

$$\begin{array}{l} 1. \quad \begin{aligned} \mathbf{x}_1 + \mathbf{x}_2 + \mathbf{x}_3 + \mathbf{x}_4 &= 2 \\ 2\mathbf{x}_1 + 3\mathbf{x}_2 + 2\mathbf{x}_3 + 4\mathbf{x}_4 &= 8 \\ 2\mathbf{x}_1 + 2\mathbf{x}_2 + \mathbf{x}_3 - 3\mathbf{x}_4 &= 1 \\ \mathbf{x}_1 + \mathbf{x}_2 + \mathbf{x}_3 - \mathbf{x}_4 &= 0 \end{aligned} \end{array}$$

$$\begin{array}{l} 2. \quad \begin{aligned} \mathbf{x}_1 + 2\mathbf{x}_2 + \mathbf{x}_3 + 2\mathbf{x}_4 &= 3 \\ 2\mathbf{x}_1 + \mathbf{x}_2 + \mathbf{x}_3 + \mathbf{x}_4 &= 4 \\ -\mathbf{x}_1 + 2\mathbf{x}_2 + \mathbf{x}_3 + \mathbf{x}_4 &= 0 \\ \mathbf{x}_2 + \mathbf{x}_3 + 2\mathbf{x}_4 &= 3 \end{aligned} \end{array}$$

$$\begin{array}{l} 3. \quad \begin{aligned} \mathbf{x}_1 + \mathbf{x}_2 + \mathbf{x}_3 + \mathbf{x}_4 &= 4 \\ \mathbf{x}_2 + \mathbf{x}_3 + \mathbf{x}_4 &= 1 \\ \mathbf{x}_1 + 2\mathbf{x}_2 + 3\mathbf{x}_3 &= 10 \\ \mathbf{x}_2 + 2\mathbf{x}_3 + 3\mathbf{x}_4 &= -2 \end{aligned} \end{array}$$

$$\begin{array}{l} 4. \quad \begin{aligned} 2\mathbf{x}_1 + \mathbf{x}_2 + 2\mathbf{x}_3 &+ 3\mathbf{x}_5 = 0 \\ \mathbf{x}_1 + 2\mathbf{x}_2 + \mathbf{x}_3 + 3\mathbf{x}_4 + \mathbf{x}_5 &= 2 \\ 3\mathbf{x}_1 + \mathbf{x}_2 - \mathbf{x}_3 + 2\mathbf{x}_4 &= -1 \\ \mathbf{x}_1 - 3\mathbf{x}_3 &- 2\mathbf{x}_5 = -4 \\ 2\mathbf{x}_1 - 3\mathbf{x}_2 &- 2\mathbf{x}_4 - 2\mathbf{x}_5 = 3 \end{aligned} \end{array}$$

$$\begin{array}{l} 5. \quad \begin{aligned} 2\mathbf{x}_1 + \mathbf{x}_2 - \mathbf{x}_3 + \mathbf{x}_4 + \mathbf{x}_5 &= 3 \\ \mathbf{x}_2 + \mathbf{x}_3 - \mathbf{x}_4 &= 5 \\ \mathbf{x}_1 - \mathbf{x}_2 + \mathbf{x}_4 &= 0 \\ \mathbf{x}_1 + \mathbf{x}_2 - \mathbf{x}_3 - \mathbf{x}_4 &= 1 \\ \mathbf{x}_4 + 2\mathbf{x}_5 &= 3 \end{aligned} \end{array}$$

$$\begin{array}{l} 6. \quad \begin{aligned} \mathbf{x}_1 - \mathbf{x}_2 + 2\mathbf{x}_3 + 3\mathbf{x}_4 &= -1 \\ 2\mathbf{x}_1 - 2\mathbf{x}_2 &+ \mathbf{x}_4 - \mathbf{x}_5 = -3 \\ \mathbf{x}_2 - \mathbf{x}_3 + 2\mathbf{x}_4 + \mathbf{x}_5 &= -6 \\ \mathbf{x}_1 - \mathbf{x}_3 + \mathbf{x}_4 - 2\mathbf{x}_5 &= -2 \\ 2\mathbf{x}_1 - 3\mathbf{x}_2 - 2\mathbf{x}_3 &+ 2\mathbf{x}_5 = -12 \end{aligned} \end{array}$$

$$\begin{array}{l} 7. \quad \begin{aligned} \mathbf{x}_1 - 3\mathbf{x}_2 + 2\mathbf{x}_3 - \mathbf{x}_4 + 2\mathbf{x}_5 &= 3 \\ 2\mathbf{x}_1 &+ \mathbf{x}_3 + \mathbf{x}_4 + 4\mathbf{x}_5 = 15 \\ \mathbf{x}_2 - 3\mathbf{x}_3 + 2\mathbf{x}_4 + \mathbf{x}_5 &= 5 \\ \mathbf{x}_3 &+ \mathbf{x}_5 = 9 \\ \mathbf{x}_1 - \mathbf{x}_2 - \mathbf{x}_3 + \mathbf{x}_4 + \mathbf{x}_5 &= 2 \end{aligned} \end{array}$$

