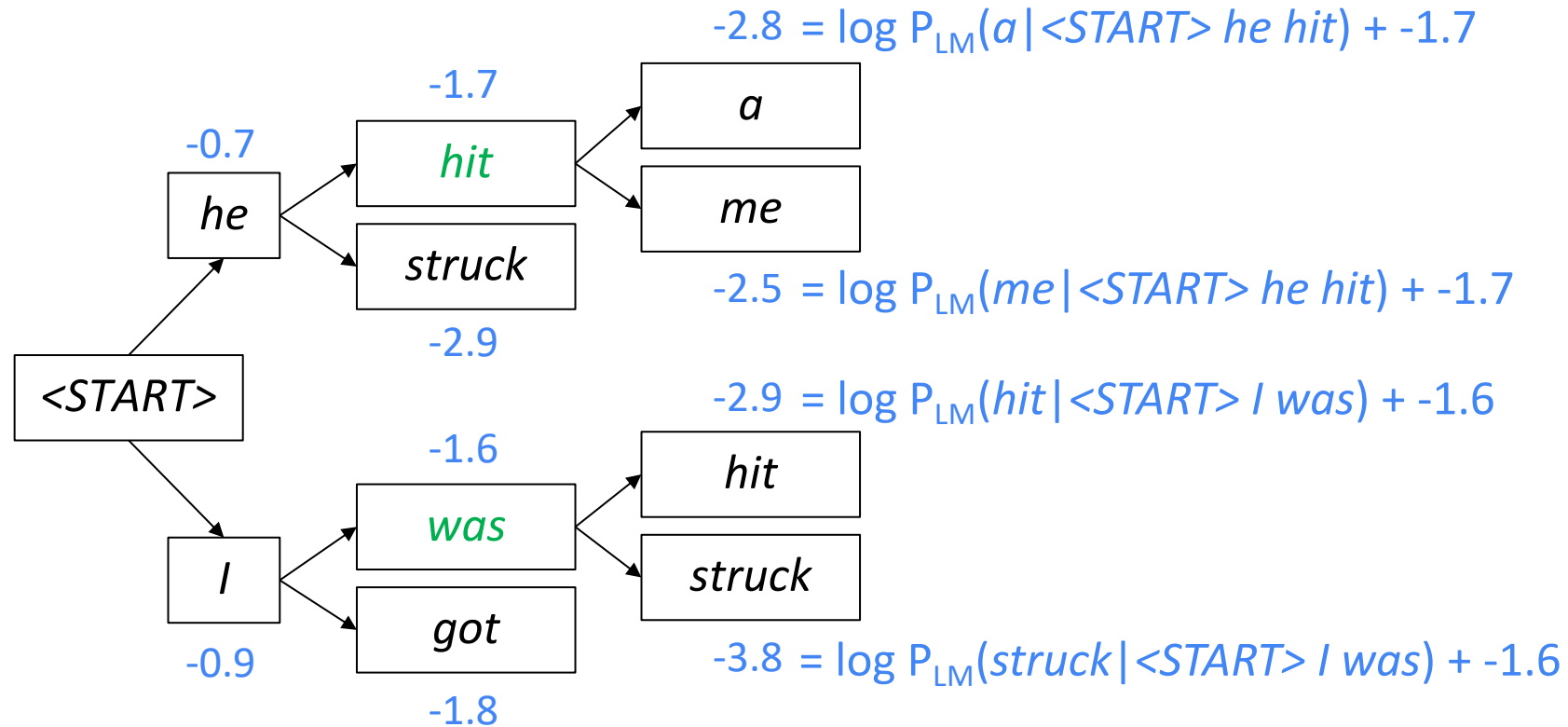
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Of these k^2 hypotheses,
just keep k with highest scores

Beam search decoding: example

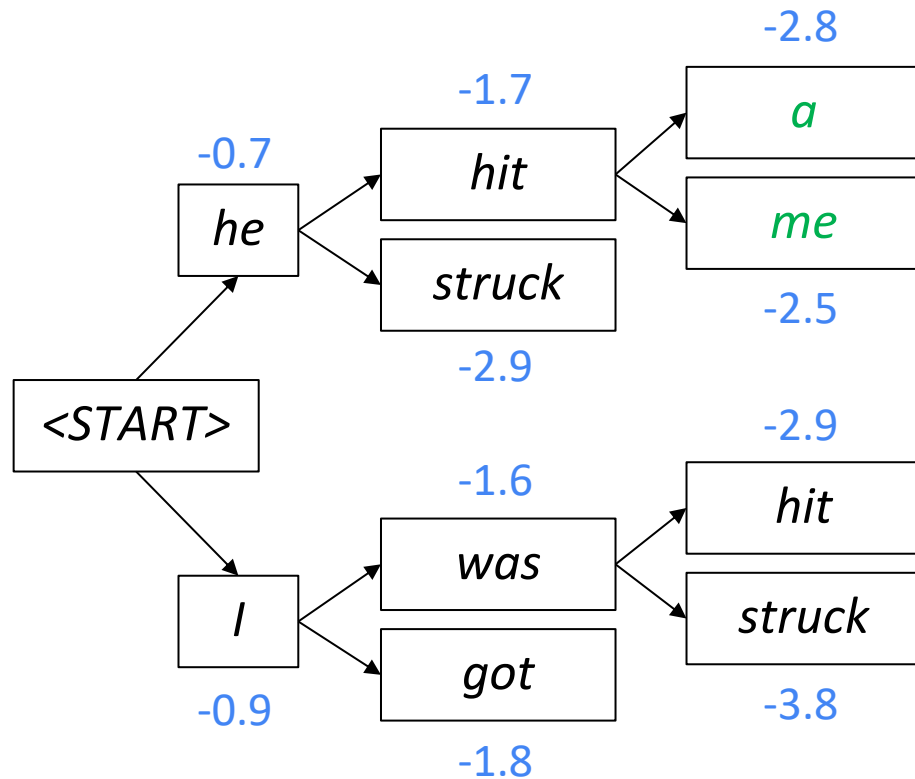
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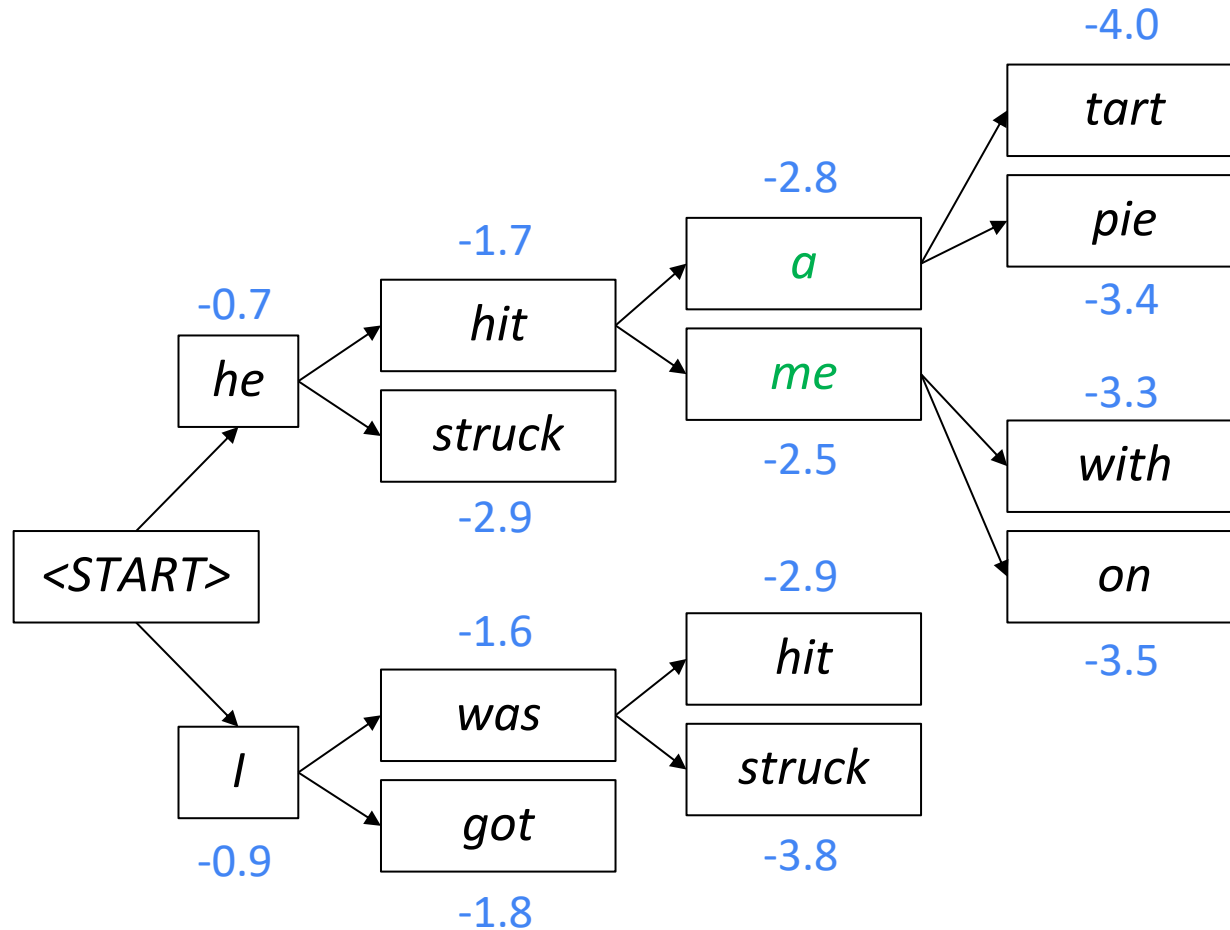
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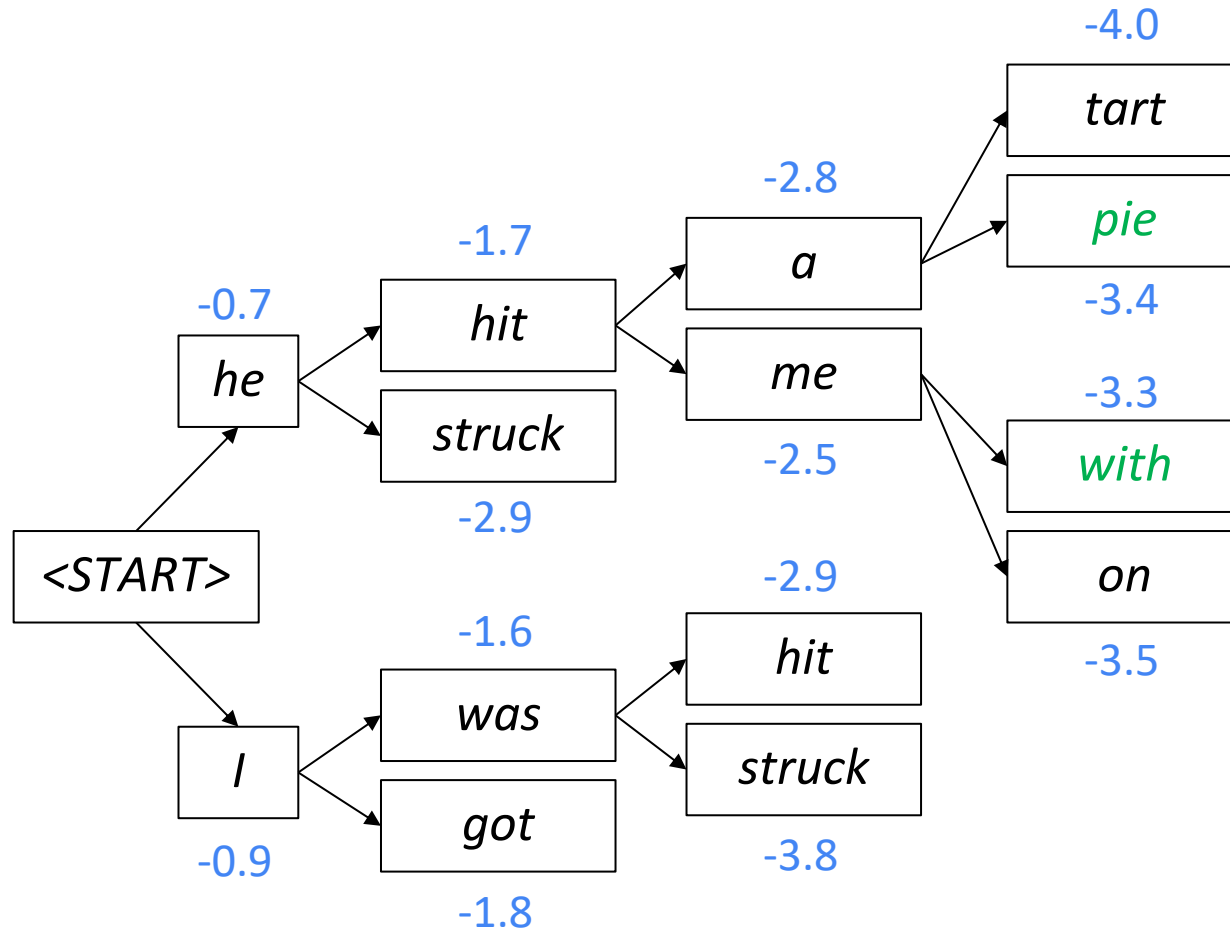
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Beam search decoding: example

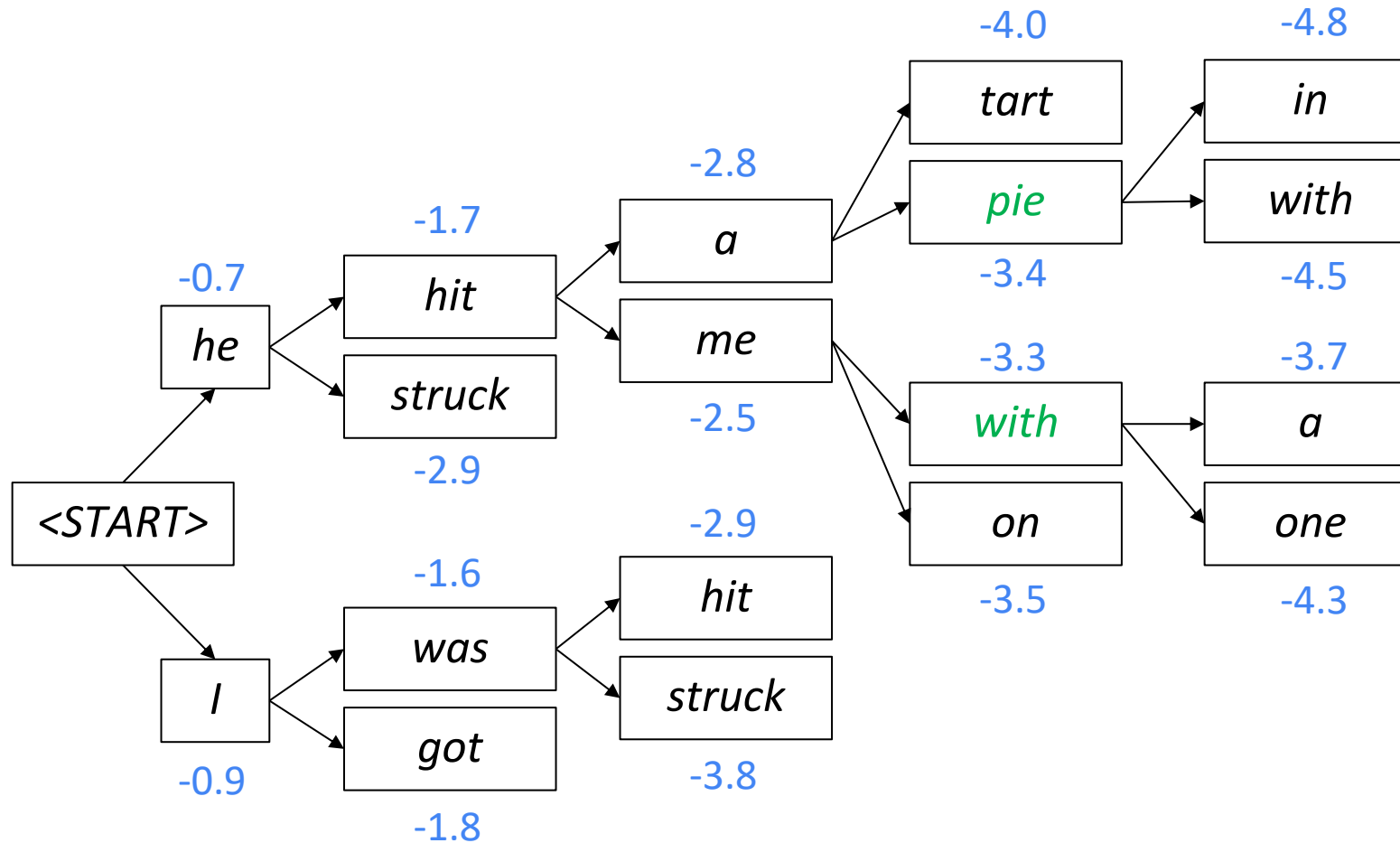
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Beam search decoding: example

