Approaches to a risk research on Roman antiquity

Why modern risk research does not consider antiquity. Rolling the dice as the root of risk research. How to calculate probability in antiquity.

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Ústav klasických studií Masarykova univerzita Brünn, 9.10.2017



Perception and Handling of Risks in Roman Antiquity

1. Monday, 9.10.2017 The term "risk". Why modern risk research does not consider antiquity. Rolling the dice as the root of risk research. How to calculate probability in antiquity?

2. Monday, 9.10.2017 Health risks: Sources of diseases and occupational risks. Indices of a reflected perspective?

3. Tuesday, 10.10.2017 *Ex voto*: the prevention of risks with the help of the gods.

4. Tuesday, 10.10.2017 Geschenke und Gelübde: *Donum dedit* und *votum solvit* in lateinischen Sakralinschriften

5. Thursday, 12.10.2017 Natural disasters: Sources of earthquakes, floods, famine and preventive measures.

6. Thursday, 12.10.2017

Risks in seafaring and ancient economy. The variety of measures in a central field of ancient life. From risk-minimizing contracts to magical practices.

What is "risk"? Why modern risk research does not consider antiquity?

1250 "**De Vetula**": list of the number of possible combinations of the dots for rolling three dices



First approach to a calculation of probability

Ps.-Ovidius, De Vetula (~ 1250)

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Hi funt fex & quinquaginta modi uentendi. Nec numerus minor effe potest, uel maior, eorum. Nam quando fimiles fuerint sibi tres numeri, qui Iactum componunt, quia sex componibiles sunt Et punctatura sunt sex, pro qualibet una.

1250 "**De Vetula**": list of the number of possible combinations of the dots for rolling three dices

Mid 17th century "Logic of Port Royal": assessment of future events not only according to possible advantages or disadvantages, but equally to its probability

Port Royal des Champs near Paris



Painting by Louise-Magdeleine Horthemels, ~ 1710

1250 "**De Vetula**": list of the number of possible combinations of the dots for rolling three dices

Mid 17th century "Logic of Port Royal": assessment of future events not only according to possible advantages or disadvantages, but equally to its probability

1713 Jakob Bernoulli "Ars conjectandi": first calculation of probability and law of large numbers

JACOBI BERNOULLI, Profeff. Bafil. & utriusque Societ. Reg. Scientiar. Gall. & Pruff. Soda!. MATHEMATICI CELEBERRIMI,

ARS CONJECTANDI,

OPUS POSTHUMUM.

Accedit

TRACTATUS DE SERIEBUS INFINITIS,

> Et Epistola Gallicè scripta DE LUDO PILÆ RETICULARIS.



BASILEE, Impenfis THURNISIORUM, Fratrum. clo. Locc XIII.

First calculation of probability

Jacob Bernoulli, Ars conjectandi (Basel 1713)



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Basics of modern risk research

Modern definition of Risk: calculable probability of damage of a certain size

Modern definition of Risk: calculable probability of damage of a certain size

no risk research for the period before the middle of the 17th century

no risk research for antiquity

WORLDWITTE STELLER AGAINST THE REMARKABLE STORY OF RISK

PETER L. BERNSTEIN

Peter Lewyn Bernstein

Against the Gods. The remarkable story of risk (1996)

Edwin G. Booz Prize for the most insightful, innovative management book published in 1996

Clarence Arthur Kelp/Elizur Wright Memorial Award from The American Risk and Insurance Association (ARIA) as an outstanding original contribution to the literature of risk and insurance 1998

more than 500.000 sold copies

Modern definition of Risk: calculable probability of damage of a certain size

no risk research for the period before the middle of the 17th century

But there exist numerous studies with usable approaches to a risk research on antiquity.

In the following sessions, we will see some examples from different spheres of life.

First, however, we will discuss the roots of the ancient understanding of risk and probability.

What role does the dice play for the idea of risk in the ancient world, and how did the Ancient deal with probability?

Is it necessary that probability can be calculated to deal rationally with risks?

