

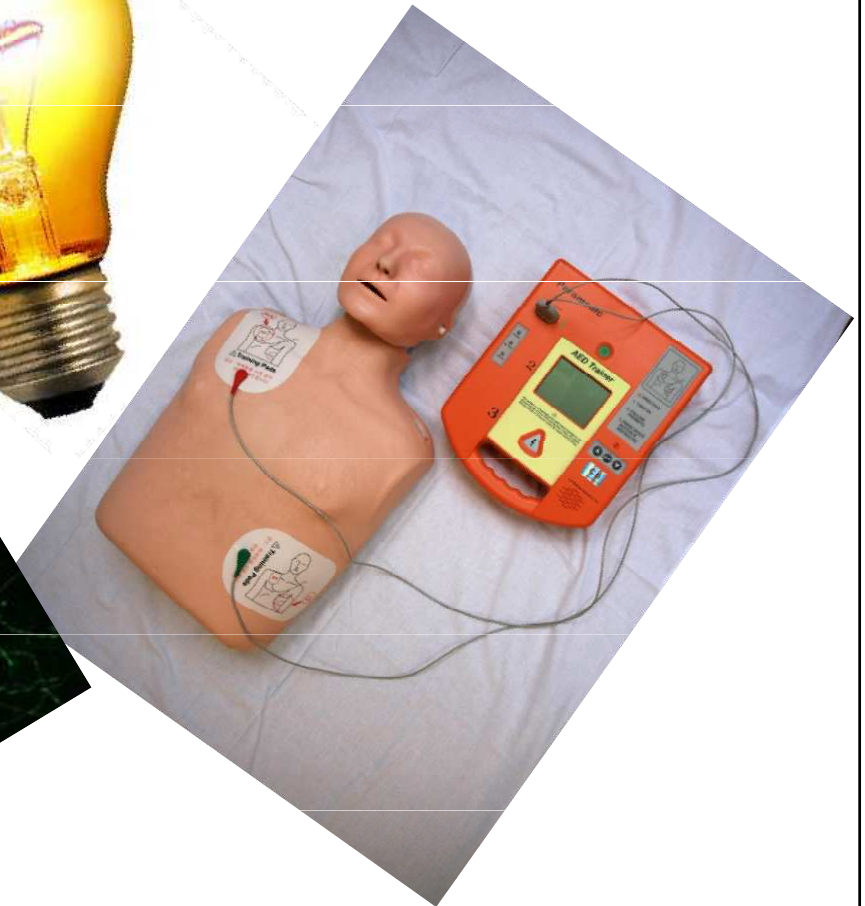
Electricity

Electric charge and Coulomb law

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Theory of electricity

- The theory of electricity is the part of physics dealing with properties of electric charge, the interactions between electric charges, and the conduction of electric charge in various materials.



Electricity

- *Electricity* is the presence and motion of charged particles.
- *Electric current* is the flow of charged particles around an closed path – *an electric circuit*.

Electric Charge

The *electric charge* Q can be imagined as “amount of electricity” in units called **coulombs** (C).
All electric charges are multiples of the electric charge of an electron.

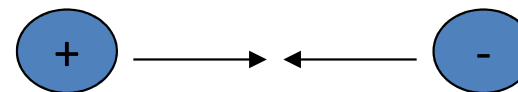
$$Q_e = e = 1.602 \times 10^{-19} \text{ C}$$

There are two types of charge, which are labeled positive and negative.

Like charges repel



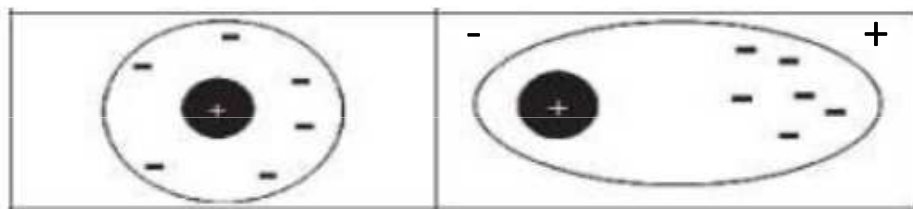
Unlike charges attract



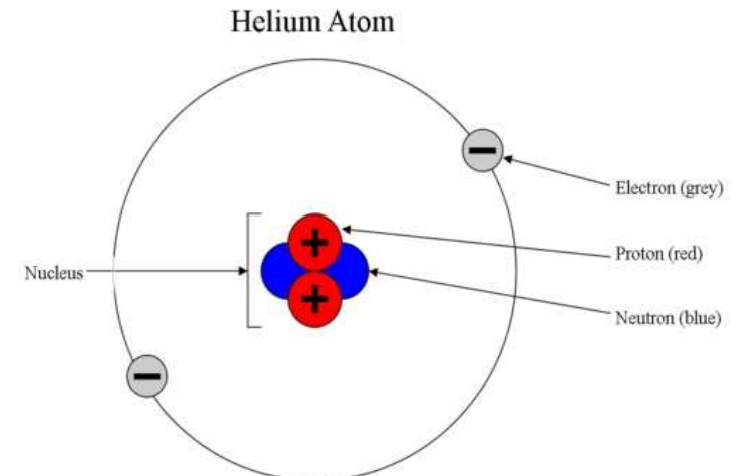
To charge an object means to transfer electrons from one object to another. They are not created or destroyed, just moved!

Electric charge

- Most electric charge is carried by the electrons and protons within an atom. Electrons carry negative charge, while protons carry positive charge.
- Protons and electrons create electric fields, which exert a force called the Coulomb force, which radiates outward in all directions.
- Because protons are generally confined to the nuclei imbedded inside atoms, they are not nearly as free to move as are electrons. Therefore, when we talk about electric charge, we nearly always mean a surplus or deficit of electrons.
- We are usually unaware of electric charge because most objects contain equal amounts of positive and negative charge that effectively neutralize each other.