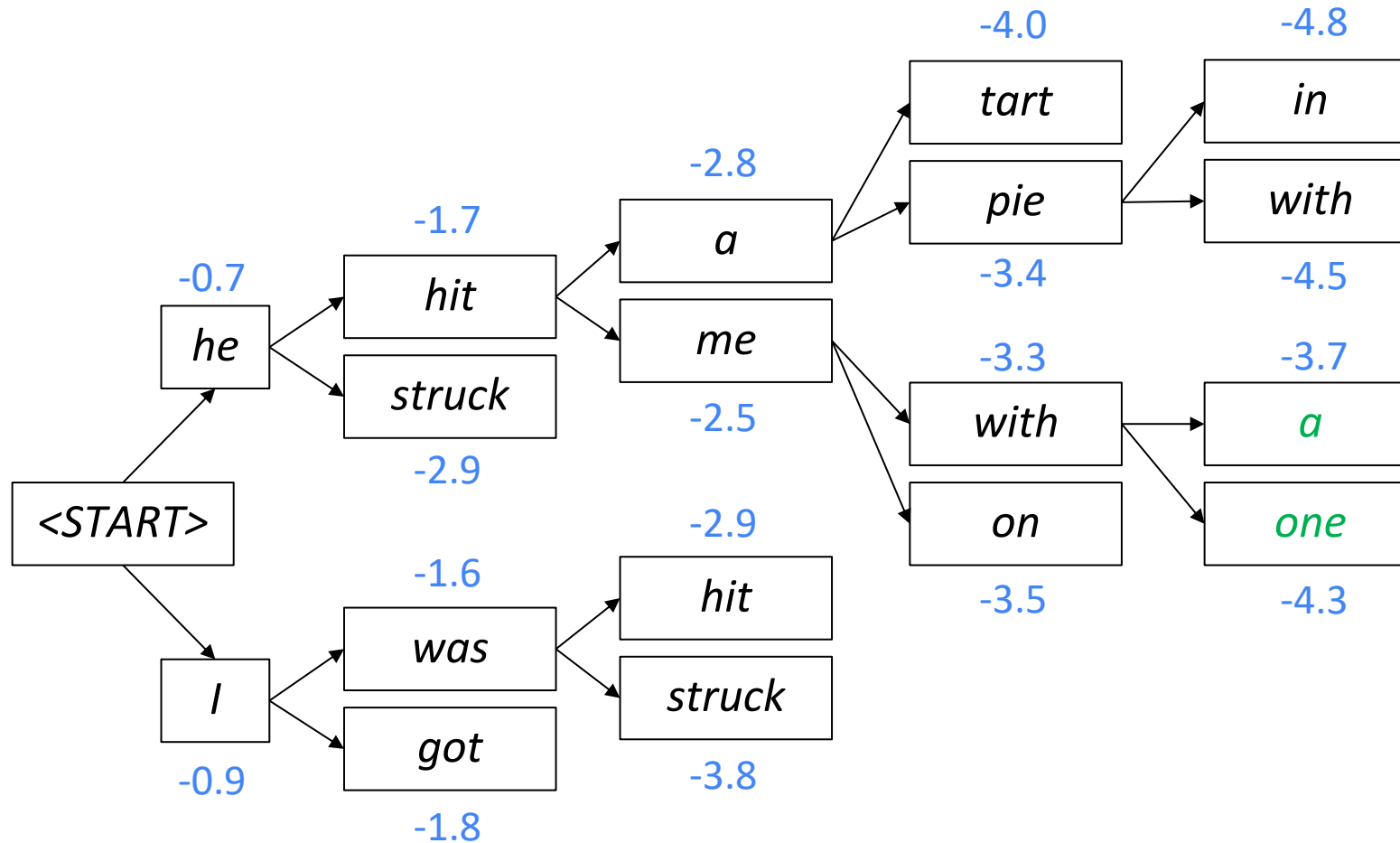
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Beam search decoding: example

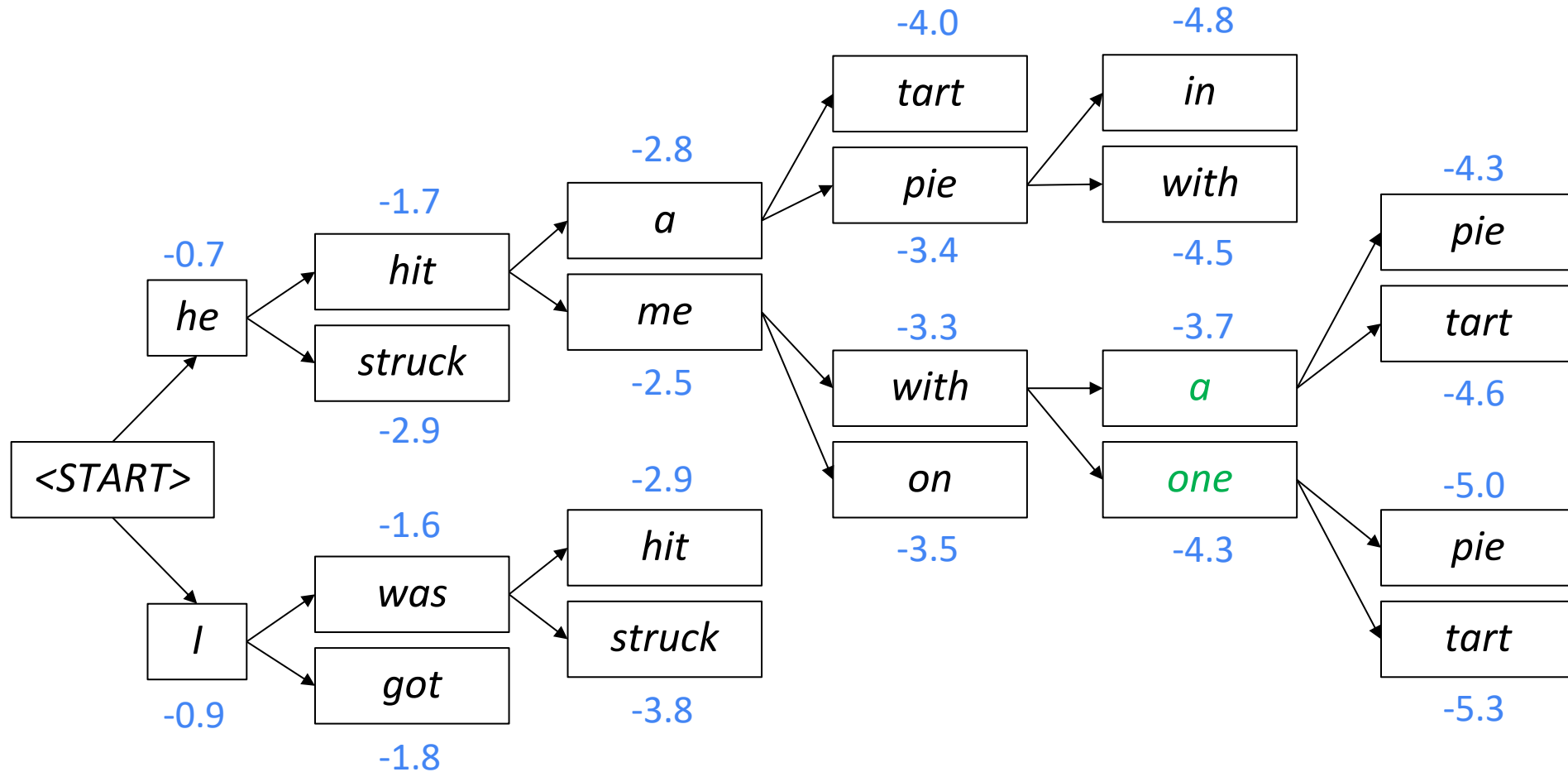
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Beam search decoding: example

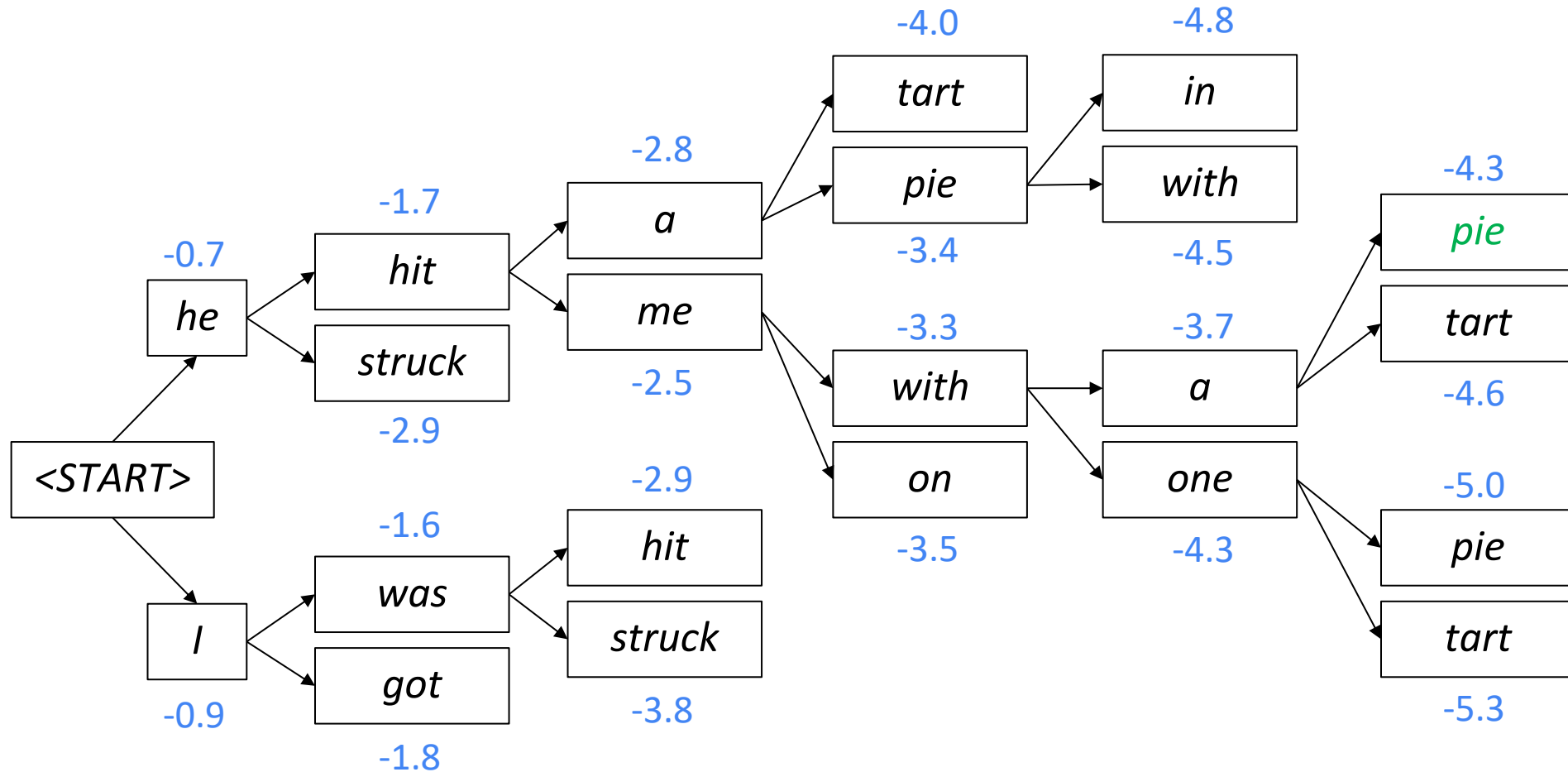
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For each of the k hypotheses, find top k next words and calculate scores

Beam search decoding: example

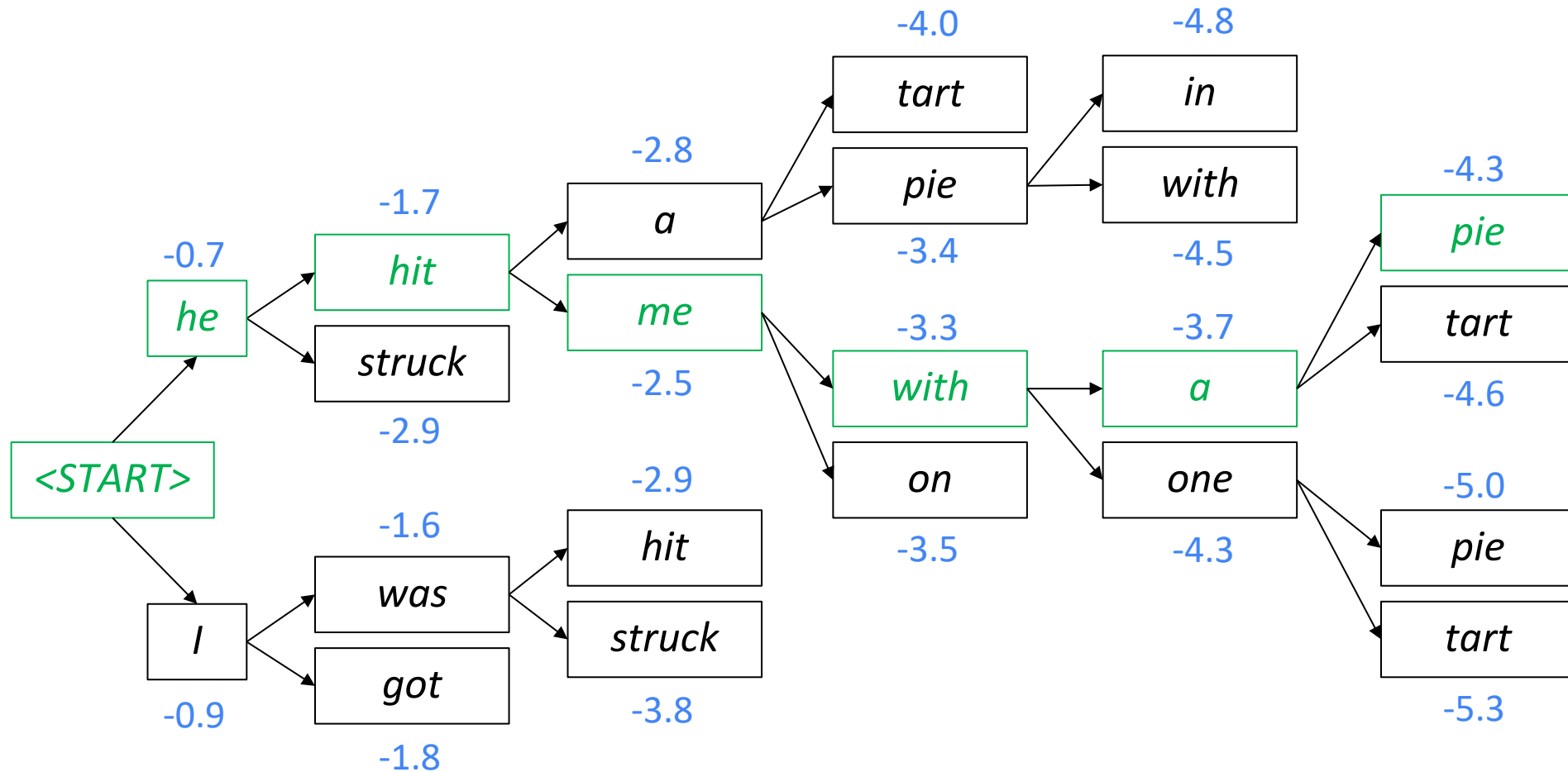
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This is the top-scoring hypothesis!

Beam search decoding: example

Beam size = $k = 2$. Blue numbers = $\text{score}(y_1, \dots, y_t) = \sum_{i=1}^t \log P_{\text{LM}}(y_i | y_1, \dots, y_{i-1}, x)$



Backtrack to obtain the full hypothesis

Beam search decoding: stopping criterion

- In **greedy decoding**, usually we decode until the model produces an **<END> token**
 - **For example:** *<START> he hit me with a pie <END>*
- In **beam search decoding**, different hypotheses may produce <END> tokens on **different timesteps**
 - When a hypothesis produces <END>, that hypothesis is **complete**.
 - **Place it aside** and continue exploring other hypotheses via beam search.
- Usually we continue beam search until:
 - We reach timestep T (where T is some pre-defined cutoff), or
 - We have at least n completed hypotheses (where n is pre-defined cutoff)

Beam search decoding: finishing up

- We have our list of completed hypotheses.
- How to select top one?

