



The background features a schematic diagram of blood circulation. A central vessel is shown with red blood cells. Arrows indicate the flow of blood. On the left, a vessel is labeled with CO_2 , indicating it carries deoxygenated blood. On the right, a vessel is labeled with O_2 , indicating it carries oxygenated blood. Below the vessel, several cells are depicted. Arrows show CO_2 moving from the cells into the vessel and O_2 moving from the vessel into the cells. The text 'Rheology of blood circulation' is centered in a yellow-to-orange gradient oval.

Rheology of blood circulation

The background of the slide is a dark red color with a faint, repeating pattern of a blood vessel. The vessel is shown in cross-section, with a central lumen and surrounding tissue. Several chemical formulas are scattered across the image: CO₂ appears in the upper and lower regions, while O₂ is located in the middle-right area. The text is centered in a white rectangular box with a slight gradient.

1. Basic physical laws of liquids

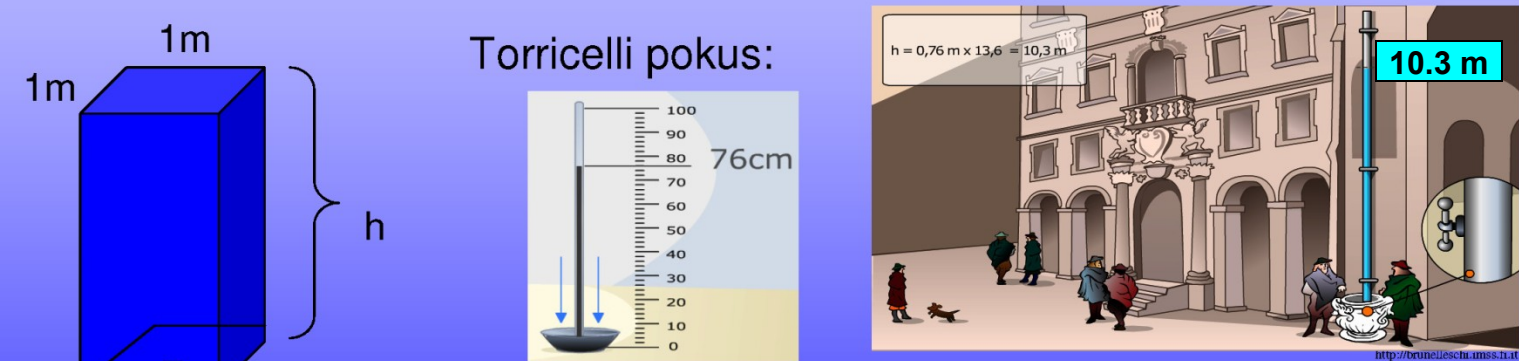
Law of Pascal

Liquid column causes a pressure (hydrostatic pressure) that is directly proportional to the height of the liquid column (h), density of the liquid (ρ) and gravitational acceleration (g).



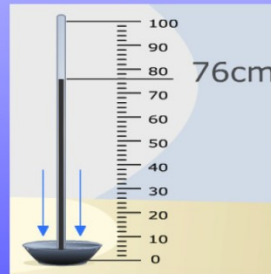
$p = h \cdot \rho \cdot g$

- h = height
- ρ = density
- g = gravitational acceleration




1m
1m
h
Pa

Torricelli pokus:



100
90
80
76cm
70
60
50
40
30
20
10
0
Hg



$h = 0,76 \text{ m} \times 13,6 = 10,3 \text{ m}$
10.3 m
H₂O
<http://brunelleschi.uniss.it>

Pa

mm Hg

mm H₂O

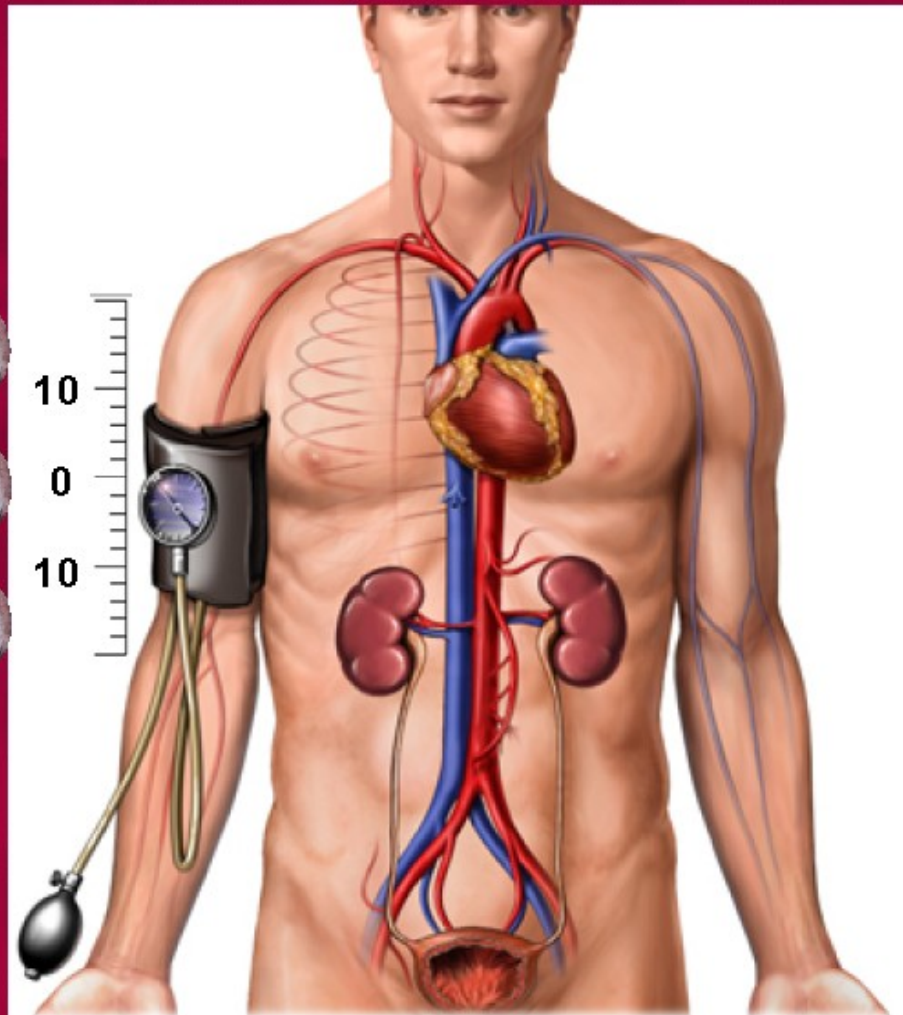
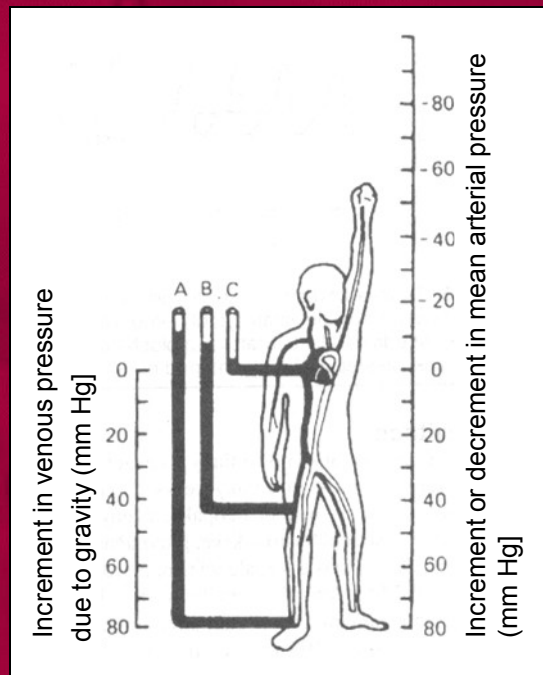
133,322 Pa = 1 mm Hg

