THE BASIC LANGUAGE OF STATISTICS

A few more terms must be defined to be able to go further in our study. We need to talk a little about variables and their types.

### Variables and Measurement

A variable is a characteristic or quality that is observed, measured, and recorded in a data file (generally, in a single column). If you need to keep track of the country of birth of the individuals in your population, you will include in your study a variable called Country of birth. You may also want to keep track of the nationality of the individuals; you will then have another variable called Nationality. The two variables are distinct, since some people may carry the nationality of a country other than the one they were born in. Here are some examples of variables used widely in social sciences:

### Socio-demographic variables

Age Sex

Religion

Level of education

Highest degree obtained

Marital status Country of birth Nationality

Mother tongue

# Psychological variables

Level of anxiety

Stimulus response time

Score obtained in a personality test

Score obtained in an aptitude test

### Economic variables

Working status

Income

Value of individual assets

Average number of hours of work

per week

## Variables that refer to units other than the individual

Number of hospitals in a country Percentage of people who can read Percentage of people who completed

high school Total population

Birth rate Fertility rate

Number of teachers per 1000 people

Number of doctors per 10,000

people

Population growth

Predominant religion

You may have noticed that some of these variables refer to qualities (such as mother tongue) and others refer to quantities, such as the total population of a country. In fact, we can distinguish two basic types of variables:

1. quantitative variables:

2. qualitative variables.

Quantitative variables are characteristics or features that are best expressed by numerical values, such as the age of a person, the number of people in a household, the size of a building, or the annual sales of a product. Qualitative variables are characteristics or qualities that are not numerical, such as mother tongue, or country of origin. The scores of the individuals of a population on the various variables are called the values of that variable.

#### Example

Suppose you have the information shown in Table 1.2 about five students in your college.

Table 1.2 Examples of qualitative and quantitative variables

Name	Age	Program of Study	Grade Point Average
John	19	Social Science	3.78
Mary	17	Pure and Applied Science	3,89
Peter	18	Commerce	
Colette	19	Office Systems Technology	3.67
Suzie	20	Graphic Design	3.90 3.82

There are three variables: Age (quantitative), Program of Study (qualitative), and Grade Point Average (quantitative).

The values, or scores, taken by the individuals for the variable Age are 17, 18, 19 (twice), and 20. The values taken for the variable Program of Study are Social Science, Pure and Applied Science, Commerce, Office Systems Technology, and Graphic Design. Qualitative variables are sometimes referred to as categorical variables because they consist of categories in which the population can be classified. For instance, we can classify all students in a college into categories according to the program of study they are in.

Careful attention must be given to the way observations pertaining to a variable are recorded. We must find a system for recording the data that is very clear, and that can be interpreted without any ambiguity. Consider, for instance, the following characteristics: age, rank in the family, and mother tongue. The first characteristic is a quantity; the second is a rank, and the third is a quality. The systems used to record our observations about these characteristics will be organized into three levels of measurement

- · measurement at the nominal level;
- · measurement at the ordinal level; and
- · measurement at the numerical scale level.

Each level of measurement allows us to perform certain statistical operations, and not others.

The nominal level of measurement is used to measure qualitative variables. It is the simplest system for writing down our observations: when we want to measure a characteristic at the nominal level, we establish a number of categories in such a way that each observation falls into one and only one of these categories. For example, if you want to write down your observations about mother tongue in the Canadian context, you may have the following categories:

- · English,
- · French.
- · Native, and
- · Other.

Depending on the subject of your research, you may have more categories to include other languages, or you may want to make a provision for those who have two mother tongues.

It is important to note that when a variable is measured at the nominal level, the categories must be

- · exhaustive, and
- mutually exclusive.

The categories are said to be **exhaustive** when they include the whole range of possible observations, that is, they exhaust all the possibilities. That means that every one of the observations can fit in one of the available categories. The categories are said to be **mutually exclusive** if they are not overlapping: every observation fits in only one category. These two properties ensure that the system used to write down the observations is clear and complete, and that there are no ambiguities when recording the observations or when reading the data file. Table 1.3 displays examples of measurements made at the nominal level.