- Each hypothesis y_1, \dots, y_t on our list has a score

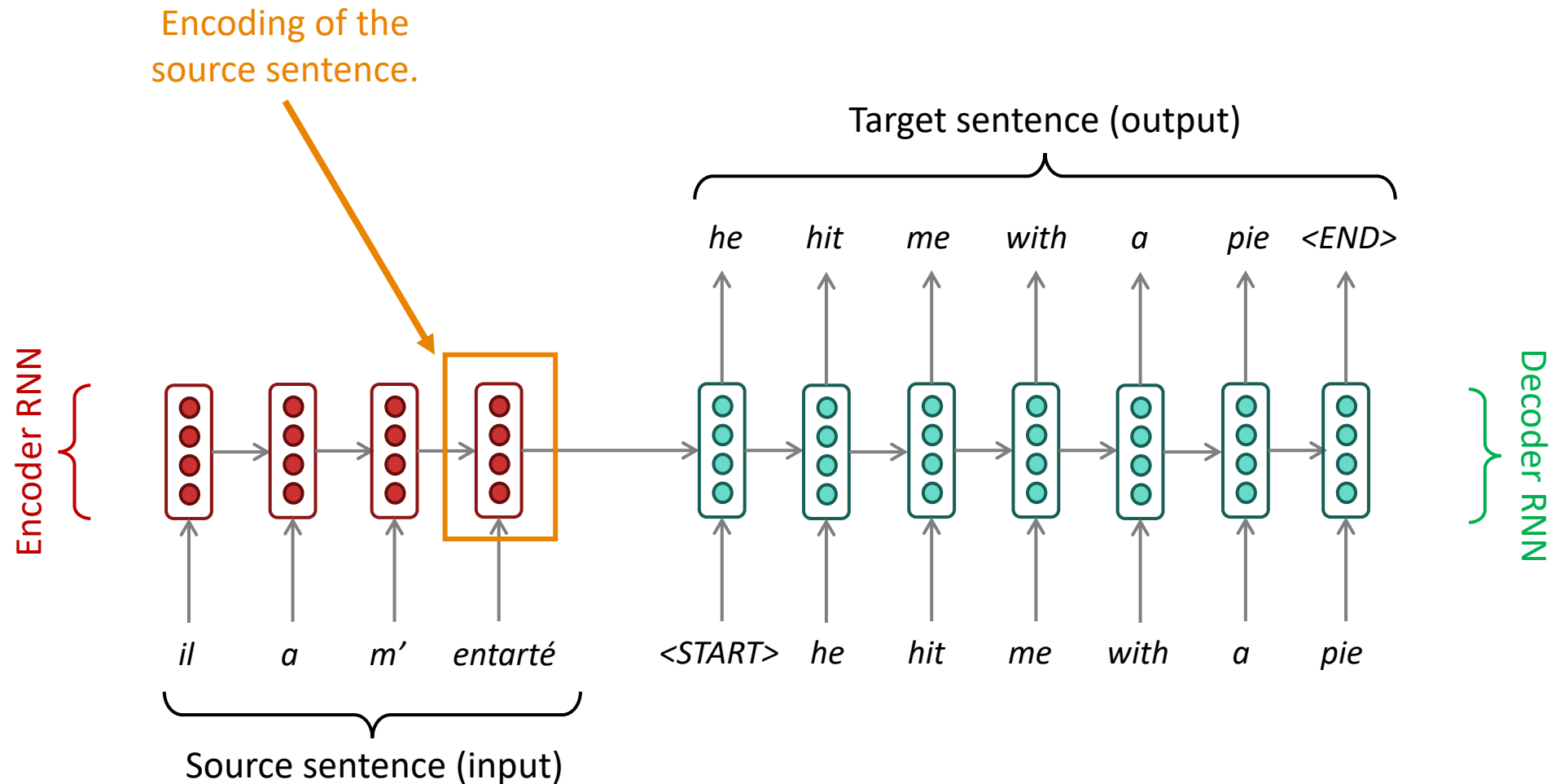
$$\text{score}(y_1, \dots, y_t) = \log P_{\text{LM}}(y_1, \dots, y_t | x) = \sum_{i=1}^t \log P_{\text{LM}}(y_i | y_1, \dots, y_{i-1}, x)$$

- **Problem with this:** longer hypotheses have lower scores
- **Fix:** Normalize by length. Use this to select top one instead:

$$\frac{1}{t} \sum_{i=1}^t \log P_{\text{LM}}(y_i | y_1, \dots, y_{i-1}, x)$$

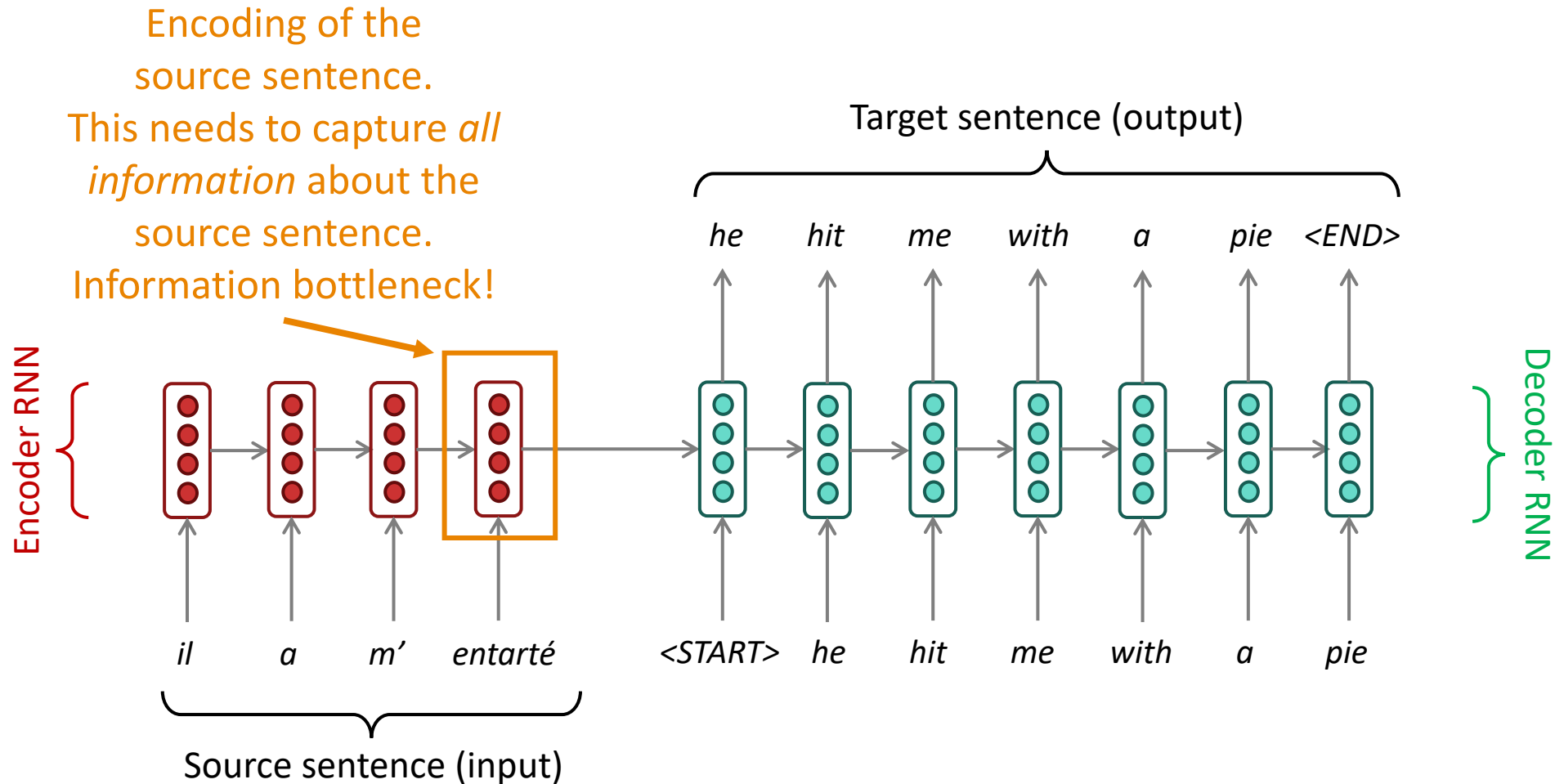
See also discussion of sampling-based decoding in the NLG lecture

2. Why attention? Sequence-to-sequence: the bottleneck problem



Problems with this architecture?

1. Why attention? Sequence-to-sequence: the bottleneck problem



Attention

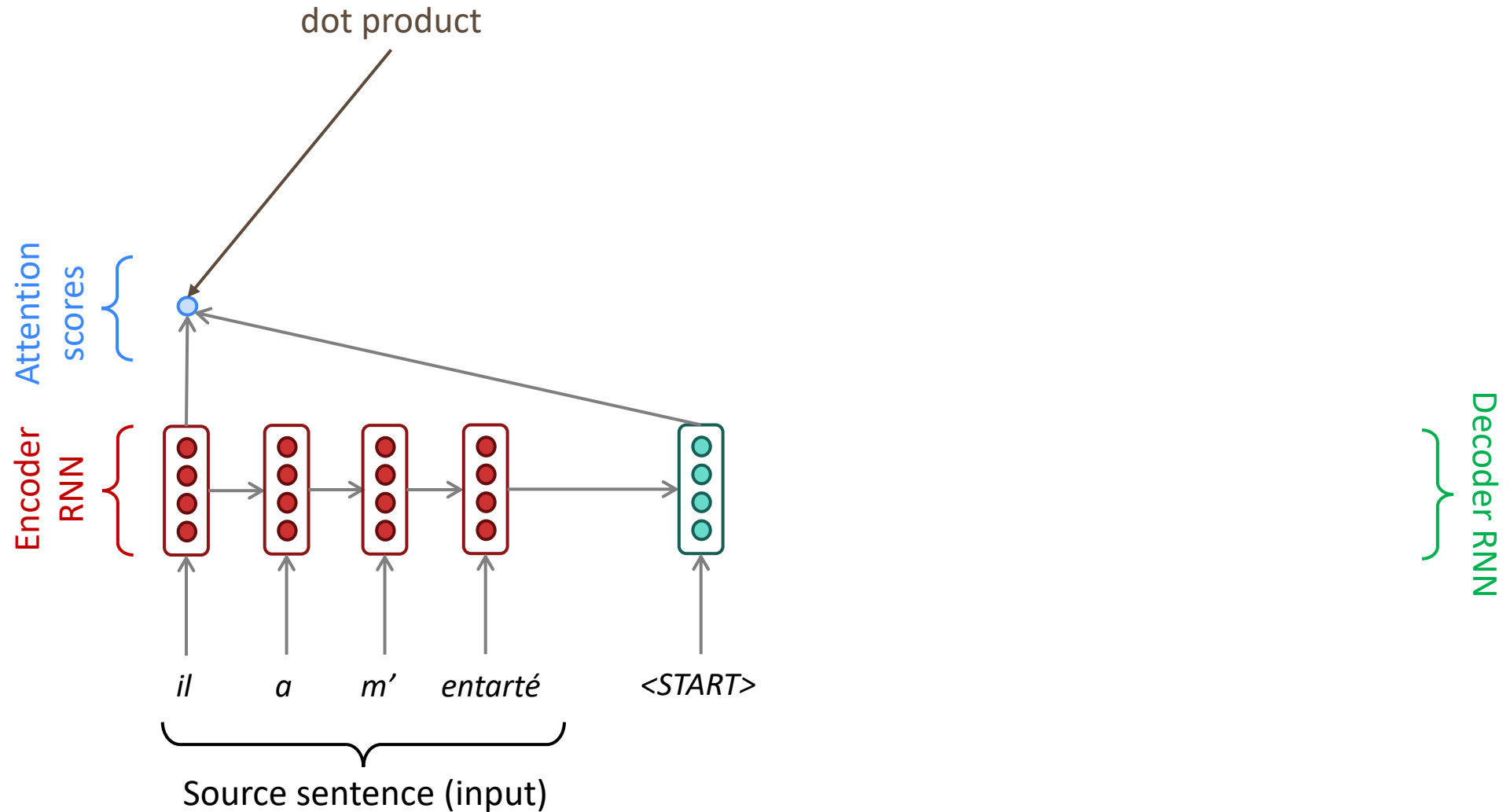
- **Attention** provides a solution to the bottleneck problem.
- **Core idea:** on each step of the decoder, *use direct connection to the encoder to focus on a particular part* of the source sequence



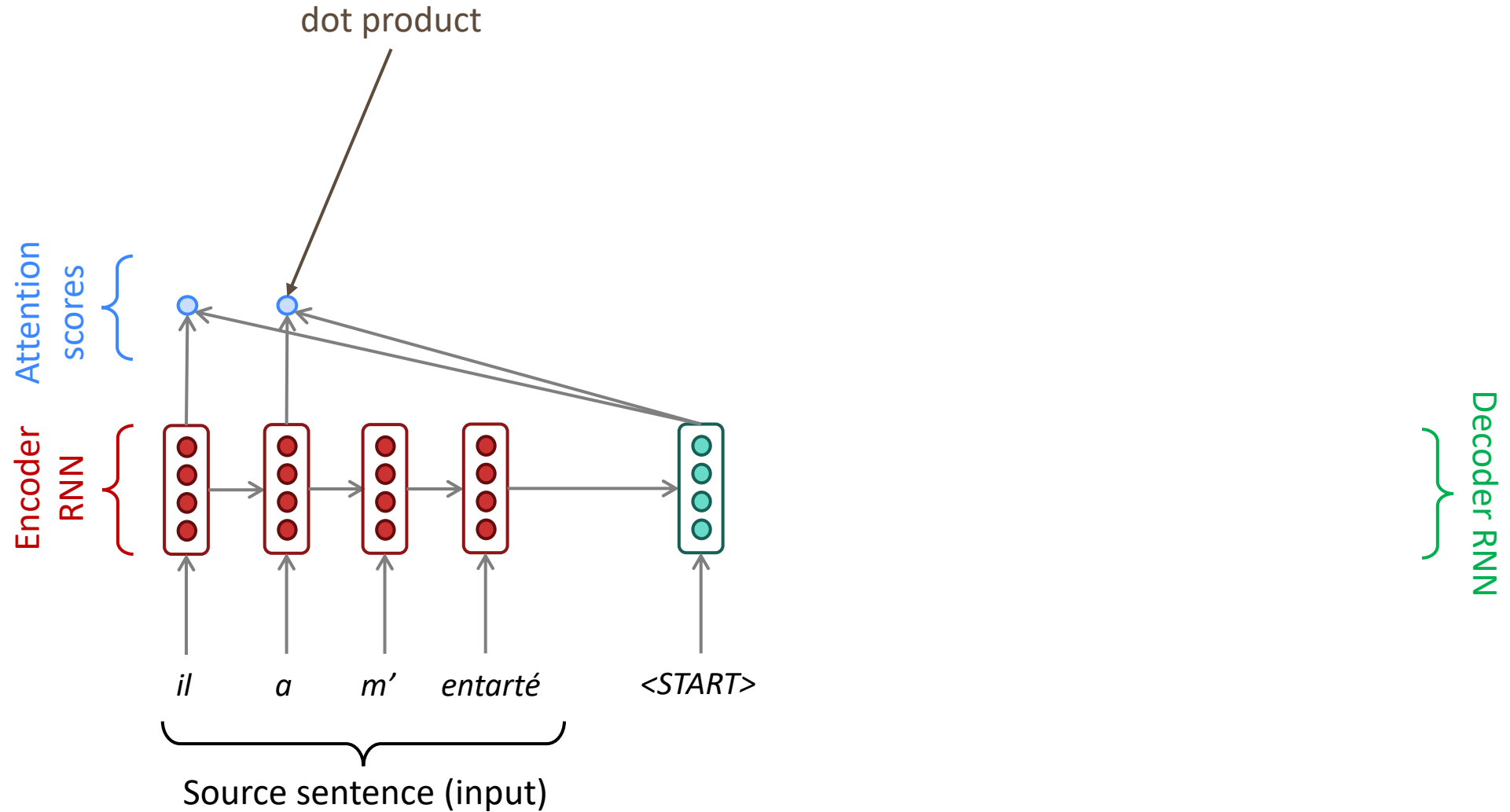
- First, we will show via diagram (no equations), then we will show with equations