Dielectric Polarization in Nonpolar Molecules. The electric field causes the shifting of charges



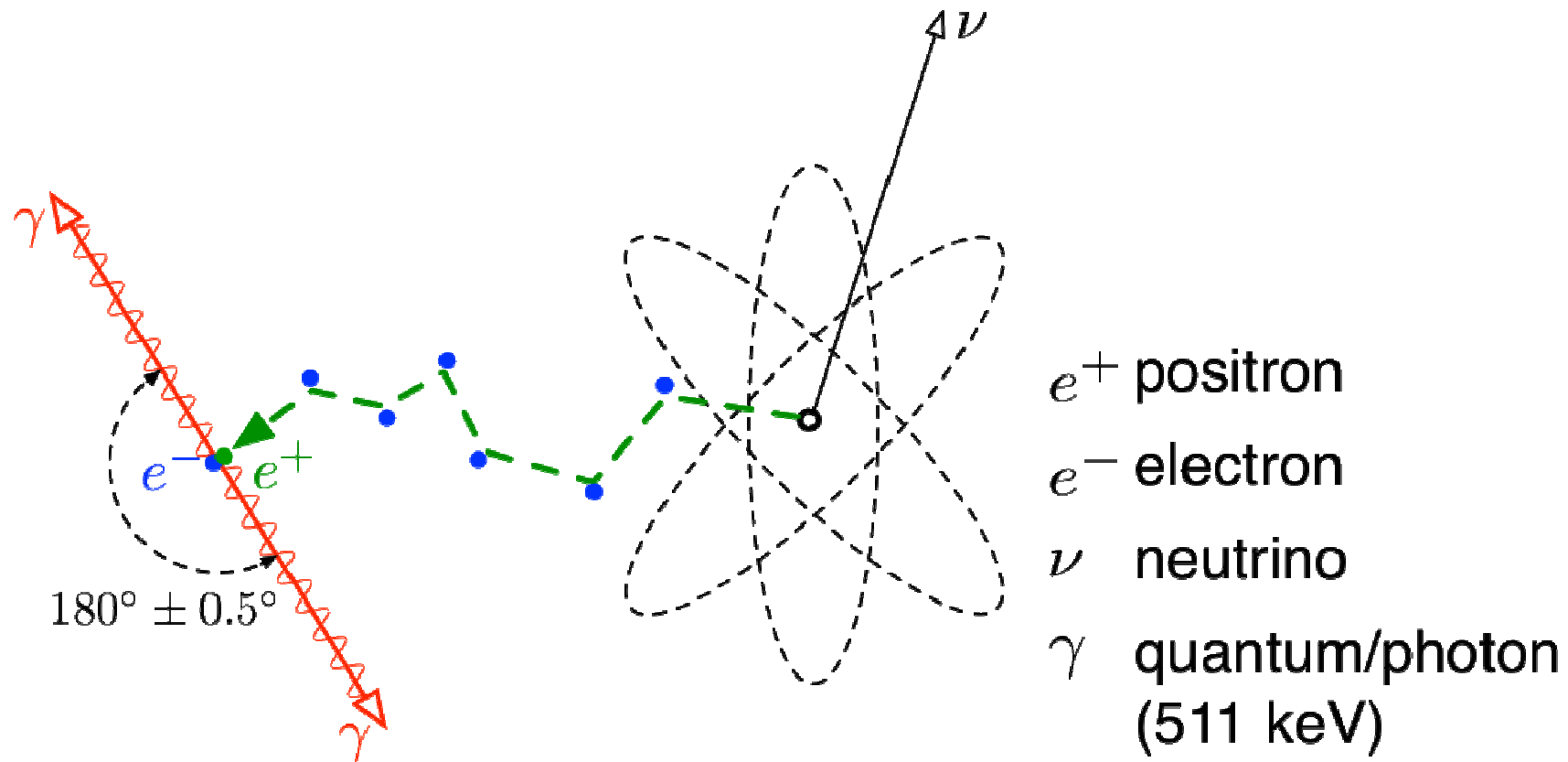
Electric charge

- It is a scalar physical quantity
- E.ch. characterized by the electrical properties of bodies
- The presence of e.ch. is important for the formation of an electric or magnetic field
- It is bound to elementary particles
- Electric charge can be „create“ by add or remove an proton or (namely) electron
- The „Law of conservation of charge“ must be valid!
- The process of „be positive/negative charged“ ...

Law of conservation of charge

- *The algebraic sum of all the electric charges in any closed system is constant.*
- The only way to change the net charge of a system is to bring in charge from elsewhere, or remove charge from the system.
- *Charge can be created and destroyed, but only in positive-negative pairs.*

Electron-positron annihilation



Charges can only be in multiples of e-

$$Q_e = e = 1.602 \times 10^{-19} \text{ Coulombs}$$

Multiples of Charges Chart

charge of an electron - Coulombs

$1e$	1.6×10^{-19}
$2e$	3.2×10^{-19}
$3e$	4.8×10^{-19}
$4e$	6.4×10^{-19}
$5e$	8.0×10^{-19}

Electric charge is when ...

