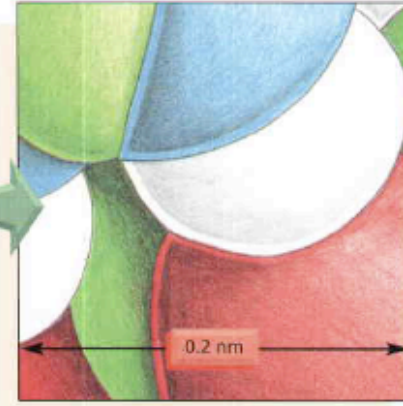
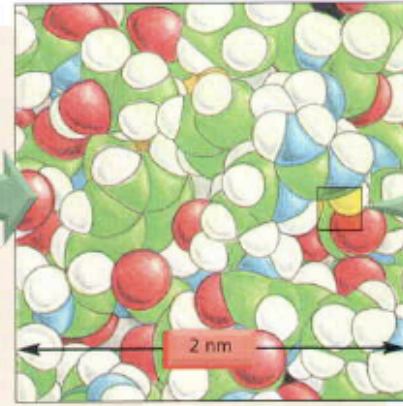
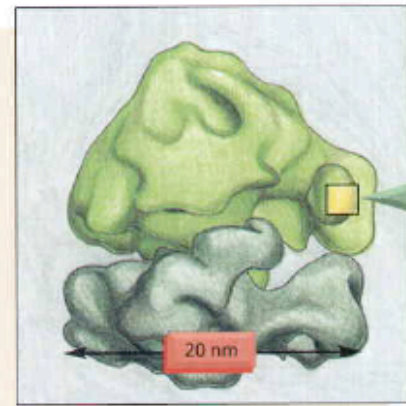
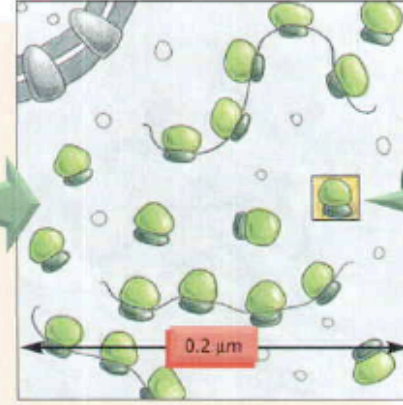
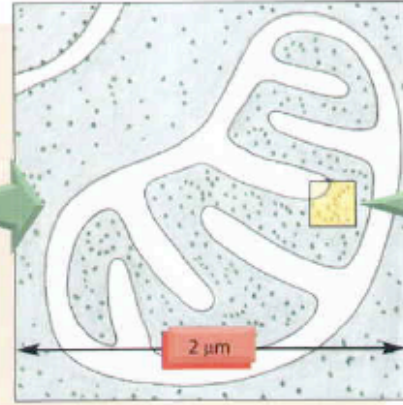
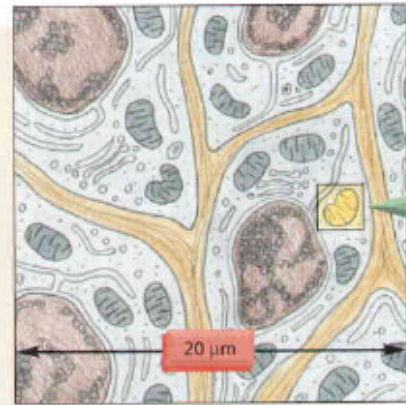
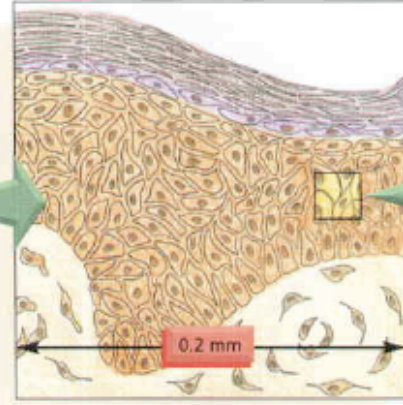
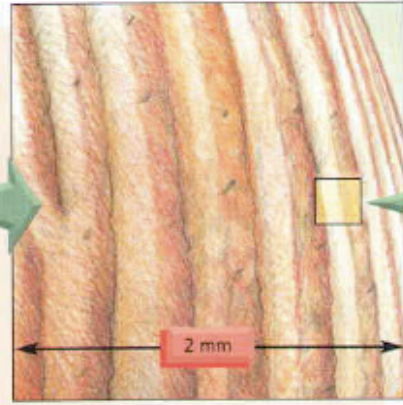
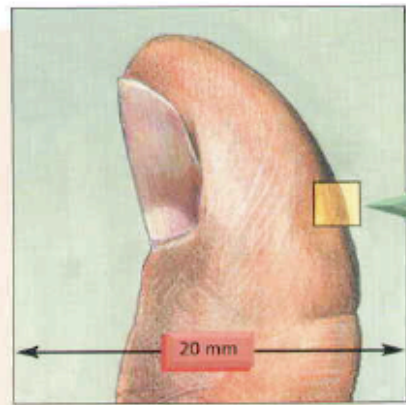