In Latin:

The meaning of "risk" is closely linked to the term *alea I* dice



Aldius nom. gent. CORP. IX 1432 (Aequi Tutici) C. Aldio Barbato C. Aldius Agr(i)cola fil. fec. cf. Aledius sub Allius? Otto. Aldualuhus, -1 cogn. vir. germ. CORP. XIII 6256 (Borbeto-

ALDIVS

magi, saec. VI/VII) hic pausat corpus Aldualuhi, cuius anima gaudet in caelo. Diehl.

Alduasdubis v. Dubis.

Aldunus, -1 nom. vir celt. INSOR. christ. Leblant Nouv. Rec. 241 Alduni Jacobsohn.

Ale vel Alae opp. Ciliciae. PLIN. nat. 5, 92. cf. STEPH. BYZ. sub Άλαί: και της Κιλικίας δε πόλις, πληθυντικώς λεγομένη Άλαί. άπὸ δὲ τούτου Αλήιον πεδίον. cf. Aleus. Diehl.

alea, -ae f. [orig. inc.; sunt qui conferant c. ind. aksah 'alea', v. Leo Meyer, Vergl. Gramm. d. griech. u. lat. Spr. I² 484. Th.] ISID. orig. 18,60 alea, id est ludus tabulae, inventa a Graecis in otio Troiani belli a quodam milite nomine Alea, a quo et ars no-men accepit (sim. GLOSS. IV 14, 26. 205, 49. 473, 51. V 165, 17. brevius V 410, 3). GLOSS. NUBSIA. NUBBIA. NOTTOS. NOTTIGUÓS. tefil (anglos.). V 424, 21 genus ludi. 262, 22 ubi nummi ad ludendum. 165, 15 alea quasi bellum quod alterum facit victum, alterum victorem. 165, 16 tabula ad ludendum eo quod alter alio victo vincet. 490, 46 lect. inc. cf. 1. aleo. forma alia: CORP. IV 2119 (cf. ALBIN. gramm. VII 297, 14) et saepius in codicibus, ex. gr. VARRO rust. 1, 4, 3 cf. PLIN. p. 1522, 34. inde a Playto in usu est.