Getting Shocked



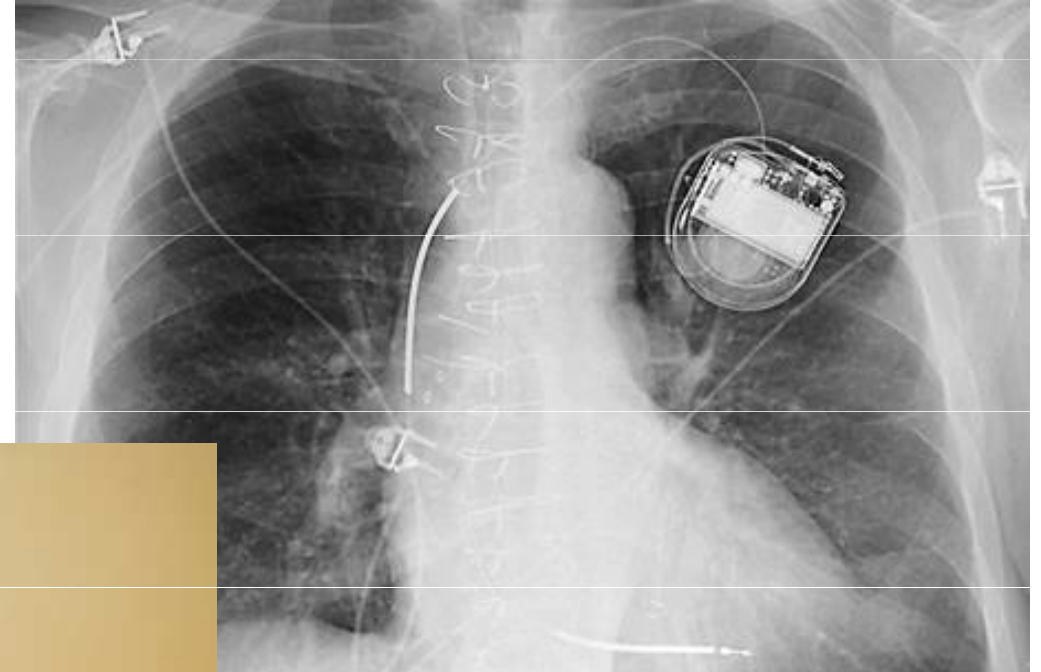
Hair sticking out



Electrostatic forces

Electric charge is when ...

defibrillator



cardiostimulator

How to make a electric charge?

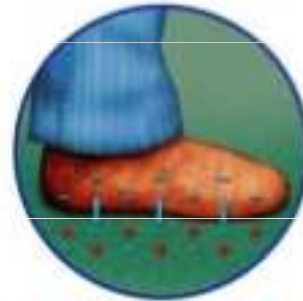
The electric charge can be obtained by:

- Direct contact
- Electrostatic induction
- Electromagnetic induction
- Friction
- Pyroelectric effect (heat)
- Piezoelectric effect (force)
- Fotoelectric effect (photon)
- Ionization

How to transfer charge?

Transferring Charge

- Three methods by which an object can become charged:
 - Friction
 - Conduction
 - Induction



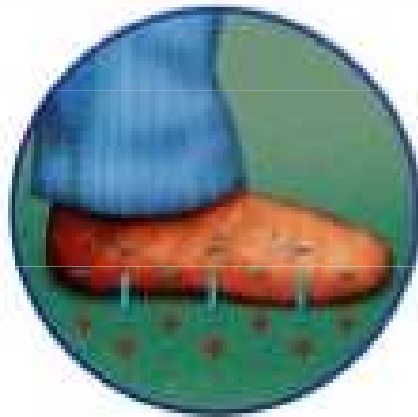
A Charging by Friction
Electrons are rubbed from the carpet to the girl's sock. The charges are distributed evenly over the sock.



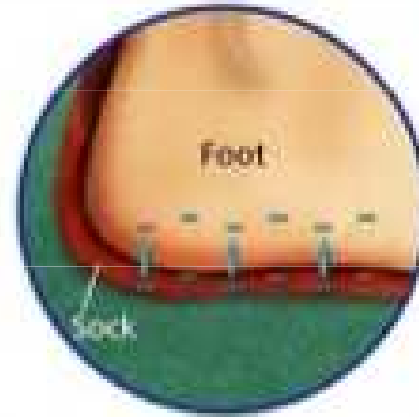
B Charging by Conduction
When the negatively charged sock touches the skin, electrons are transferred by direct contact. Electrons are then distributed throughout the girl's body.



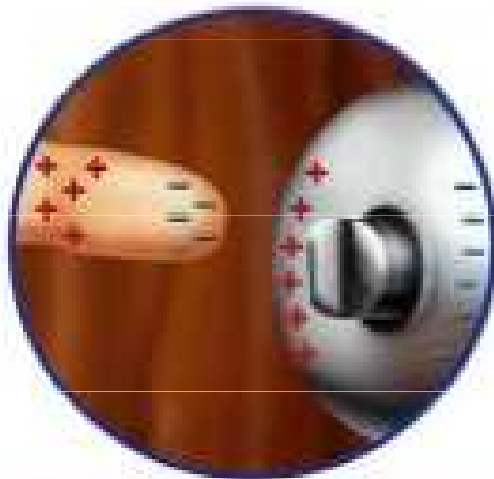
C Charging by Induction
The negative charge on the girl's fingertip produces an electric field that repels the electrons and attracts the protons on the doorknob. An area of positive charge is induced on the edge of the doorknob just by coming near (without touching it). If another person touched the doorknob's negative side, the electrons would be transferred away from the doorknob, leaving it with an overall positive charge.



A **Charging by Friction**
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Charging by Conduction

- Charging by conduction involves the **contact** of a **charged object to a neutral object**.



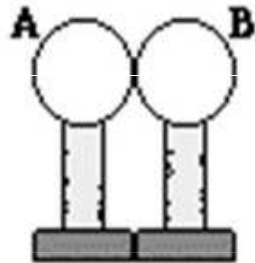
- When charging by conduction **both object have the same type of charge** when separated.
- To charge by conduction successfully, your charged and neutral object must be **conductors!**

Charging by Induction

- **charging by induction** method is to charge an object **without actually touching** the object to any other charged object.

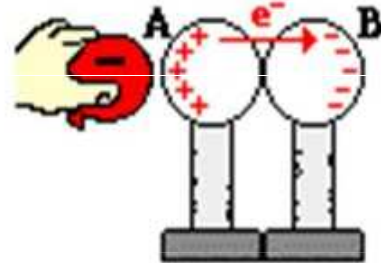
Charging by induction using negatively charged object

Diagram i.



