

ESS418 Research Methods in Social Science

Assignment 1: Qualitative Comparative Analysis

Submit due to: 30. 11. 2015

Student's name:

1) What distinguished set-theoretical methods from non-set-theoretical methods?

Set – theoretical methods are approaches to analyzing social reality which

- A) The data consists of set membership scores
- B) Relations between social phenomena are modeled in terms of set relations; and
- C) The results point the sufficient and necessary condition and emphasize causal complexity in terms of INUS and SUIN causes

See introduction, section “Set - theoretic approaches in the social sciences” (definition on p. 6);

2) In fuzzy set analysis, a truth table is produced based on fuzzy data. What does it mean when we say that a given truth table row contains x number of cases?

If a truth table row based on fuzzy sets has the outcome $Y=1$, it means that each case's membership in it is smaller than or equal to its membership in Y . Thus, the respective row is a subset of the outcome fulfilling the criterion of a sufficient condition.

3) Perform Boolean multiplication for the following pairs of expressions and simplify

the result:

a) $(A + B) * (A * B) = AB(A + B) = AAB + ABB = AB + AB = AB$

b) $(A + B) * (A + B + C) = AA + AB + AC + BA + BB + BC = A + AB +$

$AC + AB + B + BC = A + B$ (AB, AC, BC are sub-sets of A or of B)

c) $(A * B) * (\sim A * \sim B) = AB\sim A\sim B = \text{contradiction in itself}$

$$d) (A * (B+C)) * (B * (\sim A + C)) = (AB + AC) * (\sim AB + BC) = AB\sim AB + ABBC + AC\sim AB + ACBC = ABC + ABC = ABC$$

- 4) A case has a membership of 1 set A, 0 in set B, 0.6 in set C, 0.9 in set D, and 0.1 in set E. Calculate its membership in the following Boolean expressions:

$$a) A + B + D = \max (A, B, D) = \max (1, 0, 0.9) = 1$$

$$b) (A*B) + (C*\sim D) = \max (A*B, C*\sim D) =$$

$$\max (\min (A, B), \min (C, \sim D)) =$$

$$\max (\min (A, B), \min (C, 1 - D)) =$$

$$\max (\min (1, 0), \min (0.6, 1 - 0.9)) =$$

$$\max (\min (1, 0), \min (0.6, 0.1)) =$$

$$\max (0, 0.1) = 0.1$$

$$c) \sim(A*\sim B + \sim C + D*E) = 1 - \max (A*\sim B, \sim C, D*E) =$$

$$1 - \max (\min (A, \sim B), \sim C, \min (D, E)) =$$

$$1 - \max (\min (A, 1 - B), 1 - C, \min (D, E)) =$$

$$1 - \max (\min (1, 1 - 0), 1 - 0.6, \min (0.9, 0.1)) =$$

$$1 - \max (\min (1, 1), 0.4, \min (0.9, 0.1)) = 1 - 1 = 0$$

$$d) \sim((A*\sim B + \sim C) + (D*E)) = 1 - \max (A*\sim B + \sim C, D*E) =$$

$$1 - \max (\max (A*\sim B), \sim C), \min (D, E)) =$$

$$1 - \max (\max (\min (A, \sim B), \sim C), \min (D, E)) =$$

$$1 - \max (\max (\min (A, 1 - B), 1 - C), \min (D, E)) =$$

$$1 - \max (\max (\min (1, 1 - 0), 0.4), \min (0.9, 0.1)) =$$

$$1 - \max (\max (\min (1, 1), 0.4), 0.1) =$$

$$1 - \max (\max (1, 0.4), 0.1) =$$

$$1 - \max (1, 0.1) =$$

$$1 - 1 =$$

$$0$$

- 5) Minimize the following primitive expressions. Are there any logically redundant prime implicants?

$(A\sim B\sim C) + (A\sim BC) + (\sim A\sim B\sim C) + (\sim AB\sim C).$

$\sim B\sim C + A\sim B + \sim AB\sim C$

$A\sim B + \sim B\sim C + \sim A\sim C.$ Yes, $\sim B\sim C$ is logically redundant.