NMR-based Structural Biology for Studying Biomolecular Interactions

Karel Kubíček

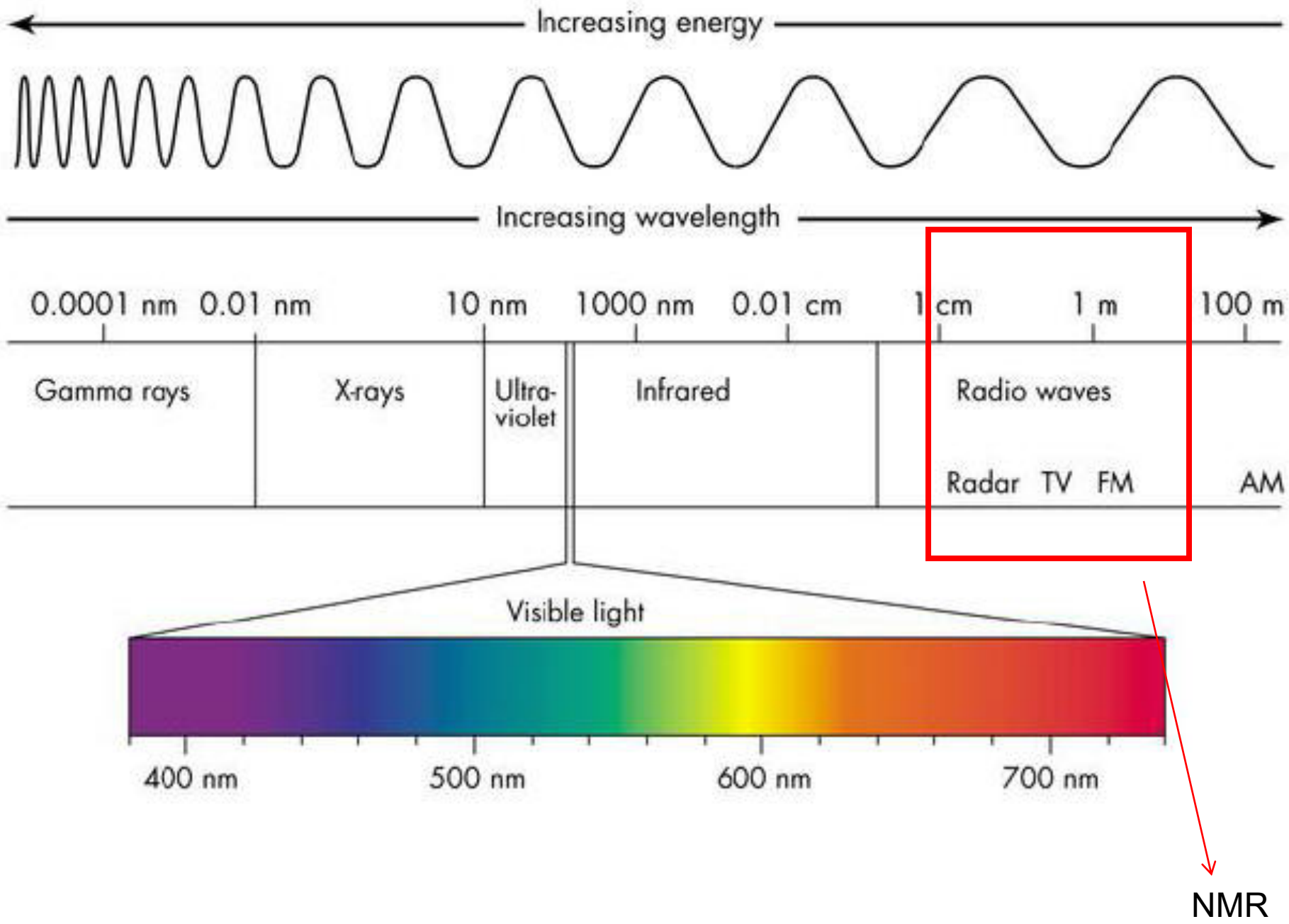


Composition of the Earth's Crust, Seawater, and the Human Body*

Earth's Crust		Seawater		Human Body [†]	
Element	%	Compound	mM	Element	%
O	47	Cl ⁻	548	H	63
Si	28	Na ⁺	470	O	25.5
Al	7.9	Mg ²⁺	54	C	9.5
Fe	4.5	SO ₄ ²⁻	28	N	1.4
Ca	3.5	Ca ²⁺	10	Ca	0.31
Na	2.5	K ⁺	10	P	0.22
K	2.5	HCO ₃ ⁻	2.3	Cl	0.08
Mg	2.2	NO ₃ ⁻	0.01	K	0.06
Ti	0.46	HPO ₄ ²⁻	<0.001	S	0.05
H	0.22			Na	0.03
C	0.19			Mg	0.01

*Figures for the earth's crust and the human body are presented as percentages of the total number of atoms; seawater data are millimoles per liter. Figures for the earth's crust do *not* include water, whereas figures for the human body do.

[†]Trace elements found in the human body serving essential biological functions include Mn, Fe, Co, Cu, Zn, Mo, I, Ni, and Se.

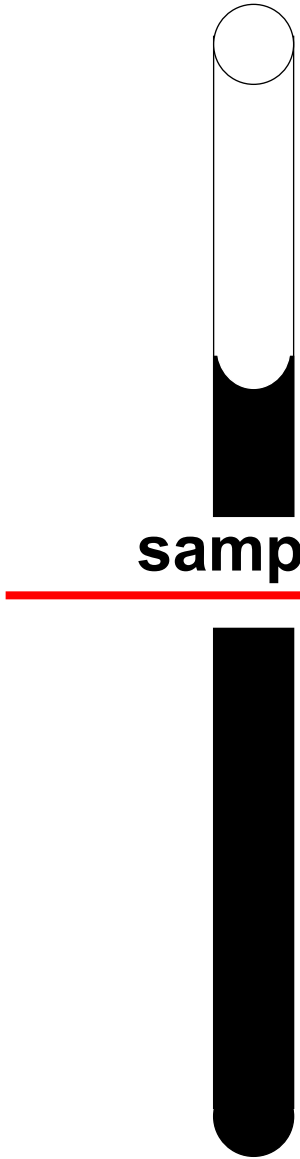


200-500 μl of
100-1000 μM compound

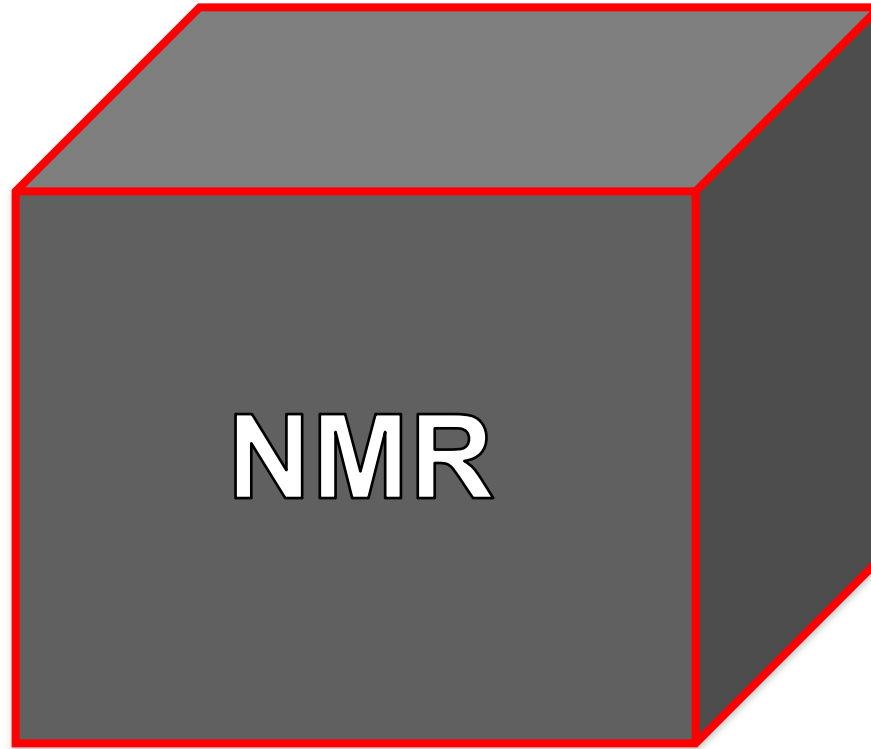
Method of choice

Data to be analyzed

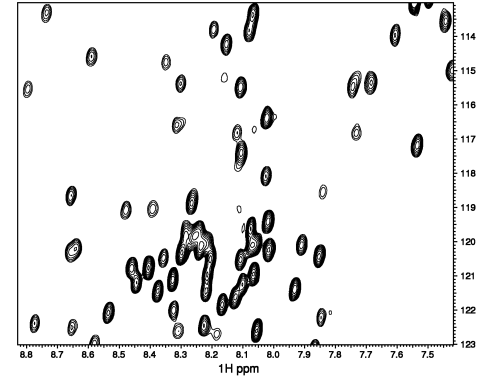
Results



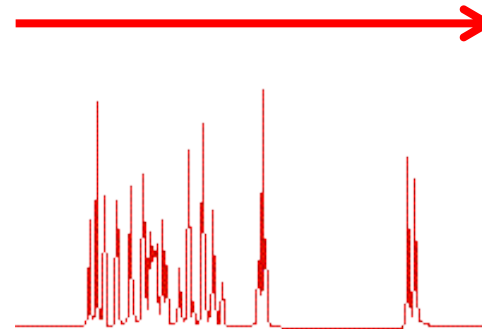
sample



NMR



spectrum



- 1) Structure
- 2) Relaxation properties
- 3) Interaction at atomic level resolution
- 4) Analysis
- 5) Image