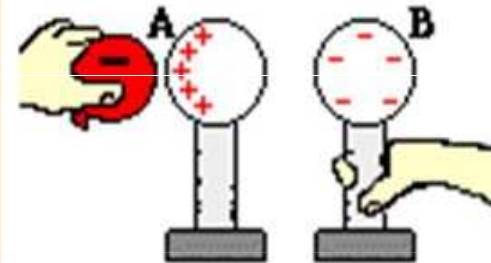
Two metal spheres are mounted on insulating stands.

Diagram ii.



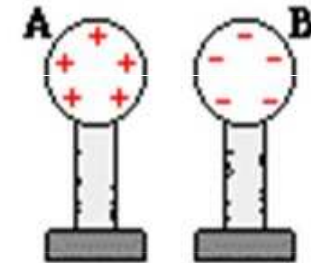
The presence of a - charge induces e^- to move from sphere A to B. The two-sphere system is polarized.

Diagram iii.



Sphere B is separated from sphere A using the insulating stand. The two spheres have opposite charges.

Diagram iv.



The excess charge distributes itself uniformly over the surface of the spheres.

Objects that tend to **give up electrons** and become **positive**:

- Glass
- Nylon
- Fur
- Hair
- Wool

Objects that tend to **attract electrons** and become **negative**:

- Rubber
- Polyester
- Styrofoam
- Saran Wrap
- PVC

When rubbed together, *materials* have a different *strength of attraction* for the *electrons*

Most Positive (+)

Easily lose electrons

Human Skin

Fur

Glass

Human Hair

Wool

Silk

Paper

Cotton



+++



+

Easily gain electrons

Rubber

Copper

Silver

Polyester

Plastic



-

Most Negative (-)

Why is static electricity more apparent in winter?

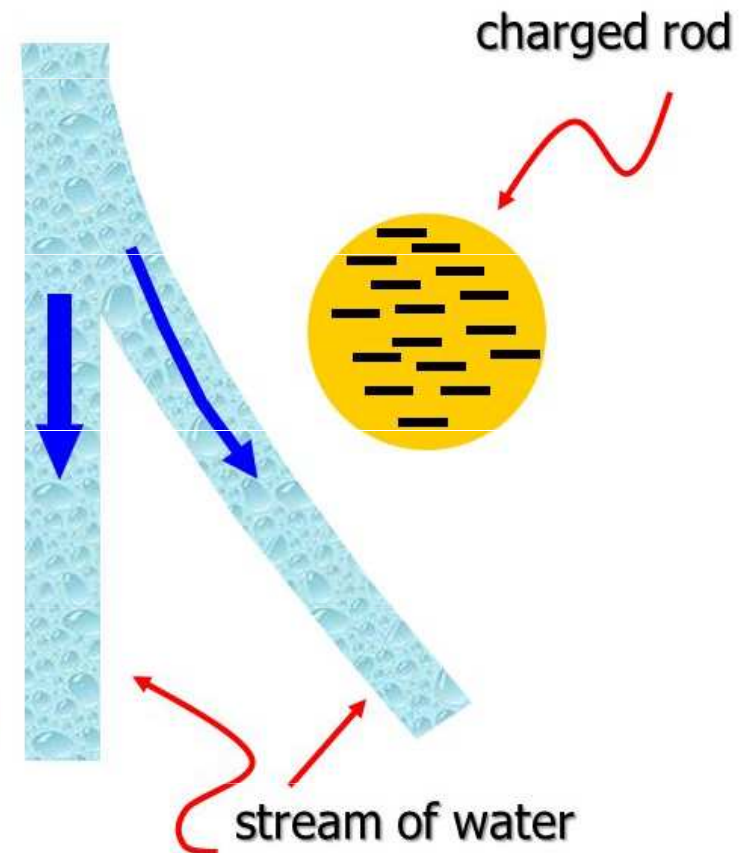
You notice static electricity much more in winter (with clothes in a dryer, or taking a sweater off, or getting a shock when you touch something after walking on carpet) than in summer because the air is much drier in winter than summer. **Dry air is a relatively good electrical insulator**, so if something is charged the charge tends to stay. In more humid conditions, such as you find on a typical summer day, water molecules, which are polarized, can quickly remove charge from a charged object.

You can bend water with charge!

The water molecule has a positive end and a negative end.

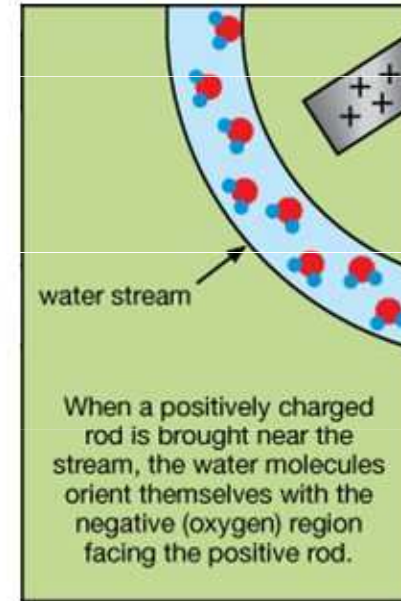
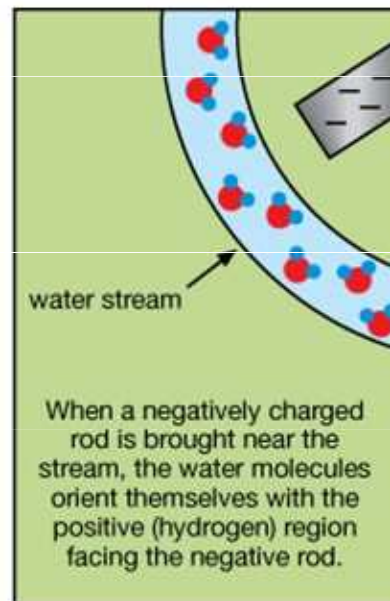
When a negative rod is brought near the stream of water, all the positive ends of the water molecules turn to the right and are attracted to the negative rod.

