

Example: Ice Cream Sales

The local ice cream shop keeps track of how much ice cream they sell versus the temperature of that day
 Formulate a null hypothesis and verify it by Pearsons and Spearman coefficients
 H0: there is no correlation between the number of sales and temperature
 H1: there is positive correlation between the number of sales and temperature

Temperature (°C)	Ice Cream Sales (\$)
14.2	215
16.4	325
11.9	185
15.2	332
18.5	406
22.1	522
19.4	412
25.1	614
23.4	544
18.1	421
22.6	445
17.2	408

rank temperature

rank sales

11	11
9	10
12	12
10	9
6	8
4	3
5	6
1	1
2	2
7	5
3	4
8	7

average average
 18.7 402.42

rs>crit value
H0 rejected

sumsq=
 n
 n^3-n
 rs=
 crit value (C

x1-xaverage	y1-yaverage	dx*dy	dx^2
-4.5	-187.42	838.6896	
-2.3	-77.42	176.1229	
-6.8	-217.42	1472.998	
-3.5	-70.42	244.6979	
-0.2	3.58	-0.62708	
3.4	119.58	409.5729	
0.7	9.58	6.947917	
6.4	211.58	1359.423	
4.7	141.58	668.9813	
-0.6	18.58	-10.6854	
3.9	42.58	167.1396	
-1.5	5.58	-8.23542	

$$r = \frac{\sum dx*dy}{\sqrt{\sum dx^2 \sum dy^2}}$$

177.0 174754.9 5325.025 sum of dx*dy

r>crit value
H0 rejected
 0.957506623 critical value= 0,576
 d.f. 10
 alpha 0.05

Pearson	On
r crit.	.05
Two	
df	.10
1	.988
2	.900
3	.805
4	.729
5	.669
6	.622
7	.582
8	.549
9	.521
10	.497

r for the last 12 days:

d

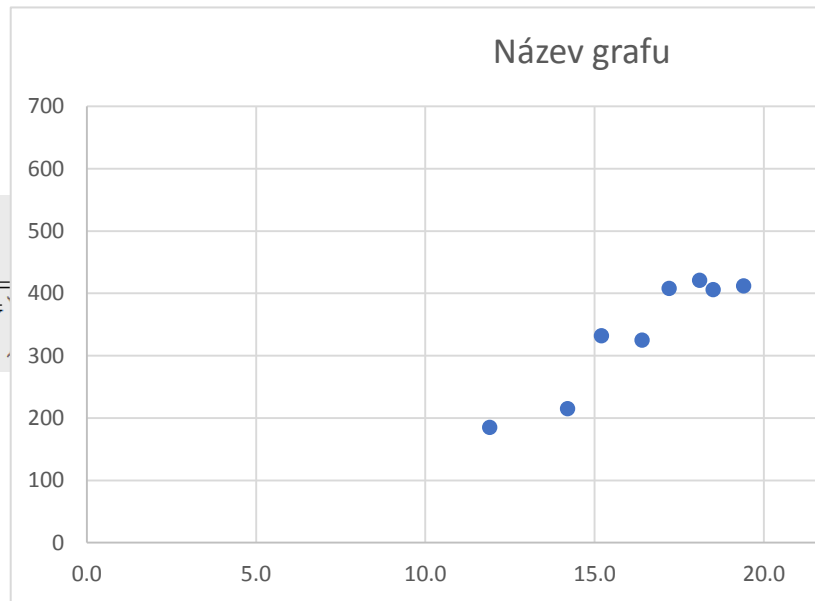
0
-1
0
1
-2
1
-1
0
0
2
-1
1
14
12
1716
0.951049
0.587

$$rs = 1 - \frac{6 \sum_{i=1}^n d_i^2}{n^3 - n}$$

n \ a	0.2	
4	1.000	1
5	0.800	1
6	0.657	1
7	0.571	1
8	0.524	1
9	0.483	1
10	0.455	1
11	0.427	1
12	0.406	1
13	0.385	1
14	0.367	1
15	0.354	1
16	0.341	1
17	0.328	1

$$\frac{\sum (X_i - \bar{X})(Y_i - \bar{Y})}{\sqrt{\sum (X_i - \bar{X})^2 \sum (Y_i - \bar{Y})^2}}$$

One-Tailed Test	
.025	.01
Two-Tailed Test	
.05	.02
.997	.9995
.950	.980
.878	.934
.811	.882
.754	.833
.707	.789
.666	.750
.632	.716
.602	.685
.576	.658



0.1	0.05	0.02	0.01	$n \backslash \alpha$	0.2	0.1	0.05	0.02	0.01
1.000	—	—	—	18	0.317	0.401	0.472	0.550	0.600
0.900	1.000	1.000	—	19	0.309	0.391	0.460	0.535	0.584
0.829	0.886	0.943	1.000	20	0.299	0.380	0.447	0.522	0.570
0.714	0.786	0.893	0.929	21	0.292	0.370	0.436	0.509	0.556
0.643	0.738	0.833	0.881	22	0.284	0.361	0.425	0.497	0.544
0.600	0.700	0.783	0.833	23	0.278	0.353	0.416	0.486	0.532
0.564	0.648	0.745	0.794	24	0.271	0.344	0.407	0.476	0.521
0.536	0.618	0.709	0.755	25	0.265	0.337	0.398	0.466	0.511
0.503	0.587	0.678	0.727	26	0.259	0.331	0.390	0.457	0.501
0.484	0.560	0.648	0.703	27	0.255	0.324	0.383	0.449	0.492
0.464	0.538	0.626	0.679	28	0.250	0.318	0.375	0.441	0.483
0.446	0.521	0.604	0.654	29	0.245	0.312	0.368	0.433	0.475
0.429	0.503	0.582	0.635	30	0.240	0.306	0.362	0.425	0.467
0.414	0.488	0.566	0.618		rho critical values for 2-tailed test				