NMR hardware

- 1) Magnet
- 2) Spectrometer
- 3) Control units



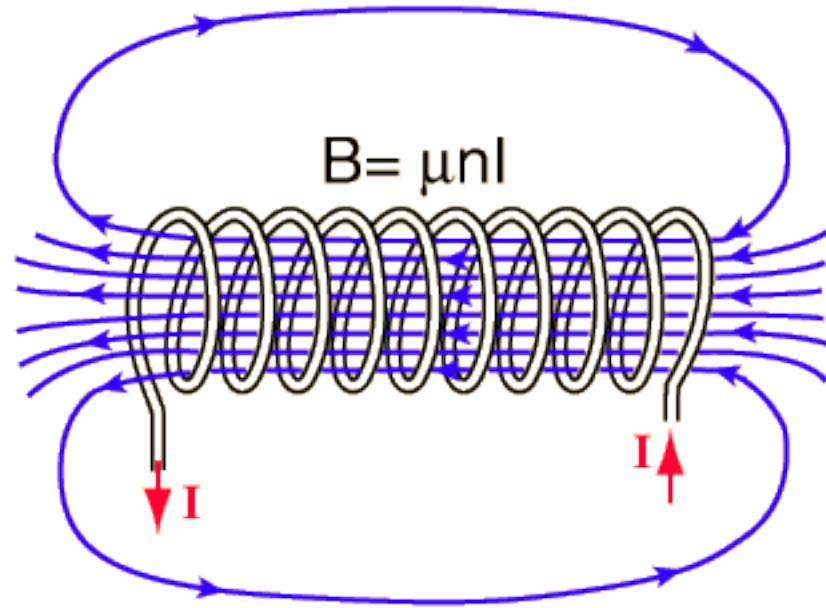
NMR spectrometer



Earth's Magnetic Field

$\sim 50\mu\text{T}$

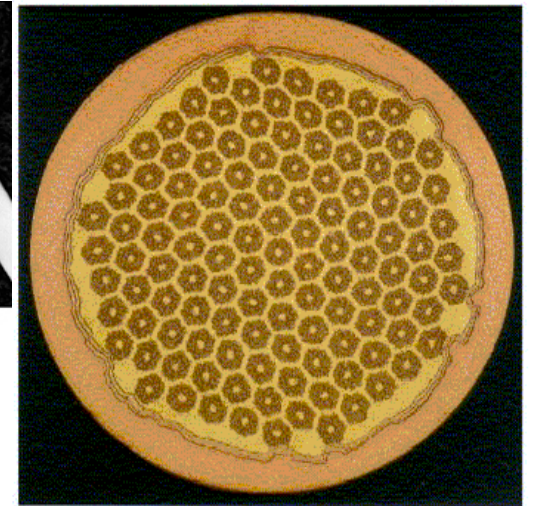
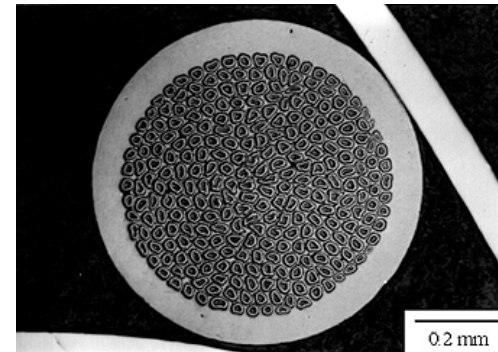
Ampere's law & solenoid



The magnetic field is concentrated into a nearly uniform field in the center of a long solenoid. The field outside is weak and divergent.

