

Vect	ors and Scalars					
What i	s a vector, how is it different from a scalar?					
Which	mathematical operations can you perform with vectors?					
	ing https://ocw.mit.edu/courses/mathematics/18-02-multivariable-calculus-fall-rideo-lectures/lecture-1-dot-product/					
Listen false.	for the first time to the lecture and decide whether the statements are true or					
What	is the nationality of the speaker?					
1)	Almost all students have heard about vectors before.					
2)	In the first week there will not be many new things to learn.					
3)	If the students have problems with vectors, they can go to the instructor's house and ask him.					
4)	Vector has both the direction and size.					
5)	If we are in the plane, we use x-y-z axis.					
6)	Vector quantity is indicated by an arrow above.					
7)	In the textbooks vectors are in bold because it is easier to read.					
8)	A vector <j> hat points along the z axis and has length one.</j>					
9)	The notation a1 and a2 is in angular brackets.					
10)	The length of a vector is a scalar quantity.					
Listen	for the second time to the lecture and try to continue the sentences.					
a)	So let's start right away with stuff that we will need to see before we can go on to					
b)	And, so, now, the way that we compute things with vectors, typically, as we introduce					
c)	When we have a vector quantity,					
d)	So, the length of a vector we denote by, if you want,					
e)	OK, so, as opposed to a vector quantity.					
f)	But, a vector doesn't really have, necessarily,					

Example: (6, 5, 4, 3, 2, 1) is an arithmetical progression because each element is formed by subtracting 1 from the preceding

000 1, 2, 3, 4, 5, 6 2, 4, 8, 16, 32 5, 4, \$, 16, 32

> و پ x, (x+a), (x+2a), (x+3a)11, 16, 21, 26, 31

### 12. Solve these problems:

An arithmetical progression begins \frac{1}{2}, \frac{1}{3}, \ldots.... What are the next

b) A geometrical progression begins 1, 1, ...... What are the next two

#### Vectors and scalars

scalar quantity, that is, it is a size, or magnitude. The first quantity, velocity, is a of 60 km h<sup>-1</sup> north. It has a speed of 60 km h<sup>-1</sup>. The second quantity, speed, is a vector, that is, it has both magnitude and direction. A car is travelling north along a road at 60 km h -1. We say that it has a velocity

are scalar quantities. is 2500 times the unit of mass, that is, the gramme. If the electrical power of a unit of magnitude. For example, if the mass of a metal cylinder is 2 500 g, then it light bulb is 40 W, then it is 40 times the unit of power the watt. Both of these The magnitude of a quantity is usually expressed in relation to a standard

need to know the direction, that is, we need the vector quantity displacement, scalar quantity. Now, if we want to know the exact location of the town, we also which consists of both distance and direction, 150 km north west. the town is 150 000 times the unit of distance, the metre. Distance, again, is a If a certain town is 150 km from London, then the distance from London to

# 14. Divide the following quantities into vector or scalar quantities:

speed, mass, displacement, weight, force, acceleration, velocity, distance, volume, temperature, momentum, power

# 15. Say whether the following statements are true or false. Correct the false

- The mass of an object is the same as the weight of the object.
- An ordinary number is a vector quantity.
- A vector quantity consists of two parts.

d) A position in the Cartesian co-ordinate system may be expressed

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Comment on this statement:

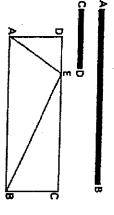
A train travels 60 km at 30 km h<sup>-1</sup>, then 60 km at 60 km h<sup>-1</sup>. Its

## NACTED INTILEGIATION THATE 7810 21411 2130

### Measurement 3 Ratio and Proportion

#### Section 1 Presentation

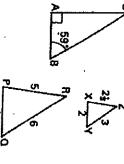
## 1. Look at these examples:



long as CD. AB is approximately three times as

twice as big as that of  $\triangle ABE$ The area of rectangle ABCD is exactly

Now make similar sentences about the following:



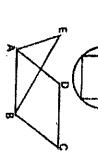
- a) ABC ..... ACB
- b) PR ..... XZ



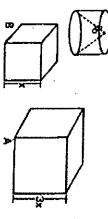
C ΔPQR ..... ΔXYZ.



d) ABCD ..... the inscribed semicircle



- 9 ..... any circle ..... the inscribed square.
- **Giameter** The circumference ..... the
- 8 ..... rhombus ABCD .....



- こ ..... cylinder ..... cone with the same base and height.
- ت ..... cube A ..... cube B.

## 2 Look at these examples:

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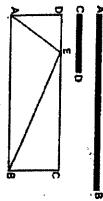
y is directly proportional to the reciprocal of x. We say that y is inversely proportional to x and that y varies

y oc xz

inversely as x.

y is directly proportional to the product of x and z.

We say that y is jointly proportional to x and z, and that y



The lengths of AB and CD are in the ratio of approximately 3:1.

The areas of ABCD and ABE are in the ratio of exactly 2:1.

Now make similar sentences about the examples in exercise 1.