Sequence-to-sequence with attention

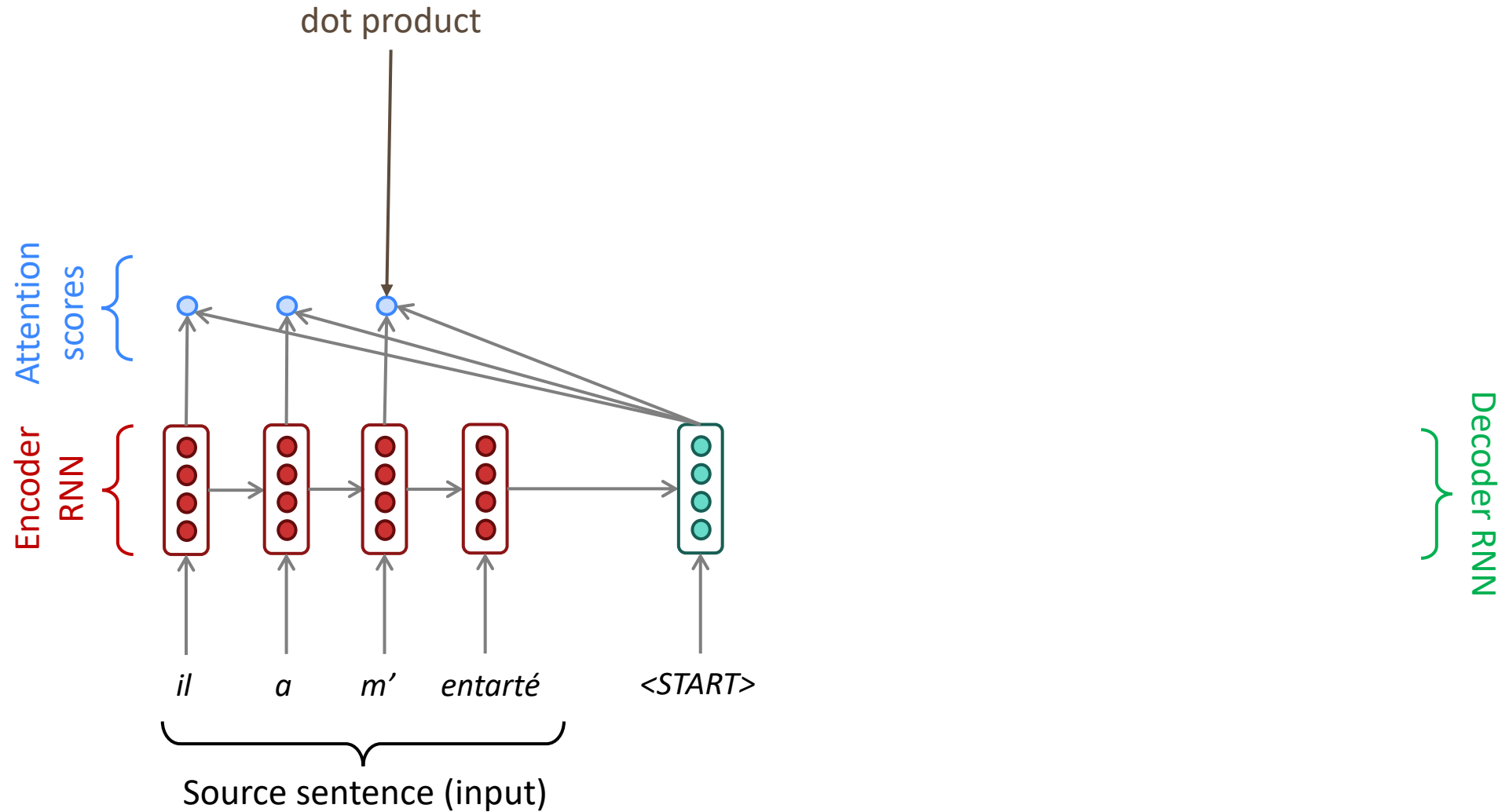
Core idea: on each step of the decoder, *use direct connection to the encoder* to *focus on a particular part* of the source sequence