What happens if the rod is charged positively?



What will happen when a charged rod or balloon is brought up close to a stream of water?

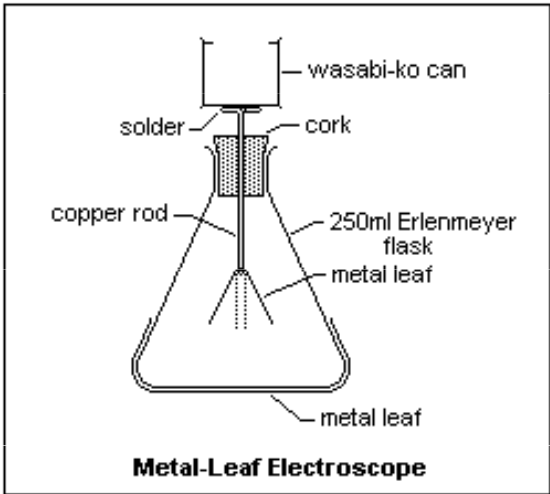
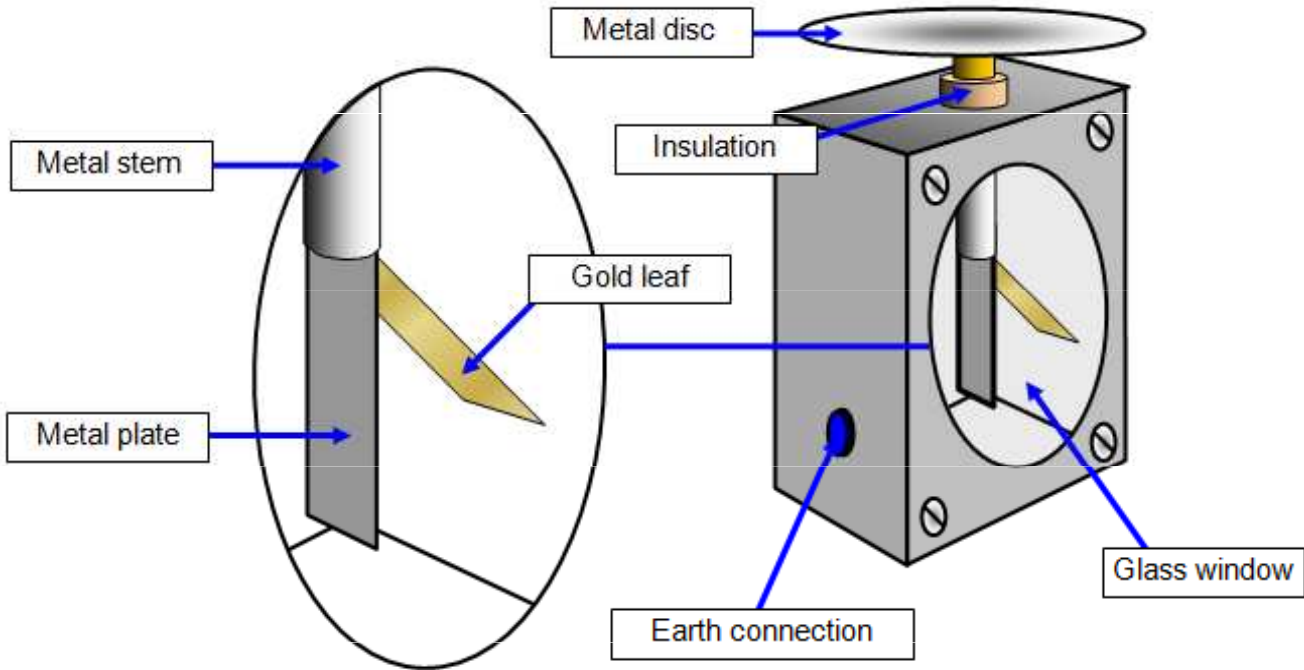
The water will be attracted toward the rod



How to measure charge?



- Electroscope



History

- „**Electron**“ came from the Greek word for amber, ἤλεκτρον (ēlektron).
- **Thales of Miletus** (624 – c. 546 BC) - Greek philosopher, mathematician and astronomer. Make an experiments with lodestone and amber - found attractive forces when rubbing it together.
- **Benjamin Franklin** (1706 – 1790) - American statesman and inventor, started studying electricity in 1742. The book *Experiments and Observations on Electricity. Theory of electrical fluid* - Franklin expressed the opinion that every non electric body contains a certain amount of electric fluid (positive or negative). Part of the electric fluid can be transferred from one body to another during the friction.
- **Charles-Augustin Coulomb** (1736-1806) - French physicist. The units of electric charge named after him : Coulomb. He developed the law descibed the force action between charges :
Coulomb law



LZ 129 Hindenburg (Luftschiff Zeppelin)