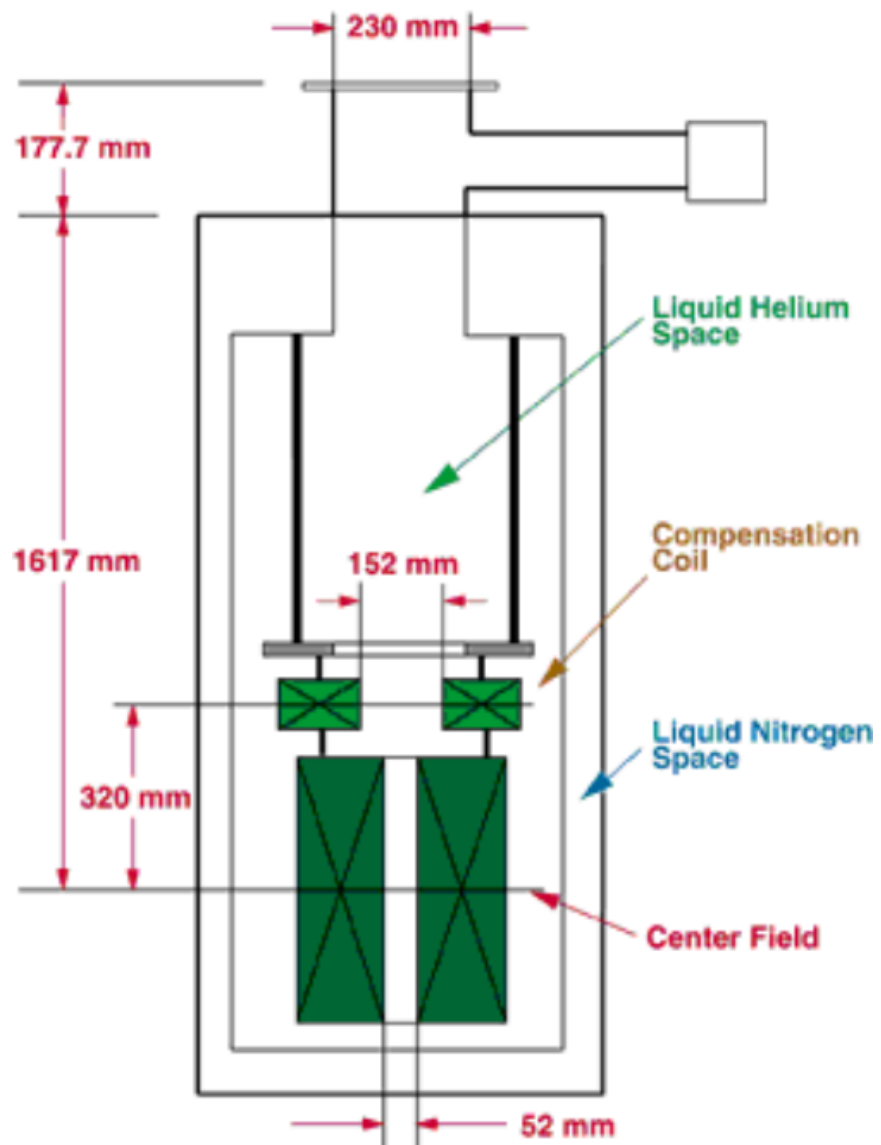
Magnet

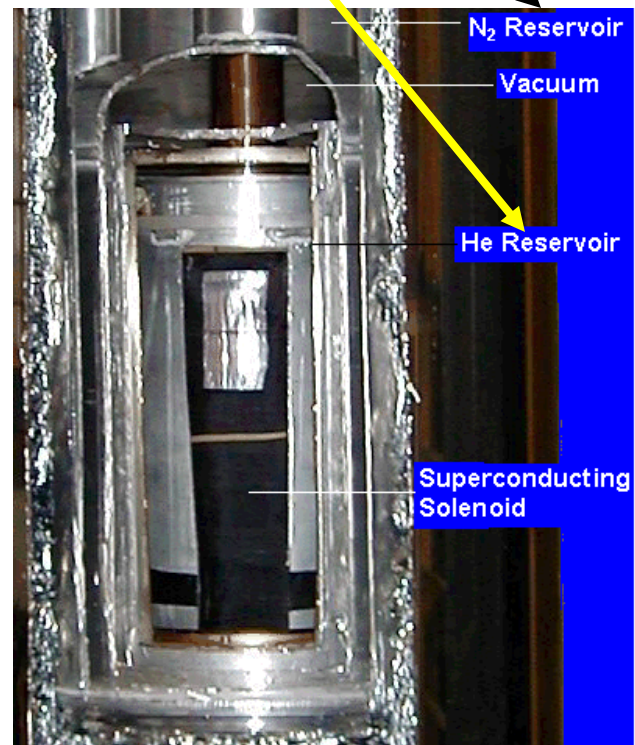
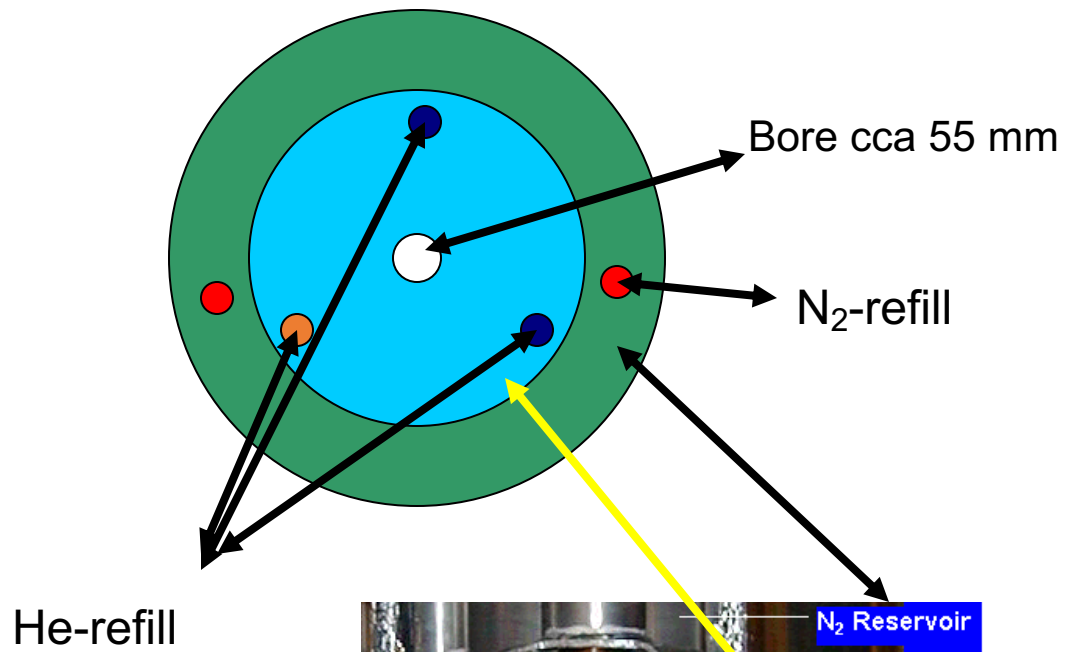
- superconducting solenoids immersed into He bath
- He-bath **~4 K** further improved to **~2.1 K** with J-T pump
- field strength 25-28 Tesla
- $(\text{Nb, Ta})_3\text{Sn}$ superconductor of 0.81 mm with ~ 271 filaments buried in OFHC copper matrix