760 mmHg = 1 atm = 10.3 m H₂O

Effect of gravity on arterial and venous pressure

Per each 10 cm

$$\Delta p = \Delta h \cdot \rho_{krve} \cdot g = 0,1 \cdot 1\,065 \cdot 9,81 \\ = 1\,045 \text{ Pa} = \mathbf{7.8 \text{ mm Hg}}$$



Law of Laplace

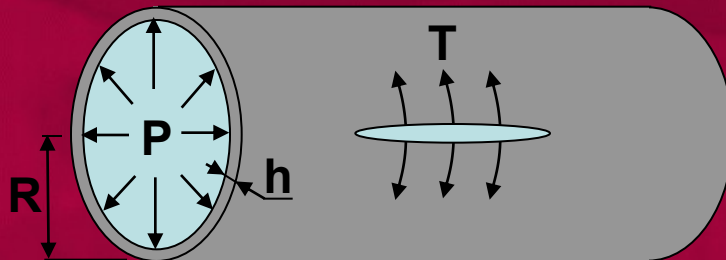
Relation between distending pressure (P [N/m^2]) and tension in the wall of hollow object (T [N/m]):

$$T = \frac{P}{\left(\frac{1}{R_1} + \frac{1}{R_2}\right)}$$

R_1 and R_2 are the biggest and the smallest radii of curvature

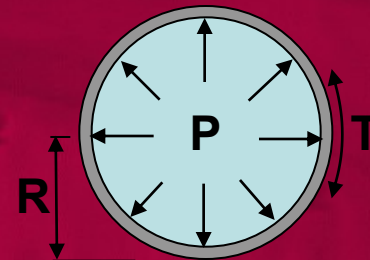
For vessel:

$$R_2 = \infty \quad T = P \cdot R$$



For sphere:

$$R_1 = R_2 \quad T = P \cdot R/2$$



Considering thickness of vessel wall (h [m]): $T = P \cdot R/h$ [N/m^2]

Characteristics of vessels

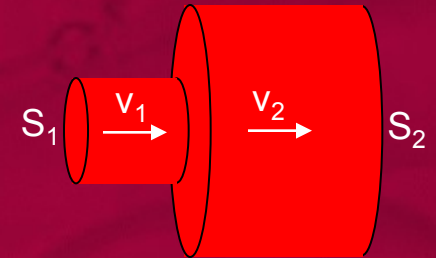
	P	R	P·R	h	P·R/h
vessel	P [kPa]	radius	tension (N/m)	wall thickness	tension (N/m ²)
aorta	13,3	13 mm nebo méně	170	2 mm	85000
arteries	12	5 mm	60	1 mm	60000
arterioles	8	150–62 μm	1,2–0,5	20 μm	40000
capillaries	4	4 μm	$1,6 \cdot 10^{-2}$	1 μm	16000
venules	2,6	10 μm	$2,6 \cdot 10^{-2}$	2 μm	13000
veins	2	200 μm a více	0,4	0,5 mm	800
vena cava	1,33	16 mm	21	1,5 mm	14000

Continuity equation

The volume of fluid flowing through a tube (vessel) per unit of time (Q [l/s]) is constant.