$$\begin{aligned}
 & \mathbf{x}_1 + \mathbf{x}_2 + \mathbf{x}_3 + \mathbf{x}_4 - 2\mathbf{x}_5 = 0 \\
 & \mathbf{x}_1 - \mathbf{x}_2 - \mathbf{x}_3 + \mathbf{x}_4 - \mathbf{x}_5 = 1 \\
 8. \quad & \mathbf{x}_1 - \mathbf{x}_2 + 2\mathbf{x}_3 + 2\mathbf{x}_4 - 2\mathbf{x}_5 = -1 \\
 & 2\mathbf{x}_1 + \mathbf{x}_2 - \mathbf{x}_3 + 2\mathbf{x}_4 - \mathbf{x}_5 = 0 \\
 & 3\mathbf{x}_1 - 2\mathbf{x}_2 - \mathbf{x}_3 - \mathbf{x}_4 + \mathbf{x}_5 = 0
 \end{aligned}$$

$$\begin{aligned}
 & \mathbf{x}_1 - 2\mathbf{x}_2 - \mathbf{x}_3 - 3\mathbf{x}_4 - 2\mathbf{x}_5 = -42 \\
 & \qquad \qquad \qquad 3\mathbf{x}_4 + 2\mathbf{x}_5 = 34 \\
 9. \quad & 8\mathbf{x}_1 + 7\mathbf{x}_2 + 6\mathbf{x}_3 + 5\mathbf{x}_4 + 4\mathbf{x}_5 = 100 \\
 & \qquad \qquad \qquad 2\mathbf{x}_4 + \mathbf{x}_5 = 20 \\
 & \qquad \qquad \qquad \mathbf{x}_2 + 3\mathbf{x}_3 + \mathbf{x}_4 + \mathbf{x}_5 = 28
 \end{aligned}$$

$$\begin{aligned}
 & 3\mathbf{x}_1 - 2\mathbf{x}_2 + 5\mathbf{x}_3 - 6\mathbf{x}_4 = 0 \\
 & 7\mathbf{x}_1 + \mathbf{x}_2 - 3\mathbf{x}_3 - 4\mathbf{x}_4 = 1 \\
 10. \quad & 6\mathbf{x}_1 + 5\mathbf{x}_2 - 13\mathbf{x}_3 + 3\mathbf{x}_4 = 1 \\
 & 2\mathbf{x}_1 - 13\mathbf{x}_2 + 40\mathbf{x}_3 - 16\mathbf{x}_4 = 13
 \end{aligned}$$

$$\begin{aligned}
 & 2\mathbf{x}_1 + \mathbf{x}_2 - \mathbf{x}_3 + \mathbf{x}_4 = 0 \\
 & \mathbf{x}_1 - \mathbf{x}_2 + \mathbf{x}_3 - \mathbf{x}_4 = 3 \\
 11. \quad & \mathbf{x}_1 + 2\mathbf{x}_2 - 2\mathbf{x}_3 + 2\mathbf{x}_4 = 1 \\
 & 2\mathbf{x}_1 + \mathbf{x}_2 + 2\mathbf{x}_4 = 3
 \end{aligned}$$

$$\begin{aligned}
 & \mathbf{x}_1 - 5\mathbf{x}_2 + \mathbf{x}_3 = 5 \\
 & 2\mathbf{x}_1 - \mathbf{x}_2 + 3\mathbf{x}_3 = 2 \\
 12. \quad & \mathbf{x}_1 + \mathbf{x}_2 - \mathbf{x}_3 = 0 \\
 & 2\mathbf{x}_1 + 2\mathbf{x}_2 + 3\mathbf{x}_3 = 3
 \end{aligned}$$

$$\begin{aligned}
 & \mathbf{x}_1 - 2\mathbf{x}_2 + 2\mathbf{x}_3 - \mathbf{x}_4 = 16 \\
 & \mathbf{x}_1 + \mathbf{x}_2 + \mathbf{x}_3 + \mathbf{x}_4 = 4 \\
 13. \quad & \mathbf{x}_1 - \mathbf{x}_2 - 2\mathbf{x}_3 + \mathbf{x}_4 = -4 \\
 & \mathbf{x}_1 - 5\mathbf{x}_2 + 3\mathbf{x}_3 - 3\mathbf{x}_4 = 28 \\
 & \mathbf{x}_1 + 3\mathbf{x}_2 + 4\mathbf{x}_3 + \mathbf{x}_4 = 14
 \end{aligned}$$