proprie: v. Mau, Leonhard, Hartmann, PW. I 1358 sq. ludere alea, aleam sim.: GLOSS. II 354, 12 κοττίζω aleam ludo. 356, 23 χυβεύω aleo, aleam ludo (III 76, 44). II 14, 33 aleam ludit κοττίζει, πυβεύει. TITIVS or. frg. Macr. sat. 3, 16, 14 ludunt alea studiose, delibuti unguentis, scortis stipati. Cic. Phil. 2, 56 vel in foro alca ludere. CARM. Suct. Aug. 70 postquam bis classe victus naves perdidit, aliquando ut vincat, ludit assidue aleam. Ov. trist. 2,471 sunt aliis scriptae, quibus alea luditur, artes. PAVL. FEST. p. 52 cybios genus piscis, quia piscantes id genus piscium velut aleam ludaut. SEN. apocol. 14 Aeacus iubet illum alea ludere pertuso fritillo. IVV. 8,10 si luditur alea pernox. SVET. Claud. 33 aleam studiosissime lusit; de cuius arte librum quoque emisit; solitus etiam in gestatione ludere, ita essedo alveoque adaptatis, ne lusus confunderetur. Nero 30 quadringentis in punctum sestertiis aleam lusit. PAVI. dig. 47, 10, 26 si aleam luserit. 11, 5, 4, 2 quod in alea lusum est. 11, 5, 4 pr. (?). EDICT. praet. Vlp. dig. 11, 5, 1 pr. apud quem alea lusum esse dicetur. ibid. alcae ludendae causa. VLP. dig. 11, 5, 1, 2. ANTH. 323, 1 ludis, nec superas, Vltor, ad aleam. Ps. CYPR. aleat. 8 alea ludes (ibid. bis aleae tabula qui ludit). 11. CAPITOL. Ver. 4,6 fertur et nocte perpeti alea lusisse. SCHOL. Hor. carm. 2, 1, 6. SVET. Claud. 39 multos ... ad aleae lusum admoneri iussit (cf. Cal. 41 ne ex lusu quidem aleae compendium spernens). MACR. sat. 1, 7, 22. AMBR. Tob. 11, 39 victus aleae ludo. Con. Just. 3, 43, 1 pr. alea-PLAVT. Cure. 355 talos poscit sibi in manum, prorum lusus. vocat me in aleam, ut ego ludam. 609 elusi militem, inquan, in alea. RHET. Her. 4, 21, 29 hic, quos homines alea vi(n)cit, eos ferro statim vincit (cf. CORP. IV 2119 vici Nuceriae in alia denarios tot fide bona. sic perdere in alea: Ctc. Phil. 2, 56 POMP. dig. 17, 2, 59, 1). CIC. Catil. 2, 10 quod si in vino et alea comissationes solum et scorta quaercrent (Phil. 13,24 in lustris, popinis, alea, vino tempus aetatis omne consumpsisses. cf. COLVM. 1, 8, 2 PLIN. paneg. 82. LAMPR. Comm. 9,1 in convivia et aleam convertit sumptum). Cic. Phil. 2, 56 hominem ... lege, quae est de alea, condemnatum (et bis ibid. cf. HOR. carm. 3, 24, 58 vetita legibus alea. Ps. Cyrr. alcat. 6 alea est quam lex odit. AMBR. Tob. 11, 38. 11, 39 aleae ... legibus oboedire Hunnos. ISID. orig. 18,68 de interdictione aleae. cf. alearius). HOR. epist. 1, 18, 21 quem damnosa Venus, quem praeceps alea nudat. Ov. ars 1,452 non cessat perdere lusor et revocat cupidas alea saepe manus. Pont. 1, 5, 46 nec tenet incertas alea blanda manus (MART. 4, 14, 7 blanda vagus alea December). 4, 2, 41 nec vinum nec me tenet alea fallax (SEN. apocol. 15). Ov. rem. 146 Nvx 75. SEN. dial. 12, 17, 4 Caligulae lugentis sororem alea solacium fuit. benef. 7, 16, 3. PERS. 5, 57 hic campo 65 indulget, hunc alea decoquit. PLIN. nat. 14, 140 quantum alea quaesierit, tantum bibit. MART. 4,66,16. 13, 1, 8. 14, 15, 2 dum sit maior, quam talis, alea saepe mihi. 14, 19 (18), 1 alea parva nuces et non damnosa videtur. Qvīnī. inst. 6, 3, 72 Ivv. 1, 88. 11, 176 turpis. 14, 4 damnosa. TAC. Germ. 24 aleam ... sobrii inter seria exercent (LAMPR. Comm. 2, 8). SVET. Aug. 70 aleae indulgens (PS. AVR. VICT. epit. 1, 21 studiosissimus aleae lusor). 71 aleae rumorem nullo modo expavit Cal. 41 glorians ... numquam se prosperiore alea usum. Claud. 5 aleae infamiam subiit. Vit. 4 Claudio per aleae studium familiaris. Dom. 21 alea se oblectabat. FRONTO p. 128, 23 N. alea in castris frequens. PAVL. dig. 44, 5, 2, 1 si in alea rem vendam, ut ludam. VLP. dig. 22, 3, 19, 4 in alea gestum esse contendatur. GELL 14, 1, 24 cur tandem non de alea quoque ac de calculis et alveolo audent dicere, quisnam ibi ludentium vincat? TERT. pall. 5 dabo catharticum ... aleae Curii et vinolentiae Antonii (cf. aleator). CYPR. Demetr. 10 alea prodigus (cf. GLOSS. sub 1.aleo p. 1524, 17). PS. CYPR. aleat. 5 aleae tabula (6. 7. 8). 9 quando se aleae auctorat. 11 fuge aleam. ibid. aleam noli respicere. CAPITOL Ver. 10, 8 aleae cupidissimus. AMM. 14, 6, 25 pugnaciter aleis certant. AMBR. Tob. 11, 39 ad unum 18. IX. 04 1522

aleae iactum. PHYSIOGN. 29 aleae deditos (88. 103 SIDON. epist. 8, 11, 8). SIDON. epist. 1, 8, 2 student pilac senes, aleae iuvenes.