$$Q = S_1 \cdot v_1 = S_2 \cdot v_2 = \text{constant}$$

v – velocity S – area



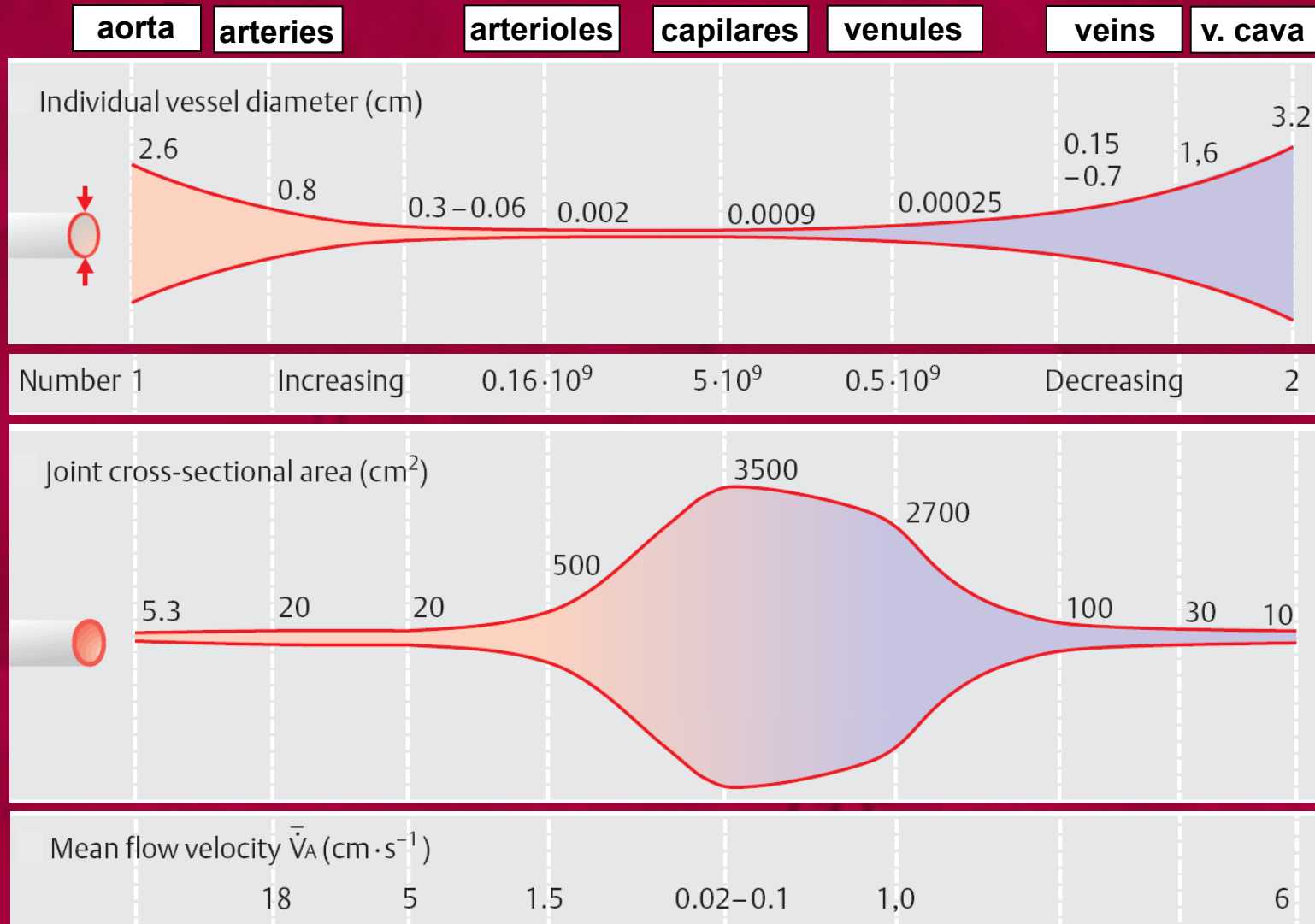
Average blood velocity in vessels

$$v = \frac{Q}{S}$$

$$Q_{rest} \approx 5.6 \text{ l/min}$$

vessel	diameter	number	total area	velocity
aorta	2.6 cm	1	5.3 cm ²	~ 18 cm/s
arterioles	20-50 μm			~ 1.5 cm/s
capillaries	4-9 μm	5×10 ⁹	2000 cm ²	~ 0.04 cm/s
venules				~ 1 cm/s
vena cava		2		~ 7 cm/s

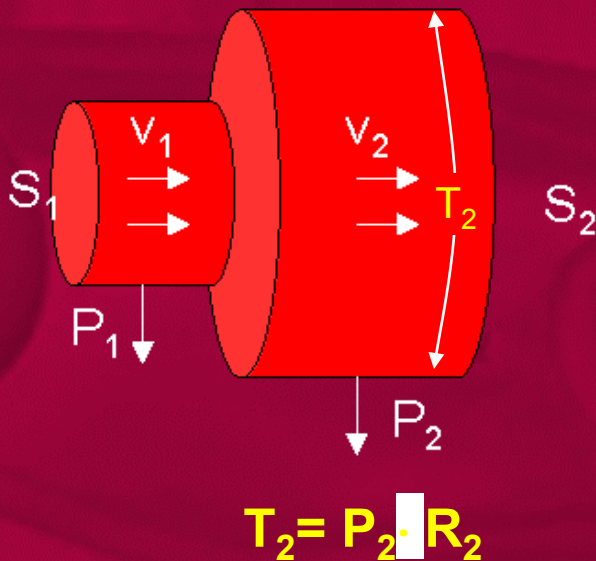
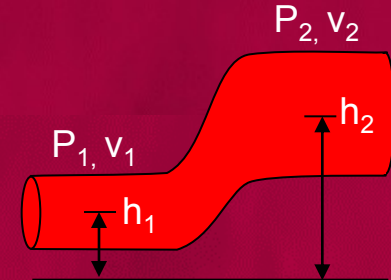
Relation between total cross-sectional area of vessels and mean blood flow velocity



Bernoulli's principle

Law of energy conservation for fluid :

$$\frac{1}{2} \rho v^2 + h \cdot \rho \cdot g + P = \text{constant}$$



Implication for aortic aneurysm

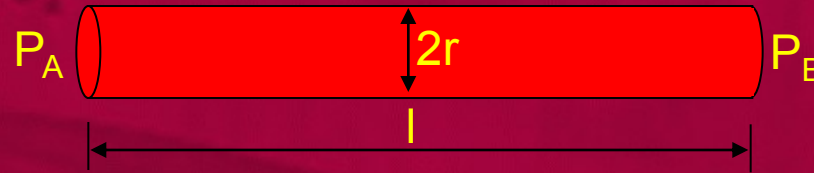
$S_1 v_1 = S_2 v_2$ a je-li $S_1 < S_2$, musí platit: $v_1 > v_2$

$$\frac{1}{2} \rho v_1^2 + \cancel{h \cdot \rho \cdot g} + P_1 = \frac{1}{2} \rho v_2^2 + \cancel{h \cdot \rho \cdot g} + P_2$$

$$\frac{1}{2} \rho v_1^2 + P_1 = \frac{1}{2} \rho v_2^2 + P_2$$

For $v_2 < v_1 \Rightarrow P_2 > P_1$

Poiseuille – Hagen equation



$$Q = \frac{\pi \cdot \Delta P \cdot r^4}{8 \cdot l \cdot \eta}$$

The flow of liquid in the cylindrical tube (Q) is directly proportional to the pressure difference between two ends of the tube ($\Delta P = P_A - P_B$), to the fourth power of the tube radius (r) and inversely proportional to tube length (l) and to the viscosity of liquid (η)

Limitation:

- For stationary flow in Newtonian fluids where viscosity is constant and independent on flow velocity.

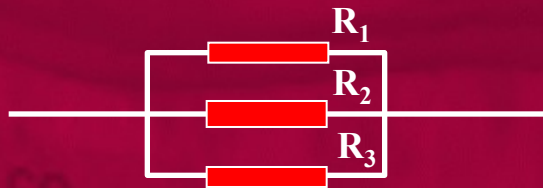
$$Q = \frac{\pi \cdot \Delta P \cdot r^4}{8 \cdot l \cdot \eta}$$

$$Q = \frac{\Delta P}{R_v}$$

Vascular resistance (R_v): a consequence of the friction between fluid and vessel wall.

$$R_v = \frac{\Delta P}{Q} = \frac{8 \cdot l \cdot \eta}{\pi \cdot r^4}$$

Parallel arrangement of vessels



$$\frac{1}{R_c} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$$

pro $R_1=R_2=R_3=R_n$

$$R_c = R/n$$

Series arrangement of vessels

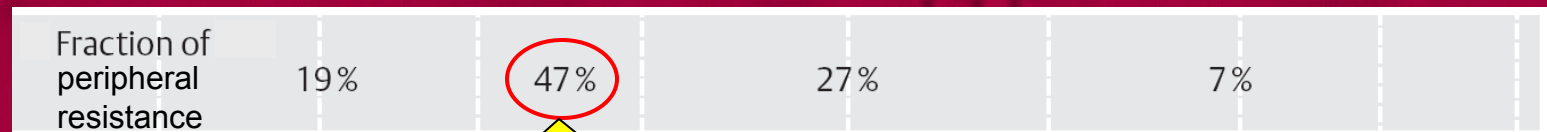
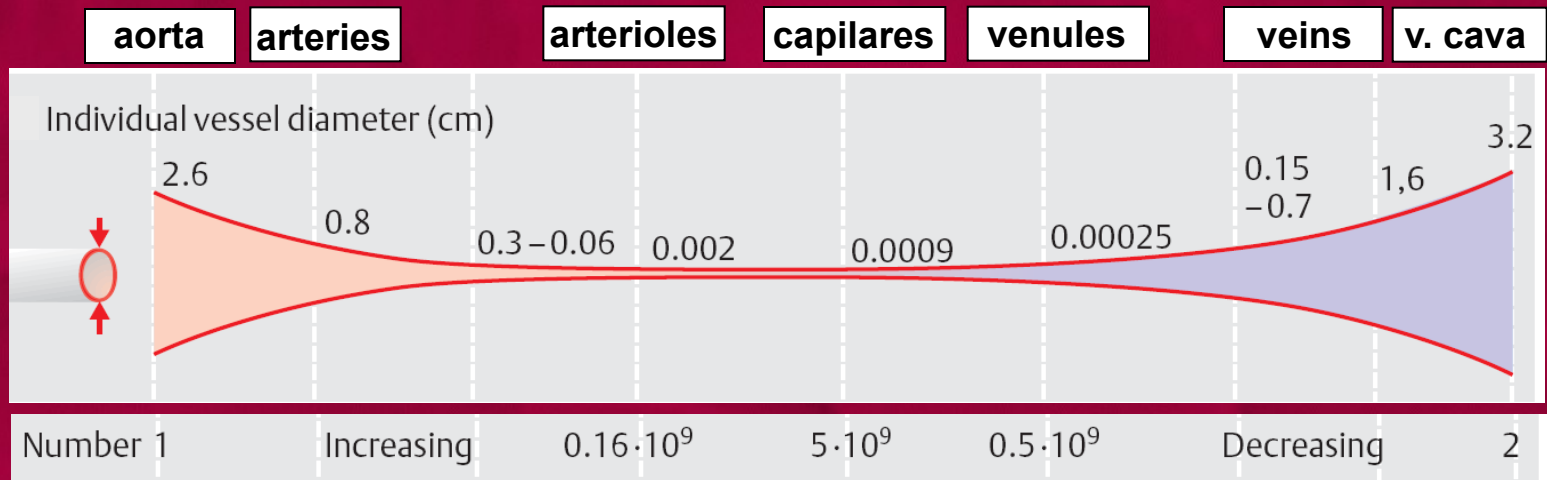