Qualitative variables must be measured at the nominal level.

The **ordinal level of measurement** is used when the observations are organized in categories that are *ranked*, or *ordered*. We can say that one category precedes another, but we cannot say by how much exactly (or if we can, we do not keep that information). Here too the categories must be exhaustive and mutually exclusive, but in addition you must be able to compare any two categories, and say which one precedes the other (or is bigger, or better, etc.). Table 1.4 displays examples of variables measured at the ordinal level.

Table 1.3 Examples of variables measured at the nominal level

Variable	Categories used
Sex	Male Female
Place of birth	The country where the survey is counducted Abroad
Work status	Working full-time Working part-time Temporarily out of work Unemployed Retired
	Housekeeper Other

Table 1.4 Examples of variables measured at the ordinal level

Variable	Ranked Categories
Rating of a restaurant	Excellent
20	Very good
	Acceptable
	Poor
	Very poor
Rank among siblings	First child
	Second child
	etc.
Income	High
	Medium
	Low

The scale used to write down an ordinal variable is often referred to as a **Likert scale**. It usually has a limited number of ranked categories; anywhere from three to seven categories, sometimes more. For instance, if people are asked to rate a service as:

Excellent	
Very good	
Good	
Poor	
Very poor	

the proposed answers constitute a five-level Likert scale.

Another example of a Likert scale, this time with four levels, is provided by the situations where a statement is given, and respondents are asked to say whether they:

□ Totally agree
 □ Agree
 □ Disagree
 □ Totally disagree.

A variable measured at the ordinal level could be either qualitative or quantitative. In Table 1.4, the variable **Income** is quantitative, and the variable **Rating of a Restaurant** is qualitative, but they are both measured at the ordinal level. For a variable measured at the ordinal level, we can say that one value precedes another, but we cannot give an exact numerical value for the difference between them. For instance, if we know that a respondent is the first child and the other is the second child in the same family, we do not keep track of the age difference between them. It could be one year in one case and five years in another case, but the values recorded under this variable do not give us this information: they only give us the rank.

When recording information about categorical variables, the information is usually *coded*. *Coding* is the operation by which we determine the categories that will be recorded, and the codes used to refer to them. For instance, if the variable is Sex, and the two possible answers are:

Male Female,

we usually code this variable as

1 Male

2 Female.

The numbers 1 and 2 are the codes, and the categories Male and Female are the values of the variable.

When coding a variable, a code must be given to the cases where no answer has been provided by the respondent, or when the respondent refuses to answer (if the answer is judged too personal or confidential, such as the exact income of a person). We refer to these answers as *missing values* and we give them different codes. Lab 9 explains how to handle them in SPSS.

Finally, some variables are measured by a **numerical scale**. Every observation is measured against the scale and assigned a numerical value, which measures a quantity. These variables are said to be **quantitative**. Table 1.5 displays examples of numerical scale variables.

Table 1.5 Examples of variables measured at the numerical scale level

Variable	Numerical Scale	
Annual income	In dollars, without decimals (no cents)	
Age	In years, with no fractions	
Age	In years, with one decimal for fractions of a year	
Temperature	In degrees Celsius	
Time	In years. A starting point must be specified	
Annual income In dollars, to the nearest thousand		

Notice that the same variable can be measured by different scales, as shown in the examples above. So, when we use a numerical scale, we must determine the units used (for instance years or months), and the number of decimals used.

Numerical scales are sometimes subdivided into interval scales and ratio scales, depending on whether there is an absolute zero to the scale or not. Thus, temperature and time are measured by interval scales, whereas age and number of children are each measured by a ratio scale. However, this distinction will not be relevant for most of what we are doing in this course, and we will simply use the term numerical scale to talk about this level of measurement. The program SPSS that we are going to use simply uses the term scale to refer to such variables.