proverbialiter et translate: cf. Otto, Spriche. p. 12. SVET. Iul. 32 iacta alca est (esto Erasmus), inquit (ἐνερρίφθω κύβος). cf. PETRON. 122 vers. 174 iudice Fortuna cadat alea. AMRR. epist. 82,8 incerti eventus quaedam, ut dicitur vulgo, alea. VARRO rust. 1, 18, 8 temptare quaedam sequentes non aleam, sed rationem aliquam. 1, 4, 3 ubi salubritas non est, cultura non aliud est atque alea (alia trad.) domini vitae ac rei familiaris. C10. div. 2, 36 non perspicitis aleam quandam esse in hostiis deligendis? Hor. carm. 2, 1, 6 periculosae plenum opus aleae (cf. PORPH. ad l.). sat. 2, 5, 50 perraro haec alea fallit. Ov. ars 1,376 talibus admissis alea grandis adest. Liv. 1, 23, 9 non contenti libertate certa in dubiam imperii servitiique aleam imus. 31, 35, 1 tam celerem aleam universi certaminis timens. 37, 36, 7 tutam fore belli aleam (HEGES. 3, 17 brevi damno totius belli aleam lusi. 5, 30 varia atquè incerta bellorum alea. Cop. Theod. 7, 17, 1 a. 412 istis...ad belli aleam praeparatis. COMMENT. Lucan. 7, 107 aleam belli temptare. SCHOL. Hor. carm. 2,1,6 cogit alea belli). LIV. 40,21,6 filios non commissurum in aleam eius ... casus (42,50,2 ut in aleam tanti casus se regnumque daret. AMM. 24, 2, 14 omnes aleae casus experiri festinans). 42, 59, 8 ne ... summam rerum temere in non necessariam aleam daret. MANIL. 1,916 repetitaque rerum alea. SEN. clem. 1, 1, 7 magnam adibat aleam populus Romanus, cum incertum esset eqs. (benef. 3, 11, 1). epist. 58,34 non exigua temporis mercede magnae rei aleam redimit. 99, 12 nihil ille perdidit nisi aleam in damnum certiorem. 117, 20 subibo (-to codd.) huius voti aleam (cf. nat. 4 praef. 7 ubi aleam pro litem Muretus. COLVM. 3, 21, 6 primum neglegentiae vindemiatoris aleam subeat. APVL. met. 4, 15 ancipitis machinae subivit aleam). COLVM. 1 praef. 8 an bellum per obsessa maris et negotiationis alea sit optabilior. 8,2,5 rixosarum avium lanistae, cuius ... patrimonium, pignus aleae, victor gallinaceus pyctes abstulit. LVOAN. 6,7 placet alca fati (6,603). PLIN. nat. praef. 7 M. Tullius extra omnem ingenii aleam (taliam codd.) positus. FRONTIN. grom. p. 44, 6 magna ... alea est, litem ad interdictum deducere. ANTH. 198,53 ubi quaeritur alea mortis. POMP. dig. 18, 1, 8, 1 aliquando ... et sine re venditio intellegitur, veluti cum quasi alea emitur (PAVL dig. 18, 4, 7). SCAEV. dig. 22, 2, 5 si modo in aleae speciem non cadat. GELL 18, 13, 1 Saturnalibus Athenis alea quadam festiva et honesta lusitabamus huiuscemodi. AMM. 26, 6, 12 aleam periculorum omnium iecit abrupte. CLAVD. 21, 365 nec constitit alea castris nutatura semel. SIDON epist. 4, 6, 3 bene factum est, quod anceps iter ... distulistis neque intra iactum tantae aleae status tantae familiae fuit. CASSIOD, var. 3,1,1 cavete subito in aleam mittere quos constat tantis temporibus

exercitia non habere.

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derivata: alearis, alearius, aleator, aleo subst. et verb. Ihm. 1. (Alea) nom. vir. v. s. alea p. 15,21, 15.

2. Alea, -ae, Mia. opp. Arcadiae. PLIN. nat. 4, 20 (ubi trad. aleae, alae). STAT. silv. 4, 6, 52 qualem Herculem Aleae (taleae Matr.) lucis vidit Tegenea sacerdos. Alea Minerva ibi culta: STAT. Theb. 4, 288 templumque Aleae nemorale Minervae. cf. Wentzel, PW I 1358.4. heros oppidi eponymus Aleus, -ī, "Alsos. Hyg. fab. 162 p. 16, 1 Auge, Alei filia (98 p. 93, 3). 14 p. 46, 24 ubi trad. egei Exc. barb. p. 240, 4 cd. Frick Aleu gen. abiit in nom. serv. CORP. VI 156 (a. 105) minister. cf. Thrämer, PW. I 1365. Diehl.
äleäris, -e ab alea. CAEL. AVR. chron. 2, 1, 25 in os immitti-

mus ceram vel tabellam alearem aut feruleam et ductu contrario fasciolae corrigere temptamus depravata.