$$R_c = R_1 + R_2 + \dots$$

pro $R_1=R_2=R_3=R_n$

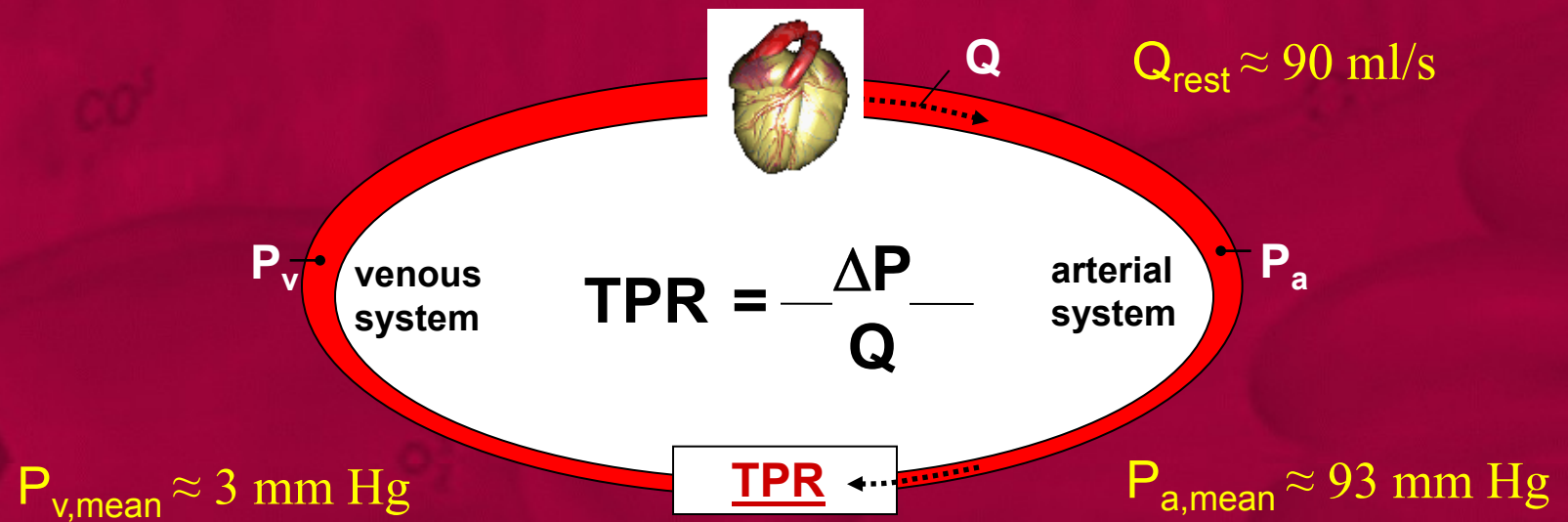
$$R_c = R \cdot n$$

Relation between vessel radius and peripheral resistance



highly variable

Total peripheral resistance (TPR) of vascular system



$$TPR = \frac{\Delta P}{Q} = \frac{P_a - P_v}{Q} \approx \frac{P_a}{Q} = \frac{93}{90} \approx 1 \frac{\text{mmHg s}}{\text{ml}}$$

For constant Q: \square PR \square P_a \square hypertension, ... cardiac disease.

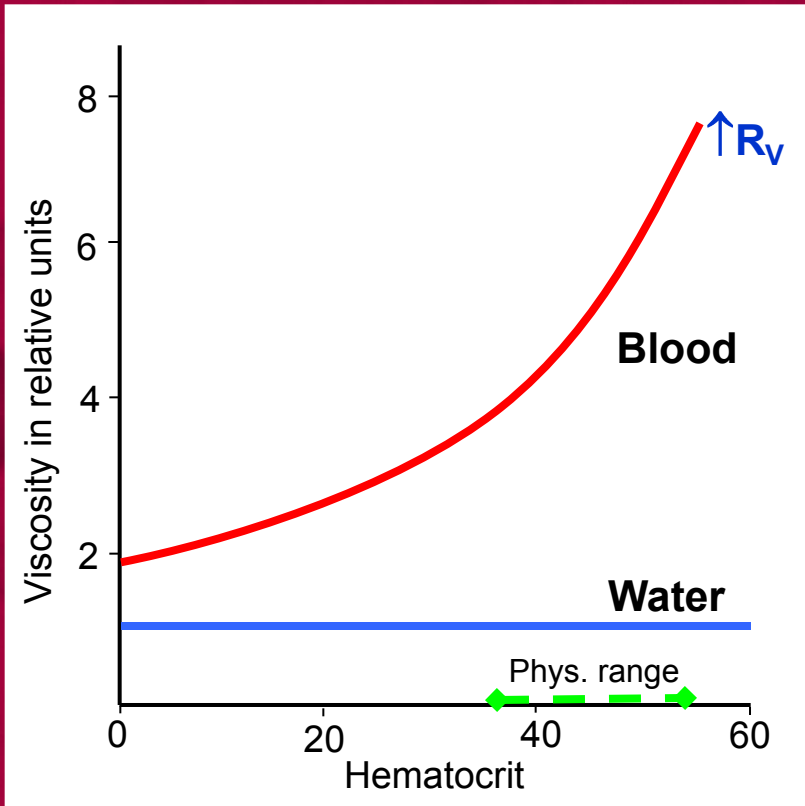
The background features a faint, light-colored diagram of a blood vessel. The vessel is shown in cross-section with a wavy, undulating wall. Several labels are scattered around the vessel: 'CO₂' appears in the upper left, upper right, and lower left areas, while 'O₂' is located in the upper right area. The entire background is a solid, deep red color.