$$\begin{aligned}
 & \mathbf{x}_1 - \mathbf{x}_2 + 2\mathbf{x}_3 - 3\mathbf{x}_4 = -1 \\
 14. \quad & 3\mathbf{x}_1 + 2\mathbf{x}_2 + \mathbf{x}_3 - \mathbf{x}_4 = -14 \\
 & \mathbf{x}_1 + 4\mathbf{x}_2 - 3\mathbf{x}_3 + 5\mathbf{x}_4 = 0
 \end{aligned}$$

$$\begin{aligned}
 & \mathbf{x}_1 + \mathbf{x}_2 - 3\mathbf{x}_3 = -1 \\
 & 2\mathbf{x}_1 + \mathbf{x}_2 - 2\mathbf{x}_3 = 1 \\
 15. \quad & \mathbf{x}_1 + \mathbf{x}_2 + \mathbf{x}_3 = 3 \\
 & \mathbf{x}_1 + 2\mathbf{x}_2 - 3\mathbf{x}_3 = 1
 \end{aligned}$$

$$\begin{aligned}
 16. \quad & 2x_1 + x_2 - x_3 + x_4 = 1 \\
 & 3x_1 - 2x_2 + 2x_3 - 3x_4 = 2 \\
 & 5x_1 + x_2 - x_3 + 2x_4 = -1 \\
 & 2x_1 - x_2 + x_3 - 3x_4 = 4
 \end{aligned}$$

$$\begin{aligned}
 17. \quad & 3x_1 + x_2 - 2x_3 + x_4 - x_5 = 1 \\
 & 2x_1 - x_2 + 7x_3 - 3x_4 + 5x_5 = 2 \\
 & x_1 + 3x_2 - 2x_3 + 5x_4 - 7x_5 = 3 \\
 & 3x_1 - 2x_2 + 7x_3 - 5x_4 + 8x_5 = 3
 \end{aligned}$$

$$\begin{aligned}
 18. \quad & x_1 + 2x_2 - 3x_3 + 2x_5 = 1 \\
 & x_1 - x_2 - 3x_3 + x_4 - 3x_5 = 2 \\
 & 2x_1 - 3x_2 + 4x_3 - 5x_4 + 2x_5 = 7 \\
 & 9x_1 - 9x_2 + 6x_3 - 16x_4 + 2x_5 = 25
 \end{aligned}$$

$$\begin{aligned}
 19. \quad & 5x_1 + 12x_2 + 9x_3 + 25x_4 = 15 \\
 & 15x_1 + 34x_2 + 25x_3 + 64x_4 = 40 \\
 & 20x_1 + 46x_2 + 34x_3 + 89x_4 = 70 \\
 & 10x_1 + 23x_2 + 17x_3 + 44x_4 = 25
 \end{aligned}$$

$$\begin{aligned}
 20. \quad & x_1 - 2x_2 + x_3 - 3x_4 = -3 \\
 & x_1 + x_2 - 2x_3 + 2x_4 = 5 \\
 & 3x_1 - 3x_3 + x_4 = 7 \\
 & 2x_1 - x_2 - x_3 - x_4 = 2
 \end{aligned}$$

$$\begin{aligned}
 21. \quad & 2x_1 - 3x_2 - 2x_3 + x_4 = 3 \\
 & x_1 - x_2 - x_3 - x_4 = 2 \\
 & x_1 - 2x_2 - x_3 + 2x_4 = 1 \\
 & 2x_1 + 2x_3 + x_4 = 1
 \end{aligned}$$

$$\begin{aligned}
 22. \quad & x_1 - x_2 + 5x_3 = 1 \\
 & x_1 - 2x_2 + 4x_3 = -1 \\
 & 2x_1 - 3x_2 + 9x_3 = 0 \\
 & 2x_1 - 4x_2 + 8x_3 = -2
 \end{aligned}$$

$$\begin{aligned}
 23. \quad & x_1 + x_2 + x_3 + x_4 = -3 \\
 & x_1 - x_2 - x_3 + x_4 = -4 \\
 & x_2 - x_3 + x_4 = 5
 \end{aligned}$$

$$\begin{aligned}
 24. \quad & x_1 + x_2 - 2x_3 - x_4 = -1 \\
 & x_1 + 2x_2 - 3x_3 + 2x_4 = -4 \\
 & 2x_1 + x_2 + x_3 - 2x_4 = 2
 \end{aligned}$$