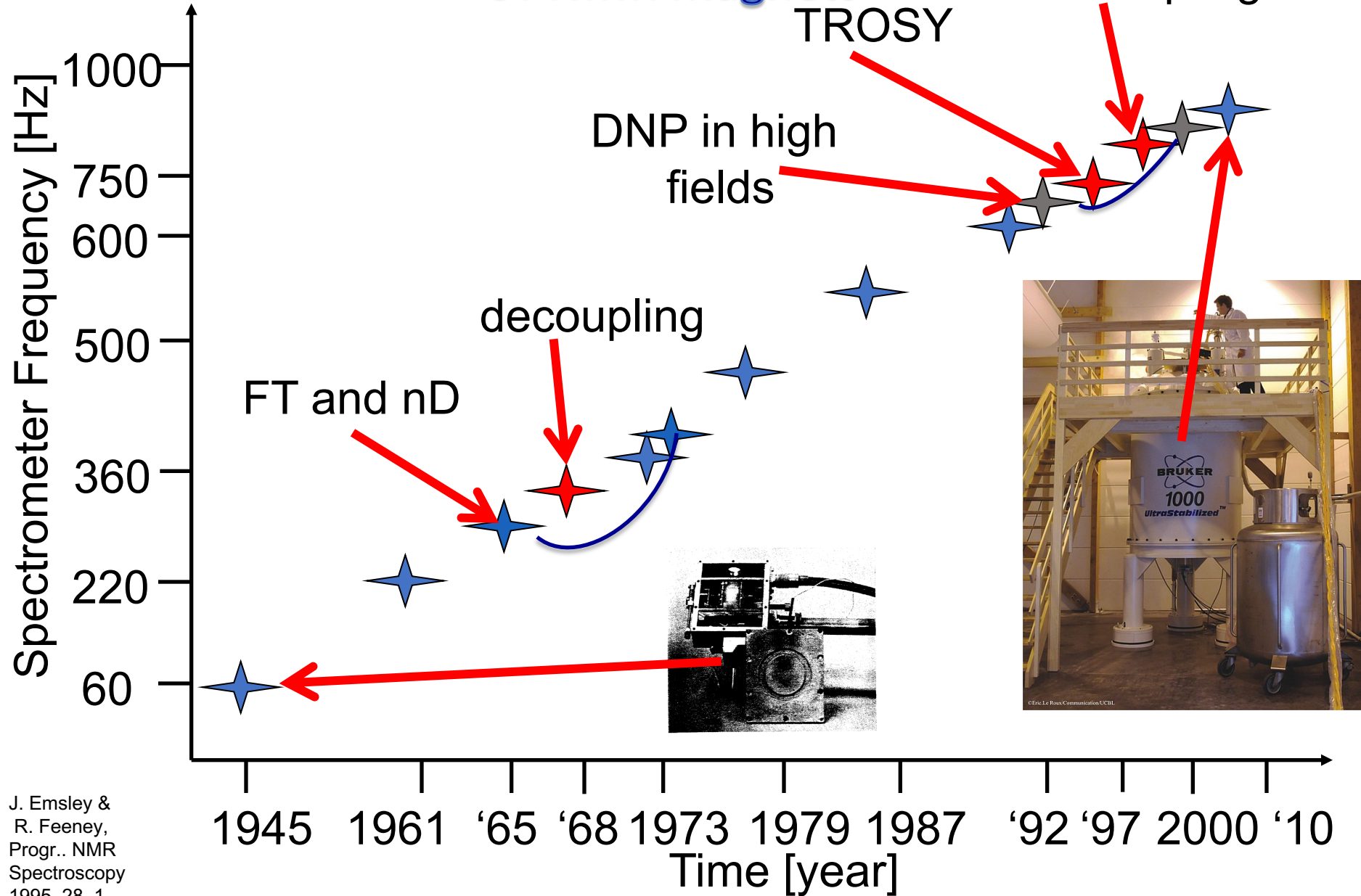


20T Superconducting Magnet





Improvement of sensitivity, resolution and signal-to-noise ratio Of NMR magnets



Quench

an **abnormal** termination of magnet operation

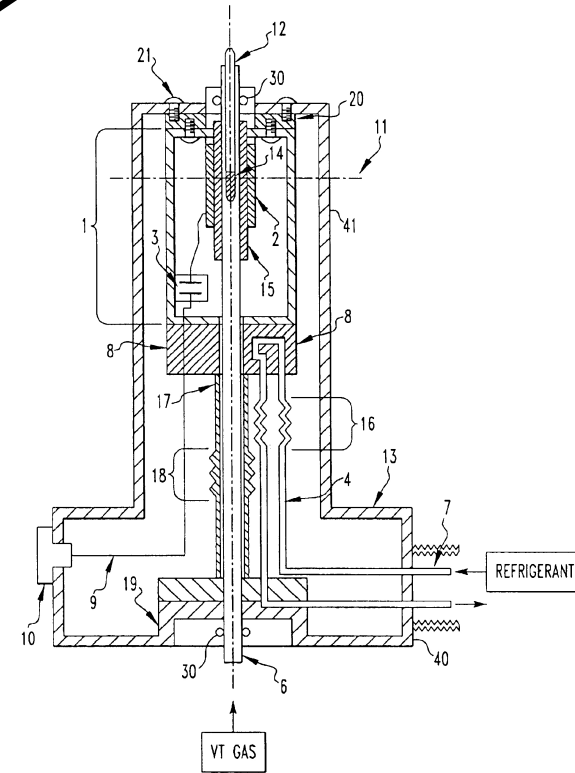
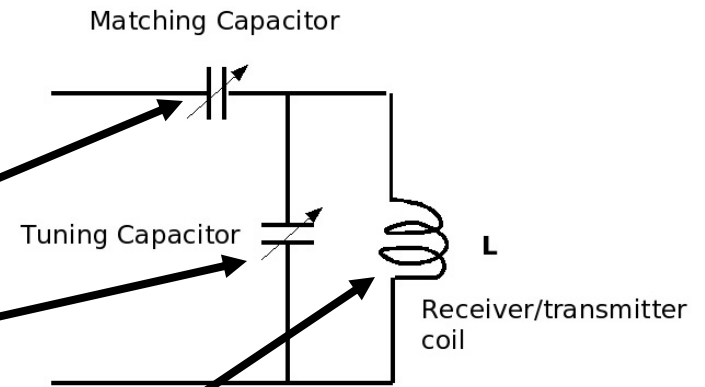
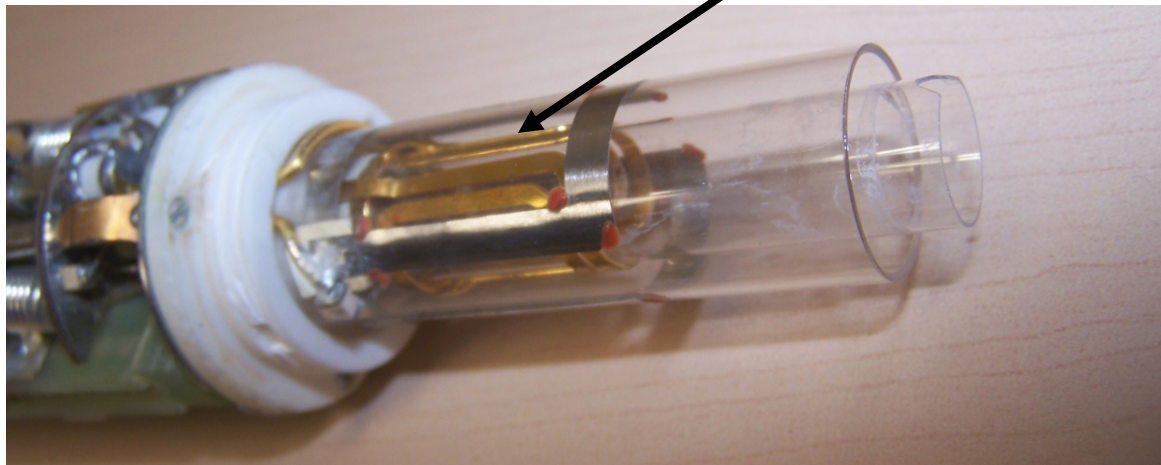
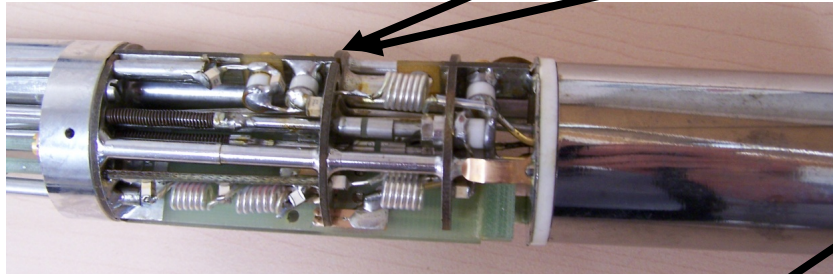
Occurs when part of the superconducting coil enters the normal (resistive) state.

This can **occur**

- i) because the field inside the magnet is too large
- ii) the rate of change of field is too large (causing eddy currents and resultant heating in the copper support matrix)
- iii) or a combination of the two.
- iv) a defect in the magnet can cause a quench.

MOVIE: https://www.youtube.com/watch?v=d-G3Kg-7n_M

NMR Probe(head)

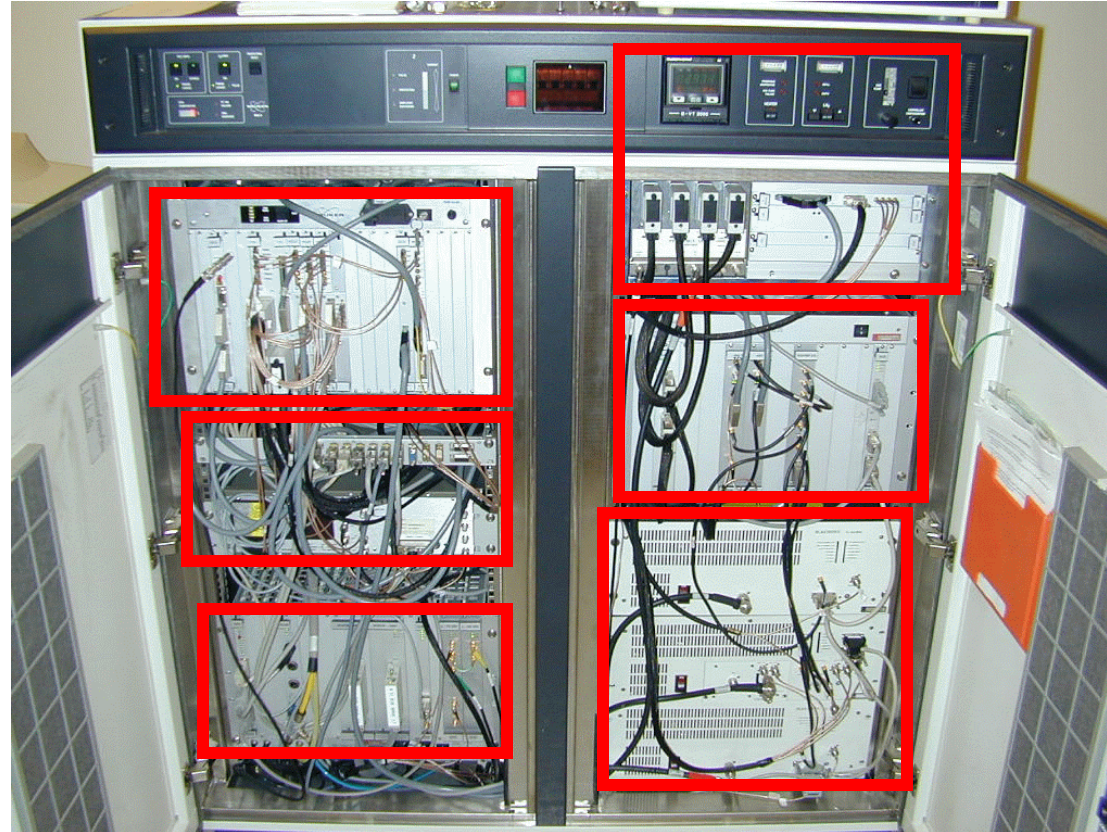


Spectrometer

CBU
Control board
unit

FGU
Frequency
gen. u.