alearius, -a, -um ab alea. PLAVT. Mil. 164 ut ne legi fraudem faciant aleariae (cf. alea p. 1521, 55 sqq.). AMM. 28, 4, 21 amicitiae aleariae (plur.). Thm

Aleasiumara, -ae nom. mul. celt. CORP. XII 1124 (Aptae) Aleasiumarae Viri f. Diehl

aleator, - oris m. [ab alea. Th.]. GLOSS. κοττιστής. κυβευτής. zυβιστής, passim. IV 474, 1 aleator: lusor cupiditatis (sic sacpius) II 566, 8 tebleri (anglos., cf. V 338, 20). V 264, 39 v. 2. aleo. Nor. Tir. 42, 35. PLAVT. Rud. 359 o Neptune ..., nec te aleator nullus est sapientior; profecto nimis lepide iecisti bolum. PVBLIL A 33 aleator quanto in arte est potior, tanto est nequior. cf. Otto, Sprichw. p. 13. CIC. Verr. 2, 33 lenonum, aleatorum, perductorum nulla mentio fiat (LACT. inst. 6, 17, 19). 6, 33 aleatoris Placentini castra commemorabuntur. Catil. 2, 23 omnes aleatores, omnes adulteri (cf. QVINT. inst. 2, 4, 22 TRXPH. dig. 50, 16, 225). Phil. 3, 35 impudicis, alcatoribus, ebriis servire (2, 67). 5, 12 ille legit alcatores, legit exules, legit Graecos. 8, 26 cavet mimis, aleatoribus, lenonibus. off 3,91 mendacem esse, aleatorem, furacem, ebriosum. Att. 14, 5, 1. IMP. AvG. epist. frg. Suet. Aug. 71 lusimus per omnis dies forumque aleatorum (codd., -rium edd.) calfecimus. Ascon. tog. cand. 96 Curius .. notissimus fuit aleator (cf. TERT. pall. 5). MART. 5, 84, 5 aedilem rogat udus aleator. QVINT. inst. 2, 4, 22 aleator pauper. DIG. 11, 5 de aleatoribus. VLP. dig. 21, 1, 4, 2 aleatores et vinarios (21, 1, 25, 6). 21, 1, 19, 1 aleatorem ... furem. PORPH. Hor. epist. 1, 8, 21. PS. CYPR. aleat. 1. 6 o aleatorum noxia ... neguitia. ibid. aleatores cum pro-

Thesaurus Linguae Latinae I / 7, München 1991, s.v. alea

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Alea used in a metaphoric sense in:

- historiography (Livius, Ammianus Marcellinus)
- administrative literature (Cassiodorus)
- specialist texts (Plinius, Frontinus, Varro, Columella)
- poetry and novels (Horatius, Ovidius, Petronius, Apuleius, Claudianus)
- letters and philosophical discourses (Cicero, Seneca, Sidonius Apollinaris)
- church historical and theological writings (Ps.-Hegesippus, Ambrosius)
- legal texts (Digesta, Codex Theodosianus)

Alea used in a metaphoric sense to describe risks

mainly from a Roman-Italian upper class

- in war: Hor. carm. 2, 1, 6 : opus plenum periculosae aleae Ps.-Heges. 3, 17. 5, 30 : varia et incerta bellorum alea Cod. Theod. 7, 17, 1 : ad belli aleam praeparatis Cassiod. var. 3, 1, 1 : in aleam mittere
- in political issues: Liv. 42, 50, 2 : *ut in aleam tanti casus se regnumque daret* Sen. clem. 1, 1, 7 : *magnam adibat aleam populus Romanus*
- in agriculture: Colum. 1 praef. 8 : maris et negotiationis alea Varro rust. 1, 4, 4 : alea domini vitae ac rei familiaris Colum. 3, 21, 6 : neglegentiae vindemiatoris alea
- when buying and selling: Pomp. dig. 18, 1, 8, 1 : *emptio spei*
- in philosophical discourses: Sen. epist. 99, 12 : nisi aleam in damnum certiorem