2. Rheological features of blood and vessels

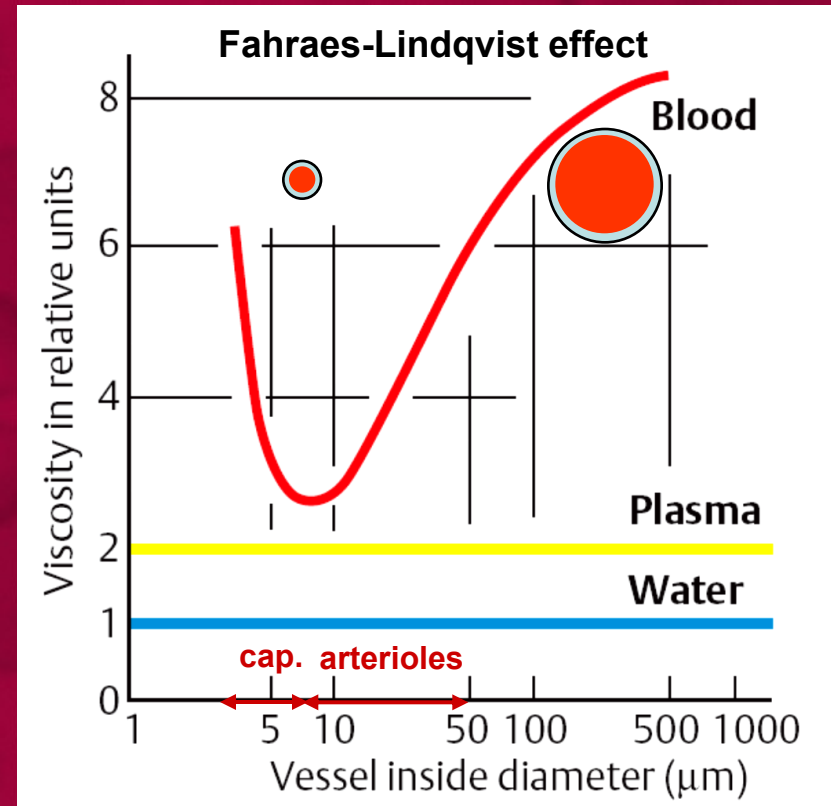
Blood viscosity

$$R_v = 8 \cdot l \cdot \eta / (\pi \cdot r^4)$$

Effect of hematocrit



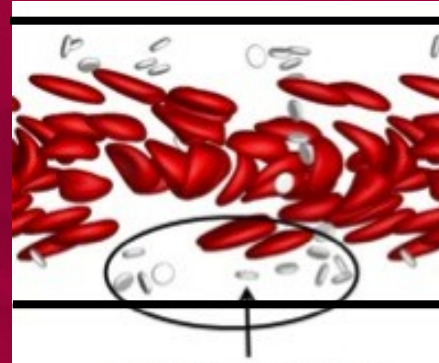
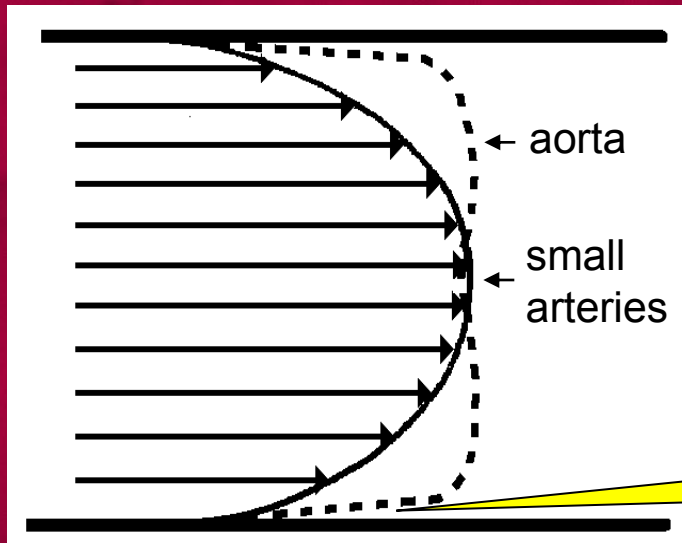
Effect of diameter in small vessels



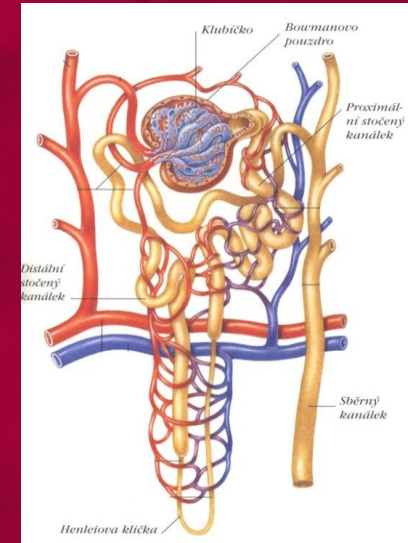
Other factors causing increase of viscosity:

- decrease of blood flow velocity
- elevation of plasma proteins

Velocity profile of the blood flow in vessels



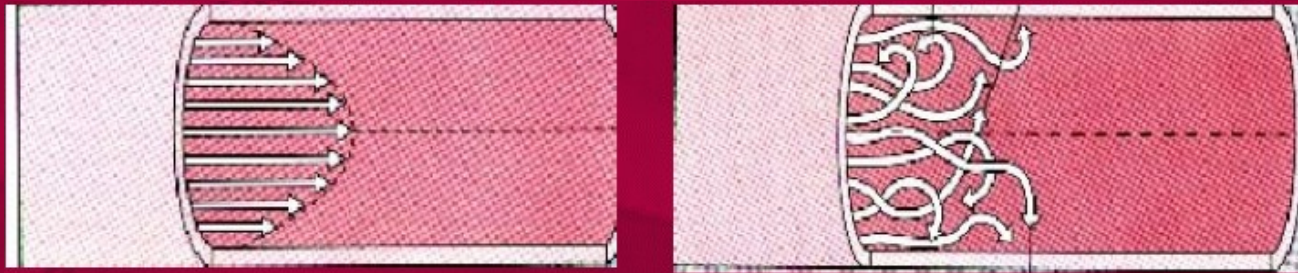
plasma-skimming



- In small arteries the velocity profile of the flowing blood has a parabolic shape. In the bigger arteries it has a piston shape.
- The layer close to vessel wall is poor of erythrocytes.

