

# Kolloquium-english.ppt

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Technical Univ. Aachen

Theoretical Physics

**Kaiserslautern, May 2009**



Expansion of space

in

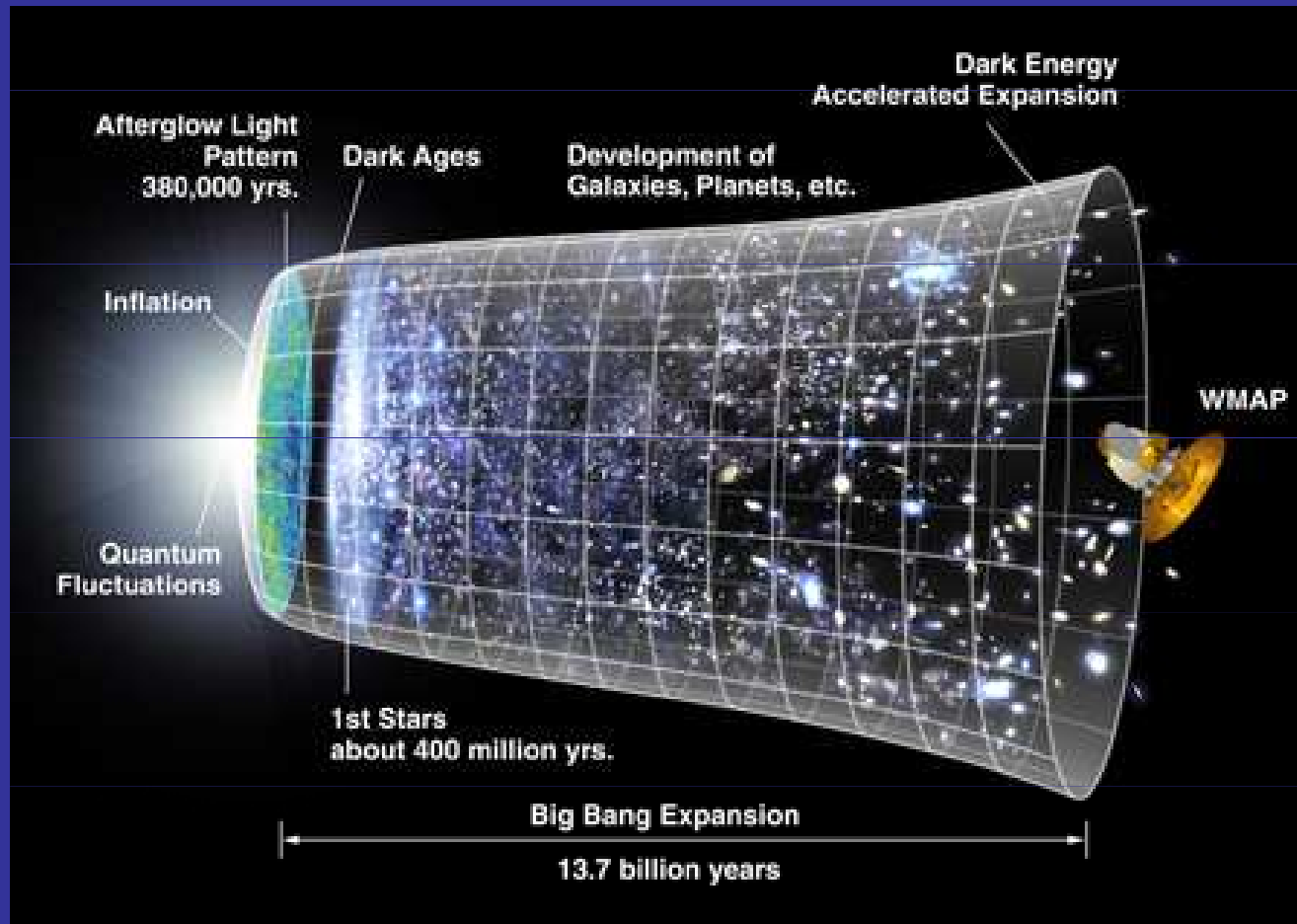
contemporary

cosmology

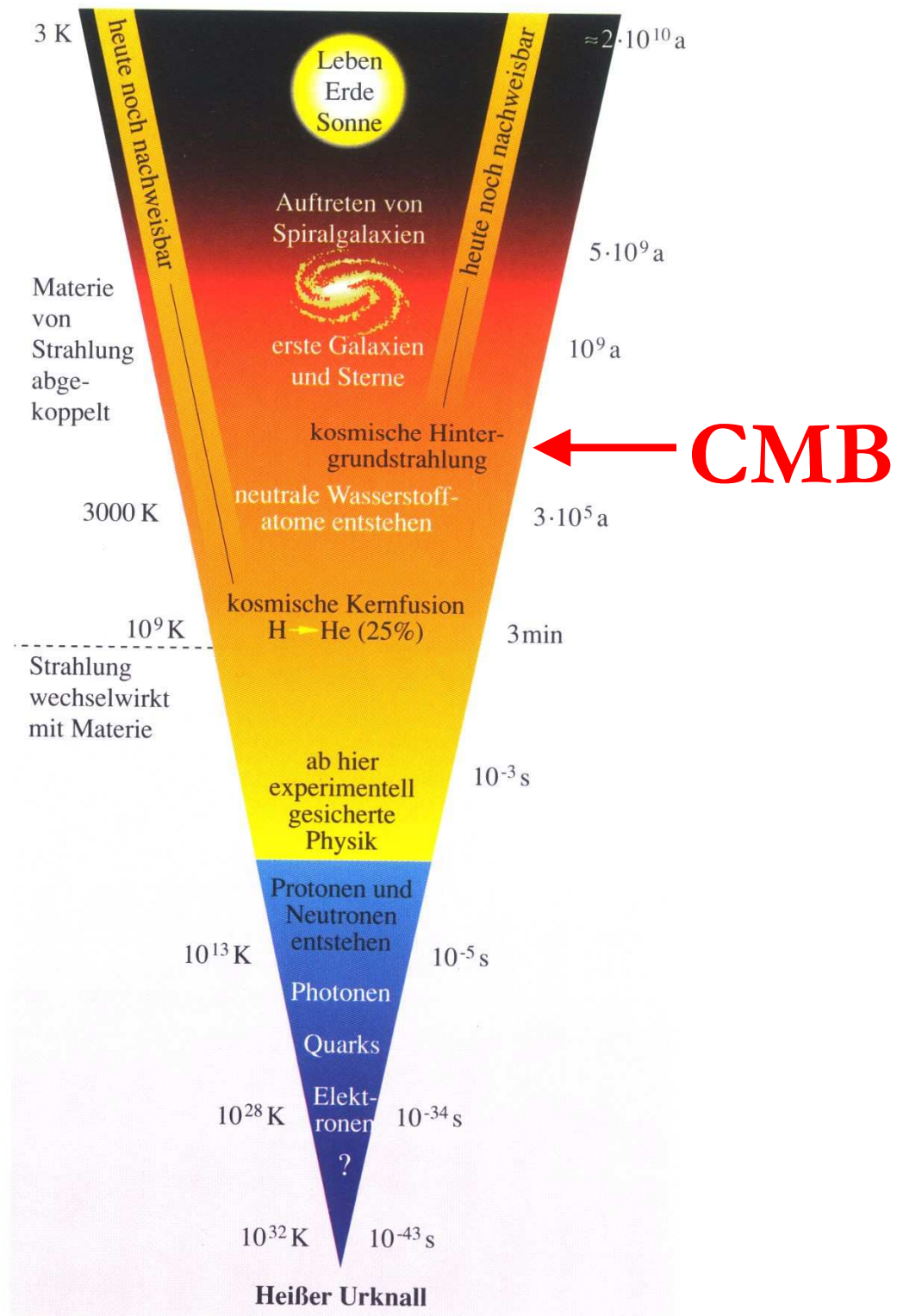
## Overview

- In the **general theory of relativity** the **elastic space can** not only be curved but it can also **expand**.
- This makes the **expansion of the Universe qualitatively easily understandable**.
- However, one should keep in mind that the special theory of relativity and conservation of energy have a limited validity.
- **Quantitatively**, the observed **expansion speed is not understood**.
- Nevertheless, a remarkably simple **phenomenological** model, the  **$\Lambda$ CDM model**, describes the expansion of the Universe quite well and explains many observations.

# One of numerous sophisticated illustrations



# History of the Universe from a German Schulbuch (Dorn-Bader)

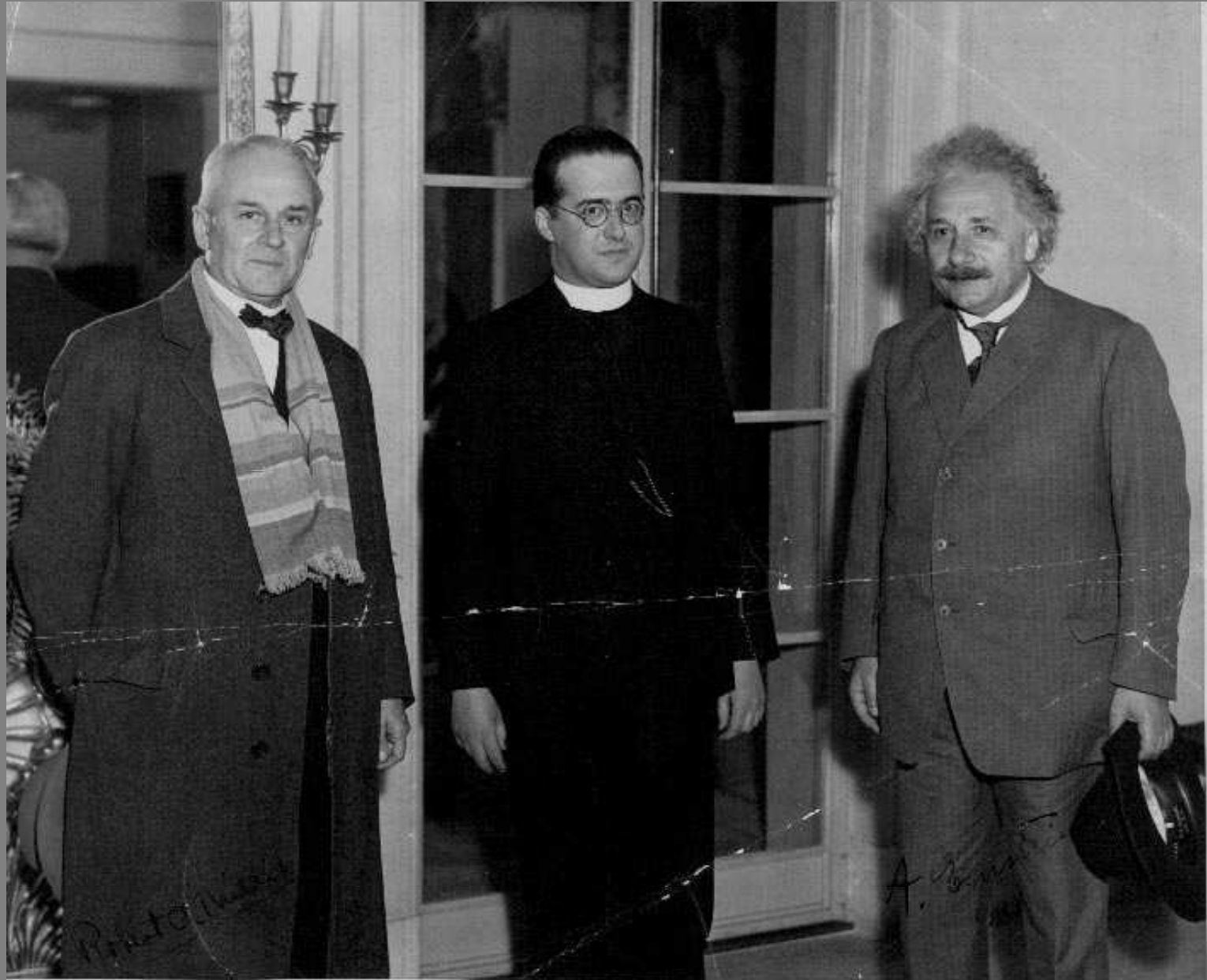


# History of the expansion paradigm (I)

- **Known** theoretically **since 1920's**  
(after GR 1915) **before Hubble**
- **Original theory** of expansion  
based on **general relativity (GR)**  
Friedmann (Russia),  
**Lemaître** (Belgium, *L'Hypothèse de l'Atome Primitif*),  
...