$$\begin{array}{rcl} \text{25.} & \boldsymbol{x}_1 - 2\boldsymbol{x}_2 + \boldsymbol{x}_3 - \boldsymbol{x}_4 = -6 \\ & 5\boldsymbol{x}_1 + \boldsymbol{x}_2 + 2\boldsymbol{x}_3 + \boldsymbol{x}_4 = 5 \\ & 7\boldsymbol{x}_1 - 3\boldsymbol{x}_2 + 4\boldsymbol{x}_3 - \boldsymbol{x}_4 = -7 \end{array}$$

$$\begin{array}{rcl} \text{26.} & \boldsymbol{x}_1 - \boldsymbol{x}_2 - 2\boldsymbol{x}_3 + 4\boldsymbol{x}_4 = 3 \\ & 2\boldsymbol{x}_1 - \boldsymbol{x}_2 + 4\boldsymbol{x}_3 - \boldsymbol{x}_4 = -1 \\ & 4\boldsymbol{x}_1 - 3\boldsymbol{x}_2 + 4\boldsymbol{x}_3 - \boldsymbol{x}_4 = -1 \\ & 4\boldsymbol{x}_1 - 3\boldsymbol{x}_2 + 7\boldsymbol{x}_4 = 5 \\ & 3\boldsymbol{x}_1 - 2\boldsymbol{x}_2 + 2\boldsymbol{x}_3 + 3\boldsymbol{x}_4 = 2 \end{array}$$

$$\begin{array}{rcl} \text{27.} & \boldsymbol{x}_1 - \boldsymbol{x}_2 - 3\boldsymbol{x}_4 = -1 \\ & 7\boldsymbol{x}_1 - 2\boldsymbol{x}_2 - 2\boldsymbol{x}_3 - 10\boldsymbol{x}_4 = -2 \\ & 7\boldsymbol{x}_1 - \boldsymbol{x}_2 + \boldsymbol{x}_3 - 9\boldsymbol{x}_4 = -4 \\ & 2\boldsymbol{x}_1 - 2\boldsymbol{x}_3 - 4\boldsymbol{x}_4 = -6 \\ & 6\boldsymbol{x}_1 - \boldsymbol{x}_2 + 2\boldsymbol{x}_3 - 7\boldsymbol{x}_4 = -1 \end{array}$$

$$\begin{array}{rcl} \text{28.} & \boldsymbol{x}_1 + \boldsymbol{x}_2 + \boldsymbol{x}_3 + \boldsymbol{x}_4 = 1 \\ & 2\boldsymbol{x}_1 + 2\boldsymbol{x}_2 + 2\boldsymbol{x}_3 = 0 \\ & \boldsymbol{x}_1 + \boldsymbol{x}_2 + 5\boldsymbol{x}_3 - \boldsymbol{x}_4 + 6\boldsymbol{x}_5 = 1 \\ & \boldsymbol{x}_1 + \boldsymbol{x}_2 - 3\boldsymbol{x}_3 + \boldsymbol{x}_4 - 6\boldsymbol{x}_5 = -1 \end{array}$$

$$\begin{array}{rcl} \text{29.} & 6\boldsymbol{x}_1 - 9\boldsymbol{x}_2 + 7\boldsymbol{x}_3 + 10\boldsymbol{x}_4 = 3 \\ & 2\boldsymbol{x}_1 - 3\boldsymbol{x}_2 - 3\boldsymbol{x}_3 - 4\boldsymbol{x}_4 = 1 \\ & 2\boldsymbol{x}_1 - 3\boldsymbol{x}_2 + 13\boldsymbol{x}_3 + 18\boldsymbol{x}_4 = 1 \end{array}$$

$$\begin{array}{rcl} \text{30.} & 3\boldsymbol{x}_1 + 4\boldsymbol{x}_2 + 2\boldsymbol{x}_3 = 2 \\ & \boldsymbol{x}_1 - 2\boldsymbol{x}_2 + 3\boldsymbol{x}_3 = 2 \\ & 2\boldsymbol{x}_1 + 6\boldsymbol{x}_2 - \boldsymbol{x}_3 = 0 \end{array}$$

$$\begin{array}{rcl} \text{31.} & 2\boldsymbol{x}_1 + 3\boldsymbol{x}_2 - 4\boldsymbol{x}_3 = -14 \\ & 2\boldsymbol{x}_1 - 3\boldsymbol{x}_2 + \boldsymbol{x}_3 = 13 \\ & 2\boldsymbol{x}_1 + 9\boldsymbol{x}_\epsilon - 9\boldsymbol{x}_3 = 20 \end{array}$$

$$\begin{array}{rcl} \text{32.} & \boldsymbol{x}_1 - \boldsymbol{x}_2 + \boldsymbol{x}_3 = 2 \\ & 2\boldsymbol{x}_1 - 3\boldsymbol{x}_2 + 4\boldsymbol{x}_3 = 4 \\ & \boldsymbol{x}_1 - \boldsymbol{x}_3 = 2 \end{array}$$