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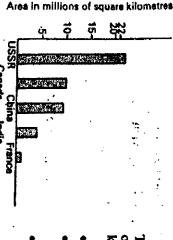
constant:

Describe the relationship between the following quantities, where k is

varies jointly as x and z.

## Section 2 Development

3. Look and read:



This bar graph shows the relative sizes of some countries in millions of square kilometres.

Look and read:

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y = kxz y:x = k y = kx بر =

- The USSR is far larger than India.
- India is considerably larger than France.
- Canada is slightly larger than China.

Now compare the other countries in the same way.

Look at the table below showing the beights of the highest mountains in the different continents. Draw a bar graph to illustrate the heights and then compare the heights of different mountains:

South America	North America	Europe	Australasia	Asia	Antarctica	Airica	Continent
Ω.		Elbrus			assif		Highest Mountain
6959	6187	5633	4693	8880	5139	5963	Height (in metres

#### Look and read:

#### Variation

 $y \propto x$  The ratio between y and x is a constant. y is directly proportional to x.

We say that y varies directly as x.





The volume of a gas is inversely proportional to its pressure. The smaller the volume, the higher the pressure.

Now make similar sentences about the following:

- the density and pressure of a gas (for a constant temperature)
- the volume and temperature of a gas (for a constant pressure)

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- the velocity of a falling body and the time it has been falling
- acceleration and mass for a constant force
- the electrical resistance of a wire and its cross-sectional area
- the circumference of a circle and its diameter
- the volume of a cylinder and its cross-sectional area and height

### Section 3 Reading

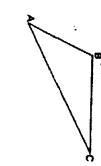
#### 7. Read this:

The ratio of two quantities is the magnitude of one quantity relative to the other. Division of the quantity a by the quantity b gives the ratio  $\frac{a}{b}$ , which can also be written as a:b and is read as 'the ratio of a to b'. For example, the ratio of boys to girls in a particular school is 3:2. If the

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## school has 230 pupils, then we can see that $\frac{3}{3}$ of these are boys and $\frac{1}{3}$ girls, i.e., there are 150 boys and 100 girls.

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Relative sizes of more than two quan-ABC has sides in exactly the same see that AC is twice as long as AB. Any example, the ratio of AB:BC:AC in triangle which is similar to triangle triangle ABC is 3:4:6. Hence we can tities may be expressed by ratio. For

proportion is that the reciprocals are also in proportion. Moreover, that a,b,c,d, are in proportion, we mean that  $\frac{a}{b} = \frac{c}{d}$ . A property of this When the ratio of one pair of quantities is equal to the ratio of another the ratio of the numerators is equal to the ratio of the denominators. pair of quantities, the two pairs are said to be in proportion. If we say

Say whether the following statements are true or false. Correct the false

- answers to incorrect answers of 3:10. In a test a student scored 30 out of 100. This gives a ratio of correct
- is 12 cm. The other sides are therefore 16 and 24 cm long. The length of the shortest side of a triangle similar to triangle ABC
- of quantities. We may use ratios to express the relationship between any number Any triangle with sides in the ratio 2:3:6 is a right-angled triangle.
- If a, b, c, d are in proportion, then ad = bc.

## 8. Complete these exercises:

of the proportion  $\frac{a}{b} = \frac{c}{d}$ . Put these two properties into mathematical The last two sentences of the reading passage contain two properties proportion. Complete the proof by adding expressions from the lists. In the calculations which follow, there are four more properties of the form, and number them 1 and 2.

From properties 2 and 5, we have Adding I to each side, we obtain From properties 2 and 3, we have

From properties 2 and 4, we have

Given Therefore Substituting, we obtain

a) 
$$\frac{2}{3} = \frac{c}{3}$$
 (.....)

b) .....
$$\frac{1}{5}+1=\frac{1}{5}+1$$

$$\dots b = 1 \text{ and } d = 1$$

d) ..... 
$$\frac{a+b}{b} = \frac{c+d}{d}$$
 (Property 3)

c) ..... 
$$\frac{a-b}{b} = \frac{c-d}{d}$$
 (Property 4)

g) 
$$\frac{a-b}{c-d} = b$$

h) 
$$\frac{a+b}{c+d} = \frac{a-b}{c-d}$$
 (Property 5)

i) ..... 
$$\frac{a+b}{a-b} = \frac{c+d}{c-d}$$
 (Property 6)

#### Section 4 Listening

## Using percentages in statistics

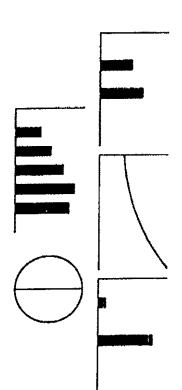
# 9. Listen to the passage and write down these words in the order in which you hear

improvement yesterday relative respectively higher while meat

passed

whereas

## 10. Copy the following diagrams, which illustrate the statistics in the five examples:



bread; (2) wages; (3) exam; (4) restaurant; (5) meat The five examples given in the passage may be summarised as: (1)

- a) Put the correct title under each diagram.
  b) Label the diagrams as a control of the diagrams.
- Label the diagrams as accurately as possible using the figures

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