# Millikan, Lemaître, Einstein



# History of the expansion paradigm (II)

- **First observations in 1920's** (Slipher, ...)

- **Redshift of close Galaxies**

increases with their distance

⇒ **Evidence of the expansion:**

**Hubble** (USA)

- **Since 1998: Distant supernovae**

⇒ **Evidence of an**

**accelerated expansion**



# Understanding of the expansion

- 1920-1990's:

„simple“ explanations of the expansion without GR

(bomb-like explosion in a rigid space,  
using Newtonian mechanics or SR only,  
evoking Doppler-effect,  
assuming energy conservation, etc.)

were applicable only at small distances (locally)

- Today: observations at large distances require use of

**general relativity**

**+ cosmological constant  $\Lambda$**

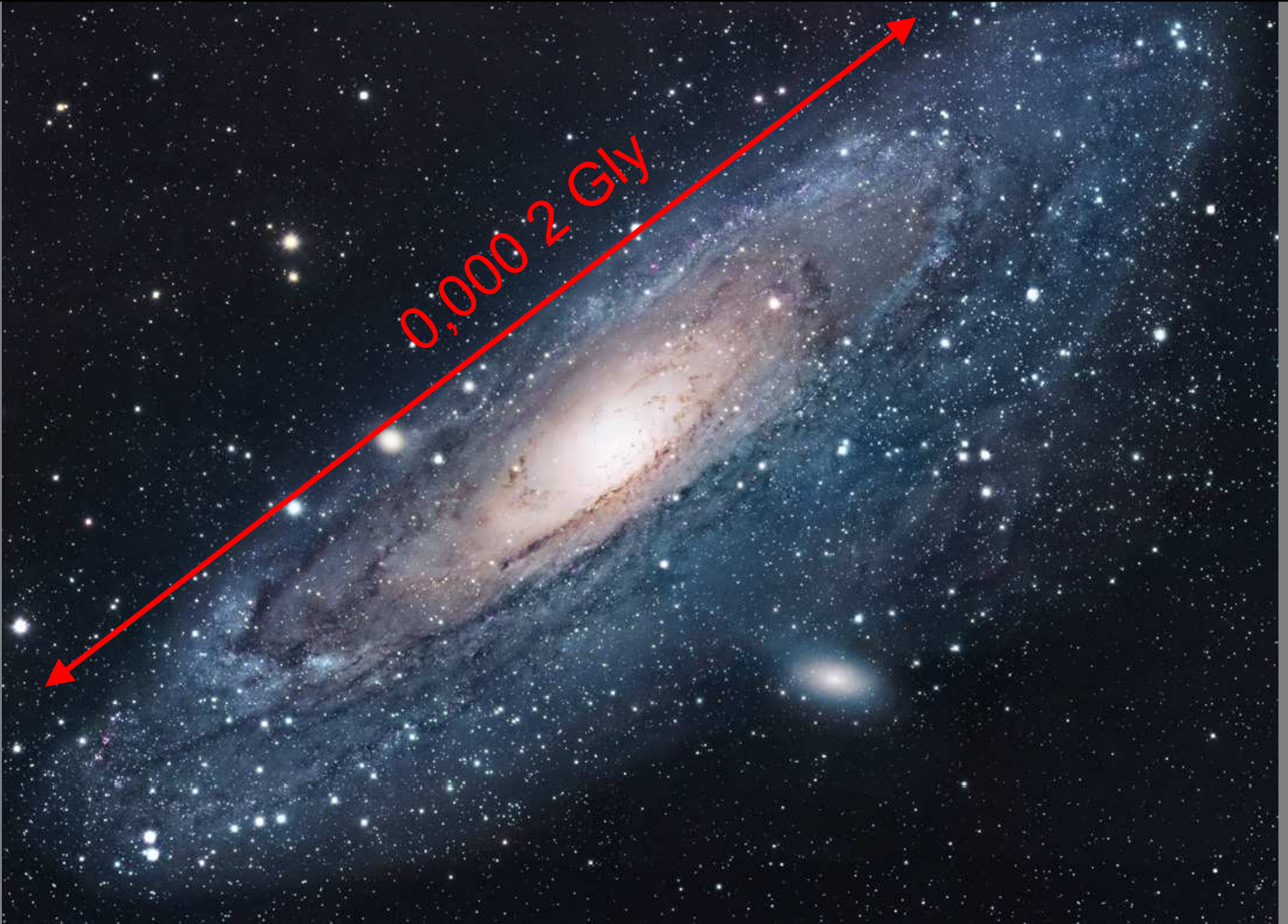
both introduced into cosmology by Einstein

# Universe on **cosmological** **time-scales** (Giga...)

- 1 Gy = 1 000 000 000 y = billion years
- Solar system age 4,5 Gy
- Our galaxy age  $\approx 10$  Gy
- Universe since the big bang  $t_0 = 14$  Gy
- Cosmic microwave background  
(CMB) origin 400 000 y = 0.000 4 Gy
- Maximum density (?)  $t \approx 0$
- Big Bang = a process! (3 min?)  $t > 0$

# Universe on **cosmological** **length-scales** (Giga...)

- 1 Gly = 1 000 000 000 ly = 1 billion light years
- Galaxies („dust particles“) 0,000 1 Gly
- Galaxy clusters 0,001 Gly
- Uniform mass distribution  
(*no structures*) from 1 Gly
- Observable Universe 46 Gly  
(source of CMB, radius today)



