

# Ruggedness, robustness, stability



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# *Ruggedness Testing*

- the degree of reproducibility of results obtained under a variety of conditions, such as different laboratories, analysts, instruments, environmental conditions, operators and materials
- a measure of reproducibility of test results under normal, expected operational conditions from laboratory to laboratory and from analyst to analyst
- determined by the analysis of aliquots from homogeneous lots in different laboratories

# Ruggedness testing

- by considering each effect separately, by repeating measurements after varying a particular parameter by a small amount (say 10%) and controlling the other conditions appropriately
- this can be labour-intensive as a large number of effects may need to be considered
- for a well-developed method, most of the effects can be expected to be small, it is possible to vary several parameters at the same time
- any stable and homogeneous sample within the scope of the method can be used for ruggedness-testing

# Plackett–Burman design of ruggedness testing

- 7 parameters, each tested at two levels (**low-high**) e.g.
  - 1. volume of sample
  - 2. time of extraction
  - 3. flow rate
  - 4. temperature
  - 5. pH
  - 6. salt concentration
  - 7. modifier addition

**128 possible combinations!**

| low        | high | Combinations |            |
|------------|------|--------------|------------|
|            | 0    | 7            | 1          |
|            | 1    | 6            | 7          |
|            | 2    | 5            | 21         |
|            | 3    | 4            | 35         |
|            | 4    | 3            | 35         |
|            | 5    | 2            | 21         |
|            | 6    | 1            | 7          |
|            | 7    | 0            | 1          |
| <b>SUM</b> |      |              | <b>128</b> |

# Plackett–Burman design of ruggedness testing

- The design described allows information to be gathered from only **eight** experiments
- **A, B, C, D, E, F** and **G** – nominal level
- **a, b, c, d, e, f** and **g** – alternative level
- The chosen levels may be the **extreme values** of the parameter, e.g. the two extremes of temperature likely to be encountered during use of the method

# Plackett–Burman design of ruggedness testing

To find if changing factor 'A' to 'a' has an effect, A is calculated

| Experiment number |   | Method parameter |   |   |   |   |   | Observed result |
|-------------------|---|------------------|---|---|---|---|---|-----------------|
| 1                 |   | B                | C | D | E | F | G |                 |
| 2                 |   | B                | c | D | e | f | g |                 |
| 3                 |   | b                | C | d | E | f | g |                 |
| 4                 |   | b                | c | d | e | F | G |                 |
| 5                 | a | B                | C | d | e | F | g | v               |
| 6                 | a | B                | c | d | E | f | G | x               |
| 7                 | a | b                | C | D | e | f | G | y               |
| 8                 | a | b                | c | D | E | F | g | z               |

$$\Delta_A =$$

$$\frac{v + x + y + z}{4}$$

# Plackett–Burman design of ruggedness testing

With this combination the effect of the other factors cancels out!

| Experiment number |   | Method parameter |   |   |   |   |   | Observed result |
|-------------------|---|------------------|---|---|---|---|---|-----------------|
| 1                 | A |                  |   |   |   |   |   |                 |
| 2                 | A |                  |   |   |   |   |   |                 |
| 3                 | A |                  |   |   |   |   |   |                 |
| 4                 | A |                  |   |   |   |   |   |                 |
| 5                 | a | B                | C | d | e | F | g | v               |
| 6                 | a | B                | c | d | E | f | G | x               |
| 7                 | a | b                | C | D | e | f | G | y               |
| 8                 | a | b                | c | D | E | F | g | z               |

$$\Delta_A = \frac{l + m + p + w}{4} - \frac{v + x + y + z}{4}$$

# Plackett–Burman design of ruggedness testing

Changing factor 'B' to 'b' is examined by calculating  $\Delta_B$ , as follows:

| Experiment number | Method parameter |   |   |   |   |   |   | Observed result |
|-------------------|------------------|---|---|---|---|---|---|-----------------|
| 1                 | A                |   | C | D | E | F | G |                 |
| 2                 | A                |   | c | D | e | f | g |                 |
| 3                 | A                | b | C | d | E | f | g | p               |
| 4                 | A                | b | c | d | e | F | G | w               |
| 5                 | a                |   | C | d | e | F | g |                 |
| 6                 | a                |   | c | d | E | f | G |                 |
| 7                 | a                | b | C | D | e | f | G | y               |
| 8                 | a                | b | c | D | E | F | g | z               |

$$\Delta_B = \text{[Yellow Box]} - \frac{p + w + y + z}{4}$$



# Plackett–Burman design of ruggedness testing

- The next step is to arrange the seven differences, A to G, in numerical order (ignoring the sign).
- To calculate if any of the differences are statistically significant, a statistical test (*t -test*) is applied.
- Equation below is used to compare the difference  $|\Delta_i|$  with the expected precision of the method,  $s$  and the level of confidence used (t-test).

$$|\Delta_i| > \frac{ts}{\sqrt{2}}$$

- For cases where **equation is true, the change from the nominal to the alternative level is significant.**

# Plackett–Burman design of ruggedness testing

- NOTE! the results of the test will be misleading if the factors investigated are not independent
- Such a study may be used to set the level of control that should be applied at particular stages of the method, e.g. adjust the pH to  $6.5 \pm 0.2$
- It is also possible to study the effect of potential interferences by using this approach