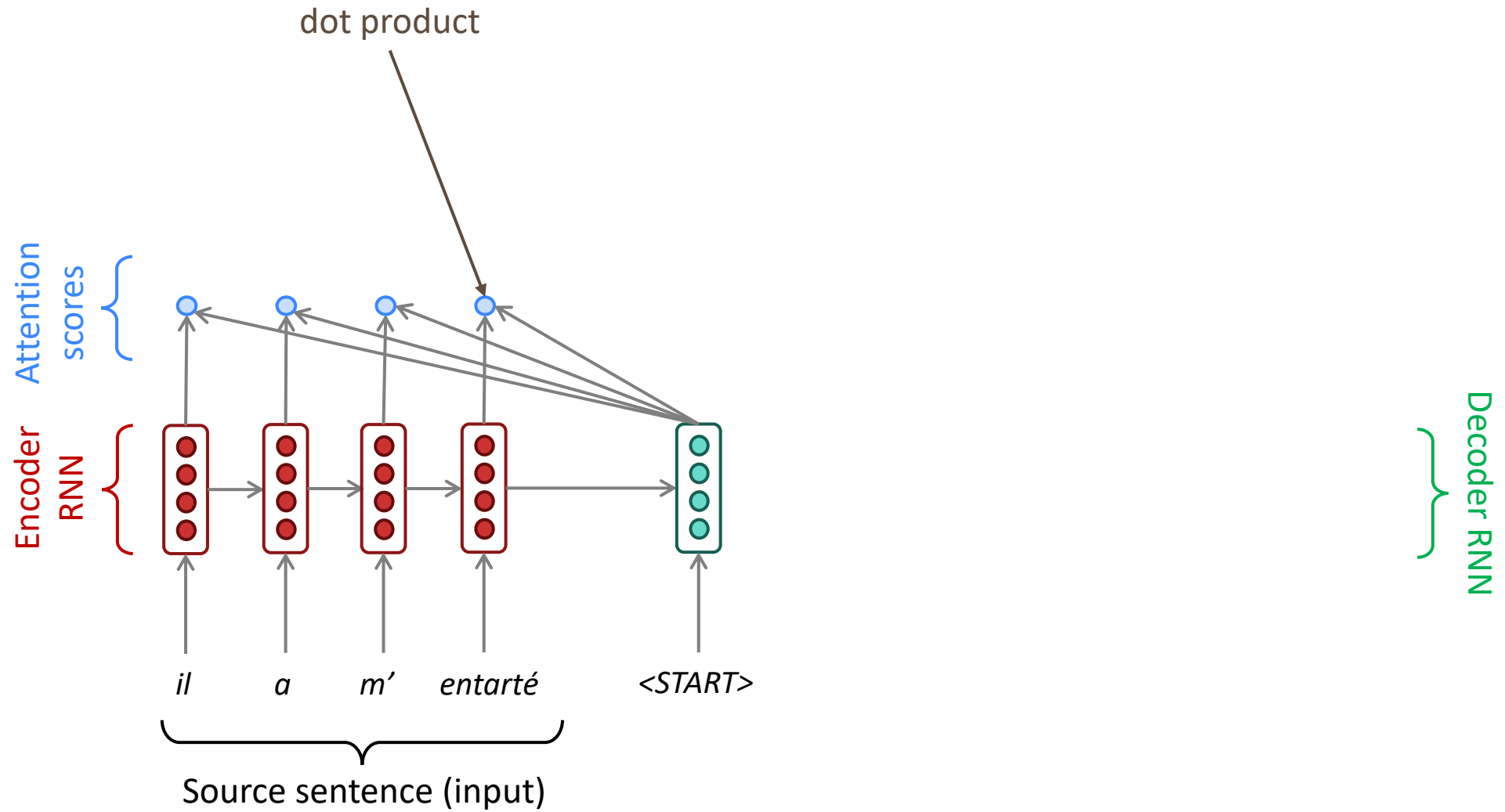
Sequence-to-sequence with attention



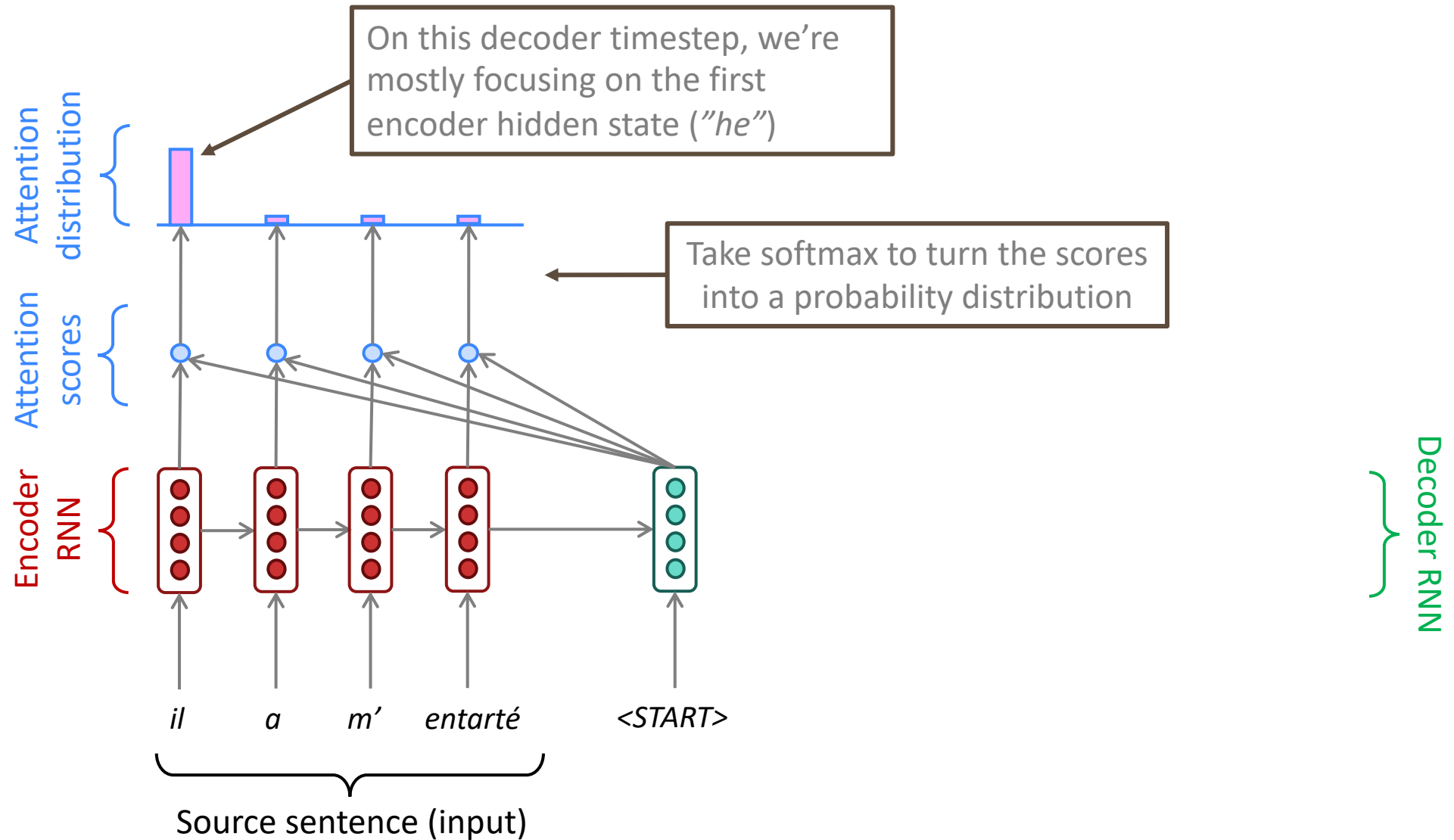
Sequence-to-sequence with attention



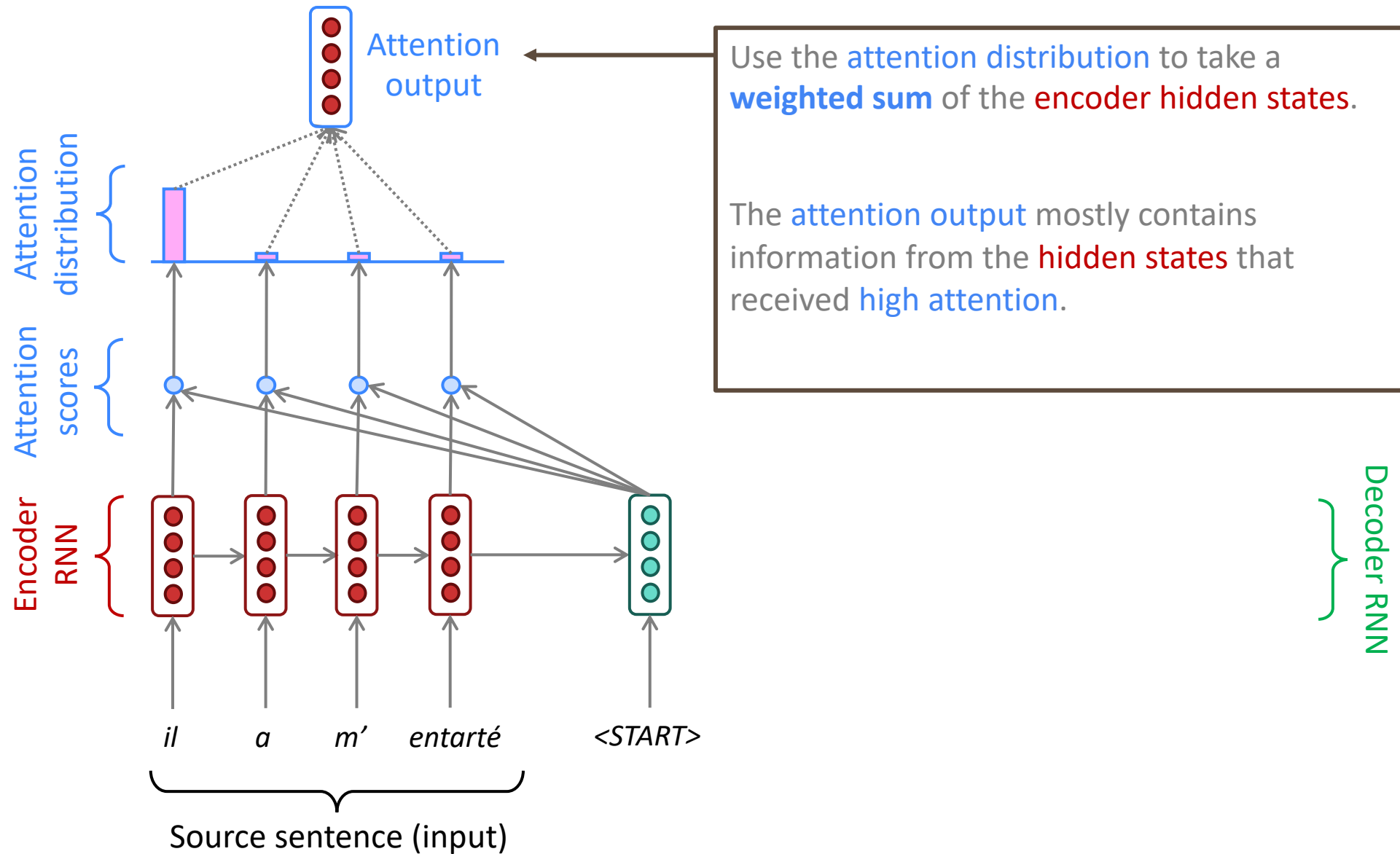
Sequence-to-sequence with attention



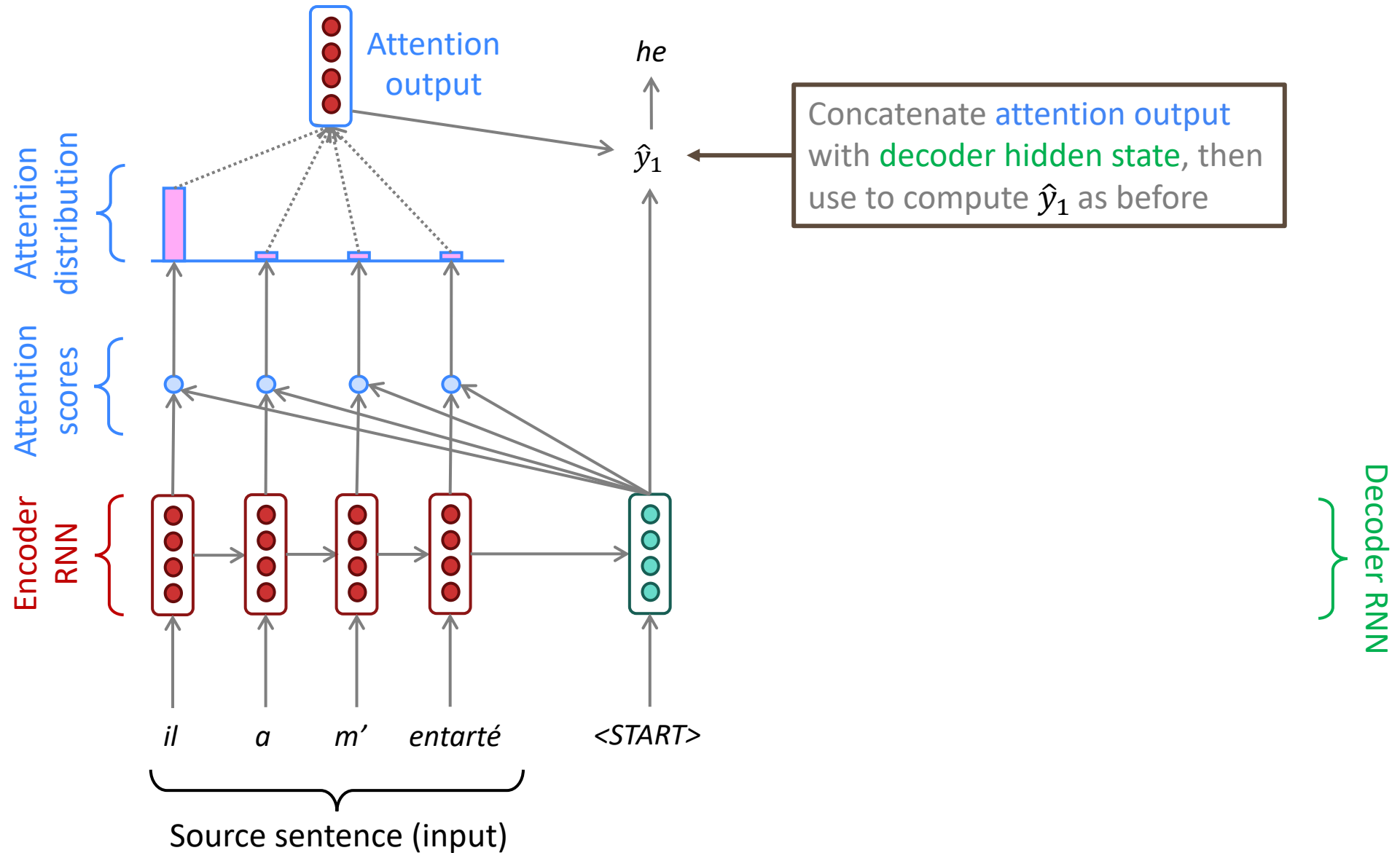
Sequence-to-sequence with attention



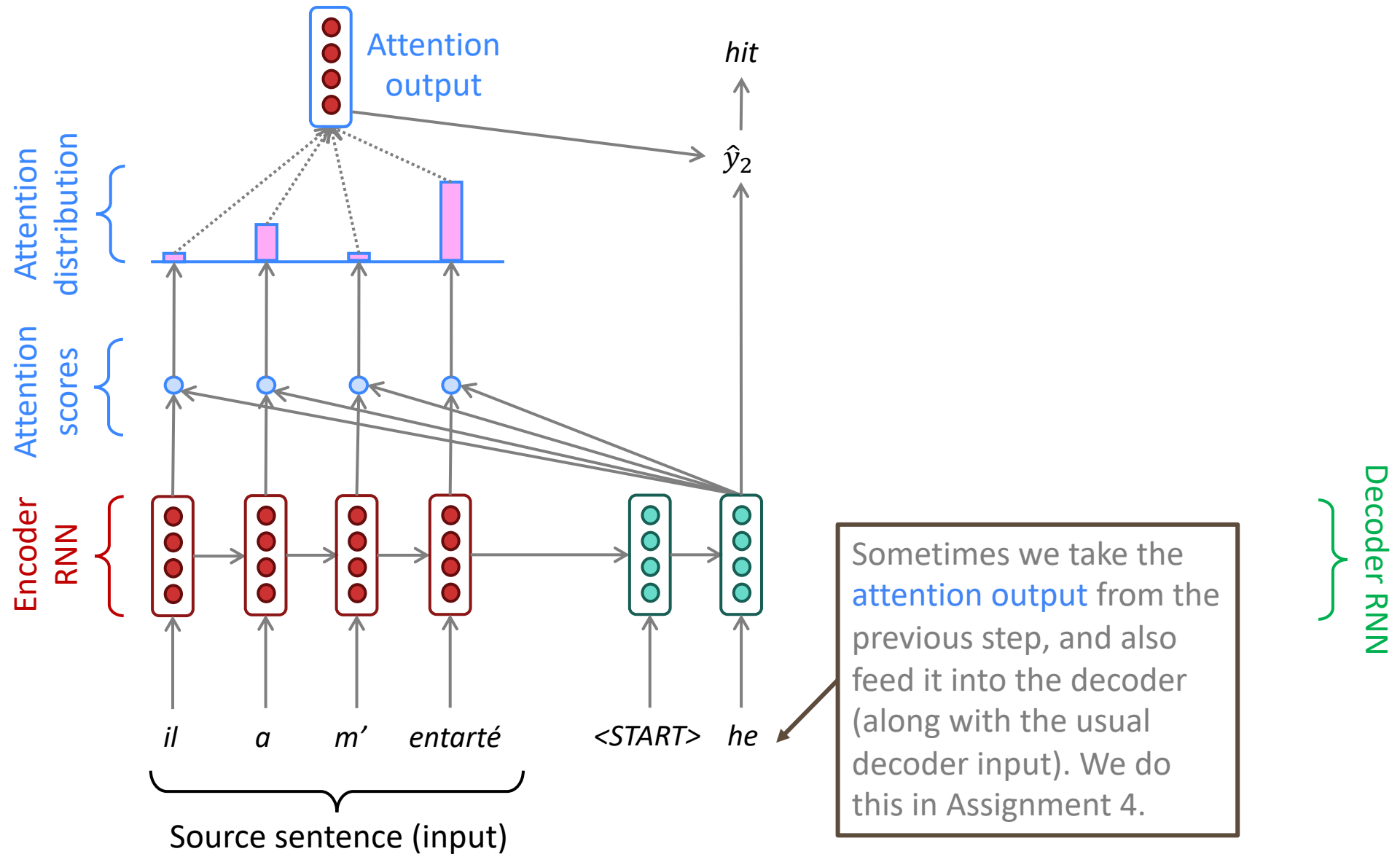
Sequence-to-sequence with attention



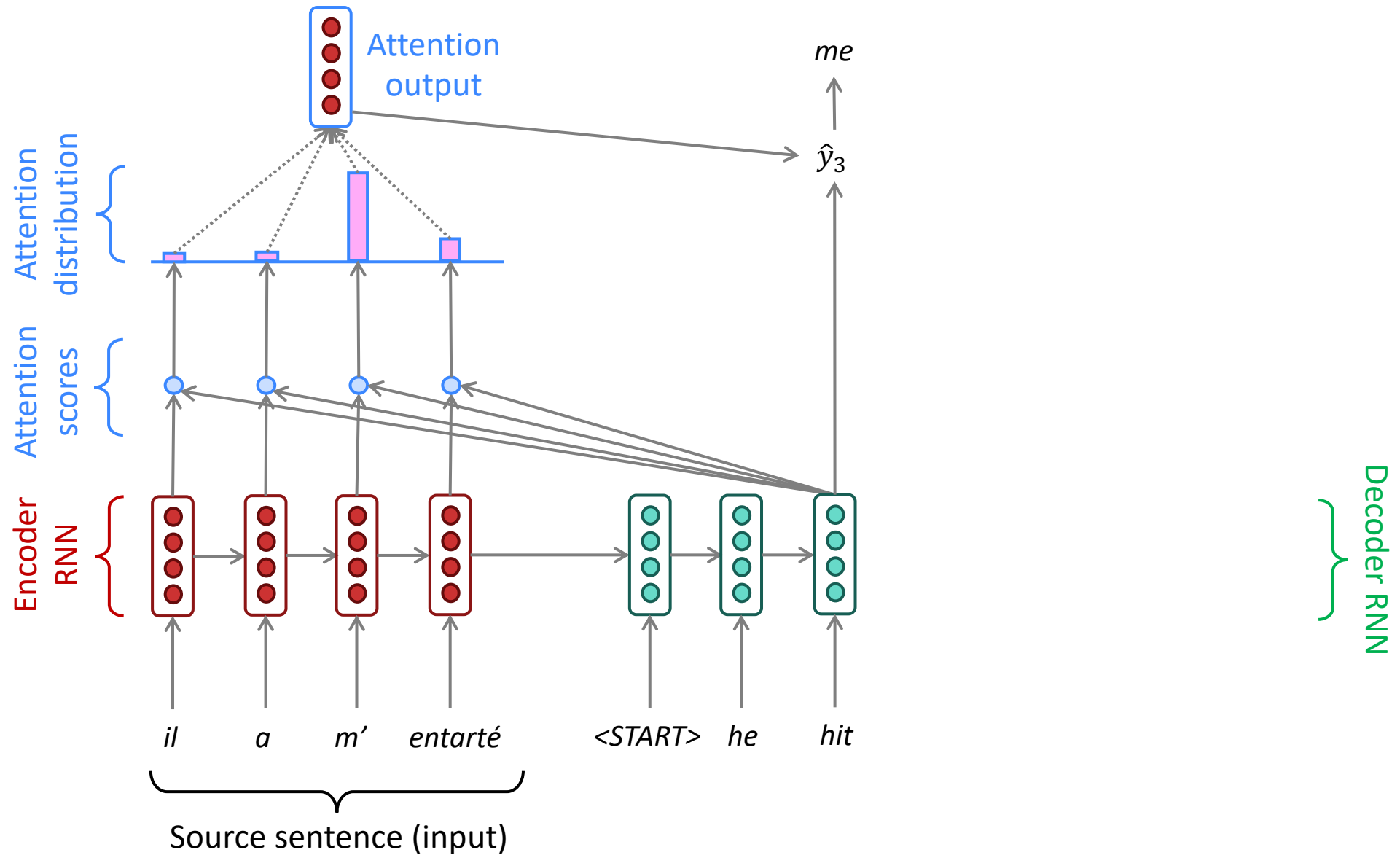
Sequence-to-sequence with attention



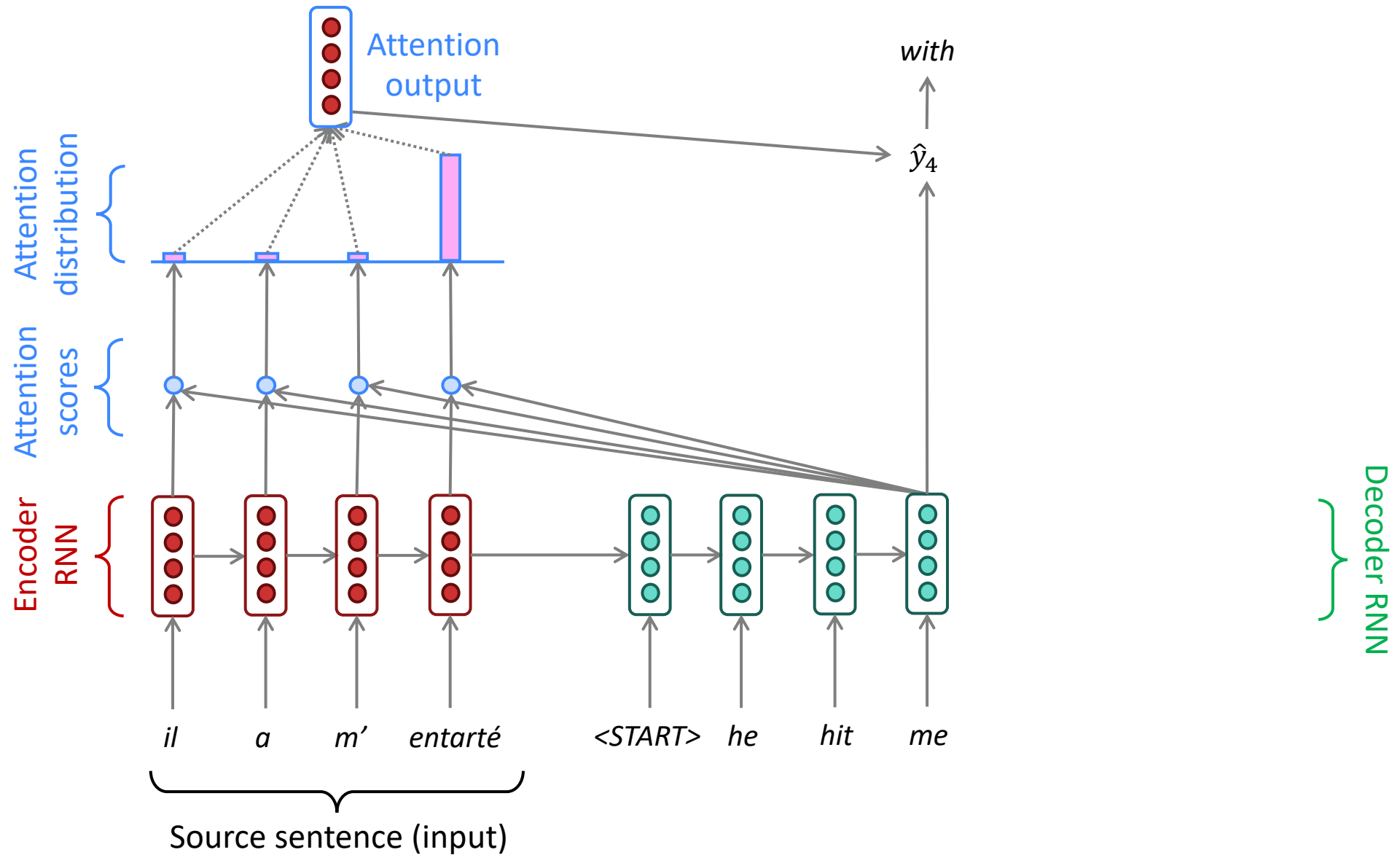
Sequence-to-sequence with attention



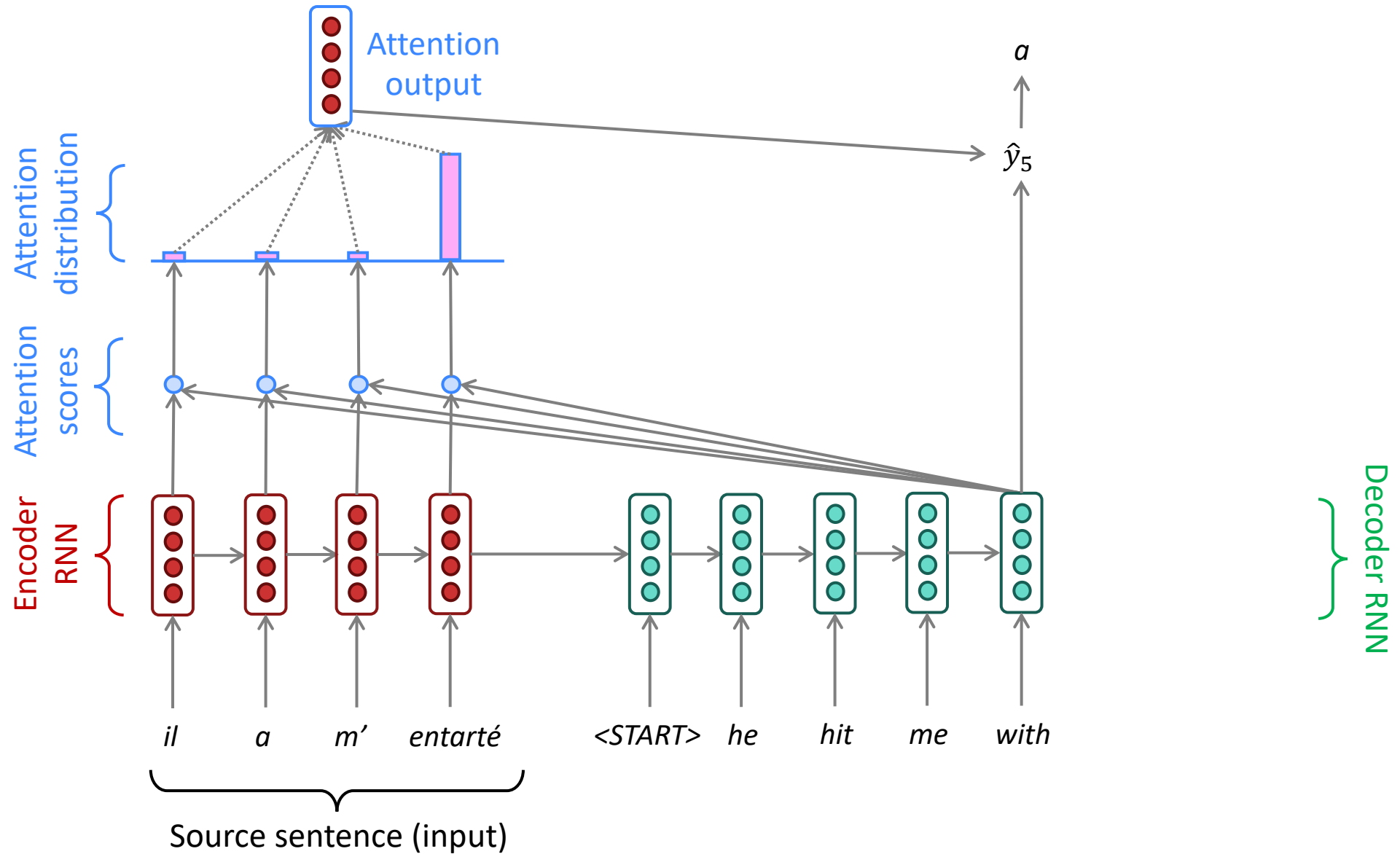
Sequence-to-sequence with attention



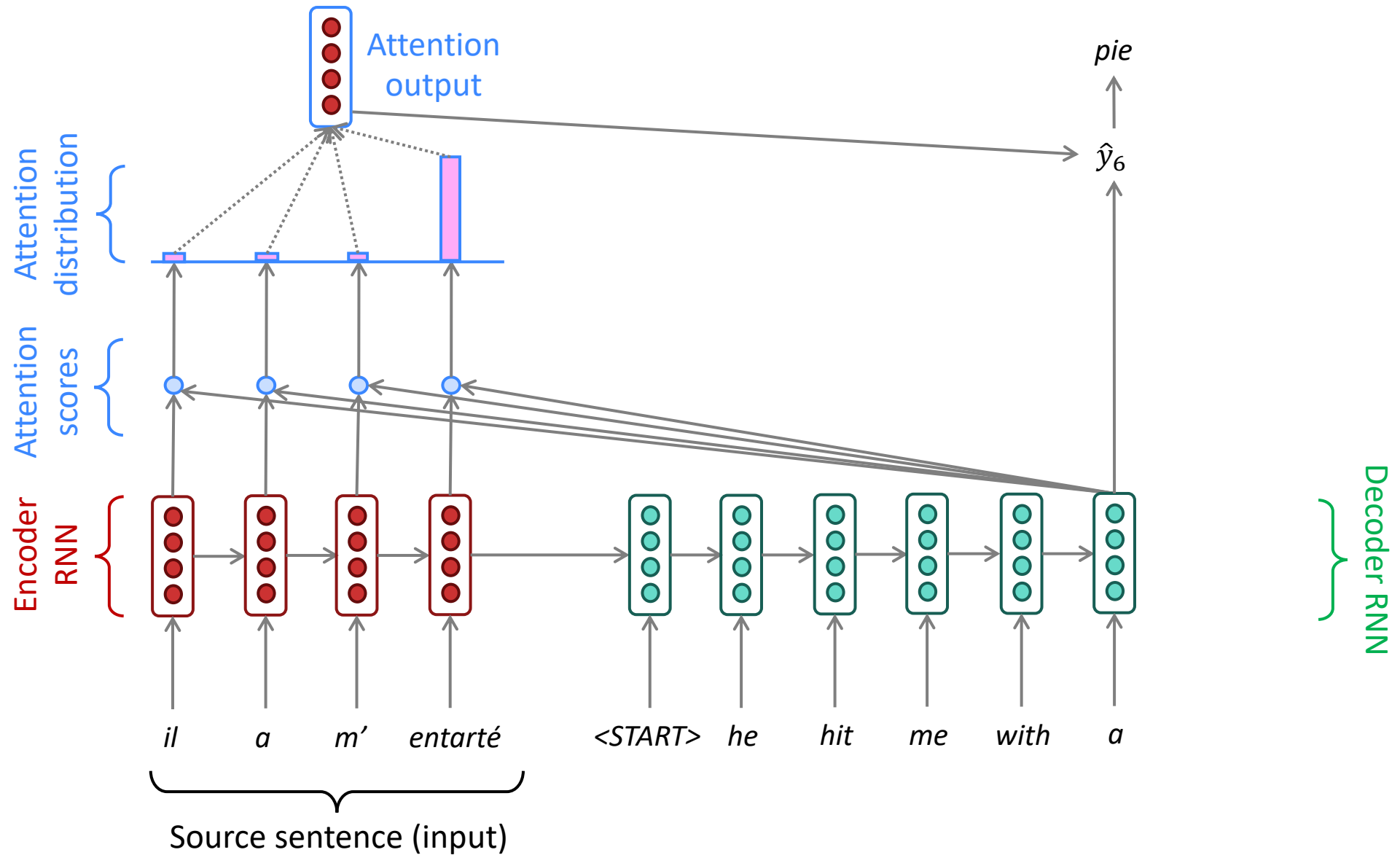
Sequence-to-sequence with attention



Sequence-to-sequence with attention



Sequence-to-sequence with attention



Attention: in equations

- We have encoder hidden states $h_1, \dots, h_N \in \mathbb{R}^h$
- On timestep t , we have decoder hidden state $s_t \in \mathbb{R}^h$
- We get the attention scores e^t for this step:

$$e^t = [s_t^T h_1, \dots, s_t^T h_N] \in \mathbb{R}^N$$

- We take softmax to get the attention distribution α^t for this step (this is a probability distribution and sums to 1)

$$\alpha^t = \text{softmax}(e^t) \in \mathbb{R}^N$$

- We use α^t to take a weighted sum of the encoder hidden states to get the attention output a_t

$$a_t = \sum_{i=1}^N \alpha_i^t h_i \in \mathbb{R}^h$$

- Finally we concatenate the attention output a_t with the decoder hidden state s_t and proceed as in the non-attention seq2seq model

$$[a_t; s_t] \in \mathbb{R}^{2h}$$

Attention is great!



- Attention significantly **improves NMT performance**
 - It's very useful to allow decoder to focus on certain parts of the source
- Attention provides a **more “human-like” model** of the MT process
 - You can look back at the source sentence while translating, rather than needing to remember it all
- Attention **solves the bottleneck problem**
 - Attention allows decoder to look directly at source; bypass bottleneck
- Attention **helps with the vanishing gradient problem**
 - Provides shortcut to faraway states
- Attention provides **some interpretability**
 - By inspecting attention distribution, we see what the decoder was focusing on
 - We get (soft) **alignment for free!**
 - This is cool because we never explicitly trained an alignment system
 - The network just learned alignment by itself

	he	hit	me	with	a	pie
il	■	□	□	□	□	□
a	□	■	□	□	□	□
m'	□	□	■	□	□	□
entarté	□	■	■	■	■	■

There are *several* attention variants

- We have some *values* $\mathbf{h}_1, \dots, \mathbf{h}_N \in \mathbb{R}^{d_1}$ and a *query* $\mathbf{s} \in \mathbb{R}^{d_2}$

- Attention always involves:

1. Computing the *attention scores* $\mathbf{e} \in \mathbb{R}^N$
2. Taking softmax to get *attention distribution* α :

There are multiple ways to do this

$$\alpha = \text{softmax}(\mathbf{e}) \in \mathbb{R}^N$$

3. Using attention distribution to take weighted sum of values:

$$\mathbf{a} = \sum_{i=1}^N \alpha_i \mathbf{h}_i \in \mathbb{R}^{d_1}$$

thus obtaining the *attention output* \mathbf{a} (sometimes called the *context vector*)

Attention variants

You'll think about the relative advantages/disadvantages of these in Assignment 4!