Andromeda, APOD



Sombbrero Galaxy • M104



Hubble  
Heritage

D





Dark matter  
in halo around  
some galaxy

dark matter  
 $\approx 10x$   
visible matter

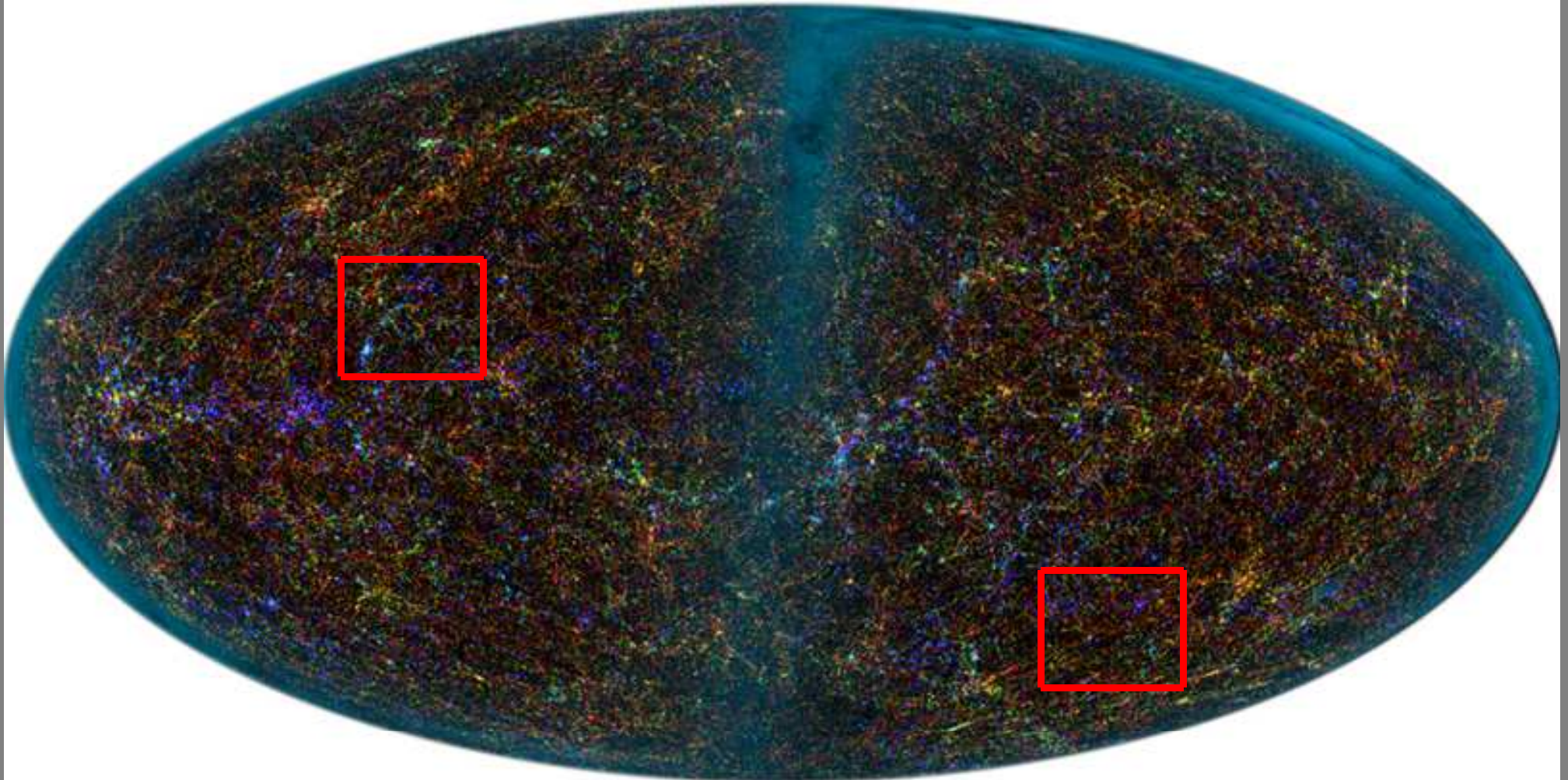
**RELEVANT**

Artist's view

D.B.Cline, SciAm March 03



# Distribution of galaxies over the whole sky

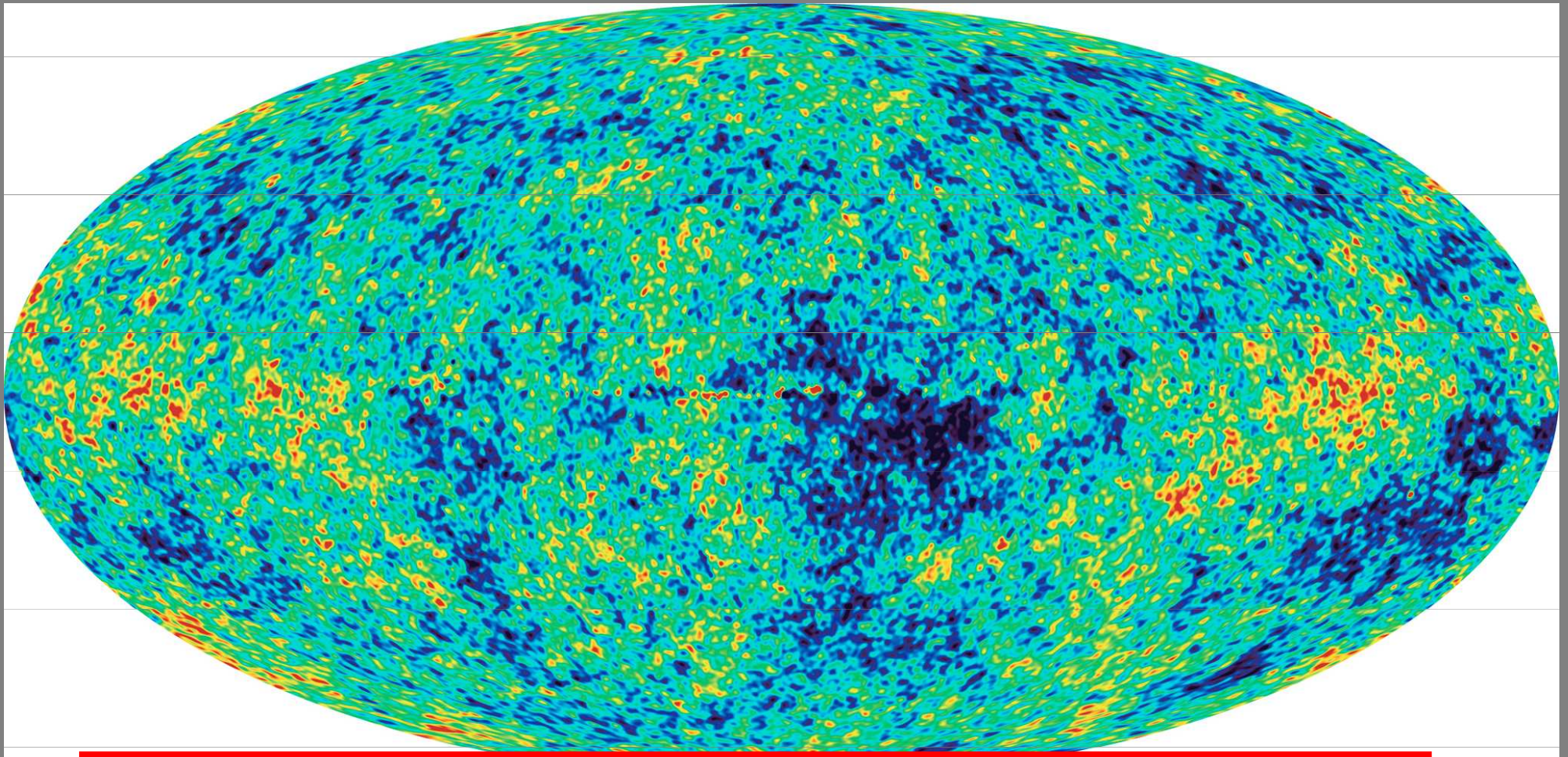




# Cosmic microwave background (CMB)

averaged over all sky directions  $T_0 = 2,730 \pm 0,001 \text{ }^\circ\text{K}$  (COBE)

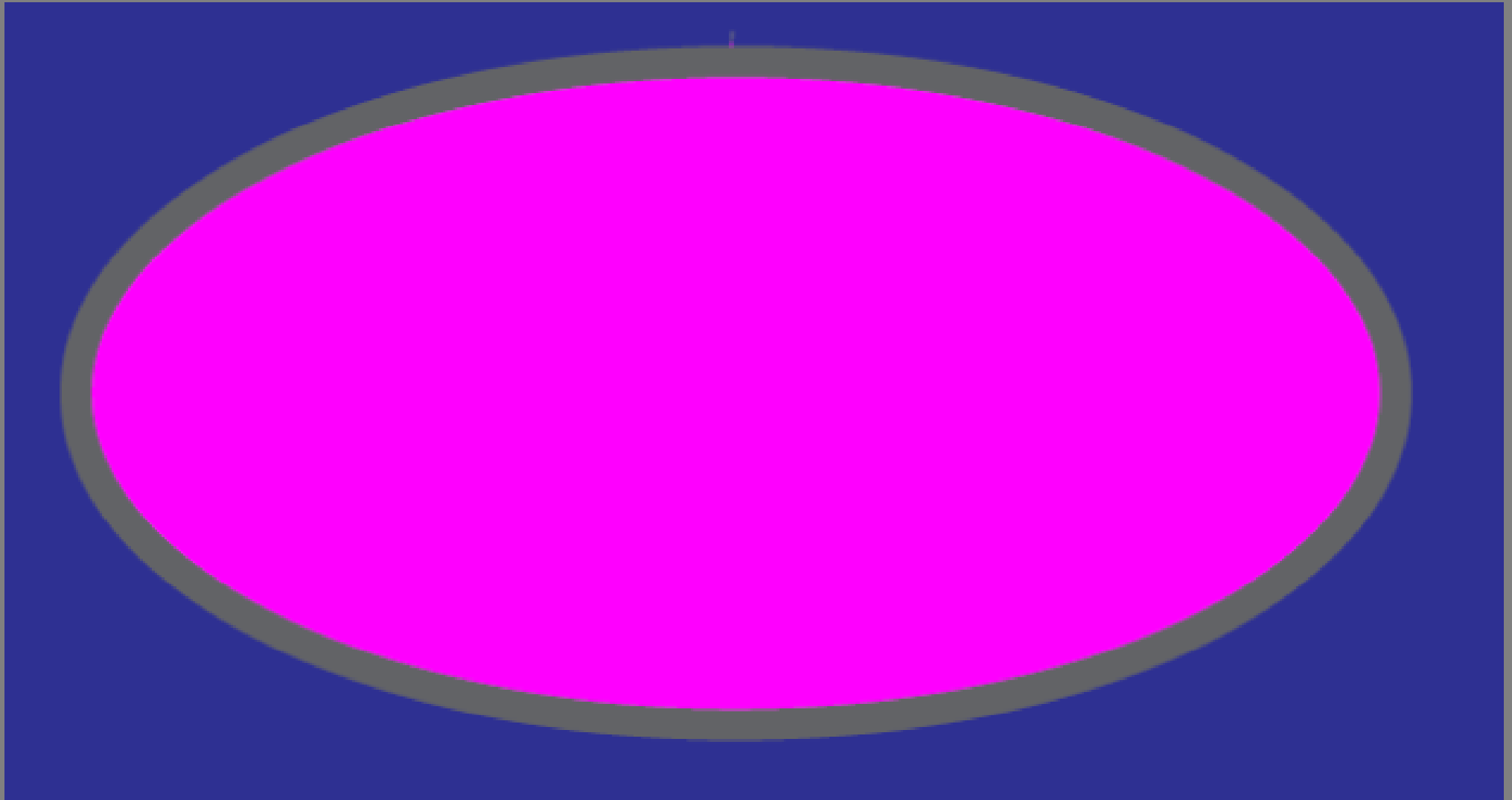
T-fluctuations only **very fine**  $0,000\ 02 \text{ }^\circ\text{K}$  (COBE and WMAP satellites)



**COBE 1989: Mather, Smoot, Nobel prize 2006**

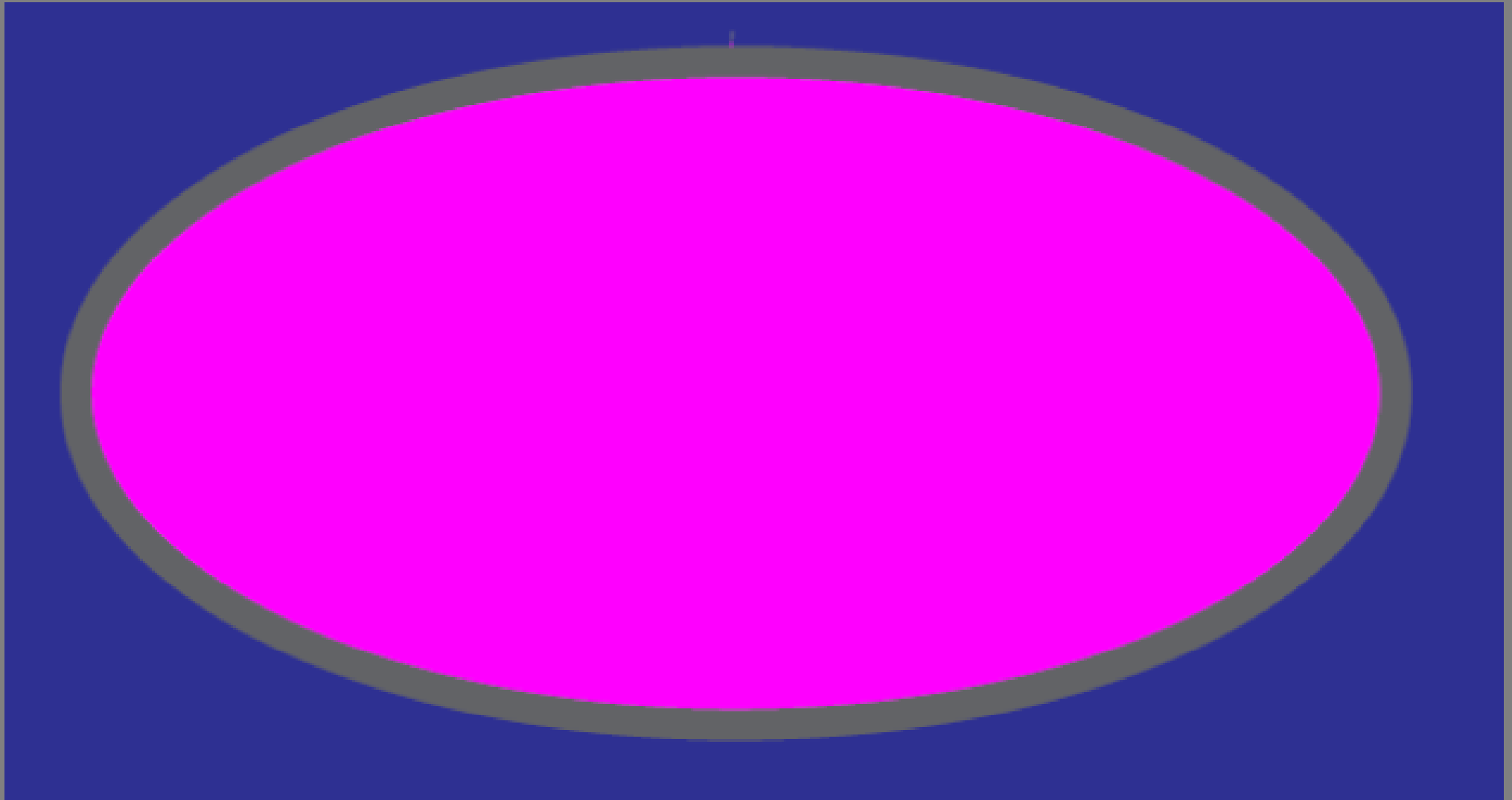
# Cosmic microwave background (CMB)

From all sky directions at **lower** T-resolution:  $T_0 = 2,7..^{\circ}\text{K}$



W. Hu, <http://background.uchicago.edu/%7ewhu/beginners/introduction.html>

On cosmological scales is the  
**observable Universe** everywhere the same



(uniform matter distribution)