idea of risk linked to alea / dice remains the idea of an educated public

Astragal oracles: distribution and the example of Tyriaion



Traduction. "Oracles d'Apollon Pythien à cinq osselets, (donnés) à Hermès. I. 1 + 1 + 11 + 1 + 1 = 5 De Zeus Olympios. Zeus mettra en ton esprit un bon conseil; il donnera la joie à tes affaires, desquelles tu te réjouiras; mais apaise Aphrodite et le fils de Zeus. II. 1 + 1 + 1 + 1 + 3 = 7 D'Athéna Aréia. Echappant à la haine et à la méchanceté, tu arriveras à ton but; tu y arriveras et Athéna la déesse aux yeux brillants te le donnera; il sera selon ton cœur le projet que tu entreprends. III. 1 + 1 + 1 + 1 + 4 = 8 Des Destinées. Cette action que tu accomplis, ne l'accomplis pas; car cela n'est pas pour le mieux; pour qui peine, la situation est difficile et sans issue; il faut aller voir à l'étranger: dans le temps il n'y aura rien de mal. IV. 1 + 1 + 1 + 3 + 3 = 9 De l'Aigle de Zeus. Aigle qui vole haut, à la droite du voyageur, présage de bon augure, avec Zeus Très Grand tu réaliseras l'action dans laquelle tu te lances; ne crains rien. V. 1 + 1 + 1 + 1 + 6 =10 Du Très Grand Daimôn. La promesse que tu as faite au Daimôn, quelle qu'elle soit, il vaut mieux la tenir si tu veux accomplir ce que tu médites dans ton esprit; Déméter et Zeus te seront des sauveurs. VI. 1 + 1 + 1 + 4 + 3 = 10 De Tychè Protectrice. L'action que tu entreprends à présent, ne l'accomplis pas; étant dans la maladie, les dieux eux-mêmes te sauvegardent, ils mettront fin à ta peine, et rien de mal n'arrivera. VII. 3+3+3+1+1 = 11 De la Victoire. Accomplis complètement ton action; car cela sera pour le mieux;



Probability (P) for each of the 56 possible combinations of dots in an oracle where you roll the dice (astragal) five times



The life table of Ulpian and later authors



cf: A. Charpentier, Ajuster les tables de mortalité : le rôle des actuaires, Risques 72, 2007, 127–130.

Ulpian's life table and the customary life table					
Appuitant's procent age (v)	Corresponding figure				
Annultant's present age (x)	Ulpian	Customary			
0–19	30	30			
20–24	28				
25–29	25				
30–34	22				
35–39	20				
40-49	(60- <i>x</i> -1)	(60-x)			
50–54	9				
55–59	7				
60-	5	0 (?)			
After Frier, "Roman life expectancy", 217, table 1.					



Edict of Ti. Iulius Alexander from the year 68 AD at the Hibis-Temple in Egypt

lines 5-10 preamble;

- 10-15 the induction of unwilling tax collectors and lease holders;
- 15-26 debts: (1) the cession of debts, (2) the execution of debts upon the person of the debtor, (3) the abuse of $\pi\rho\omega\tau\sigma\pi\rho\alpha\xii\alpha$ (the right of first lien upon the possessions of the debtor enjoyed by the fiscus), (4) the seizure of the dowries of foreign women in satisfaction of debts;
- 27-32 exemptions from, and abatements of taxes;
- 32-34 the induction of Alexandrian citizens into liturgies;
- 35 the appointment of *strategi*;
- 36-44 the introduction into the prefect's court of matters already passed upon by previous prefects;
- 44 the emendation of the gnomon of the idiologus;
- 45-56 new taxes: (1) charged against property within the last five years, (2) based upon the average rise of the Nile for a number of years instead of the current rise:



60–61 the measurement of certain ancient tracts of land near Alexandria.



P. Oxy. XXXI 2561

μάτριξ – monthly military list of troop strength and rations (293/305 AD)



Fragment of a parapegma from Milet (Pergamonmus., Berlin, SK 1606)





for the annual calculation of needs