There are **several ways** you can compute $e \in \mathbb{R}^N$ from $\mathbf{h}_1, \dots, \mathbf{h}_N \in \mathbb{R}^{d_1}$ and $\mathbf{s} \in \mathbb{R}^{d_2}$:

- Basic dot-product attention: $e_i = \mathbf{s}^T \mathbf{h}_i \in \mathbb{R}$
 - Note: this assumes $d_1 = d_2$. This is the version we saw earlier.
- Multiplicative attention: $e_i = \mathbf{s}^T \mathbf{W} \mathbf{h}_i \in \mathbb{R}$ [Luong, Pham, and Manning 2015]
 - Where $\mathbf{W} \in \mathbb{R}^{d_2 \times d_1}$ is a weight matrix. Perhaps better called “bilinear attention”
- Reduced-rank multiplicative attention: $e_i = \mathbf{s}^T (\mathbf{U}^T \mathbf{V}) \mathbf{h}_i = (\mathbf{U} \mathbf{s})^T (\mathbf{V} \mathbf{h}_i)$ ← Remember this when we look at Transformers next week!
 - For low rank matrices $\mathbf{U} \in \mathbb{R}^{k \times d_2}$, $\mathbf{V} \in \mathbb{R}^{k \times d_1}$, $k \ll d_1, d_2$
- Additive attention: $e_i = \mathbf{v}^T \tanh(\mathbf{W}_1 \mathbf{h}_i + \mathbf{W}_2 \mathbf{s}) \in \mathbb{R}$ [Bahdanau, Cho, and Bengio 2014]
 - Where $\mathbf{W}_1 \in \mathbb{R}^{d_3 \times d_1}$, $\mathbf{W}_2 \in \mathbb{R}^{d_3 \times d_2}$ are weight matrices and $\mathbf{v} \in \mathbb{R}^{d_3}$ is a weight vector.
 - d_3 (the attention dimensionality) is a hyperparameter
 - “Additive” is a weird/bad name. It’s really using a feed-forward neural net layer.

More information: “Deep Learning for NLP Best Practices”, Ruder, 2017. <http://ruder.io/deep-learning-nlp-best-practices/index.html#attention>
“Massive Exploration of Neural Machine Translation Architectures”, Britz et al, 2017, <https://arxiv.org/pdf/1703.03906.pdf>

Attention is a *general* Deep Learning technique

- We've seen that attention is a great way to improve the sequence-to-sequence model for Machine Translation.
- However: You can use attention in **many architectures** (not just seq2seq) and **many tasks** (not just MT)
- **More general definition of attention**:
 - Given a set of vector **values**, and a vector **query**, **attention** is a technique to compute a weighted sum of the values, dependent on the query.
- We sometimes say that the **query attends to the values**.
- For example, in the seq2seq + attention model, each decoder hidden state (query) *attends to* all the encoder hidden states (values).

Attention is a *general* Deep Learning technique

- More general definition of attention:
 - Given a set of vector *values*, and a vector *query*, attention is a technique to compute a weighted sum of the values, dependent on the query.

Intuition:

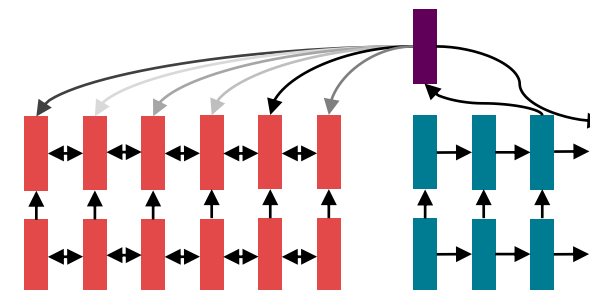
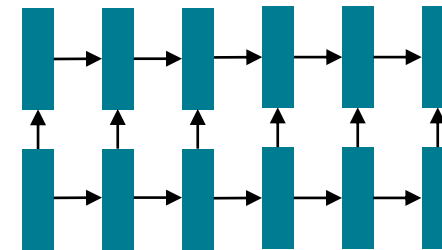
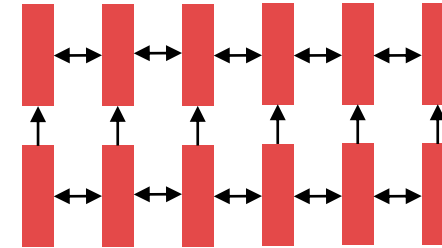
- The weighted sum is a *selective summary* of the information contained in the values, where the query determines which values to focus on.
- Attention is a way to obtain a *fixed-size representation of an arbitrary set of representations* (the values), dependent on some other representation (the query).

Upshot:

- Attention has become the powerful, flexible, general way pointer and memory manipulation in all deep learning models. A new idea from after 2010! From NMT!

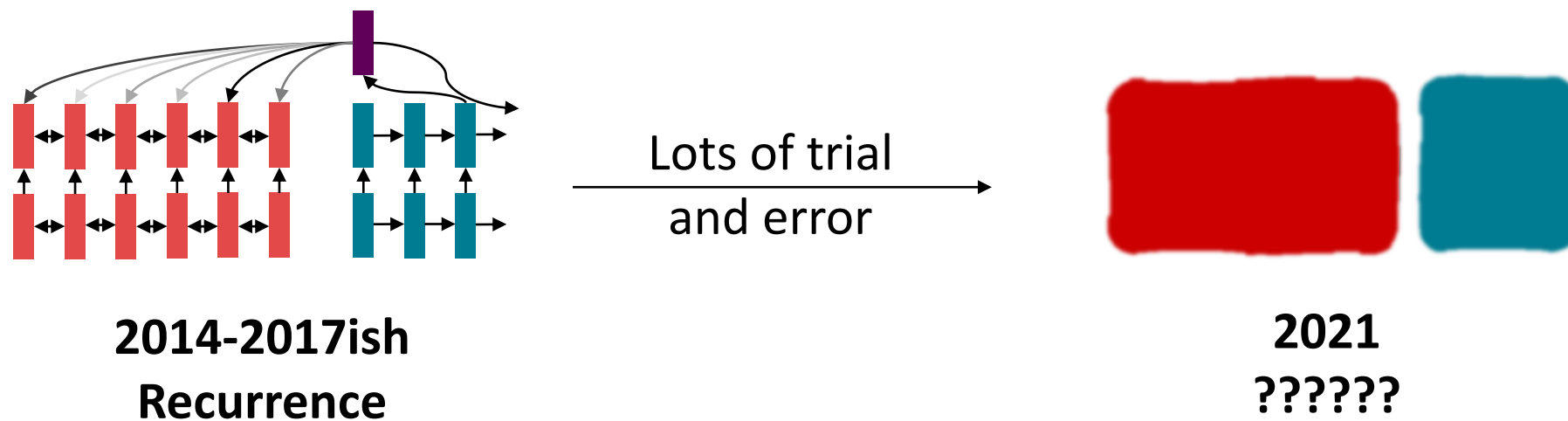
As of last lecture: recurrent models for (most) NLP!