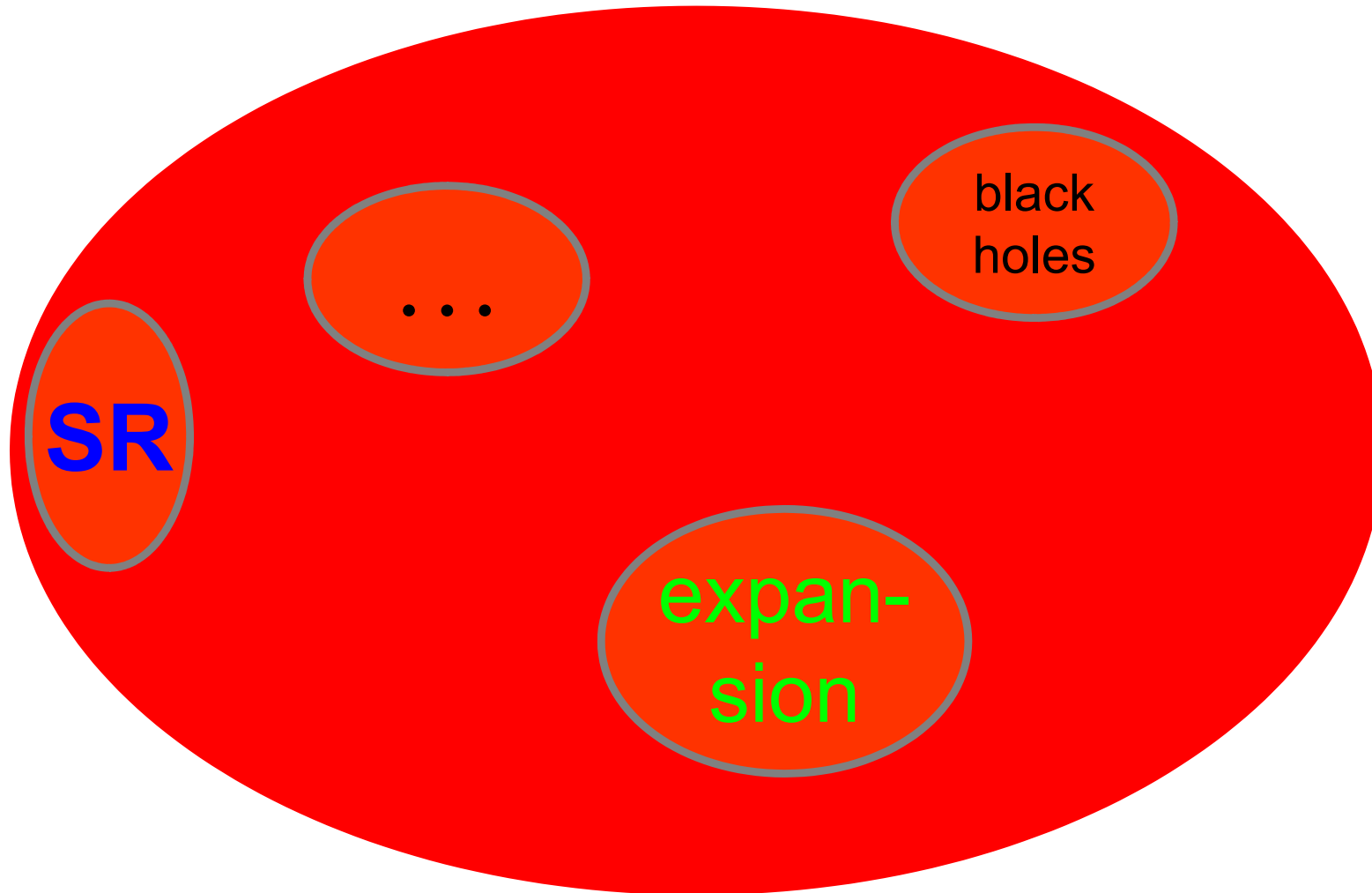
**The observable Universe  
is equal everywhere.**

**Thus it expands everywhere,  
at all observable distances.**

For an understanding of the expansion at large distances is the general theory of relativity (**GR**) with elastic space necessary

The special theory of relativity (**SR**) with rigid space is NOT applicable, since a rigid space can approximate an elastic space only locally.

Correct theory of spacetime is **GR**  
**SR**, black holes, ..., **expansion**



# Cosmic time $t$

applicable in the whole observable Universe

GR => no global inertial system is required

(different from SR)

Since the Universe is equal everywhere,  
it has also the same age everywhere

⇒ Cosmic age  $t$

Defined by the expansion as by a sandglass

Now (today):  $t = t_0$  (= 14 Gy)



# 2-dim model of expansion

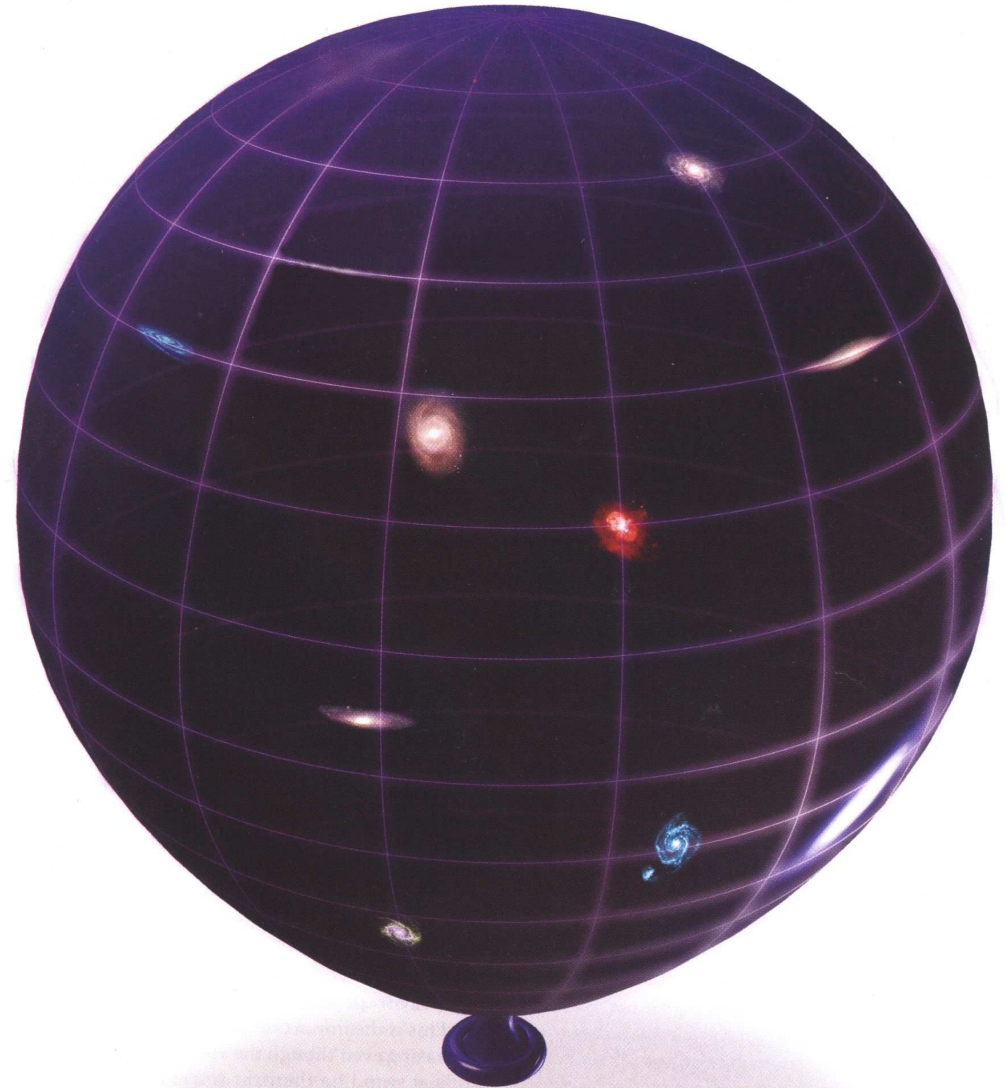
C.H.Lineweaver and T.M.Davis,  
Scientific American, March 2005

Read, please

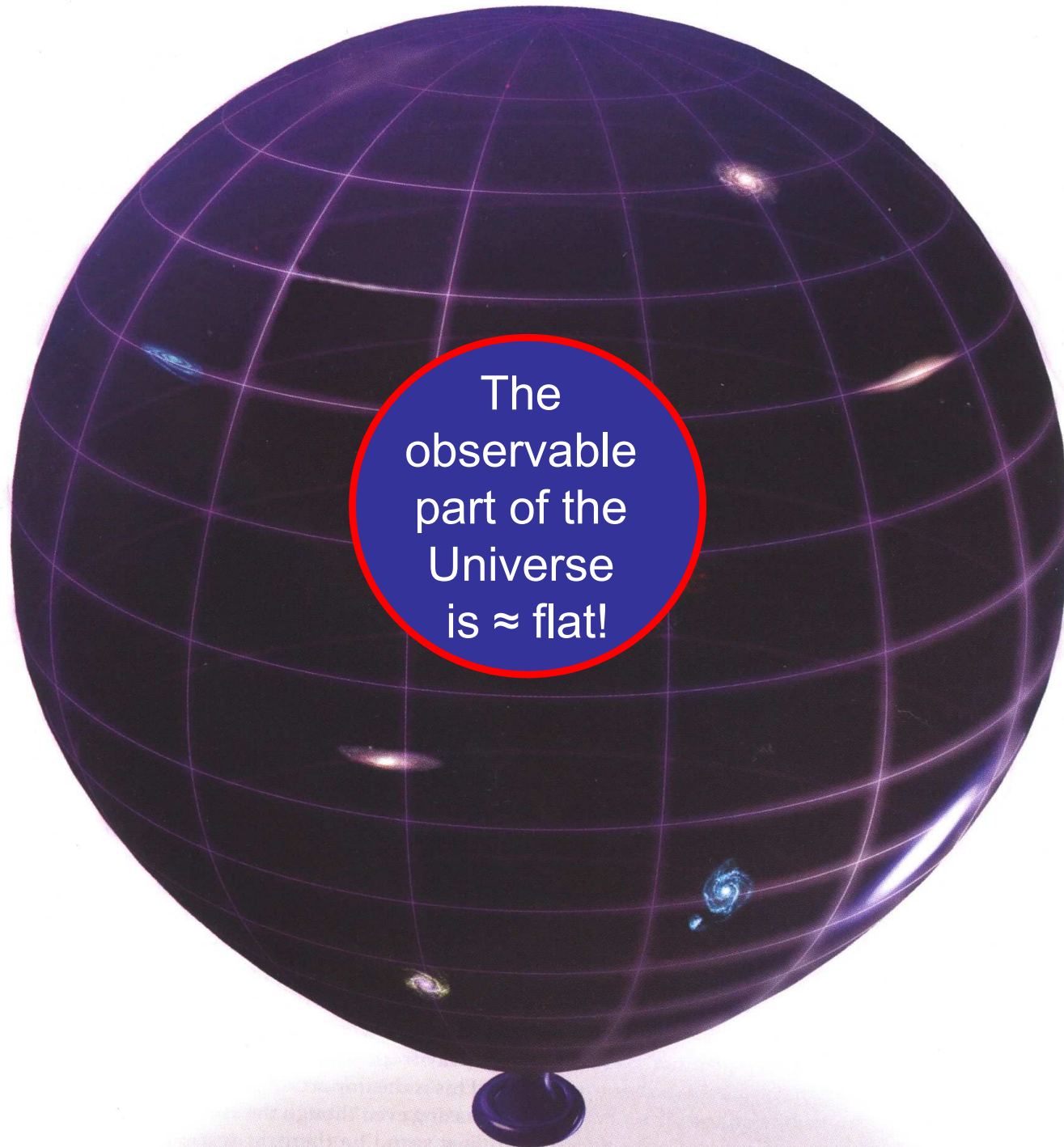
## BIG BANG

Baffled by the expansion of the universe?  
You're not alone. Even astronomers  
frequently get it wrong

By Charles H. Lineweaver and  
Tamara M. Davis







A **curved**  
2-dim surface of  
an air balloon  
is a **model** of the  
**whole** Universe,

not of the  
observable part of  
the Universe

# Cosmic („proper“) distance $D(t)$

All directions are equal:

It suffices to consider the distance  $D(t)$

between pairs of distant galaxies

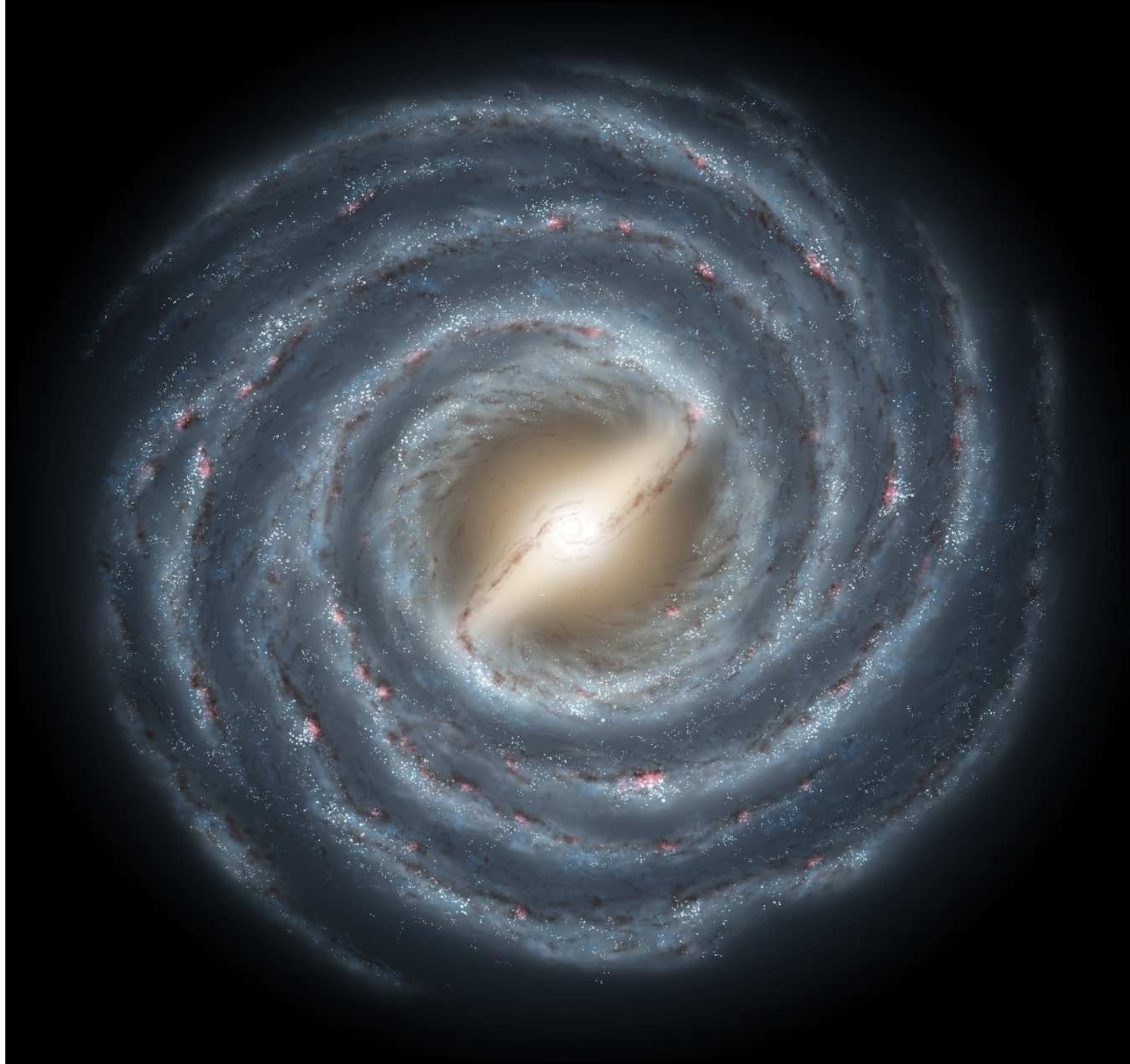
in arbitrary directions

Space is flat:

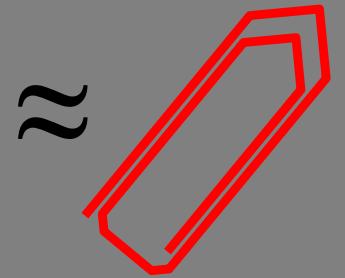
A Euclidean model of elastic space is suitable

- 1-dim GR-space: a straight rubber band



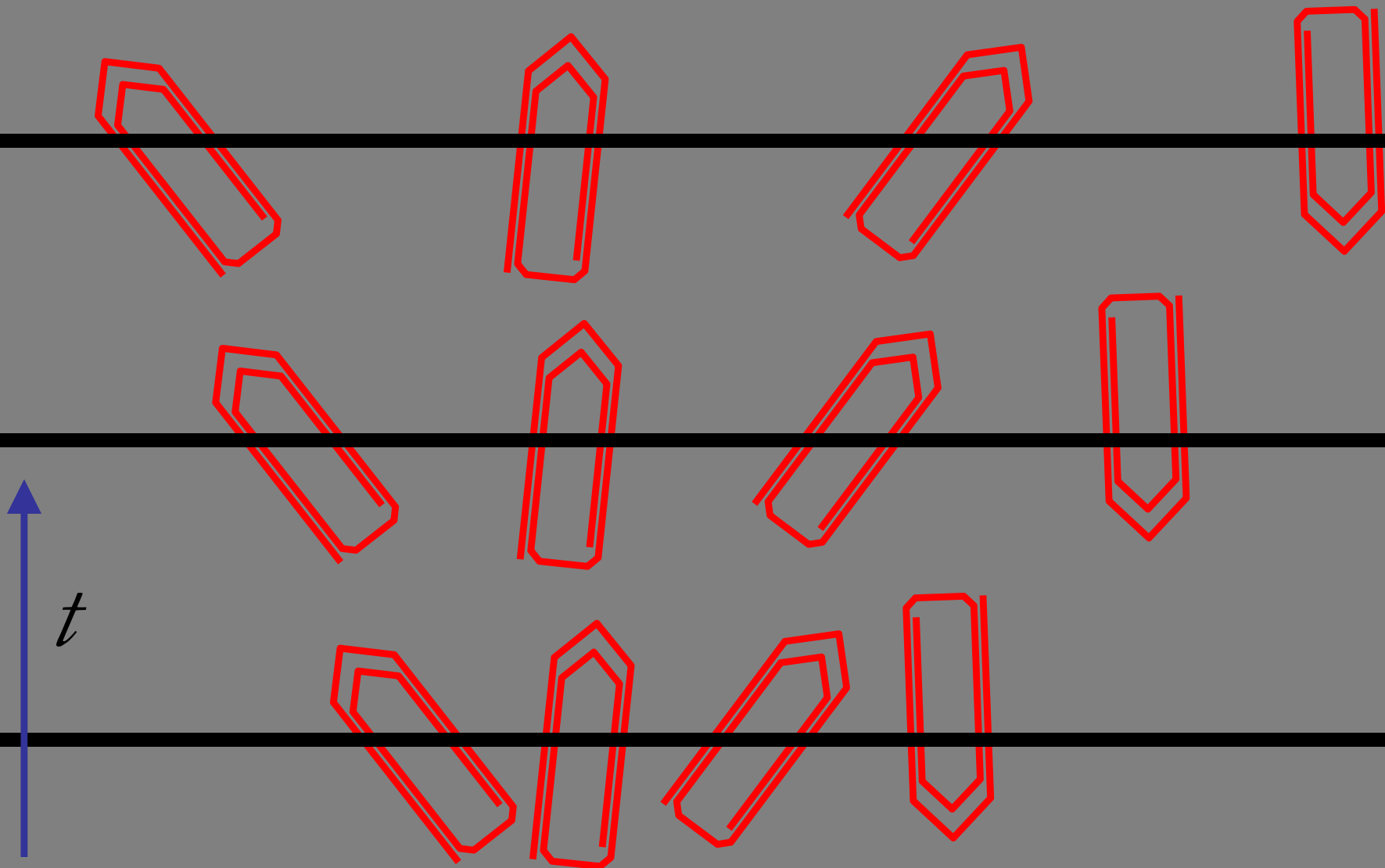


good  
approximation:



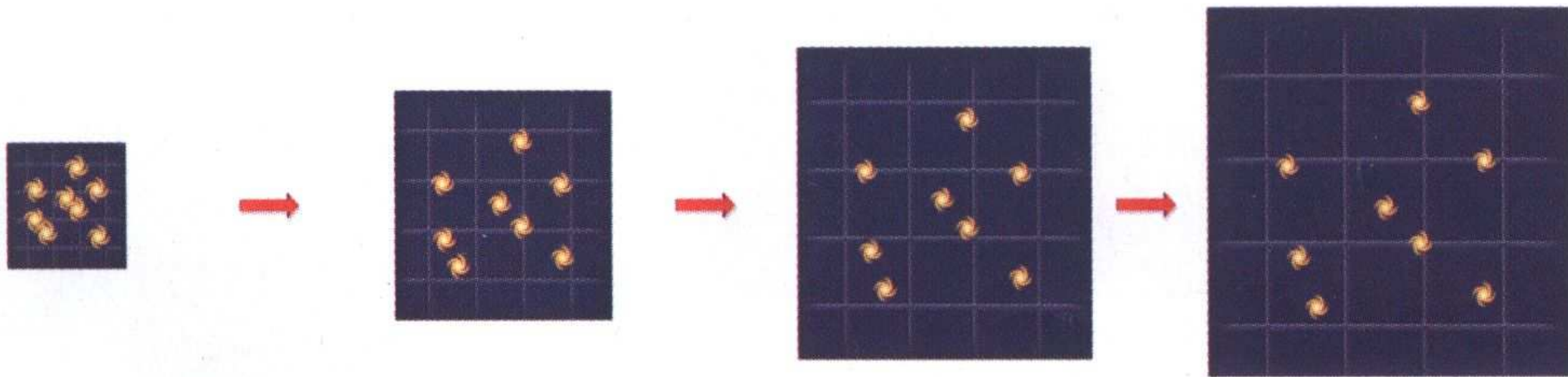
APOD

The space expands,  
but remains locally always the same.  
**Galaxies** recede from each other,  
but they **are at rest** in space and **do not expand**.





The distance between **galaxies** grows, since the **space between them expands**  
**A flat elastic membrane model:**



$t$

# What is the expansion:

- Expansion =  
stretching of elastic space

Therefore galaxies recede from each other

- Recession velocity  $u$   
of the galaxies **at rest**

is not a mechanical motion

of the galaxies through the space!

# The Hubble law

(in a modern form)

**Recession** velocity  $u$  of galaxies  
is **rigorously** proportional to their **distance**  $D$

$$u(t) = H(t) \cdot D(t)$$

$H(t)$  ... Hubble expansion parameter  
measures the expansion velocity of the space