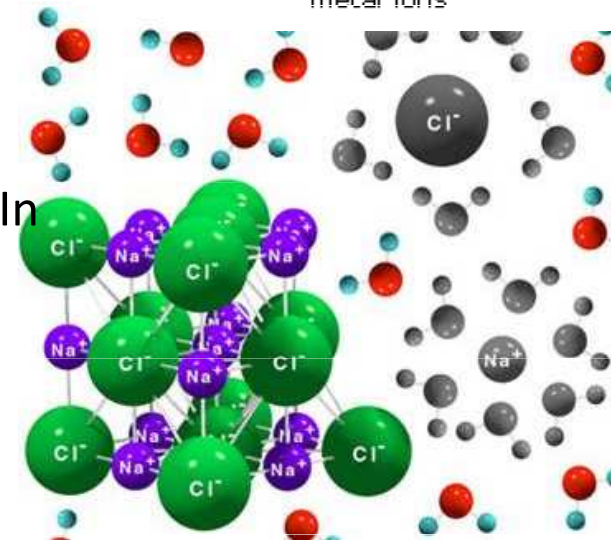
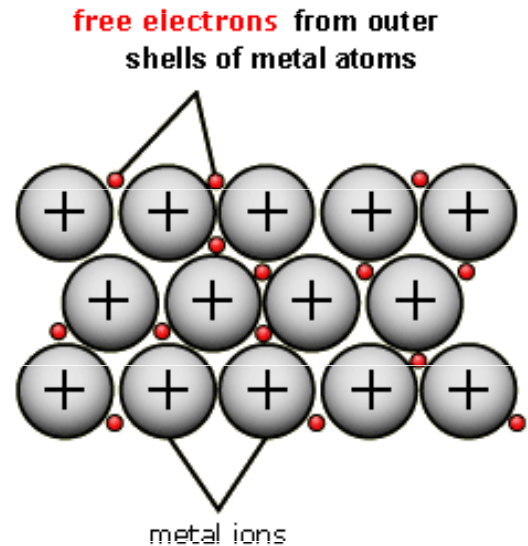
Large German commercial passenger-carrying rigid airship – destroyed 1937

Fire caused the spark that resulted from the **accumulation of static charge**... maybe

Basic types of electric charge carriers and conducting media: conductors

- **1st class conductors** are metals in which electrons (which behaviour resembles gas) enable electrical phenomena.

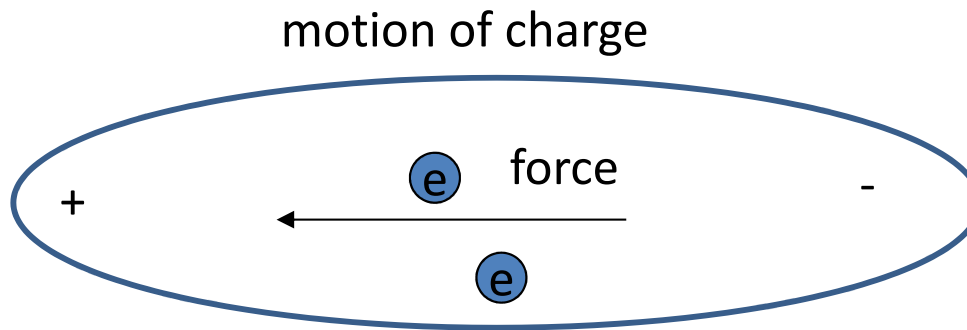
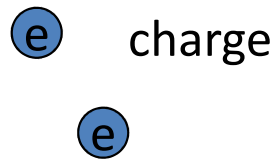
- **2nd class conductors** are electrolytes consisting of solutions of dissociated ionic compounds (e.g. NaCl). In this case, the anions and cations are the carriers of electric charge.



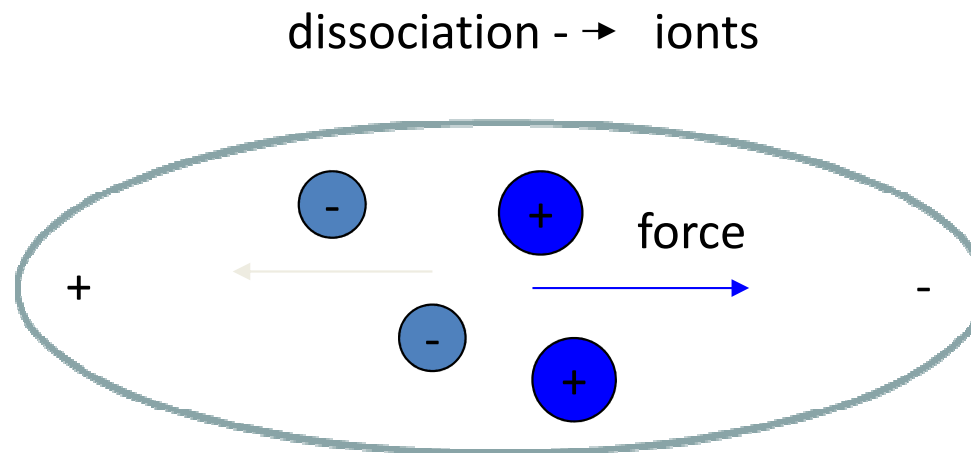
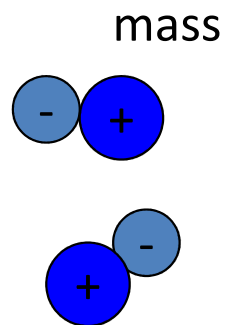
Example – effect of electric field



Conductors – electron flow



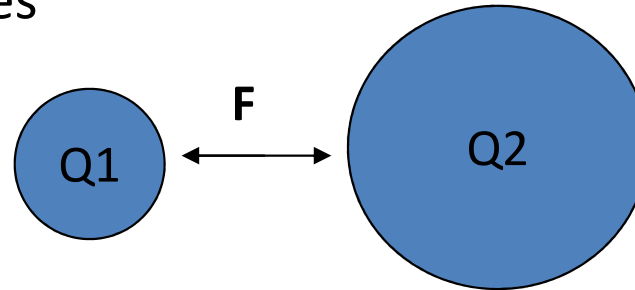
Electrolyte



Coulomb's law:

- This law describes the **force** existing between electric charges at rest.