Laminar and turbulent flow

Velocity profile in laminar and turbulent flow



The character of the flow is determined by Reynolds number

$$R_e = \frac{v \cdot \rho \cdot r}{\eta}$$

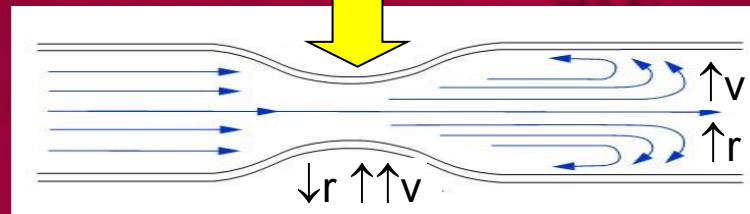
laminar flow

$Re < 2000$

turbulent flow

$Re > 3000$

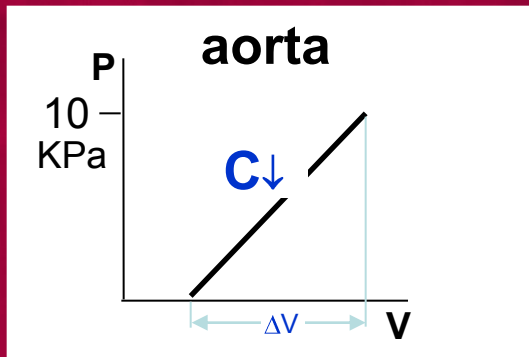
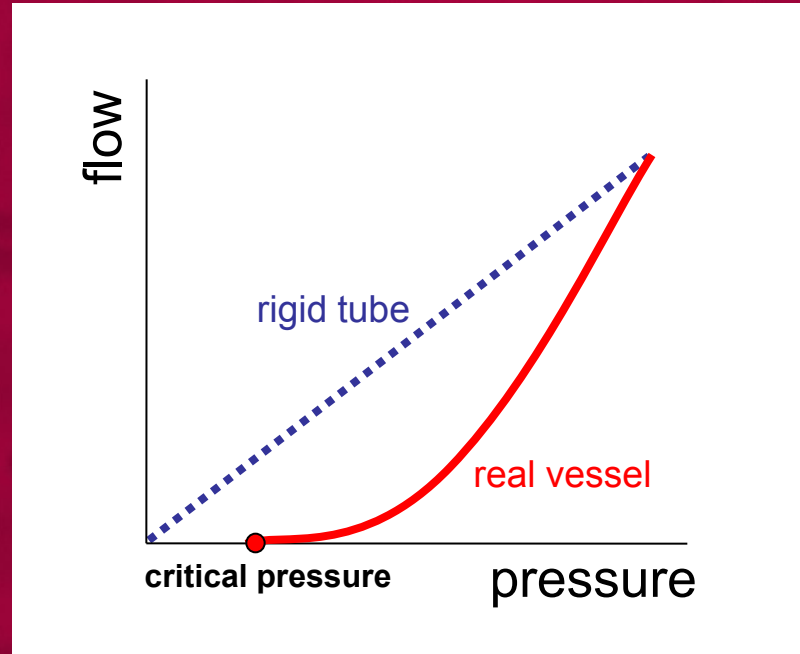
Sudden change of vessel diameter



$$\uparrow R_e \Rightarrow R_v$$

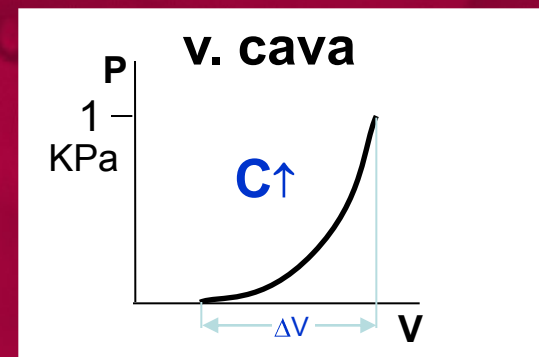
Pathological states causing turbulent flow: aneurisma, stenosis, arteriosclerosis, decreased blood viscosity, .

Elasticity of vessels

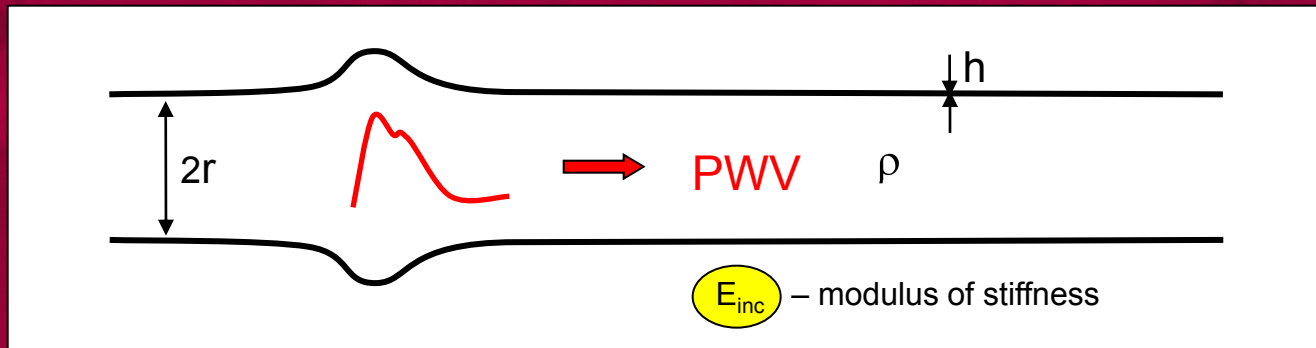


compliance

$$C = -\frac{\Delta V}{\Delta P}$$



Pulse wave velocity (PWV)