# Hubble distance $D_H(t)$ :

$$H(t) D(t) = u(t) = c$$

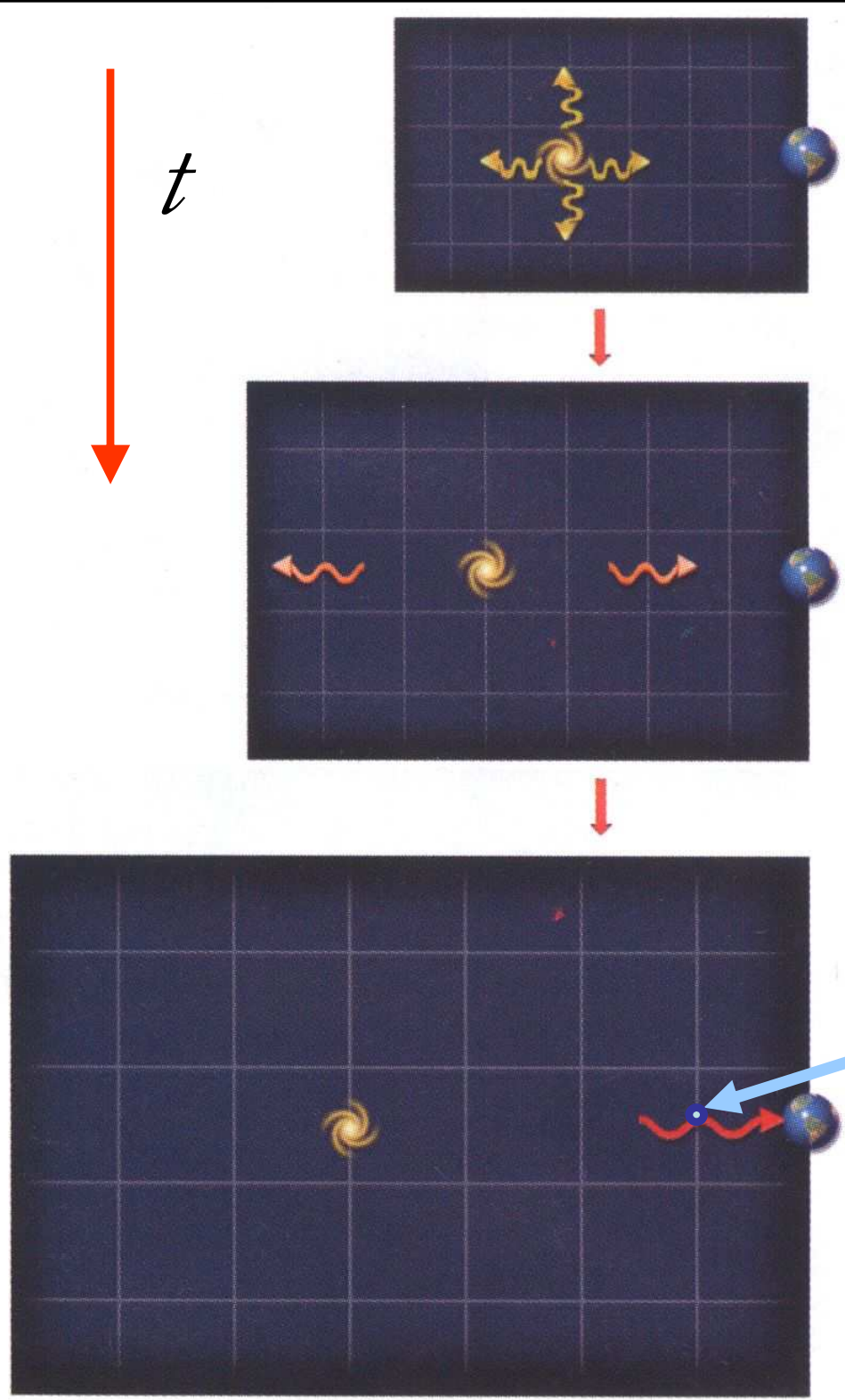
$$D_H(t) = c/H(t)$$

For  $D(t) > D_H(t)$  is

$$u(t) > c \quad !!!$$

# It is in no contradiction with SR

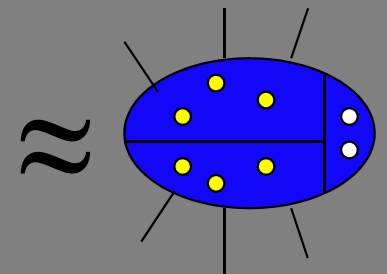
- Expansion cannot transmit a **signal**
- SR holds around any place  
= locally (in any galaxy)
- **Locally**, the light velocity is always  $c$
- **Locally**,  $c$  is the **maximal velocity**
- **At large distances (nonlocally), SR is not applicable**



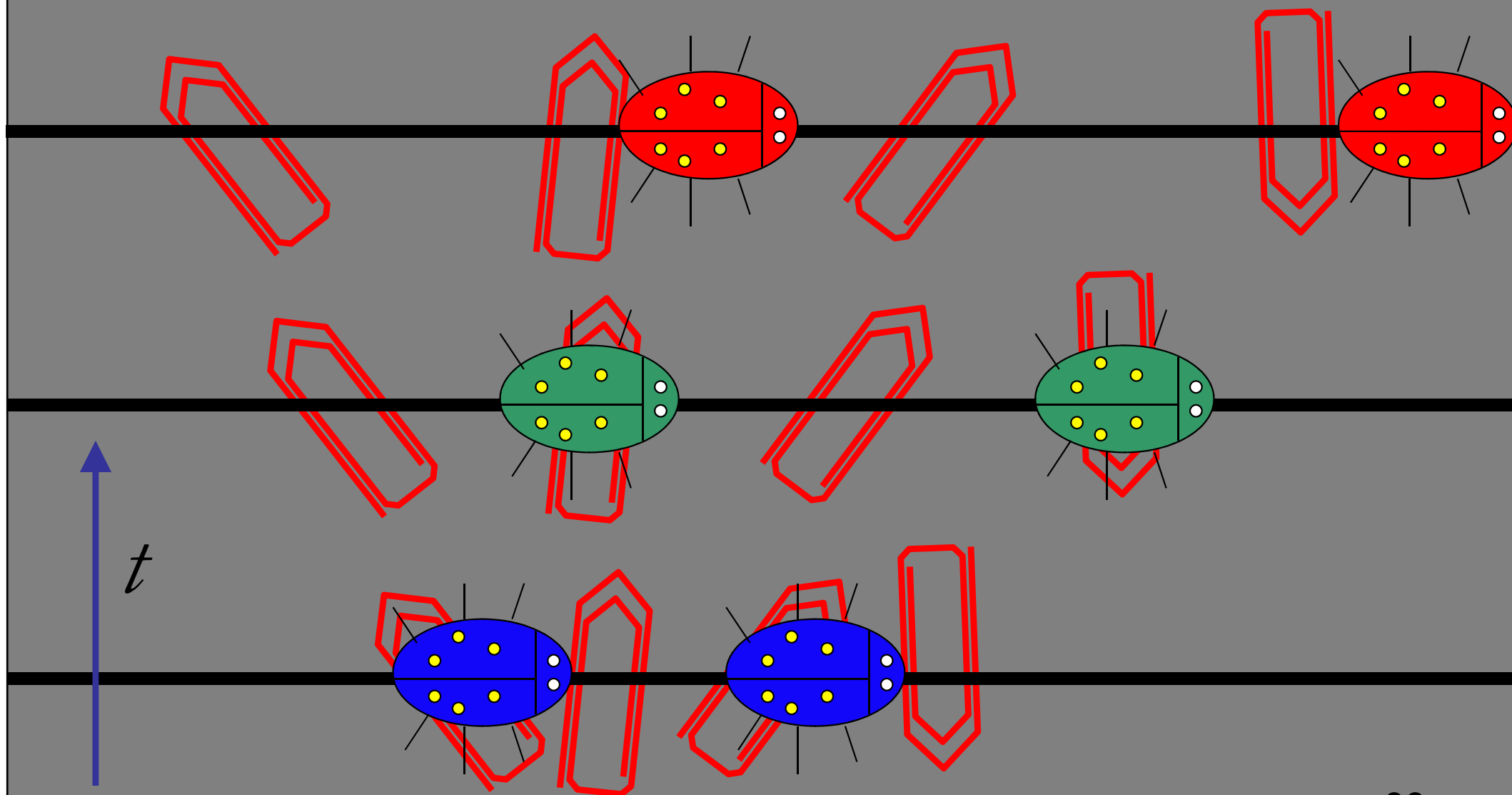
# Cosmological redshift

$z$

Wave-  
crest



The distance between **wave crests of light** increases





# Cosmological redshift $z$

- Expansion of the wave length  $\lambda$  of the light during its travel to us through the expanding space
- It has NOTHING to do with the motion of the source  
=> **NOT the Doppler effect!**
- Energy of redshifted photons decreases without any compensation (Universe cools down)

$$1 + z = \frac{\lambda_{obs}}{\lambda_{emis}}$$

# Typical observed values of $z$

- Observations by Hubble 1929:

$$D < 0,04 \text{ Gly} \quad z < 0,0003$$

- Galaxies at the Hubble distance

$$D = D_H = 14 \text{ Gly} \quad u = c \quad z = 1,5$$

- Quasars up to  $u = 2c$   $z \approx 6,4$

- CMB source:  $u = 3c$   $z = 1090$

# Universe on **cosmological** **velocity** scales

$$c = 1 \text{ Gly/Gy} = 300\,000 \text{ km/s}$$

Mechanical velocities through the space:

- Earth around Sun  $0,0001c$
- Typical motion of galaxies  $0,003c$

Large recession velocities  $u$ :

- Galaxies with  $z > 1,5$  (thousands observed!)  $> c$
- Source of CMB today ( $z = 1090$ )  $3c$
- Source of CMB „then“  $50c_{36}$

# Cosmic scale factor $a(t)$

- Distances normalized with respect to the present ones

$$a(t) = \frac{D(t)}{D(t_0)}$$

- All length scales in cosmology are proportional to the cosmic scale

$$D(t) = D(t_0) \cdot a(t)$$

$a(t)$  determines the expansion  
at all distances simultaneously

# $a(t)$ describes the expansion

- $a(t_0) = 1$   $D(t_0)$  today
- $a(t') = 2$   $D(t') = 2D(t_0)$
- $a(t'') = 1/1000$   $D(t'') = D(t_0)/1000$

$$H(t) = \frac{\dot{a}(t)}{a(t)}$$



# $z$ - $a(t)$ relation

Rigorous:

$$1 + z = \frac{1}{a(t)}$$

- $t$  ... time of emission ( $t < t_0$ )
- $1 + z$  measures the expansion of space  
between  $t$  and  $t_0$
- $z > 0$  is an evidence of the expansion

# Empirical properties of $H(t)$ :

- Hubble-law:  $v(t) = H(t) D(t)$
- $H(t)$  is  $t$ -dependent
- After the big bang it **decreased** for  $\approx 7$  Gy

$H(t) \sim 1/t \Rightarrow$  decelerated expansion

- Since  $\approx 7$  Gy

$H(t) \approx \text{const} \Rightarrow$  accelerated expansion

- The present value („Hubble-constant“):

$$H(t_0) = 70 \text{ km/s Mpc} \quad (1\text{Mpc} = 0,003 \text{ Gly})$$

... and a **THEORY ???**

# Qualitative description of changes of the expansion velocity:

**Matter decelerates** the expansion

$$\ddot{a}(t) < 0$$

Einstein's cosmological constant  $\Lambda$   
**accelerates** the expansion

$$\ddot{a}(t) > 0$$

# A. Friedmann



# THEORY of space expansion

- **Simplified** eqs. of the Einstein's general relativity

(Friedmann-Lemaître eqs. without radiation and the pressure term)

$$t > 0.000 \text{ 1 Gy}$$

$$H^2(t) = \left( \frac{\dot{a}}{a} \right)^2 = \frac{8\pi G}{3} \rho_{matter}(t) + \frac{1}{3} \Lambda - (\text{curvature})$$

$$\ddot{a}(t) = \frac{1}{3} \left( -4\pi G \cdot \rho_{matter}(t) + \Lambda \right) a(t)$$



# „Cold“ matter

- Negative contribution to the acceleration
- Decelerates the expansion
- Ist density decreases during the expansion:

$$\rho_{matter}(t) \propto \frac{1}{a^3(t)} \xrightarrow{a \rightarrow \infty} 0$$

# Cosmological constant $\Lambda$

- Positive contribution to the acceleration,  
accelerates the expansion
- Remains constant with  $t$
- **Tension of space** („negative pressure“)
- **The second greatest discovery by Einstein**  
(next to GR)
- $\Lambda \neq 0$  is **generic** in GR

( $\Lambda g_{\mu\nu}$  term in E. eqs., but ist value ???)

# Willem de Sitter



# De Sitter Universe

- Universe without matter, only  $\Lambda$
- De Sitter (the Netherlands) 1917:

$$\ddot{a}(t) = \frac{\Lambda}{3} \cdot a(t)$$

$$a(t) \propto e^{H_\infty \cdot t}$$

$$H_\infty = \sqrt{\Lambda / 3} = \text{const}$$

Exponentially accelerated expansion

# Discovery during the last 10 years:

- Distant supernovae observations =>

The expansion  
accelerates!

Some accelerating term  
like  $\Lambda$  is required



# The cause of the acceleration?

- **New constant of Nature**

= cosmological constant  $\Lambda$  à la Einstein?

- **Energy of the vacuum (quantum effect)?**

To be expected, but theoreticians cannot calculate its value

- **Quintessence? A new scalar field  $\approx \Lambda(t)$ ?**

Suggested first by Ch. Wetterich (Heidelberg)



Quintessence !

Fire , air,  
water, earth!

← Standard-  
model of  
the antic  
Greeks

Constant of Nature  $\Lambda$ , Quintessence,

Vacuum energy, ???