Most statistical software packages include more specific ways of writing down the observations pertaining to a numerical scale. For instance, SPSS will offer the possibility of specifying that the variable is a currency, or a date.

Moreover, it is also possible to group the values of a quantitative variable into classes. Thus, when observing the variable age, we can write down the exact age of a person in years, or we can simply write the age group the person falls in, as is done in the following example:

- 18 to 30 years
- 31 to 40 years
- 41 to 50 years
- 50 to 60 years
- Over 60.

When we group a variable such as age into a small number of categories as we have just done, we must code the categories as we do for categorical variables. For example,

- 1 would stand for the category 18 to 30 years
- 2 would stand for the category 31 to 40 years etc.

In such situations, we cannot perform the same statistical operations that we do when the values are not grouped. For instance, the mean, or average of the variable age is best calculated when the ages are not grouped. When we group the values, it is because we want to know the relative importance (that is, the frequency, in percentage) of one group as compared to the others. The information that 50% of the population is under 20 years old in some developing countries is obtained by grouping the ages into 20 years old or less and more than 20 years old. When we collect the data, it is always better to collect it in actual years, since we can easily group it later on in the data file with the help of a statistical software package. In this case, a new column is added to the data file, and it contains the grouped data of the quantitative variable. For example, in the GSS93 subset data file that we use in the SPSS labs, you will find two variables for age: one is called age, and the other one is called agecat4. The latter is calculated from the former, by grouping individuals into four age groups. In the column of agecat4, the specific age of an individual is not recorded: only the age group of the individual is recorded.

Finally, numerical scales can be either **continuous** or **discrete**. A scale is said to be *continuous* if the observations can theoretically take any value over a certain range, including fractions of a unit. For instance, age, weight, length are continuous variables because they are not limited to specific values, and they can take any value within a certain range. A variable is said to be *discrete* if it can take only a limited number of possible values, but not values in between. For instance, the variable *Number of children* is measured by a discrete scale because it can only be equal to a whole number: 0, 1, 2, etc.

### Importance of the Level of Measurement

The level of measurement used for a variable depends on whether it is qualitative or quantitative.

Qualitative variables must be measured at the nominal or ordinal level. They cannot be measured at the numerical scale level, even when their categories are coded with numbers. For instance, as shown above, we usually code the variable Sex as follows:

- 1 Male
- 2 Female

In this case, the numbers 1 and 2 have no numerical value. They are simply codes. It is shorter to write 1 than male, and we could have assigned the numbers differently. If you ask SPSS to compute the mean (or average) for a variable coded in this way, you will get a numerical answer. But you must always keep in mind that such a numerical answer is totally meaningless because the level of measurement

of that variable is nominal. The numbers used to record the information are simply codes.

Quantitative variables are usually measured by a numerical scale, but they could be measured at the ordinal level also. For instance, if you have the annual income of an individual, you may treat it as a numerical scale, but you could also group the values into Low, Medium and High income and treat the variable at the ordinal level.

When you perform a statistical analysis of data, it is very important to pay attention to the level of measurement of each variable. Some statistical computations are appropriate only to a given level of measurement, and should not be performed if the variable is measured at a different level.

## Concepts, Dimensions, and Indicators

We often want to observe social phenomena that are too abstract and complex to be expressed by a single variable. Suppose for instance that we want to observe and measure the degree of religious inclination (or the tendency of a person towards religion) in a given social group. Religious inclination can be manifested in many ways: people may have or not have certain beliefs about their religion; they may also perform or not certain rituals such as attending religious services, fasting, praying, etc.; they may also seek the advice of the religious leadership on important decisions, or ignore such leadership; finally, they may seek to look at everything from the point of view of religion, and apply the teachings of their religion in their daily lives, or ignore them. All these aspects are not found all the time in all individuals. Some individuals may have strong beliefs, while avoiding the religious services. Other may attend all services while being skeptical about some of the religious dogma. The way to handle this complexity is to subdivide the concept of religious inclination into dimensions, which are themselves measured by several indicators. If we were to study religious inclination in the Catholic religion, we would get a set of dimensions and indicators that would look as in Table 1.6 (we are simplifying the issues a little, of course).