$$F = \frac{1}{4\pi\epsilon} \frac{Q_1 Q_2}{r^2} \text{ [N]},$$

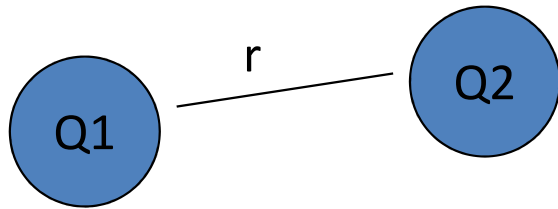


where F is the electrostatic force, Q_1 , and Q_2 are the interacting charges, r is the distance between the charges (centres of charged spheres), and ϵ is the **electric permittivity** of the medium between charges.

$$\epsilon = \epsilon_0 \epsilon_r \quad \frac{1}{4\pi\epsilon} = k = 8.987 \times 10^9 \text{ N m}^2 \text{ C}^{-2}$$

where ϵ_0 is the permittivity of vacuum ($8.85 \times 10^{-12} \text{ C}^2 \text{ m}^{-2} \text{ N}^{-1}$), a very important physical constant. ϵ_r is the relative permittivity (vacuum = 1)

An example



$$Q1 = -20 \text{ nC}$$

$$Q2 = +80 \text{ nC}$$

$$r = 10 \text{ cm}$$

vacuum

$$F = ???$$

$$F = \frac{1}{4\pi\epsilon} \frac{Q_1 Q_2}{r^2}$$

insert values

$$F = k \cdot \frac{20 \times 10^{-9} \cdot 80 \times 10^{-9}}{0.1^2}$$

conversion of units

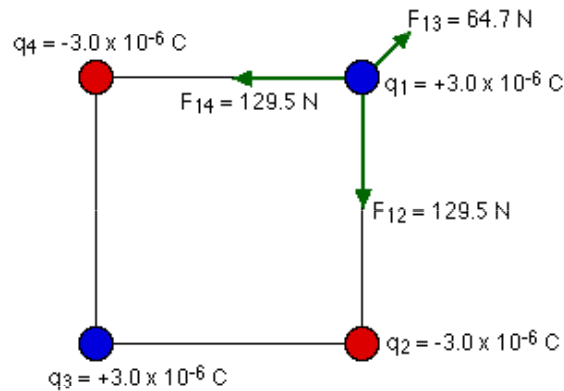
$$k = 8.987 \times 10^9 \text{ N m}^2 \text{ C}^{-9}$$

calculation

$$\underline{\underline{F = 1.4 \times 10^{-3} \text{ N}}}$$

The value of force is $1.4 \times 10^{-3} \text{ N}$.

An example



Four charges are arranged in a square with sides of length 2.5 cm. The two charges in the top right and bottom left corners are $+3.0 \times 10^{-6}$ C. The charges in the other two corners are -3.0×10^{-6} C. What is the net force exerted on the charge in the top right corner by the other three charges?

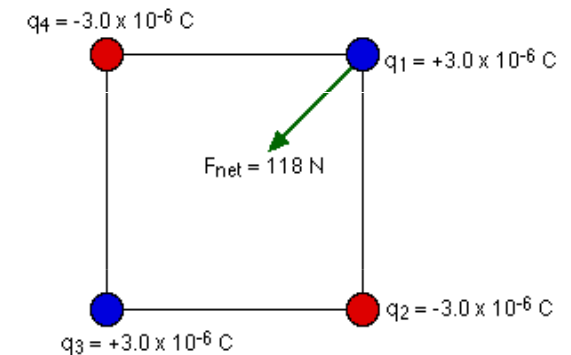
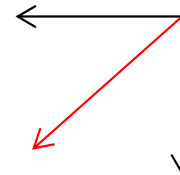
To solve any problem like this, the simplest thing to do is to draw a good diagram showing the forces acting on the charge. You should also let your diagram handle your signs for you. Force is a vector, and any time you have a minus sign associated with a vector all it does is tell you about the direction of the vector. If you have the arrows giving you the direction on your diagram, you can just drop any signs that come out of the equation for Coulomb's law.

Consider the forces exerted on the charge in the top right by the other three:

from charge 2 : $F_{12} = k q_1 q_2 / r^2 = (8.99 \times 10^9)(+3.0 \times 10^{-6})(-3.0 \times 10^{-6}) / (0.025)^2$
 $= -129.5 \text{ N} = +129.5 \text{ N}$ in the direction shown on the diagram

from charge 3 : (note that $r = 0.03536$ m)
 $F_{13} = k q_1 q_3 / r^2 = (8.99 \times 10^9)(+3.0 \times 10^{-6})(+3.0 \times 10^{-6}) / (0.03536)^2$
 $= +64.7 \text{ N} = +64.7 \text{ N}$ in the direction shown on the diagram

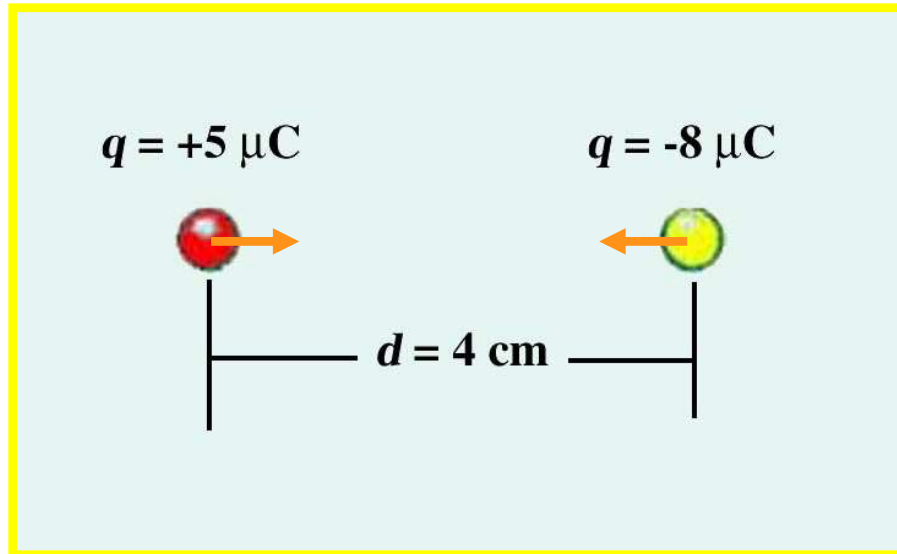
from charge 4 : $F_{14} = F_{12} = +129.5 \text{ N}$ in the direction shown on the diagram



You have to be very careful to add these forces as vectors to get the net force. In this problem we can take advantage of the symmetry, and combine the forces from charges 2 and 4 into a force along the diagonal (opposite to the force from charge 3) of magnitude 183.1 N. When this is combined with the 64.7 N force in the opposite direction, the result is a net force of 118 N pointing along the diagonal of the square.