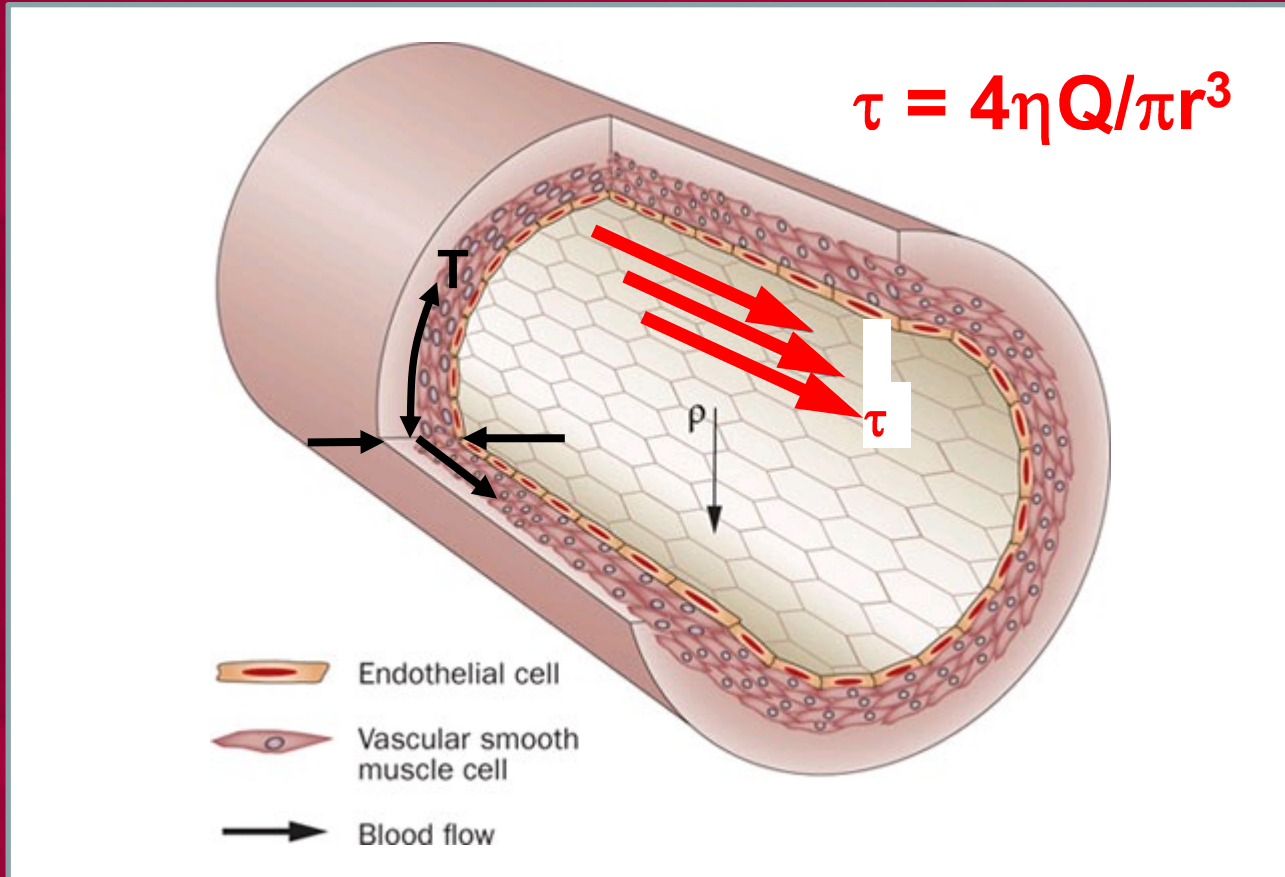


Moens-Korteweg (1878)

$$PWV = \sqrt{\frac{E_{inc} \cdot h}{2 \cdot r \cdot \rho}}$$

In aorta $PWV = 4 - 6 \text{ m/s}$

Share stress in vessel wall

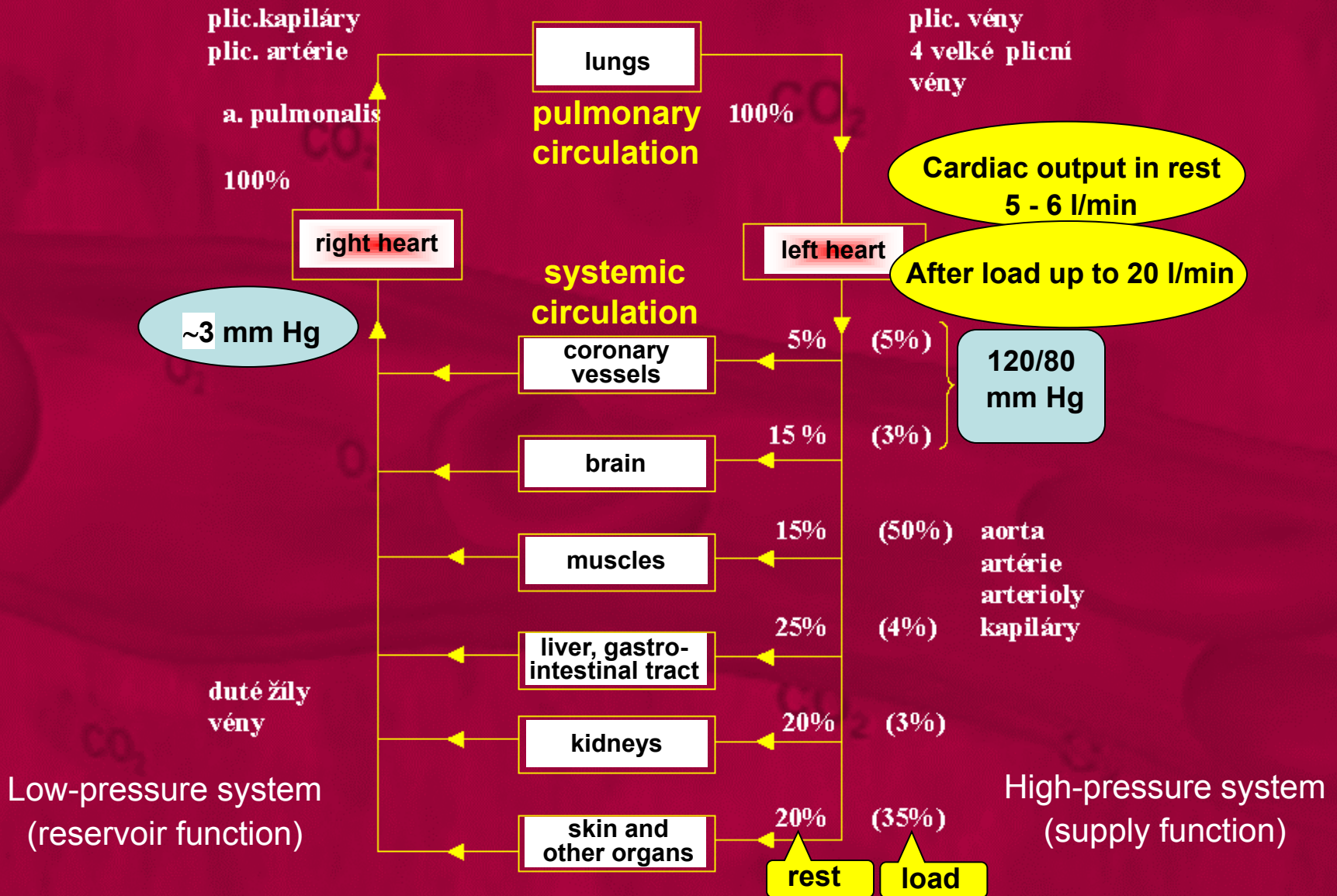


- Share stress in vessel wall may lead to a tear in endothelial layer and to arterial dissection.

The background features a faint, light-colored diagram on a dark red background. It depicts a network of blood vessels (arteries and veins) and several cells. Arrows indicate the flow of blood and the exchange of gases: CO₂ is shown moving from the cells into the blood, and O₂ is shown moving from the blood into the cells. The diagram is semi-transparent and serves as a thematic backdrop for the text.