$$\begin{array}{rcl} \text{33.} & \boldsymbol{x}_1 - 2\boldsymbol{x}_2 + 5\boldsymbol{x}_3 = 9 \\ & 3\boldsymbol{x}_1 + \boldsymbol{x}_2 - 3\boldsymbol{x}_3 = -12 \\ & 5\boldsymbol{x}_1 - 2\boldsymbol{x}_2 + 3\boldsymbol{x}_3 = -1 \\ & \boldsymbol{x}_1 - \boldsymbol{x}_2 + \boldsymbol{x}_3 = 2 \end{array}$$

$$\begin{aligned}
 34. \quad & 2x_1 - 3x_2 + 6x_3 - x_4 = 1 \\
 & x_1 + 2x_2 - x_3 = 0 \\
 & x_1 + 3x_2 - x_3 - x_4 = -2 \\
 & 9x_1 - x_2 + 15x_3 - 5x_4 = 1
 \end{aligned}$$

$$\begin{aligned}
 35. \quad & 2x_1 - 3x_2 + x_3 = 0 \\
 & x_1 + 2x_2 - x_3 = 3 \\
 & 2x_1 + x_2 + x_3 = 12
 \end{aligned}$$

$$\begin{aligned}
 36. \quad & 2x_1 + 2x_2 + 7x_3 + 2x_4 = 6 \\
 & 6x_1 + 4x_2 + x_3 + x_4 = 6 \\
 & x_1 - 2x_2 + 6x_3 - x_4 = 0 \\
 & 3x_1 - 8x_2 + 3x_3 - x_4 = -2
 \end{aligned}$$

$$\begin{aligned}
 37. \quad & x_1 + 2x_2 - x_3 - 2x_4 = -2 \\
 & 2x_1 + x_2 + x_3 + x_4 = 8 \\
 & x_1 - x_2 - x_3 + x_4 = 1 \\
 & x_1 + 2x_2 + 2x_3 - x_4 = 4
 \end{aligned}$$

$$\begin{aligned}
 38. \quad & 3x_1 - x_2 + 2x_3 - x_4 = 0 \\
 & x_1 - 10x_2 + x_3 + x_4 = 1 \\
 & 2x_1 + 4x_2 + 4x_3 + 2x_4 = 3 \\
 & -x_1 - 4x_2 + 4x_3 + 5x_4 = 5
 \end{aligned}$$

$$\begin{aligned}
 39. \quad & 4x_1 + 3x_2 - x_3 + x_4 + x_5 = 15 \\
 & x_1 - x_2 + x_3 - x_4 + x_5 = 2 \\
 & 3x_1 - 2x_2 + x_3 - x_4 - 2x_5 = 5 \\
 & 2x_1 + 3x_3 + x_2 + x_4 = 0
 \end{aligned}$$

$$\begin{aligned}
 40. \quad & x_1 - 2x_2 + 2x_3 = -9 \\
 & 3x_1 + 5x_2 + 4x_3 = 10 \\
 & 5x_1 + 12x_2 + 6x_3 = 29
 \end{aligned}$$

$$\begin{aligned}
 41. \quad & x_1 + 2x_2 - x_3 = 2 \\
 & 3x_1 - x_2 + 2x_3 = 7 \\
 & x_1 - x_3 = -2 \\
 & 2x_1 + x_2 + x_3 = 7
 \end{aligned}$$

$$\begin{aligned}
 42. \quad & 2x_1 - x_2 + x_3 = 4 \\
 & x_1 + x_2 - x_3 = -1 \\
 & 3x_1 - 7x_2 - 2x_3 = -1 \\
 & -2x_1 + 5x_2 + x_3 = 1
 \end{aligned}$$