The items listed on the right-hand side of Table 1.6 are indicators of the concept of religious inclination. None of them, taken alone, is a measure of religious inclination, but each of them constitutes one aspect of it. Indicators that are seen as similar are grouped together to form one dimension of the concept. And finally the various dimensions, taken together, capture the concept as a whole. This way of breaking down a complex concept into dimensions and indicators is called the operationalization of the concept. As an illustration, we may want to see how economists operationalize the concept of cost of living. They estimate the average cost of most of the standard expenses a family of four is expected to incur. The various expenses are divided into main dimensions such as food, housing, transportation, education, and leisure. Each dimension is then subdivided into smaller dimensions; themselves subdivided further until indicators are reached. For instance, food is

Table 1.6 Example of how a concept can be broken down into dimensions and indicators

Concept	Dimensions	Indicators
	1. Beliefs	Belief in God
		Belief in the Holy Trinity
		Belief in the main dogma
		etc.
RELIGIOUS	II. Rituals	Attendance of services
INCLINATION		Performing prayers
		Baptizing children
		etc.
	III. Guidance	Consulting the priest about important decisions Consulting the official opinions of the church on
	**********	certain issues such as birth control etc.
	IV. Daily life	Being kind and generous to people
		Not cheating others in commercial transactions
		etc.

broken down as: meat, vegetables, milk products, etc., themselves subdivided into specific items such as: tomatoes, lettuce, etc. Finally, for each of these indicators, the increase or decrease in the cost of living is measured against the corresponding cost in some year, called the base year. By combining these indicators, economists are able to measure how the cost of living has changed, on the average, for a family of four.

The way a concept is broken down, or operationalized, into dimensions and indicators depends on the theoretical framework adopted for a study. Researchers may not agree on how to operationalize a concept, and you will find in the literature different studies that operationalize concepts in completely different ways, because they rely on different theoretical frameworks.

### Summary

Quantitative methods are procedures and techniques for collecting, organizing, describing, analyzing, and interpreting data. In this chapter we have learned the basic vocabulary used to talk about quantitative methods. Data is organized into electronic data files with the help of statistical packages. A data file contains the values taken by a number of cases (which are the units of the population under study) over some variables. Every row represents a case, while every column represents a variable. The units in the data file usually form a sample, which is itself a subset of the whole population. Sometimes, the data file refers to the whole population.

The variables can be either qualitative or quantitative. The system used to record the information is called a measurement scale. There are three levels of measurement: nominal, ordinal and numerical (interval or ratio). The level of measurement of a variable will determine what statistical procedures can be performed, and what kind of graphs must be used to illustrate the data. When a concept is complex, it is not measured directly. It is usually broken down into dimensions and indicators, which are then combined to provide a single measure.

The statistical procedures themselves fall into two broad categories: descriptive statistics and inferential statistics. Descriptive statistical techniques aim at describing the data by summarizing it, while inferential statistical techniques aim at generalizing to a whole population what has been observed on a sample.

## Keywords

Students should be able to define and explain all the following terms.

Data	Case	Continuous numerical scales
Data file	Unit	Discrete numerical scales
Quantitative methods	Sample	Codes
Variable	Population	Coding
Variable label	Level of measurement	Codebook
Value	Nominal level	Statistics (the two meanings)
Value label	Ordinal level	Descriptive statistics
Variable type	Numerical level (interval or ratio)	Inferential statistics
Quantitative variable	Exhaustive categories	Dimensions of a concept
Qualitative variable	Mutually exclusive categories	Indicators of a concept
	Likert scale	Operationalization of a concept

## Suggestions for Further Reading

Blalock Jr., Hubert M. (1982) Conceptualization and Measurement in the Social Sciences. London; Sage Publications.

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