Shimms

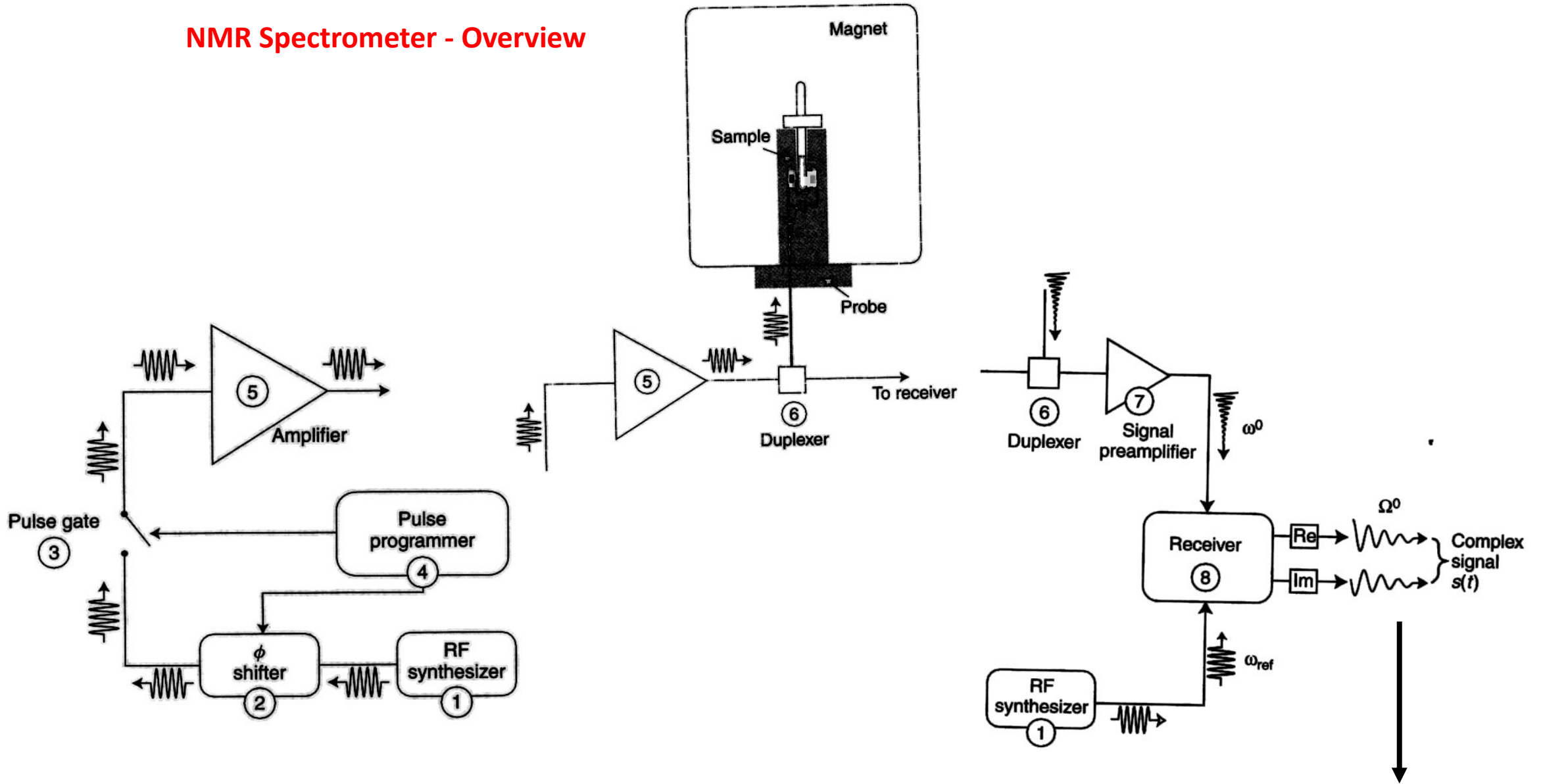


**Temperature
Unit**

**Acquisition Con
troller**

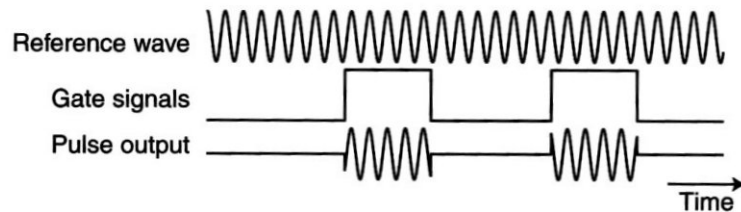
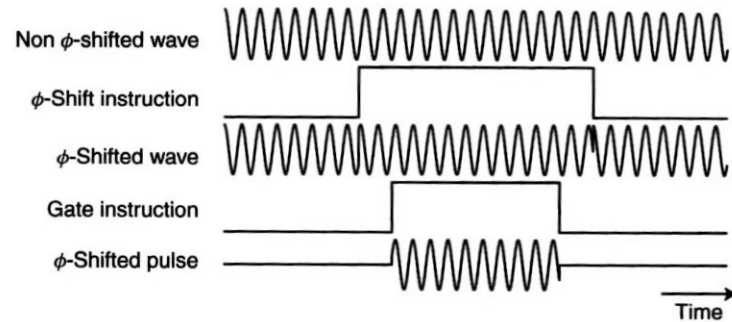
Transmitter

NMR Spectrometer - Overview



Signal - $s_1(t) = \sum s_i(t)$

NMR radiofrequency pulse



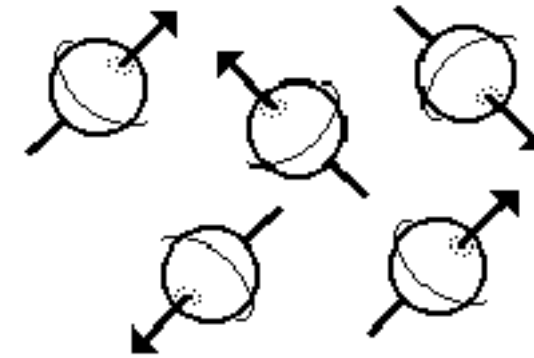
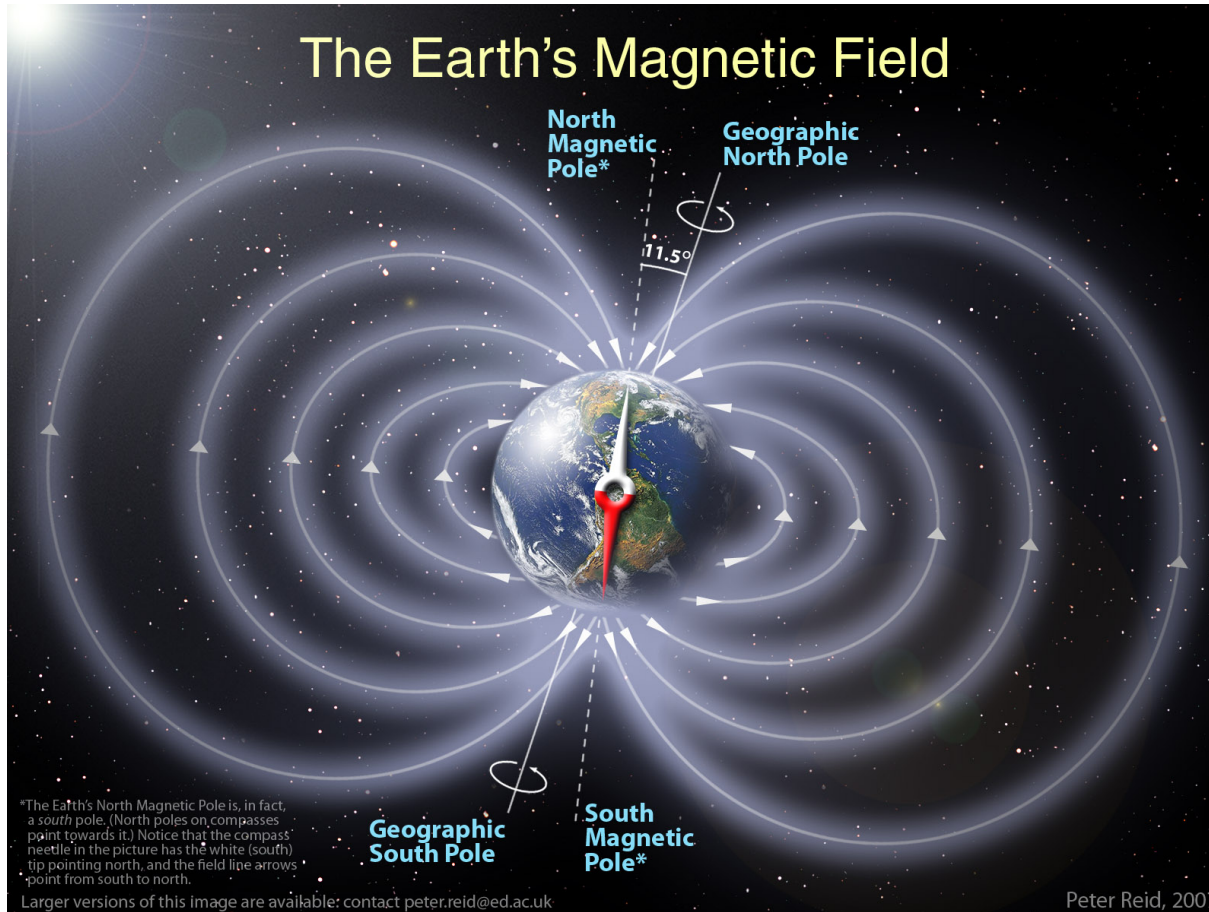
R.f. phase	Jargon
$\phi = 0$	'x-pulse'
$\phi = \pi/2$	'y-pulse'
$\phi = \pi$	'x-pulse' or '-x-pulse'
$\phi = 3\pi/2$	'y-pulse' or '-y-pulse'