- 43.
- $$\begin{aligned} 7x_1 + 14x_2 - 21x_3 &= 7 \\ x_1 + 2x_2 - 3x_3 &= 1 \\ 5x_1 + 10x_2 + 15x_3 &= 5 \\ 3x_1 + 6x_2 - 9x_3 &= 3 \end{aligned}$$
- 44.
- $$\begin{aligned} 4x_1 + x_2 - x_3 - x_4 &= 3 \\ 2x_1 - 11x_2 + 5x_3 + ix_4 &= 2 \\ 2x_1 + 12x_2 - 6x_3 - 10x_4 &= 1 \end{aligned}$$
- 45.
- $$\begin{aligned} 5x_1 + 3x_2 + 3x_3 + x_4 &= 11 \\ x_1 - x_2 + x_3 &= -2 \\ 3x_1 + 3x_2 + 2x_3 + x_4 &= 10 \\ x_1 - 3x_2 + 2x_3 &= -7 \\ 4x_1 + x_2 + 3x_3 + x_4 &= 8 \end{aligned}$$
- 46.
- $$\begin{aligned} x_1 + 8x_2 + 2x_3 + x_4 &= -3 \\ 3x_1 + 10x_2 + 2x_3 - x_4 &= -2 \\ 2x_1 &= 1 \\ 4x_1 + 3x_2 + x_3 + x_4 &= 5 \\ -2x_1 + 2x_2 &= -6 \end{aligned}$$
- 47.
- $$\begin{aligned} 3x_1 + x_2 - x_3 + 2x_4 &= 0 \\ x_1 + 2x_2 + x_3 - x_4 &= 0 \\ 2x_1 - x_2 + 2x_3 + x_4 &= 0 \\ x_1 + 3x_2 + x_3 + 3x_4 &= 0 \end{aligned}$$
- 48.
- $$\begin{aligned} 3x_1 + 2x_2 - x_3 + x_4 &= 0 \\ 2x_1 - x_2 + 4x_3 - 3x_4 &= 0 \\ x_1 + x_2 - x_3 &= 0 \end{aligned}$$
- 49.
- $$\begin{aligned} 2x_1 + 2x_2 - 2x_3 - 3x_4 &= 0 \\ x_1 - x_2 &+ x_4 = 0 \\ x_1 + 2x_2 + x_3 + x_4 &= 0 \end{aligned}$$
- 50.
- $$\begin{aligned} 3x_1 + x_2 + x_3 - x_4 &= 0 \\ 7x_1 + x_2 - x_3 + x_4 &= 0 \\ x_1 - x_2 - 3x_3 + 3x_4 &= 0 \end{aligned}$$
- 51.
- $$\begin{aligned} x_1 - 3x_2 + x_3 + 4x_4 &= 0 \\ x_1 + x_2 + 4x_3 - 2x_4 &= 0 \\ x_1 - x_2 + x_3 - 2x_4 &= 0 \end{aligned}$$

52.

$$\begin{aligned} 4x_1 + 2x_2 + x_3 - 2x_4 + x_5 &= 0 \\ 3x_1 + 4x_2 + x_3 + x_4 - 2x_5 &= 0 \\ 2x_1 - 2x_2 + 3x_3 - 2x_4 - 2x_5 &= 0 \\ x_1 + 3x_2 + 4x_3 - 2x_4 &= 0 \end{aligned}$$

53.

$$\begin{aligned} 2x_1 - 2x_2 + 3x_3 - 3x_4 + x_5 &= 0 \\ x_1 + 2x_2 + x_3 + 2x_4 - 3x_5 &= 0 \\ 3x_1 + 4x_3 - x_4 - 2x_5 &= 0 \\ 5x_1 - 2x_2 + 7x_3 - 4x_4 - x_5 &= 0 \end{aligned}$$

54.

$$\begin{aligned} 4x_1 - 2x_2 + x_3 &= 0 \\ x_1 + x_2 - x_3 &= 0 \\ x_1 - 2x_2 + x_3 &= 0 \\ 2x_1 - x_2 + x_3 &= 0 \end{aligned}$$

55.

$$\begin{aligned} x_1 - 2x_2 + x_3 &= 0 \\ x_1 - 3x_2 + 3x_3 &= 0 \\ 2x_1 - x_2 - 4x_3 &= 0 \\ x_1 + x_2 - 5x_3 &= 0 \end{aligned}$$

56.

$$\begin{aligned} 2x_1 + 3x_2 - x_3 + 5x_4 &= 0 \\ 3x_1 - x_2 + 2x_3 - 7x_4 &= 0 \\ 4x_1 + x_2 - 3x_3 + 6x_4 &= 0 \\ x_1 - 2x_2 + 4x_3 - 7x_4 &= 0 \end{aligned}$$

57.

$$\begin{aligned} 3x_1 + 4x_2 - 5x_3 + 7x_4 &= 0 \\ 2x_1 - 3x_2 + 3x_3 - 2x_4 &= 0 \\ 4x_1 + 11x_2 - 13x_3 + 16x_4 &= 0 \\ 7x_1 - 2x_2 + x_3 + 3x_4 &= 0 \end{aligned}$$

58.

$$\begin{aligned} x_1 + x_2 - 3x_4 - x_5 &= 0 \\ x_1 - x_2 + 2x_3 - x_4 &= 0 \\ 4x_1 - 2x_2 + 6x_3 + 3x_4 - 4x_5 &= 0 \\ 2x_1 + 4x_2 - 2x_3 + 4x_4 - 7x_5 &= 0 \end{aligned}$$

59.

$$\begin{aligned} x_1 - 2x_2 + x_3 - x_4 + x_5 &= 0 \\ 2x_1 + x_2 - x_3 + 2x_4 - 3x_5 &= 0 \\ 3x_1 - 2x_2 - x_3 + x_4 - 2x_5 &= 0 \\ 2x_1 - 5x_2 + x_3 - 2x_4 + 2x_5 &= 0 \end{aligned}$$

