

Example: Ice Cream Sales

The local ice cream shop keeps track of how much ice cream they sell versus the temperature of that day for th
 Formulate a null hypothesis and verify it by Pearsons and Spearman coefficients

Ho: there is no correlation between t
 H1: there is a correlation between t

Temperature (°C)	Ice Cream Sales (\$)
14.2	215
16.4	325
11.9	185
15.2	332
18.5	406
22.1	522
19.4	412
25.1	614
23.4	544
18.1	421
22.6	445
17.2	408

N: 12
 N^3: 1728

Spearman coefficients

Rank temperature	Rank ice cream sales
11	11
9	10
12	12
10	9
6	8
4	3
5	6
1	1
2	2
7	5
3	4
8	7

rs:
 critical value:

Ho is rejected, there is a cor

Average: 18.7 402.42

Diferrences

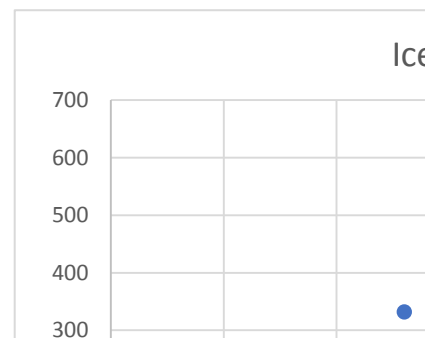
-4.5	-187.42	838.69
-2.3	-77.42	176.12
-6.8	-217.42	1473.00
-3.5	-70.42	244.70
-0.2	3.58	-0.63
3.4	119.58	409.57
0.7	9.58	6.95
6.4	211.58	1359.42
4.7	141.58	668.98
-0.6	18.58	-10.69
3.9	42.58	167.14
-1.5	5.58	-8.24

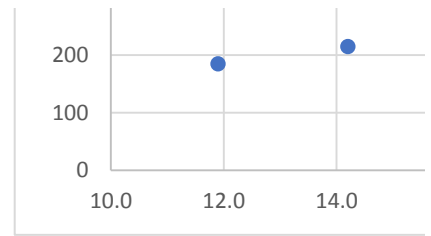
177.0 174754.92 5325.03

Pearsons coefficients

alpha: 0.05
 D.O.F 10
 r: 0.9575
 critical value: 0.576

Ho is rejected, there is a cor





the last 12 days:

the number of ice cream sell and the temperature
 the number of ice cream sell and the temperature

difference
 0
 -1
 0
 1
 -2
 1
 -1
 0
 0
 2
 -1
 1
 14
 0.951049
 0.587

$$r_s = 1 - \frac{6 \sum_{i=1}^n d_i^2}{n^3 - n}$$

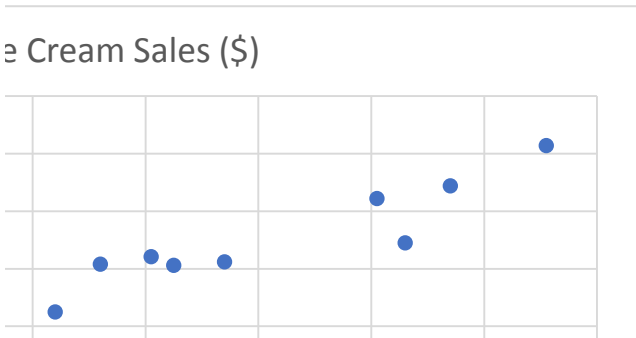
n \ α	0.2	
4	1.000	1.
5	0.800	0.
6	0.657	0.
7	0.571	0.
8	0.524	0.
9	0.483	0.
10	0.455	0.
11	0.427	0.
12	0.406	0.
13	0.385	0.
14	0.367	0.
15	0.354	0.
16	0.341	0.
17	0.328	0.

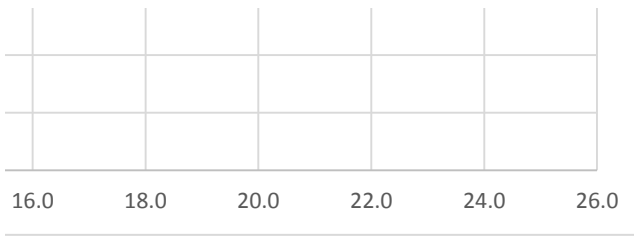
relation between the number of ice cream sell and the temperature

Pearson On	
r crit.	.05
Two	
df	.10
1	.988
2	.900
3	.805
4	.729
5	.669
6	.622
7	.582
8	.549
9	.521
10	.497

relation between the number of ice cream sell and the temperature

$$r = \frac{\sum (X_i - \bar{X})(Y_i - \bar{Y})}{\sqrt{\sum (X_i - \bar{X})^2 \sum (Y_i - \bar{Y})^2}}$$





0.1	0.05	0.02	0.01	n \ α	0.2	0.1	0.05	0.02	0.01
.000	—	—	—	18	0.317	0.401	0.472	0.550	0.600
.900	1.000	1.000	—	19	0.309	0.391	0.460	0.535	0.584
.829	0.886	0.943	1.000	20	0.299	0.380	0.447	0.522	0.570
.714	0.786	0.893	0.929	21	0.292	0.370	0.436	0.509	0.556
.643	0.738	0.833	0.881	22	0.284	0.361	0.425	0.497	0.544
.600	0.700	0.783	0.833	23	0.278	0.353	0.416	0.486	0.532
.564	0.648	0.745	0.794	24	0.271	0.344	0.407	0.476	0.521
.536	0.618	0.709	0.755	25	0.265	0.337	0.398	0.466	0.511
.503	0.587	0.678	0.727	26	0.259	0.331	0.390	0.457	0.501
.484	0.560	0.648	0.703	27	0.255	0.324	0.383	0.449	0.492
.464	0.538	0.626	0.679	28	0.250	0.318	0.375	0.441	0.483
.446	0.521	0.604	0.654	29	0.245	0.312	0.368	0.433	0.475
.429	0.503	0.582	0.635	30	0.240	0.306	0.362	0.425	0.467
.414	0.488	0.566	0.618						

rho critical values for 2-tailed test

One-Tailed Test

.025	.01
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Two-Tailed Test

.05	.02
.997	.9995
.950	.980
.878	.934
.811	.882
.754	.833
.707	.789
.666	.750
.632	.716
.602	.685
.576	.658

$$\frac{-\bar{X}(Y_i - \bar{Y})}{\bar{X}^2 \sum (Y_i - \bar{Y})^2}$$