- Circa 2016, the de facto strategy in NLP is to **encode** sentences with a bidirectional LSTM: (for example, the source sentence in a translation)
- Define your output (parse, sentence, summary) as a sequence, and use an LSTM to generate it.
- Use attention to allow flexible access to memory



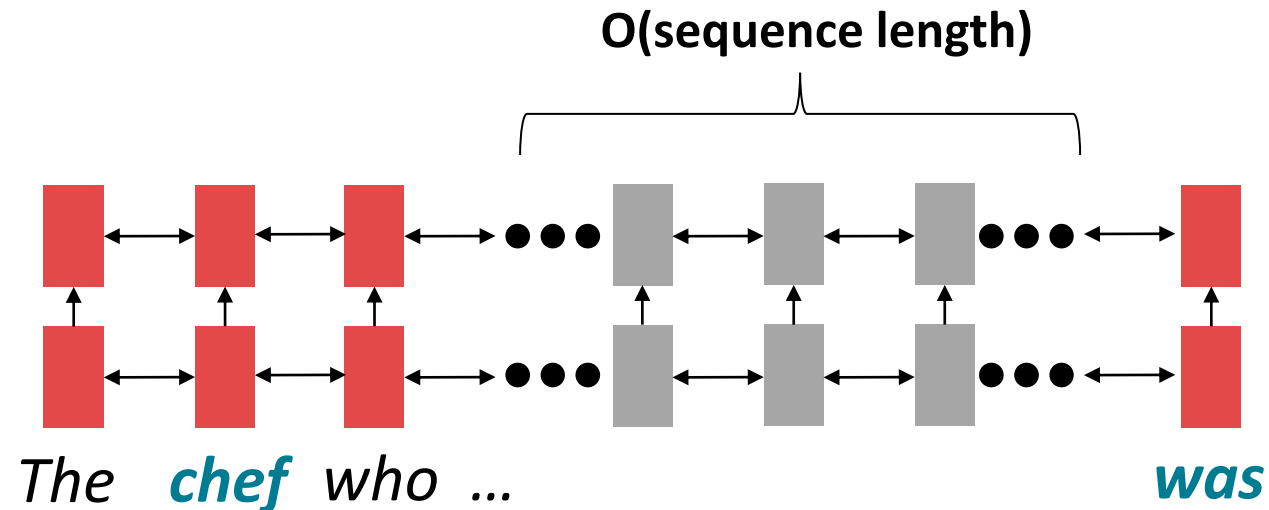
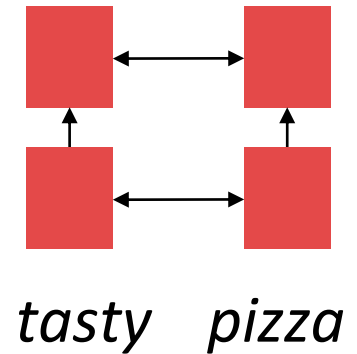
Today: Same goals, different building blocks

- Last week, we learned about sequence-to-sequence problems and encoder-decoder models.
- Today, we're **not** trying to motivate entirely new ways of looking at problems (like Machine Translation)
- Instead, we're trying to find the best **building blocks** to plug into our models and enable broad progress.



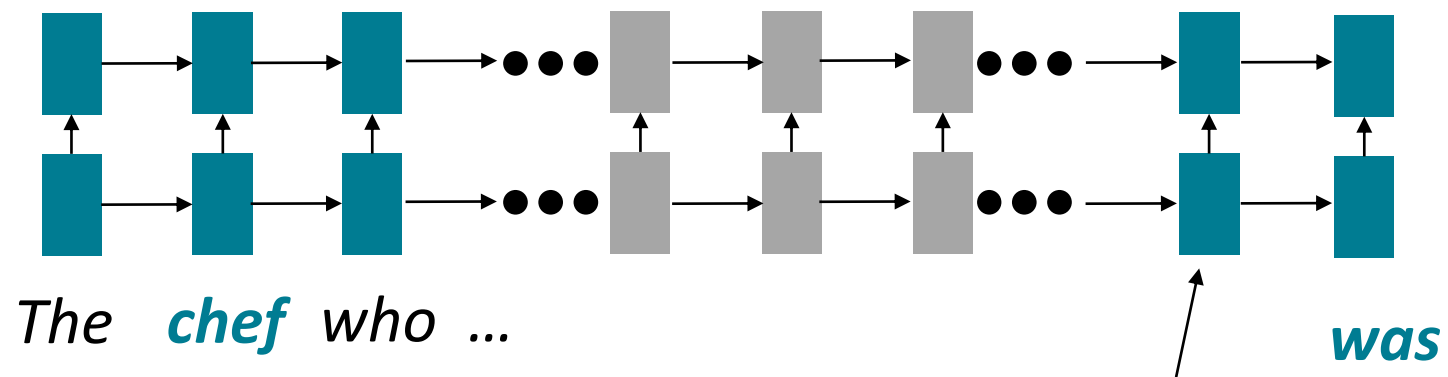
Issues with recurrent models: Linear interaction distance

- RNNs are unrolled “left-to-right”.
- This encodes linear locality: a useful heuristic!
 - Nearby words often affect each other’s meanings
- **Problem:** RNNs take $O(\text{sequence length})$ steps for distant word pairs to interact.



Issues with recurrent models: Linear interaction distance

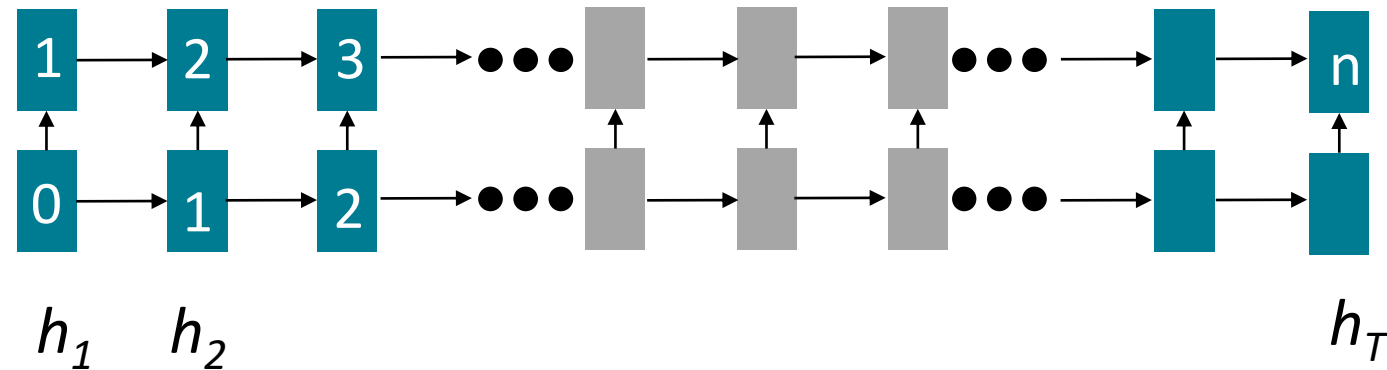
- **O(sequence length)** steps for distant word pairs to interact means:
 - Hard to learn long-distance dependencies (because gradient problems!)
 - Linear order of words is “baked in”; we already know linear order isn’t the right way to think about sentences...



Info of *chef* has gone through $O(\text{sequence length})$ many layers!

Issues with recurrent models: Lack of parallelizability

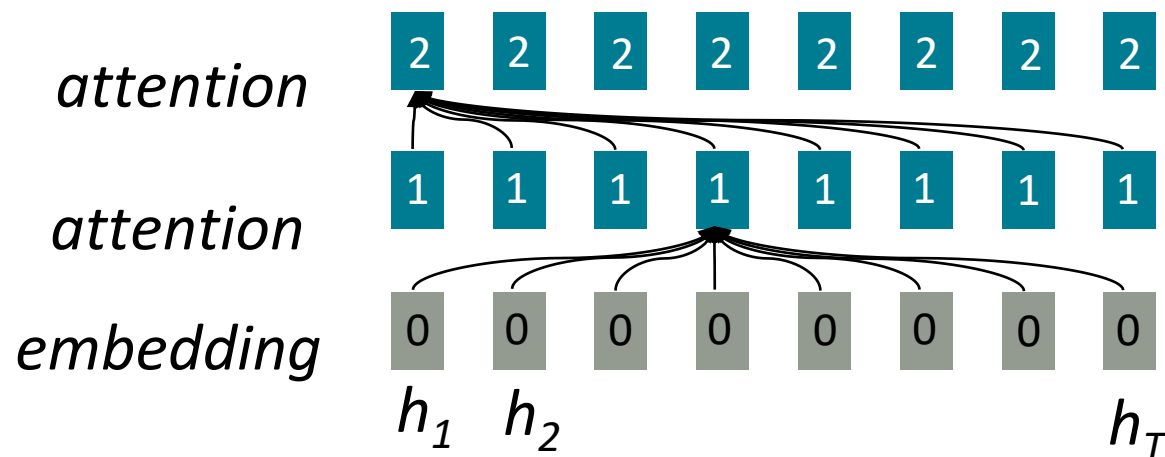
- Forward and backward passes have **$O(\text{sequence length})$** unparallelizable operations
 - GPUs can perform a bunch of independent computations at once!
 - But future RNN hidden states can't be computed in full before past RNN hidden states have been computed
 - Inhibits training on very large datasets!



Numbers indicate min # of steps before a state can be computed

If not recurrence, then what? **How about attention?**

- **Attention** treats each word's representation as a **query** to access and incorporate information from **a set of values**.
 - We saw attention from the **decoder** to the **encoder**; today we'll think about attention **within a single sentence**.
- Number of unparallelizable operations does not increase with sequence length.
- Maximum interaction distance: $O(1)$, since all words interact at every layer!

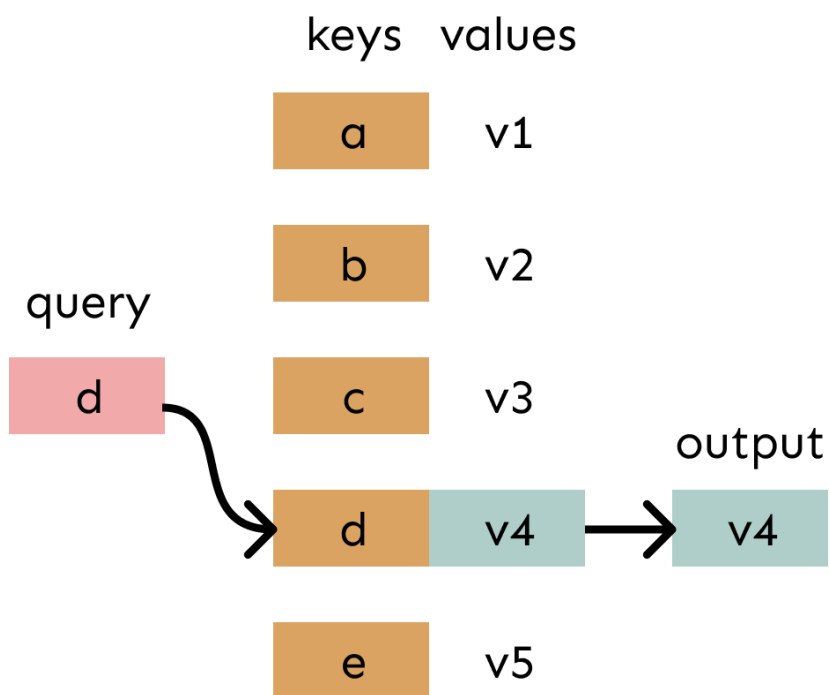


All words attend to all words in previous layer; most arrows here are omitted

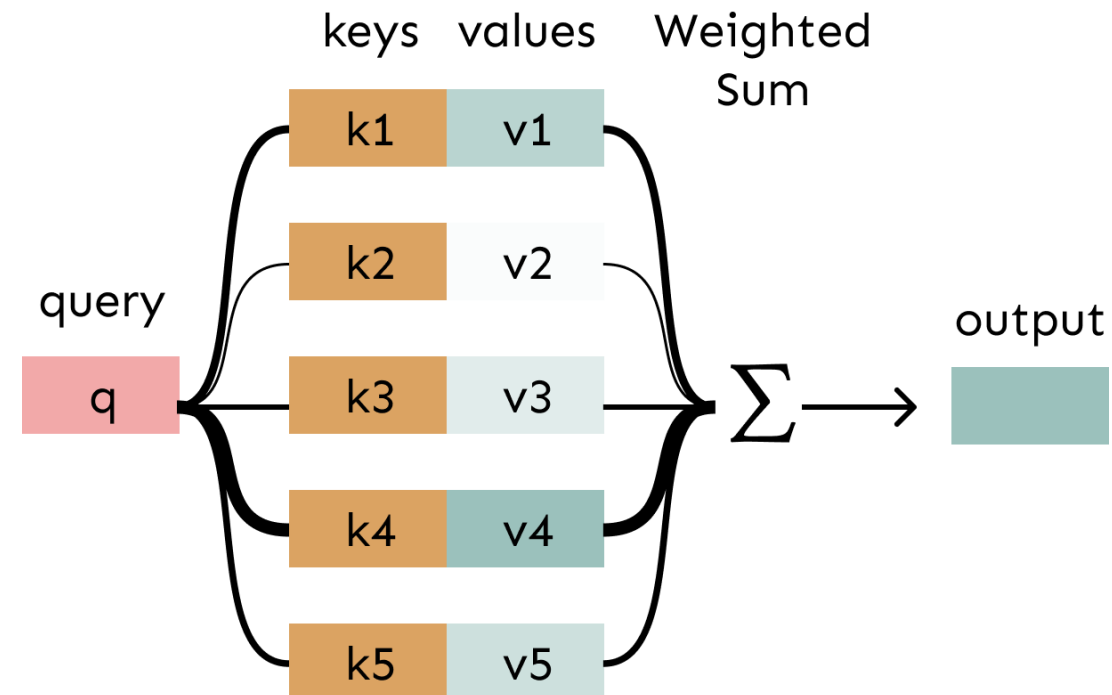
Attention as a soft, averaging lookup table

We can think of **attention** as performing fuzzy lookup in a key-value store.

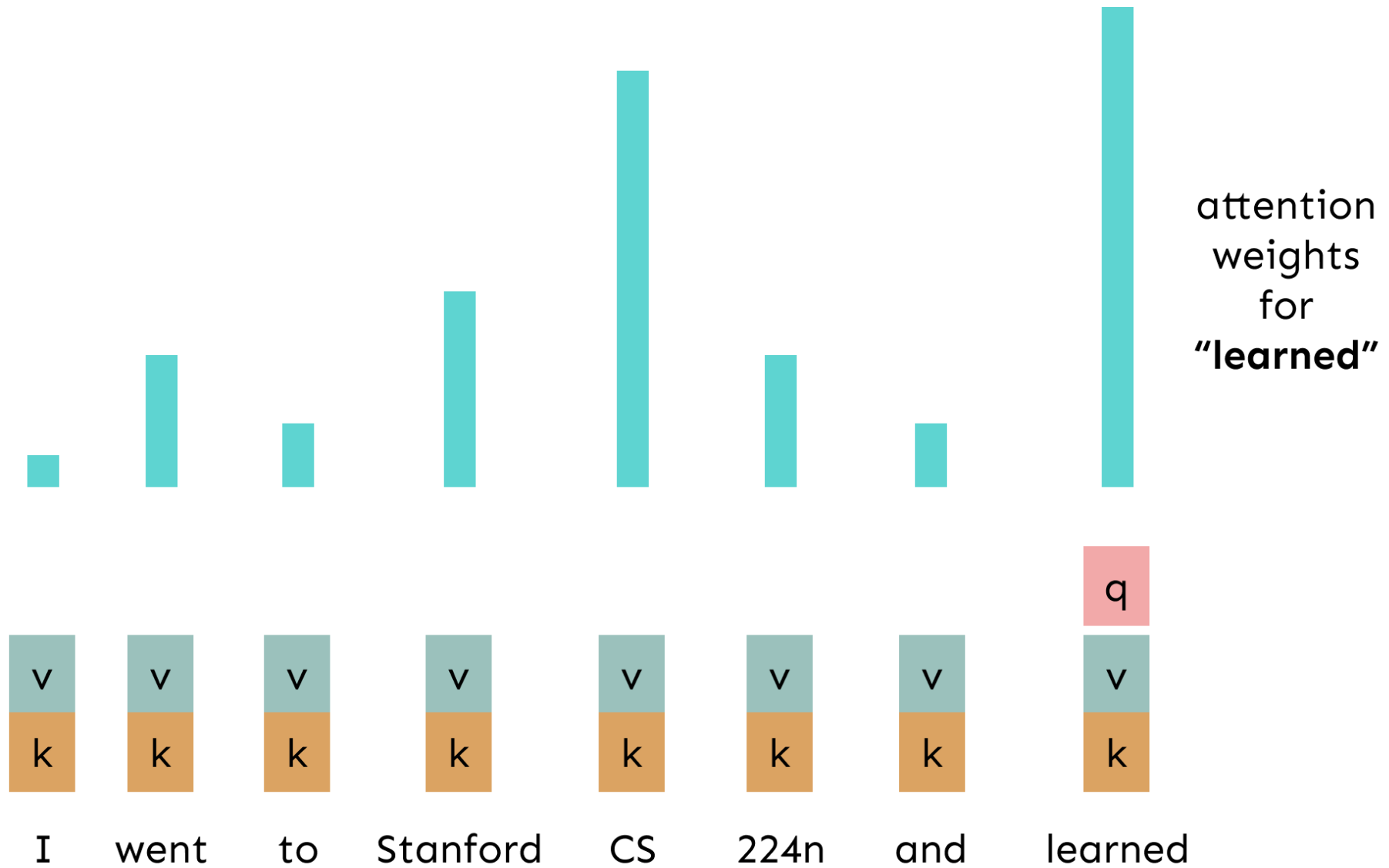
In a **lookup table**, we have a table of **keys** that map to **values**. The **query** matches one of the keys, returning its value.