60.

$$\begin{aligned} x_1 - 2x_2 + x_3 + x_4 - x_5 &= 0 \\ 2x_1 + x_2 - x_3 - x_4 + x_5 &= 0 \\ x_1 + 7x_2 - 5x_3 - 5x_4 + 5x_5 &= 0 \\ 3x_1 - x_2 - 2x_3 + x_4 - x_5 &= 0 \end{aligned}$$

61. Pro které hodnoty parametru a má soustava $\begin{array}{rcl} a \cdot x & + y & + z = 1 \\ x & + a \cdot y & - z = 1 \\ x & + y & + a \cdot z = 1 \end{array}$ právě jedno řešení?
62. $\begin{array}{rcl} x_1 & + 2x_2 & + 3x_3 & + 4x_4 & + 5x_5 = 1 \\ -2x_1 & + 3x_2 & + 4x_3 & + 5x_4 & + 6x_5 = 2 \\ -3x_1 & + 4x_2 & + 5x_3 & + 6x_4 & + 7x_5 = 3 \\ -4x_1 & + 5x_2 & + 6x_3 & + 7x_4 & + 8x_5 = 4 \end{array}$
63. $\begin{array}{rcl} x_1 & - 3x_2 & + x_3 & + 4x_4 = 0 \\ x_1 & + x_2 & + 4x_3 & - 2x_4 = 0 \\ x_1 & - x_2 & + x_3 & - 2x_4 = 0 \end{array}$
64. Vytvořte si potřebné vektory a matice a zapište pomocí nich soustavu lineárních rovnic
 (soustavu nijak neupravujte): $\begin{array}{rcl} x_1 = & -x_1 & + 3x_2 & + 2x_3 & -x_4 & + 3 \\ x_2 = & x_1 & -x_2 & -x_3 & + 2x_4 & - 1 \\ x_3 = & -2x_1 & -x_2 & -x_3 & -x_4 & + 1 \\ x_4 = & x_1 & -x_2 & -x_3 & & - 2 \end{array}$
65. $\begin{array}{rcl} 2x_1 & - 5x_2 & + x_3 = -2 \\ 4x_1 & - 8x_2 & - 2x_3 = 18 \\ 2x_1 & - 3x_2 & - 3x_3 = 20 \\ x_1 & - 4x_2 & - x_3 = 5 \end{array}.$
66. $\begin{array}{rcl} 4x_1 & + x_2 & + x_3 & - x_4 = 0 \\ x_1 & + 2x_2 & - 3x_3 & + 2x_4 = 0 \\ 2x_1 & - 5x_2 & + 7x_3 & - 5x_4 = 0 \\ 7x_1 & - 4x_2 & + 5x_3 & - 4x_4 = 0 \end{array}$
67. $\begin{array}{rcl} 3x_1 & + 2x_2 & - x_3 & + x_4 = 0 \\ x_1 & + x_2 & - x_3 & + 5x_4 = 0 \\ 2x_1 & + x_2 & + 3x_3 & - x_4 = 0 \end{array}$
68. $\begin{array}{rcl} x_1 & + 2x_2 & + 8x_3 = 9 \\ 2x_1 & + x_2 & + 7x_3 = 6 \\ 3x_1 & + x_2 & + 9x_3 = 7 \\ 2x_1 & - x_2 & + x_3 = -2 \end{array}$
69. $\begin{array}{rcl} 4x_1 & - x_2 & + 2x_3 = 0 \\ x_1 & + x_2 & + 2x_3 = 0 \\ 5x_1 & - x_2 & - 3x_3 = 0 \end{array}$
70. Vyřešte soustavu rovnic $\begin{array}{rcl} x & - 2y & + z = 1 \\ x & - y & + 3z = 0 \\ x & - 4y & - 3z = k \end{array}$ a proveděte diskusi vzhledem k parametru k .

71. Určete k tak, aby soustava rovnic

$$\begin{array}{rcl} 2x_1 & -x_2 & +x_3 & +x_4 = 1 \\ x_1 & +2x_2 & -x_3 & +4x_4 = 2 \\ x_1 & +7x_2 & -4x_3 & +11x_4 = k \end{array}$$

72.

$$\begin{array}{rcl} x_1 & -2x_2 & -x_3 & +x_4 = 9 \\ x_1 & -3x_2 & +5x_3 & -6x_4 = 7 \\ x_1 & -x_2 & +2x_3 & -x_4 = 2 \\ -x_1 & +x_2 & +x_3 & -2x_4 = -5 \end{array}$$

73.