Pulzy:

- tvrdé – 7-30 μs @-3~+3dB
- selektivní – ms~s@>30db
- adiabatické

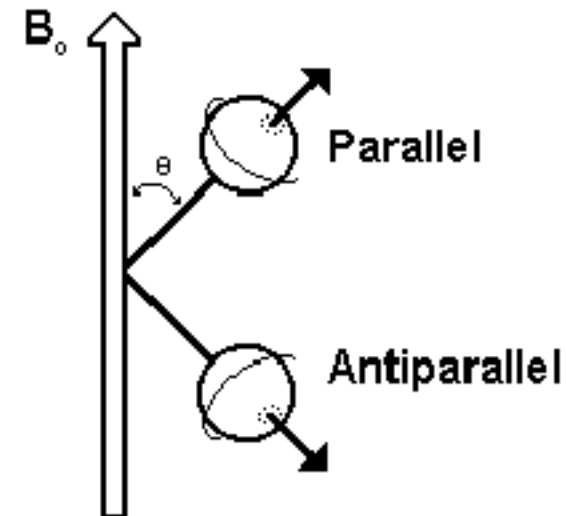
For NMR, nuclear spin is needed!!!

Spin analogy to a compass needle



magnetic field = 0

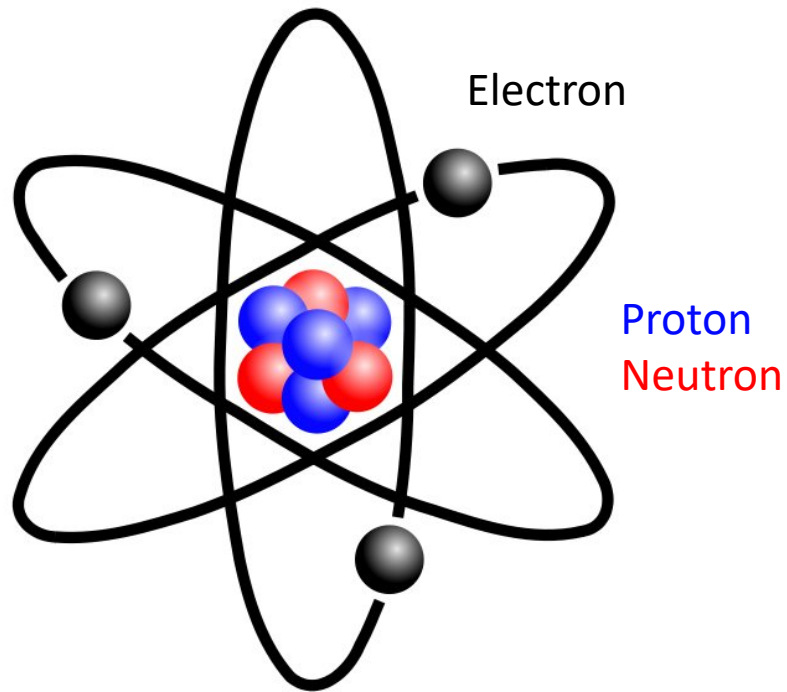
Randomly oriented nuclear magnetic moments



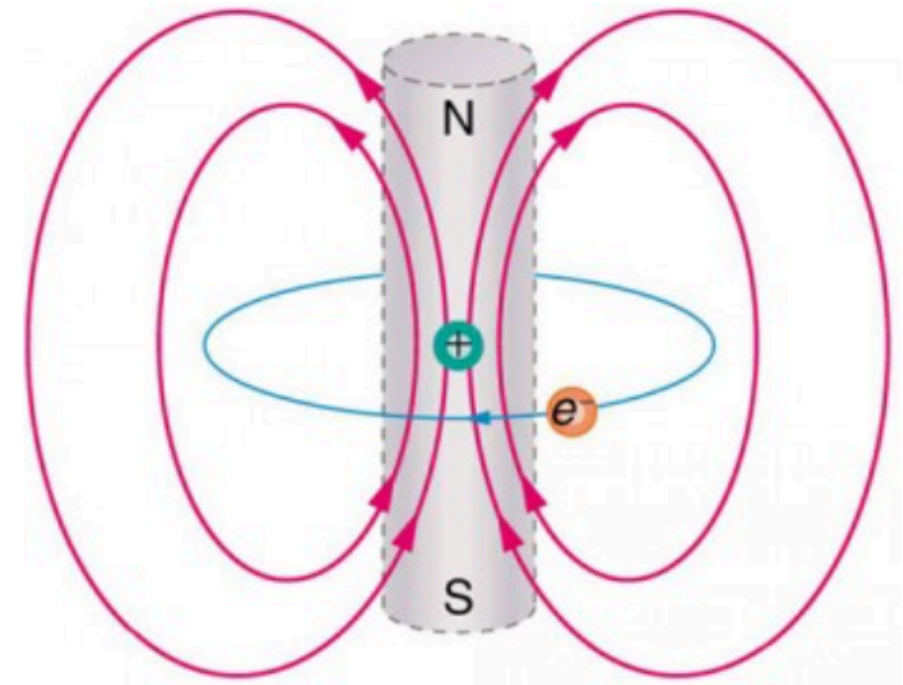
magnetic field > 0

Nuclear magnetic moments in the presence of an external field

Atom



=

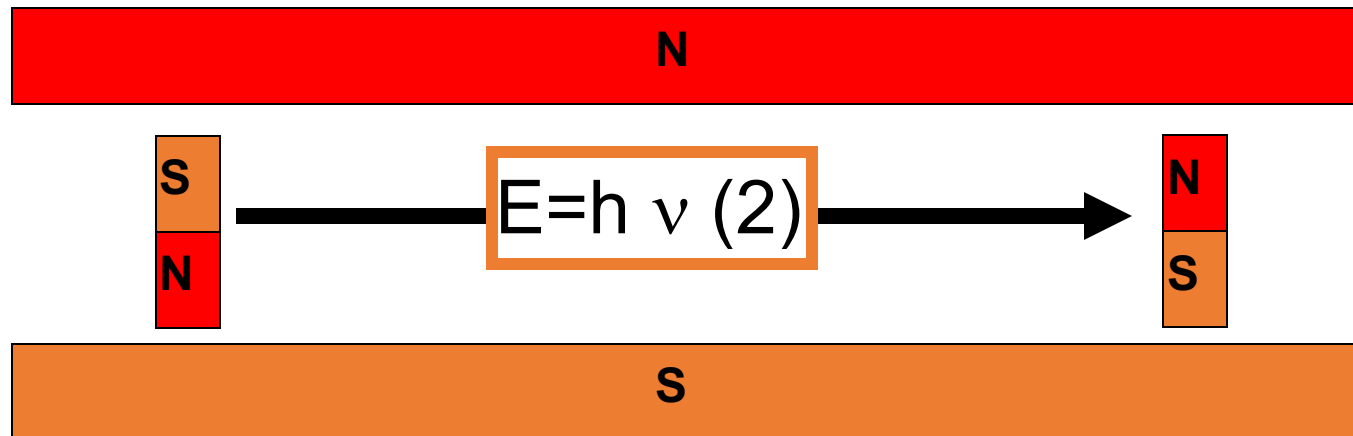


In the planetary model of the atom, an **electron orbits a nucleus**, forming a closed-current loop and **producing a magnetic field** with a north pole and a south pole.