Cosmologists need *something* like that:

„**DARK ENERGY**“

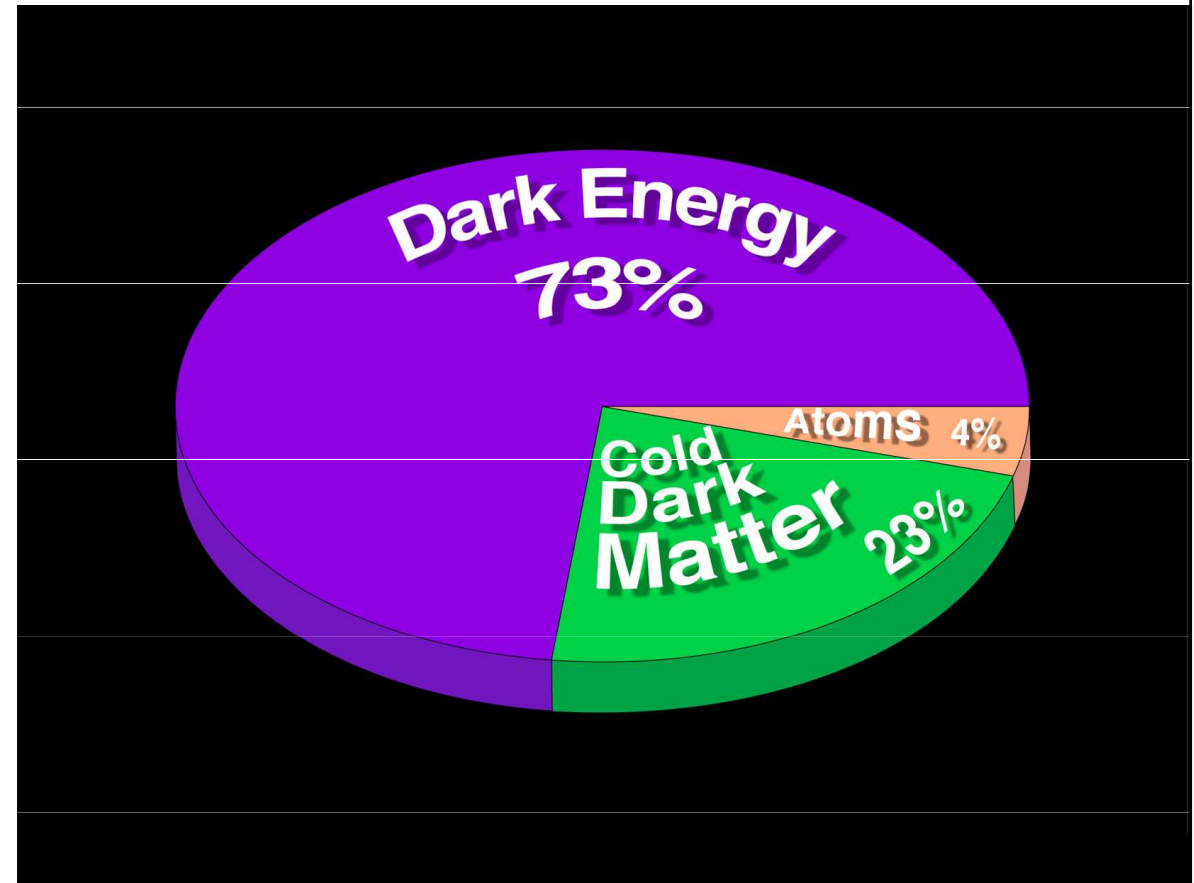
Nobody knows, what it is,

since it is **transparent** (unobservable)!

- A completely new category  
(**tension of space**)?

# Energy in contemporary observable Universe

- 73±% dark energy dominates
- 23±% unknown matter („dark matter“)
- 4% known matter  
≈ atoms (stars, H-gas, ourselves)
- Matter slows down, dark energy speeds up the expansion

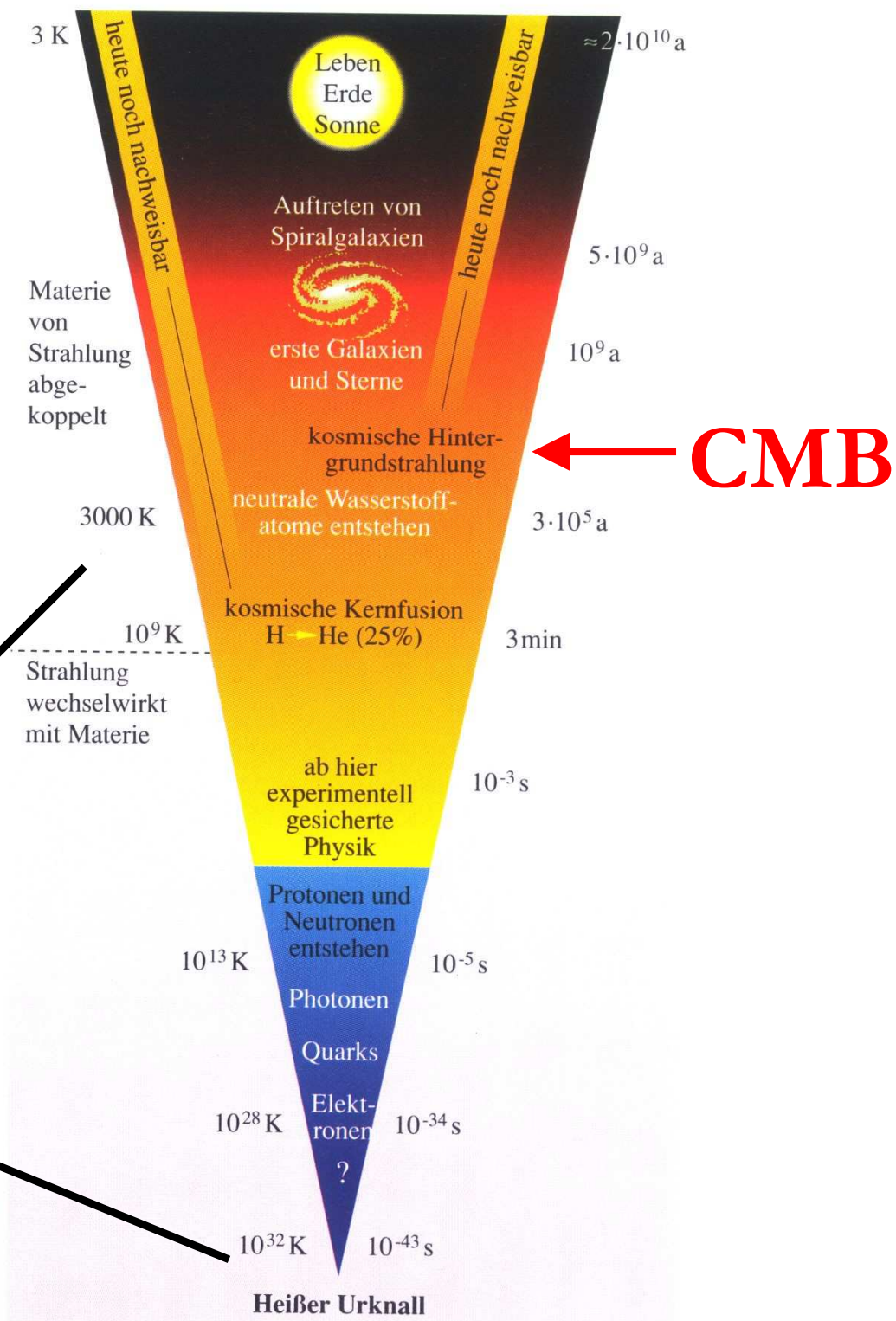


WMAP



# History of the Universe

Early Universe





# Further components in the **early Universe**

- $t < 0,000\ 1\ \text{Gy}$ : **radiation** must be included (photons, neutrinos, other particles with  $v \approx c$ ) [phys. straightforward, but math. more complex].
- **Seeds of inhomogeneities** must be included [models].
- $t < 0,0...01\ \text{sec}$ : **big speculations about big bang** (inflation, quantum gravity, big bounce, pre-big bang universe, ekpyrotic universe, strings, branes, multiverse, baby universes, ...)
- „Cosmologists are often wrong, but never in doubt“  
L.D. Landau
- I am not cosmologist
- **New ideas and surprises to be expected!**

**$t > 0,000\ 1\ \text{Gy}$ : simplified  $\Lambda\text{CDM}$  model  
is reliable on cosmological scales  
(above the scales of inhomogeneities)**

# $\Lambda$ CDM model of our Universe

## Assumptions on cosmological scales:

- (1) Observable Universe is („cosmological principle“) homogeneous and isotropic
- (2) CMB ((1)  $\rightarrow$  isotropic, observable everywhere)
- (3) Expanding space is flat
- (4) Simplified GR eq. of motion for  $a(t)$
- (5) Evolution of  $a(t)$  is determined ( $t > 0.000$  1Gy) by
  - cold dark matter (**CDM**) (dominates earlier epoch)
  - cosmological constant  $\Lambda$  (dominates later epoch)

# (1) → Hubble law

- Recession velocity of distant points

$$D(t) = a(t)D(t_0)$$

$$u(t) = \dot{D}(t) = \dot{a}(t)D(t_0) = \frac{\dot{a}(t)}{a(t)}D(t)$$

$$H(t) = \frac{\dot{a}(t)}{a(t)}$$

Thus linear dependence on the distance at fixed  $t$

$$u(t) = H(t)D(t)$$

**(1)** → Cosmological redshift  $z$

$$\lambda_{obs} = (1 + z)\lambda_{em}$$

$$D(t) = a(t)D(t_0)$$

$$t = t_{em}$$

$$1 + z(t_{em}) = 1/a(t_{em})$$

# (1)-(5) $\rightarrow$ Eq. of motion for $a(t)$

- Conveniently reparameterized form:

$$\ddot{a}(t) = H_0^2 \left( -\frac{1}{2} \Omega_M \frac{1}{a^2(t)} + \Omega_\Lambda a(t) \right)$$

$$\Omega_M = 0.24, \quad \Omega_\Lambda = 0.76$$

$$H_0 = 73 \frac{\text{km}}{\text{s.Mpc}} = 0.075 \frac{c}{\text{Gly}}$$

$$H_0^2 = \frac{1}{3} (8\pi G \rho_M(t_0) + c^2 \Lambda),$$

$$\Omega_M = \frac{8\pi G}{3H_0^2} \rho_M(t_0), \quad \Omega_\Lambda = \frac{c^2 \Lambda}{3H_0^2}$$

# Exact solution

$$a(t) = \left( \frac{\Omega_M}{\Omega_\Lambda} \right)^{1/3} \sinh^{2/3} \left( 3\sqrt{\Omega_\Lambda} H_0 t / 2 \right)$$

**Small  $t$ :**

$$a(t) \propto t^{2/3}, \quad \ddot{a}(t) \propto -t^{-4/3}, \quad H(t) \propto t^{-1}, \quad D_H(t) \propto t$$