$$\begin{array}{rcl} x_1 & +x_2 & +2x_3 & +2x_4 = 0 \\ x_1 & -x_2 & -3x_3 & +3x_4 = 5 \\ 2x_1 & -x_2 & -2x_3 & +x_4 = -3 \\ 4x_1 & -x_2 & -3x_3 & +6x_4 = 2 \end{array}$$

74.

$$\begin{array}{rcl} 2x_1 & -x_2 & -x_3 & +x_4 = 0 \\ 3x_1 & +2x_2 & +2x_3 & -x_4 = 0 \\ x_1 & +3x_2 & +3x_3 & -2x_4 = 0 \end{array}$$

75.

$$\begin{array}{rcl} x & +2y & -z & +u = 9 \\ x & -y & +2z & -u = 2 \\ -x & +y & +z & -2u = -5 \\ 2x & -y & -z & +u = 2 \end{array}$$

1.	(1, 2, -2, 1)	23.	(-2, 2 - t, -3, t)
2.	(1, -1, 2, 1)	24.	(9/4 + 13t, -11/4 - 15t, 1/4 - 3t, 4t)
3.	(3, 2, 1, -2)	25.	(r, 1 + 6r + 3s, s, 4 - 11r - 5s)
4.	(0, -1, 2 1 -1)	26.	(5 - 7t, 5 - 7t, -3/2 + 2t, t)
5.	(2, 1, 3, -1, 2)	27.	(2, -9/2, 0, 5/2)
6.	(1, 2, 3, -2, 1)	28.	(3a, 3b + 1, 1 - 3a - 3b, 1, 2a + 2b + 1)
7.	(1, 2, -1,-2, 4)	29.	(a, b, 22a - 33b - 11, -16a + 24b + 8)
8.	(2, 3, 4, 1, 5)	30.	(6/5 - 16t, -2/5 + 7t, 10t)
9.	(0, 2, 4, 6, 8)	31.	nemá řešení
10.	(1, 1, 1, 1)	32.	(t + 2, 2t, t)
11.	nemá řešení	33.	(-2, 3, 1)
12.	nemá řešení	34.	nemá řešení
13.	nemá řešení	35.	(2, 3, 5)
14.	nemá řešení	36.	(1/2, 3/8, 1/4, 5/4)
15.	nemá řešení	37.	(1, 2, 1, 3)
16.	nemá řešení	38.	(11, 2, 26, 83)/100
17.	nemá řešení	39.	(3, 0, -2, 0, 1)
18.	nemá řešení	40.	(-18a + 1, 2a + 3, 11a - 2)
19.	nemá řešení	41.	(1, 2, 3)
20.	(r, 5r - 4s, s, 7 - 3r + 3s)	42.	nemá řešení
21.	(5/2 + t, 1 + 6t, -1/2 - 7t, 2t)	43.	(1 - 2a, a, 0)
22.	(3 - 6t, 2 - t, t)	44.	(a + 3b + 1/2, 19a + 11b - 1, 23b - 2, 23a)

45.	$(3, 0, -5, 11)$	67.	$(-10t, 16t, t)$
46.	nemá řešení	68.	$(1 + 2t, 4 + 3t, -t)$
47.	$(0, 0, 0, 0)$	69.	$(0, 0, 0)$
48.	$(t, 2t, 3t, 4t)$	70.	$k = 3$, řeš.: $(-1 - 5t, -1 - 2t, t)$, $k \neq 3$, nemá řeš.
49.	$(-t, t, -3t, 2t)$	71.	$k = 5$
50.	$(r, -5r, 2r + s, s)$	72.	$(2t, -4 + t, -1 - t, -t)$
51.	$(7t, 3t, -2t, t)$	73.	$(-1, -t, 15 - 7t, -7 + 3t, t)$
52.	$(t, -t, 2t, 3t, 2t)$	74.	$(t, 2 - t, -s, -7t)$
53.	$(2r, -7r - 9s + 7t, 2s, 6r + 8s - 3t, 2t)$	75.	$(2, 3, 4, 5)$
54.	$(0, 0, 0)$		
55.	$(3t, 2t, t)$		
56.	$(0, 0, 0, 0)$		
57.	$(3r - 13s, 19r - 20s, 17r, 17s)$		
58.	$(7t - s, 5t + s, s, 2t, 6t)$		
59.	$(-4t + 7s, -4t + 5s, 4t - 5s, 8t, 8s)$		
60.	$(0, 0, 0, t, t)$		
61.	$a \neq 0$, $a \neq \pm 1$		
62.	$(0, 2 + s + 2t, -1 - 2s - 3t, s, t)$		
63.	$(-7, -3, 2)$		
64.	$X = A X + B$		
65.	$(4, 1, -5)$		
66.	$(t, 0, 9t, 13t)$		