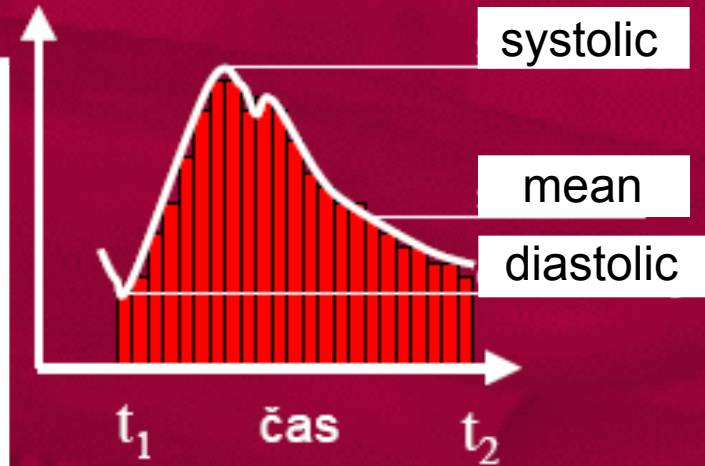
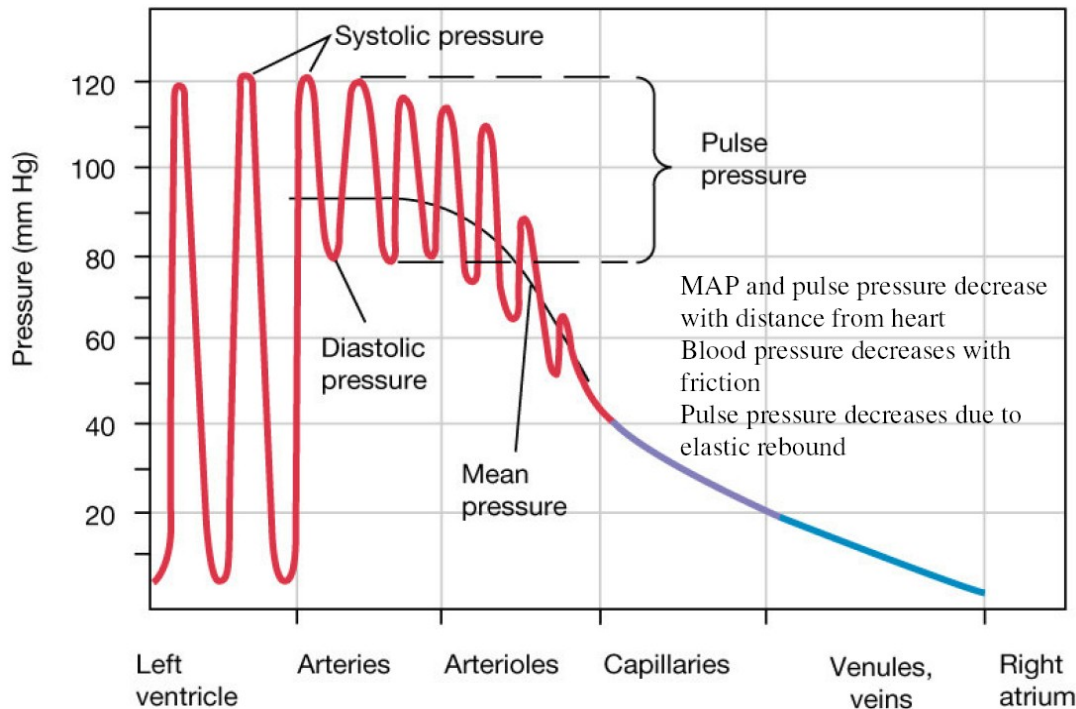
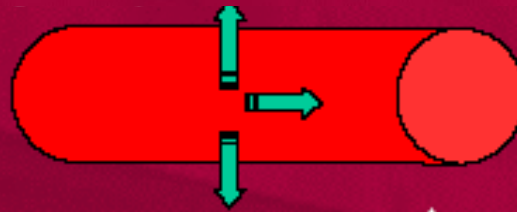
3. Blood circulation and pressure

Blood circulation



Blood pressure

Blood pressure (BP) is the pressure exerted by circulating blood upon the walls of blood vessels.

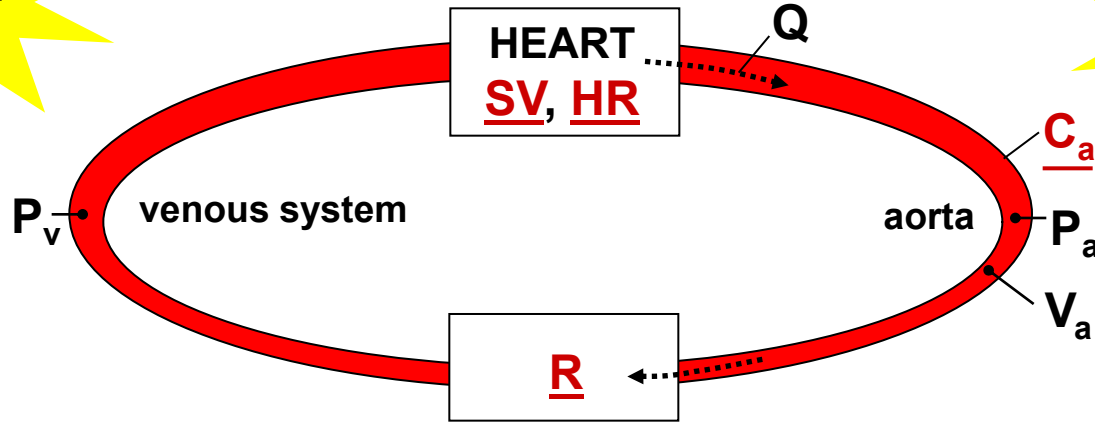


$$P_{mean} = \int_{t_1}^{t_2} \frac{P dt}{t_2 - t_1}$$

$$P_{mean} \cong Pd + \frac{1}{3}(Ps - Pd)$$

Dependence of blood pressure on cardiac output and vascular parameters

$$Q = \frac{\Delta P}{R}$$



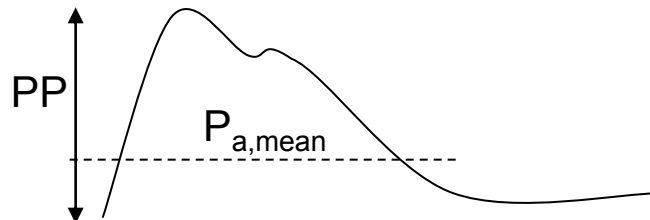
$$C = \frac{\Delta V}{\Delta P}$$

$$P_{a,mean} - P_{v,mean} = Q \cdot R$$

$$\Delta V \cong SV$$

$$P_{a,mean} = SV \cdot HR \cdot R + P_{v,mean}$$

$$P_{a,mean} \cong SV \cdot HR \cdot R$$



$$PP \cong \frac{SV}{C}$$

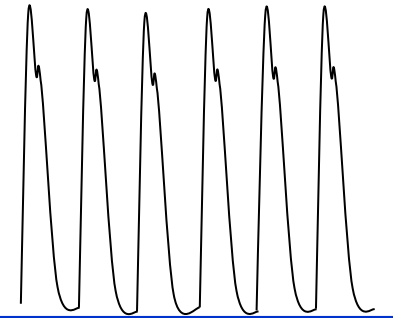
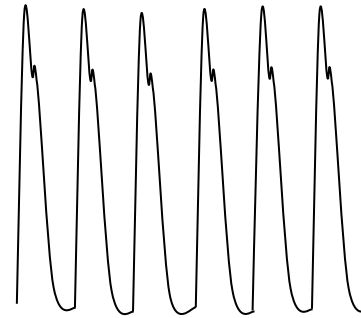
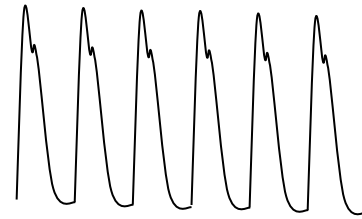
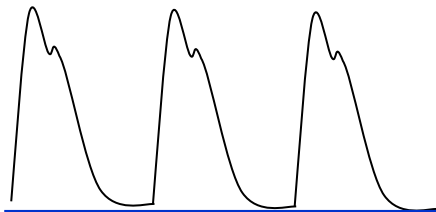
resting state

activity

+SV↑

HR↑

+R↓



$$P_{a, \text{mean}} \approx SV \cdot HR \cdot R$$

$$PP \approx \frac{SV}{C}$$

Model of blood pressure changes in aorta