The symmetry here makes things a little easier. If it wasn't so symmetric, all you'd have to do is split the vectors up into x and y components, add them to find the x and y components of the net force, and then calculate the magnitude and direction of the net force from the components.

EXAMPLE 1 - Find the force between these two charges

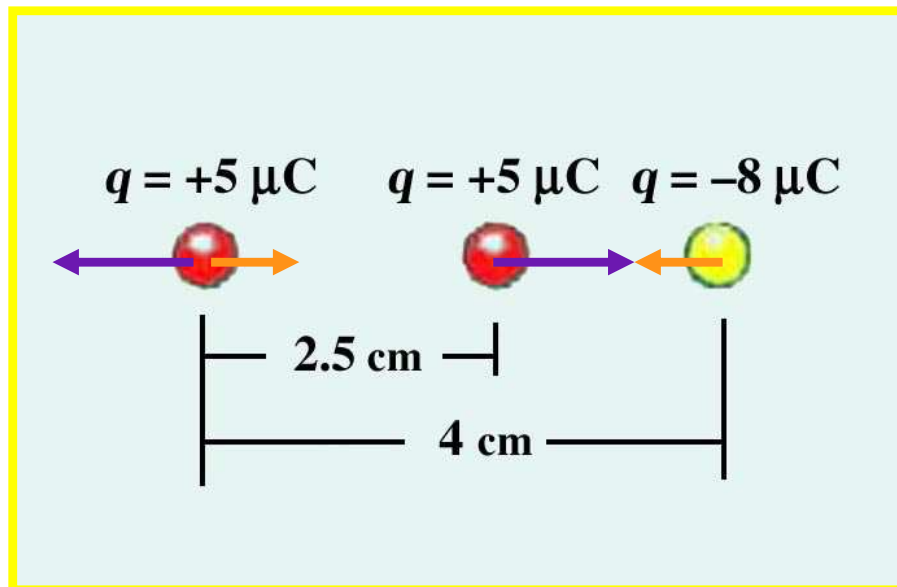


$$F_e = \frac{(9.0 \times 10^9)(5 \times 10^{-6} \text{ C})(-8 \times 10^{-6} \text{ C})}{(0.04 \text{ m})^2}$$

$$F_e = -225 \text{ N}$$

The negative signs means force of attraction, but does not indicate left or right direction

EXAMPLE 2 - Find the net force on the left charge



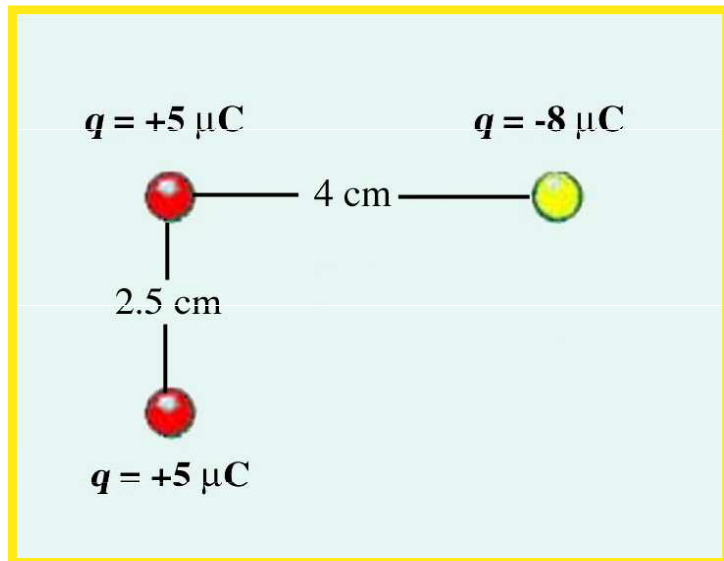
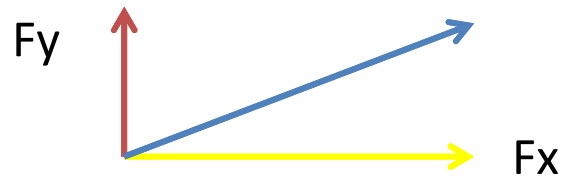
$$F_e = \frac{(9.0 \times 10^9)(5 \times 10^{-6} \text{ C})(5 \times 10^{-6} \text{ C})}{(0.025 \text{ m})^2}$$

$$F_e = 360 \text{ N} \quad (\text{force of repulsion})$$

$$F_{net} = F_{left} - F_{right}$$

$$F_{net} = 360 \text{ N} - 225 \text{ N} = 135 \text{ N, to the left}$$

EXAMPLE 3 - Find the net force on the upper left charge



$$F_{e,x} = 225 \text{ N, right} \quad F_{e,y} = 360 \text{ N, up}$$

$$\Sigma F_e = \sqrt{F_{e,x}^2 + F_{e,y}^2} = \sqrt{225^2 + 360^2} = 425 \text{ N}$$

$$\theta = \tan^{-1}\left(\frac{F_{e,y}}{F_{e,x}}\right) = \tan^{-1}\left(\frac{360}{225}\right) = 58.0^\circ$$