In **attention**, the **query** matches all **keys** *softly*, to a weight between 0 and 1. The keys' **values** are multiplied by the weights and summed.



Self-Attention Hypothetical Example



Self-Attention: keys, queries, values from the same sequence

Let $\mathbf{w}_{1:n}$ be a sequence of words in vocabulary V , like *Zuko made his uncle tea*.

For each \mathbf{w}_i , let $\mathbf{x}_i = E\mathbf{w}_i$, where $E \in \mathbb{R}^{d \times |V|}$ is an embedding matrix.

1. Transform each word embedding with weight matrices Q, K, V , each in $\mathbb{R}^{d \times d}$

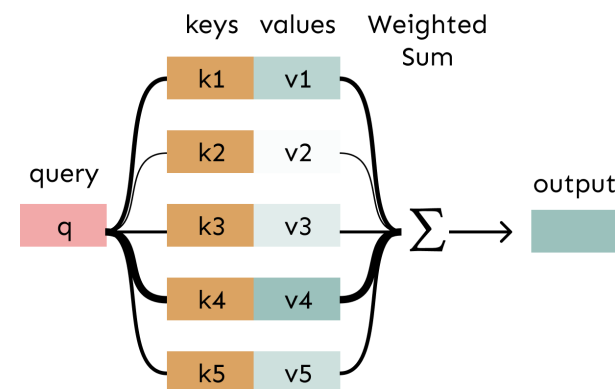
$$\mathbf{q}_i = Q\mathbf{x}_i \text{ (queries)} \quad \mathbf{k}_i = K\mathbf{x}_i \text{ (keys)} \quad \mathbf{v}_i = V\mathbf{x}_i \text{ (values)}$$

2. Compute pairwise similarities between keys and queries; normalize with softmax

$$\mathbf{e}_{ij} = \mathbf{q}_i^\top \mathbf{k}_j \quad \alpha_{ij} = \frac{\exp(\mathbf{e}_{ij})}{\sum_{j'} \exp(\mathbf{e}_{ij'})}$$

3. Compute output for each word as weighted sum of values

$$\mathbf{o}_i = \sum_j \alpha_{ij} \mathbf{v}_j$$



Barriers and solutions for Self-Attention as a building block

Barriers

- Doesn't have an inherent notion of order!



Solutions

Fixing the first self-attention problem: **sequence order**

- Since self-attention doesn't build in order information, we need to encode the order of the sentence in our keys, queries, and values.
- Consider representing each **sequence index** as a **vector**

$\mathbf{p}_i \in \mathbb{R}^d$, for $i \in \{1, 2, \dots, n\}$ are position vectors

- Don't worry about what the p_i are made of yet!
- Easy to incorporate this info into our self-attention block: just add the \mathbf{p}_i to our inputs!
- Recall that \mathbf{x}_i is the embedding of the word at index i . The positioned embedding is:

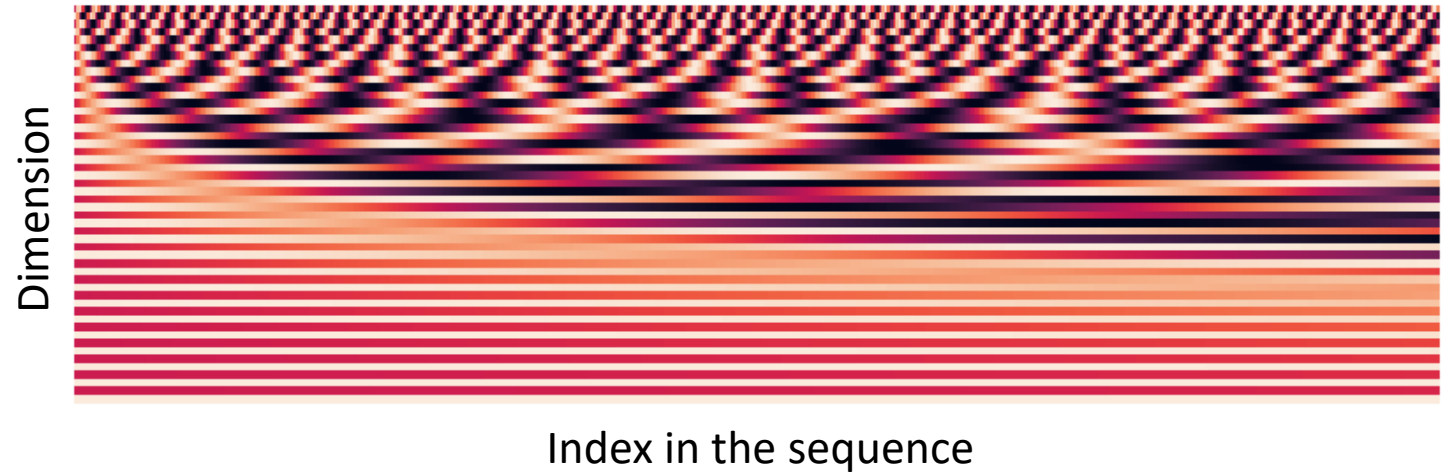
$$\tilde{\mathbf{x}}_i = \mathbf{x}_i + \mathbf{p}_i$$

In deep self-attention networks, we do this at the first layer! You could concatenate them as well, but people mostly just add...

Position representation vectors through sinusoids

- **Sinusoidal position representations:** concatenate sinusoidal functions of varying periods:

$$p_i = \begin{pmatrix} \sin(i/10000^{2*1/d}) \\ \cos(i/10000^{2*1/d}) \\ \vdots \\ \sin(i/10000^{2*\frac{d}{2}/d}) \\ \cos(i/10000^{2*\frac{d}{2}/d}) \end{pmatrix}$$



- Pros:
 - Periodicity indicates that maybe “absolute position” isn’t as important
 - Maybe can extrapolate to longer sequences as periods restart!
- Cons:
 - Not learnable; also the extrapolation doesn’t really work!

Position representation vectors learned from scratch

- **Learned absolute position representations:** Let all p_i be learnable parameters!
Learn a matrix $\mathbf{p} \in \mathbb{R}^{d \times n}$, and let each \mathbf{p}_i be a column of that matrix!
- Pros:
 - Flexibility: each position gets to be learned to fit the data
- Cons:
 - Definitely can't extrapolate to indices outside $1, \dots, n$.
- Most systems use this!
- Sometimes people try more flexible representations of position:
 - Relative linear position attention [\[Shaw et al., 2018\]](#)
 - Dependency syntax-based position [\[Wang et al., 2019\]](#)

Barriers and solutions for Self-Attention as a building block

Barriers

- Doesn't have an inherent notion of order!
- No nonlinearities for deep learning! It's all just weighted averages



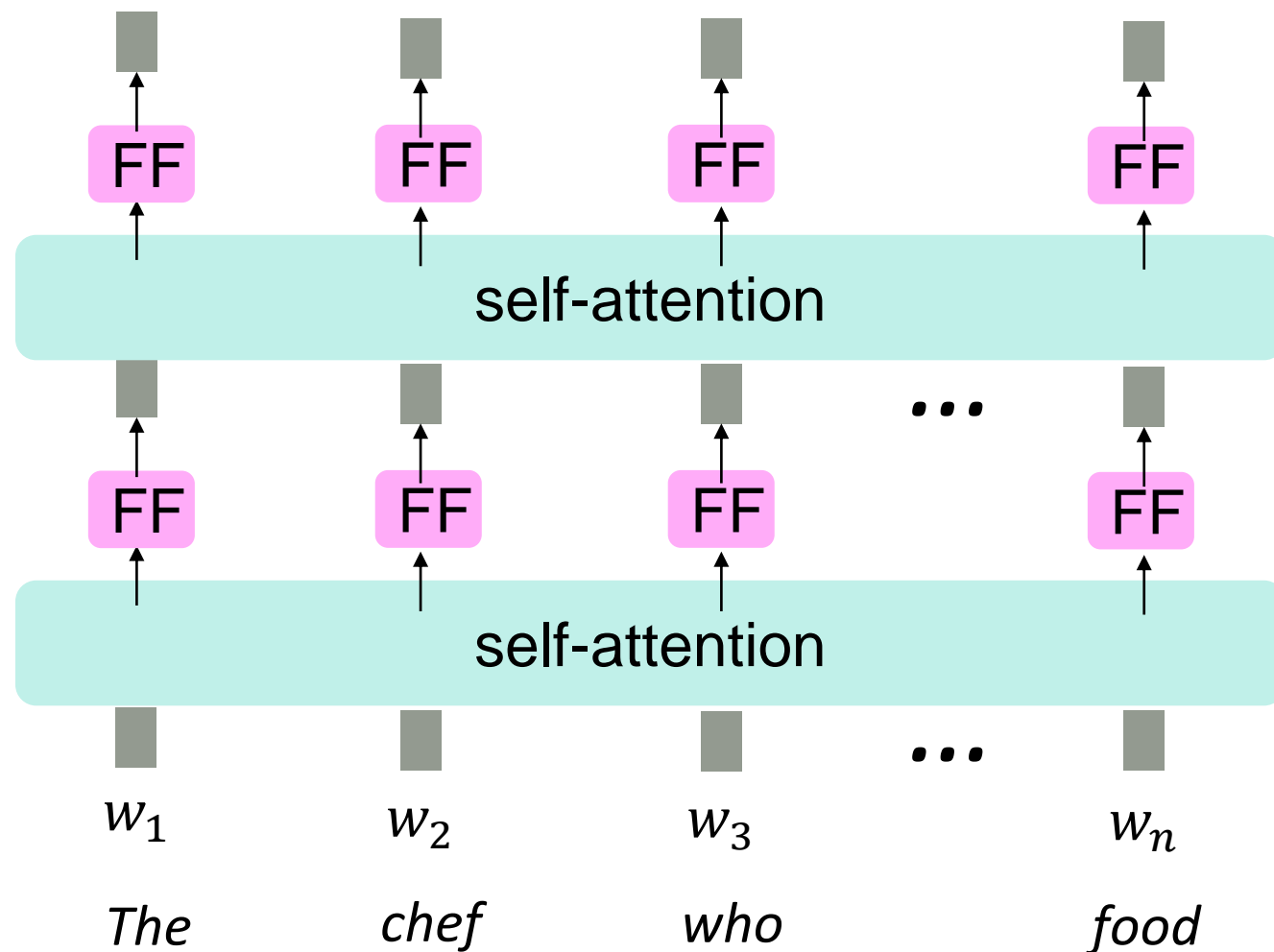
Solutions

- Add position representations to the inputs

Adding nonlinearities in self-attention

- Note that there are no elementwise nonlinearities in self-attention; stacking more self-attention layers just re-averages **value** vectors (Why? Look at the notes!)
- Easy fix: add a **feed-forward network** to post-process each output vector.

$$\begin{aligned} m_i &= MLP(\text{output}_i) \\ &= W_2 * \text{ReLU}(W_1 \text{output}_i + b_1) + b_2 \end{aligned}$$



Intuition: the FF network processes the result of attention

Barriers and solutions for Self-Attention as a building block

Barriers

- Doesn't have an inherent notion of order!
- No nonlinearities for deep learning magic! It's all just weighted averages
- Need to ensure we don't "look at the future" when predicting a sequence
 - Like in machine translation
 - Or language modeling



Solutions

- Add position representations to the inputs
- Easy fix: apply the same feedforward network to each self-attention output.

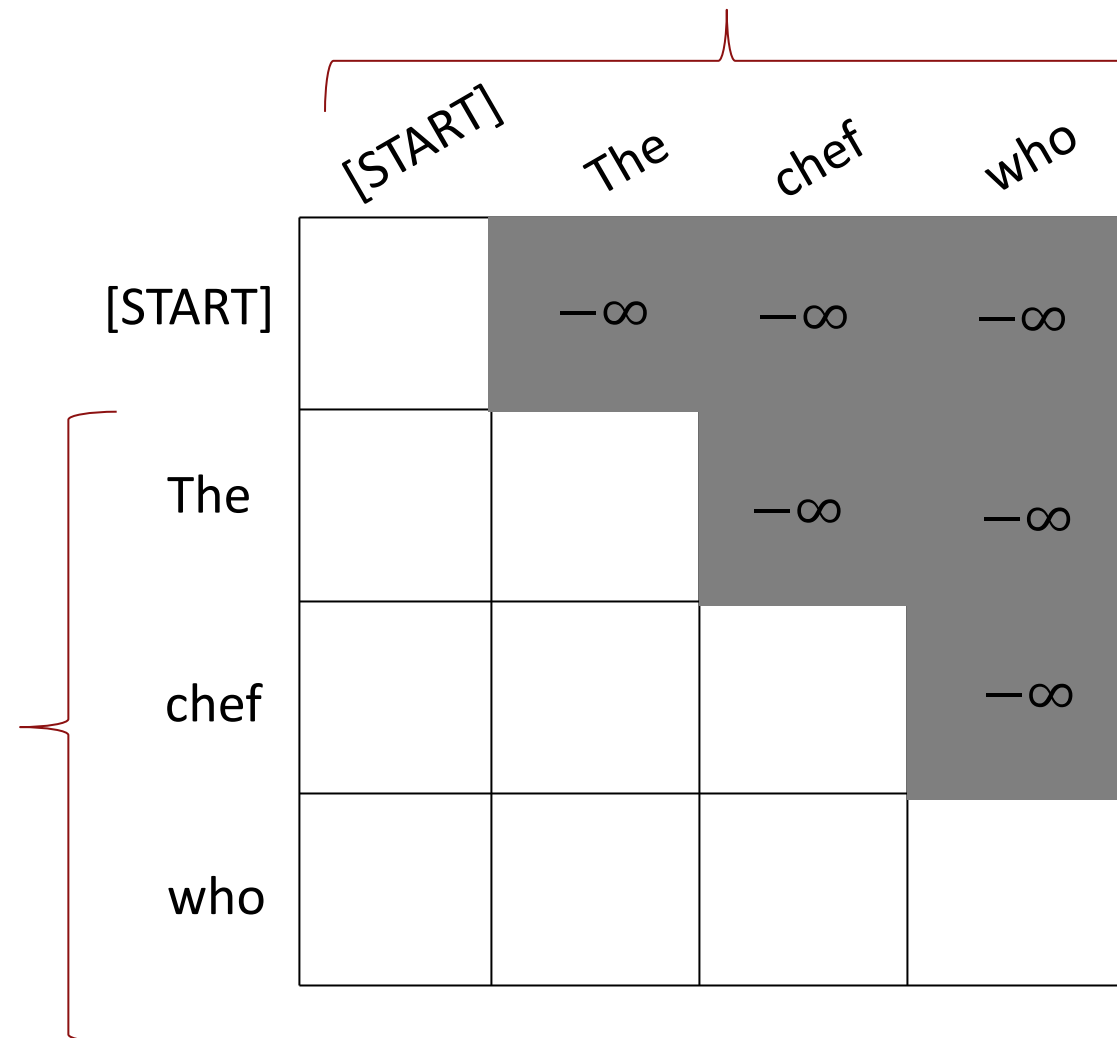
Masking the future in self-attention

- To use self-attention in **decoders**, we need to ensure we can't peek at the future.
- At every timestep, we could change the set of **keys and queries** to include only past words. (Inefficient!)
- To enable parallelization, we **mask out attention** to future words by setting attention scores to $-\infty$.

$$e_{ij} = \begin{cases} q_i^\top k_j, & j \leq i \\ -\infty, & j > i \end{cases}$$

For encoding these words

We can look at these (not greyed out) words



Barriers and solutions for Self-Attention as a building block

Barriers

- Doesn't have an inherent notion of order!
- No nonlinearities for deep learning magic! It's all just weighted averages
- Need to ensure we don't "look at the future" when predicting a sequence
 - Like in machine translation
 - Or language modeling



Solutions

- Add position representations to the inputs
- Easy fix: apply the same feedforward network to each self-attention output.
- Mask out the future by artificially setting attention weights to 0!

Necessities for a self-attention building block:

- **Self-attention:**
 - the basis of the method.
- **Position representations:**
 - Specify the sequence order, since self-attention is an unordered function of its inputs.
- **Nonlinearities:**
 - At the output of the self-attention block
 - Frequently implemented as a simple feed-forward network.
- **Masking:**
 - In order to parallelize operations while not looking at the future.
 - Keeps information about the future from “leaking” to the past.