**Large  $t$ :**

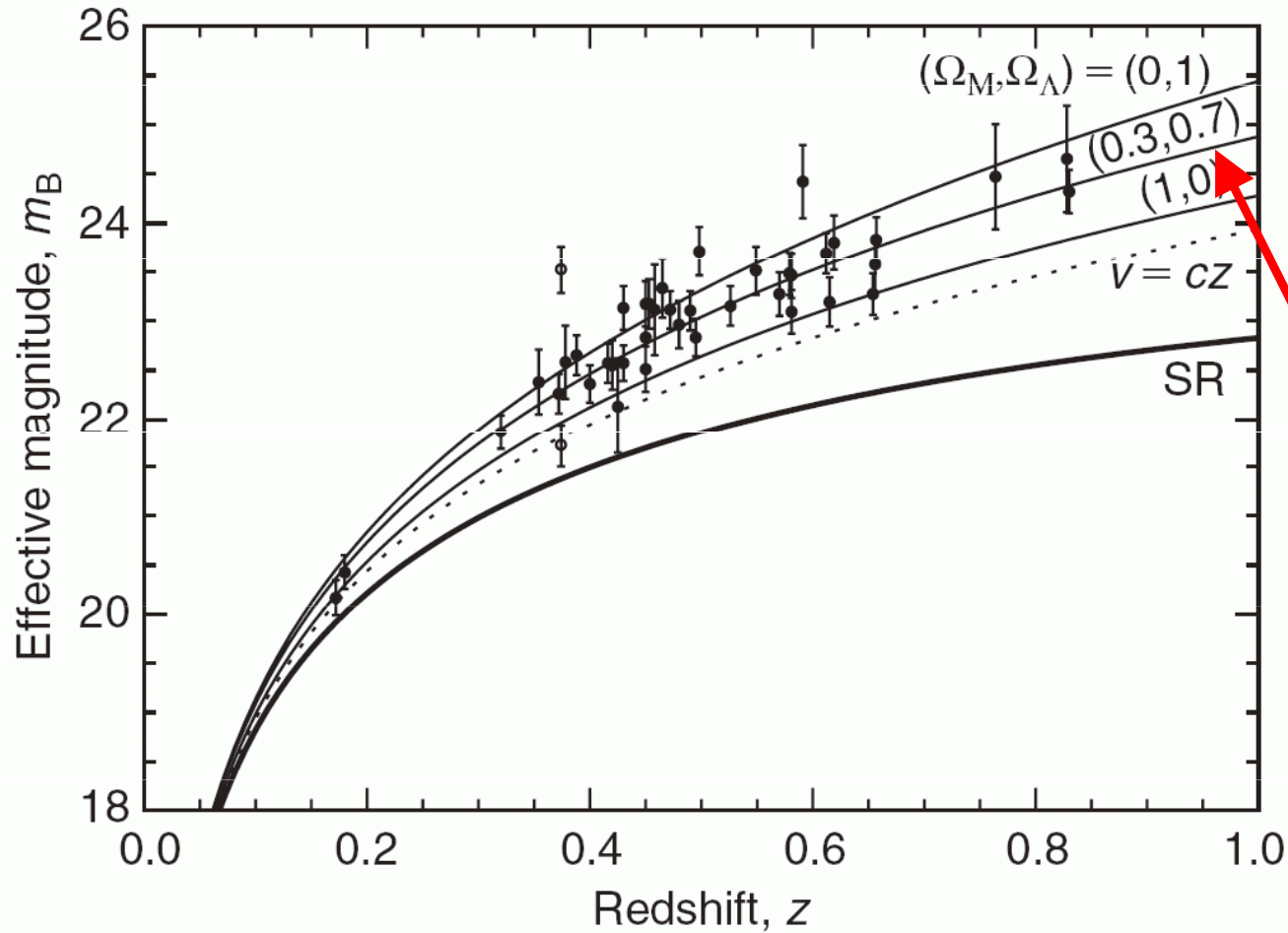
$$\ddot{a}(t) \propto a(t) \propto \exp(H_\infty t)$$

$$H_\infty = H(t = \infty) = H_0 \sqrt{\Omega_\Lambda}$$



# Some models

(Fig.5 from: <http://www.mso.anu.edu.au/~charley/papers/DavisLineweaver04.pdf> )



# Our light cone

- World lines of light we observe today
- Emitted

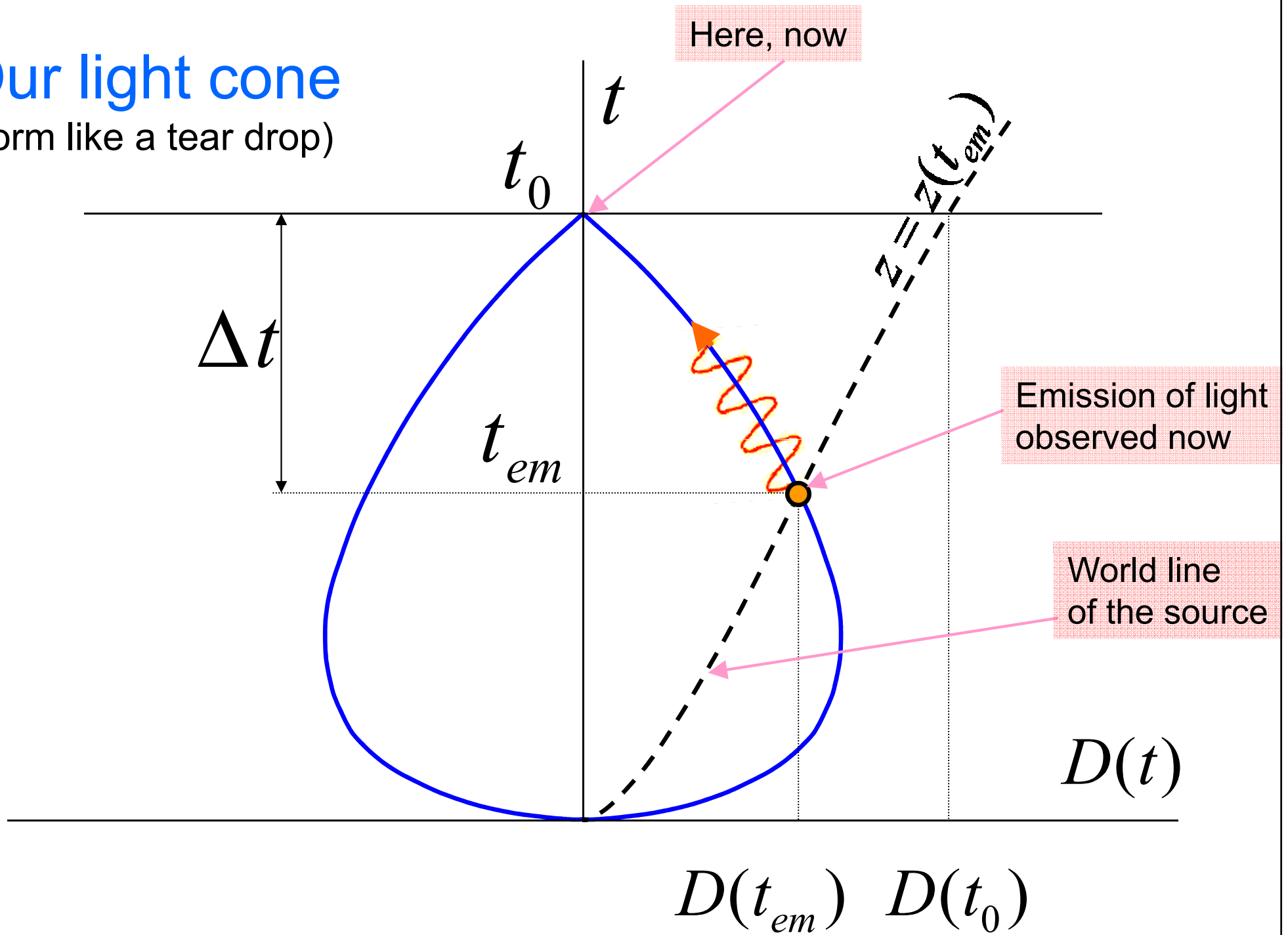
at various times  $t_{em}$

at distances  $D(t_{em})$

$$D(t_{em}) = a(t_{em})c \int_{t_{em}}^{t_0} \frac{dt'}{a(t')}$$

# Our light cone

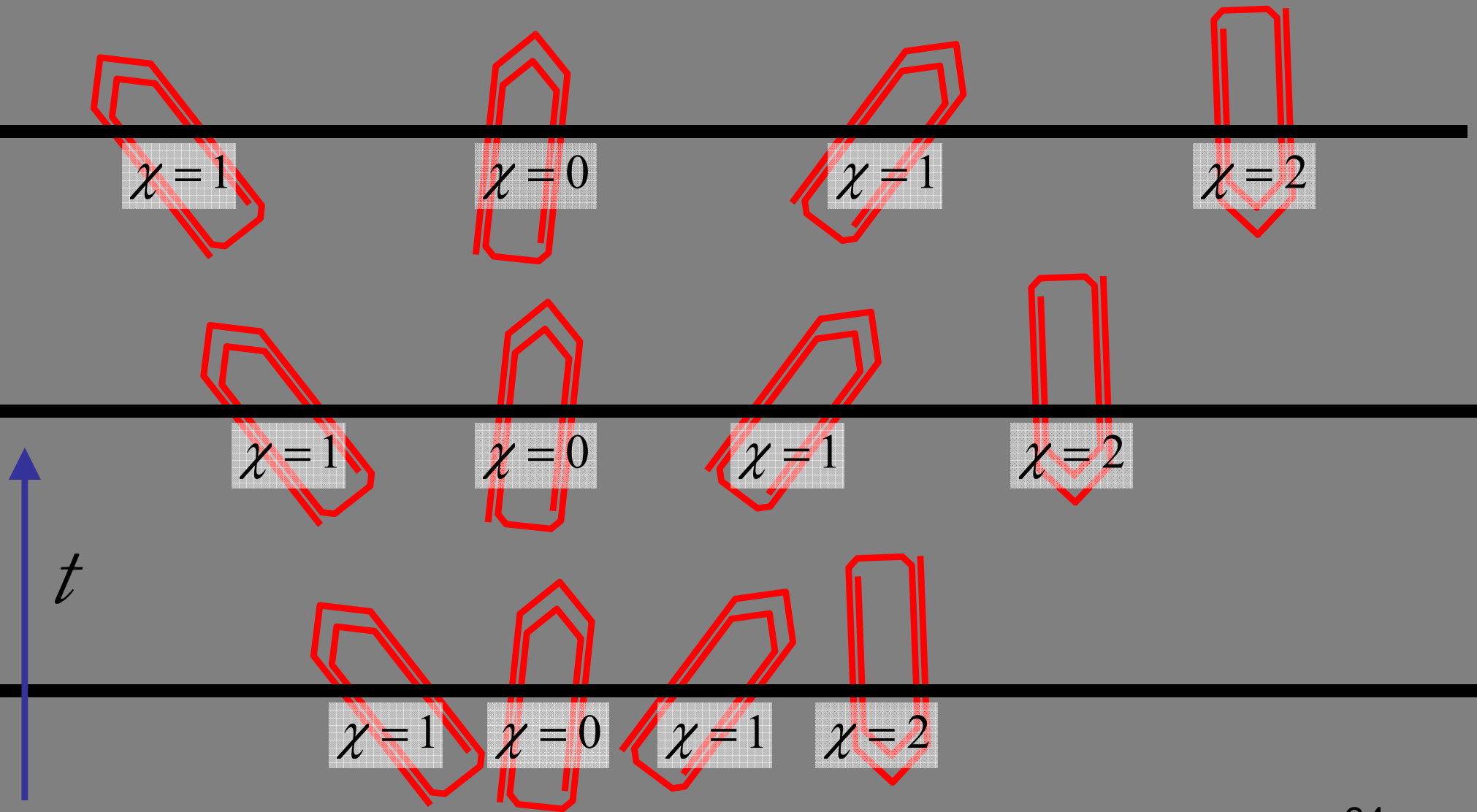
(form like a tear drop)



# (1)(2) → Fixed points in space

- Origins of local reference frames in which CMB is isotropic
- Defined by a global method (SR not applicable!)
- Such points are in **absolute rest** with respect to the surrounding space
- They obey the Hubble law rigorously
- **Distant galaxies** can be in good approximation identified with **fixed points**  
(recession velocities  $\gg$  peculiar velocities)
- Clocks at rest at fixed points **define the absolute cosmic time  $t$**

# Comoving coordinates of fixed points (galaxies) $\chi$



# Comoving coordinate $\chi$

- Dimensionless coordinates of fixed points (galaxies) in space
- Defined by the present distances of these points

$$D(t_0) = R_0 \chi$$

- $t$  -independent
- $R_0$  ... distance of a point with  $\chi = 1$

$$D(t) = a(t) D(t_0) = a(t) R_0 \chi$$



# Suitable internet addresses

- <http://tpe.physik.rwth-aachen.de/jersak/expansion.html>
- <http://www.mso.anu.edu.au/~charley/papers/LineweaverDavisSciAm.pdf>  
<http://www.mso.anu.edu.au/~charley/papers/DavisLineweaver04.pdf>  
[http://www.astro.virginia.edu/class/whittle/astr553/Topic16/t16\\_light\\_cones.html](http://www.astro.virginia.edu/class/whittle/astr553/Topic16/t16_light_cones.html)  
<http://www.astro.ucla.edu/~wright/cosmolog.htm>  
[http://en.wikipedia.org/wiki/Expansion\\_of\\_space#Overview\\_of\\_metrics](http://en.wikipedia.org/wiki/Expansion_of_space#Overview_of_metrics)  
<http://www.talkorigins.org/faqs/astronomy/bigbang.html#misconceptions>  
[http://en.wikipedia.org/wiki/Georges\\_Lema%C3%AAtre](http://en.wikipedia.org/wiki/Georges_Lema%C3%AAtre)



# Kosmologie mal anders