Molecule is hence a group of small magnetic fields and each atom within the molecule experiences different local magnetic field.

NMR - Refresh

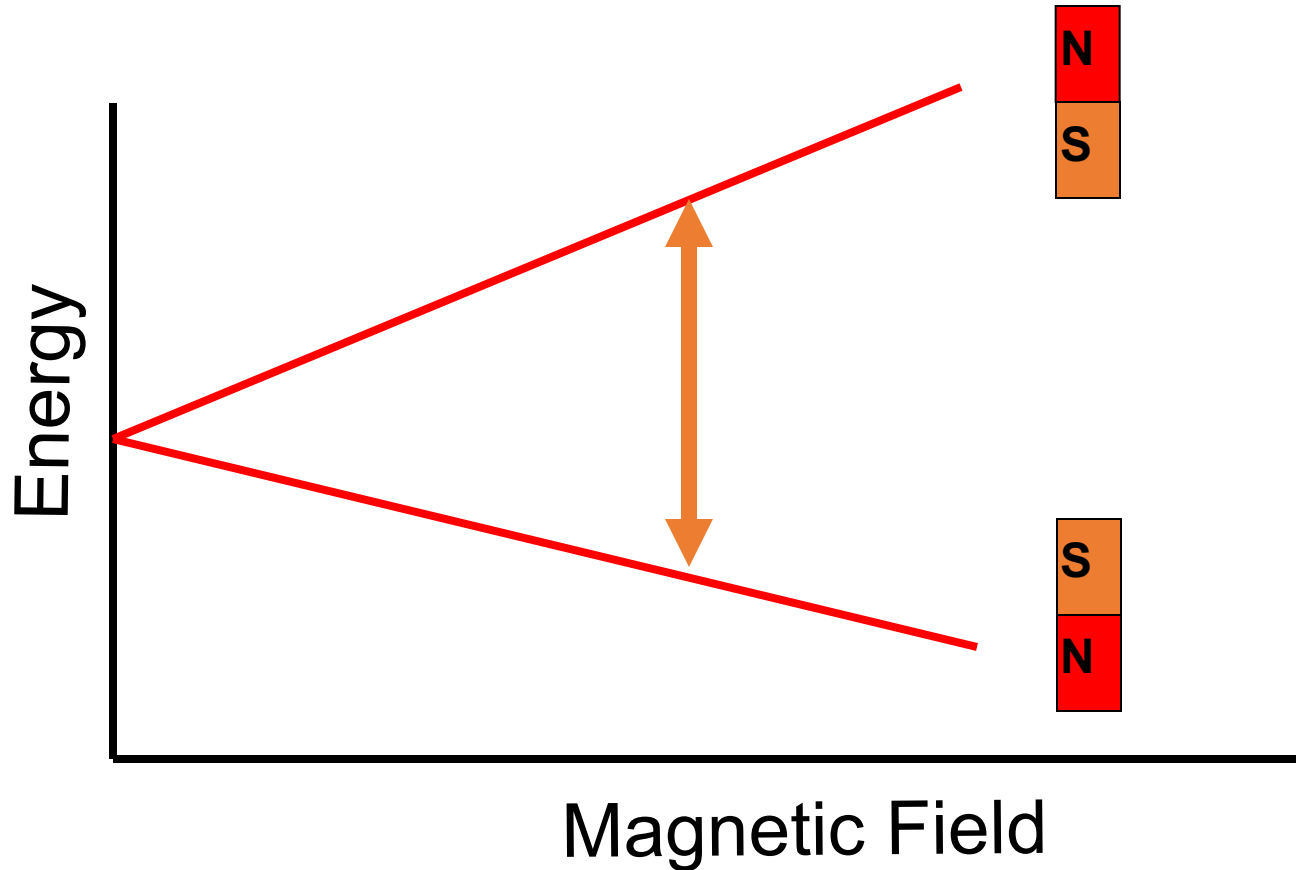
- 1) nuclear spin $\neq 0$ (^1H , ^{13}C , ^{15}N , ^{31}P)
 - number of neutrons **and** the number of protons **both even** \Rightarrow **NO nuclear spin**
 - number of neutrons **plus** the number of protons **odd** \Rightarrow **half-integer spin** (i.e. $\frac{1}{2}$, $\frac{3}{2}$, $\frac{5}{2}$)
 - number of neutrons **and** the number of protons **both odd** \Rightarrow **integer spin** (i.e. 1, 2, 3)
- 2) $\nu = \gamma \cdot B$ (1) - when placed in a magnetic field of strength **B**, a nuclei with a net spin can absorb a photon, of frequency ν . The frequency ν depends on the gyromagnetic ratio, γ of the nuclei
- 3) from quantum mechanics we know that nucleus with spin I can have $2I + 1$ orientations \Rightarrow **nuclei with a spin $\frac{1}{2}$** can have **two orientations in an external magnetic field**— **low / high energy**

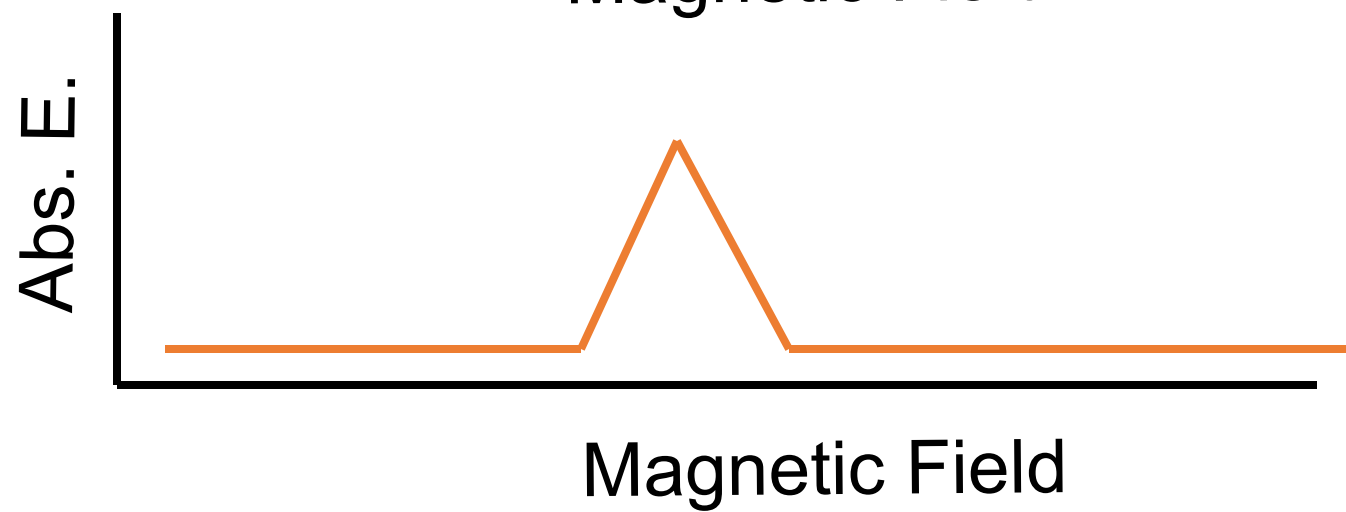
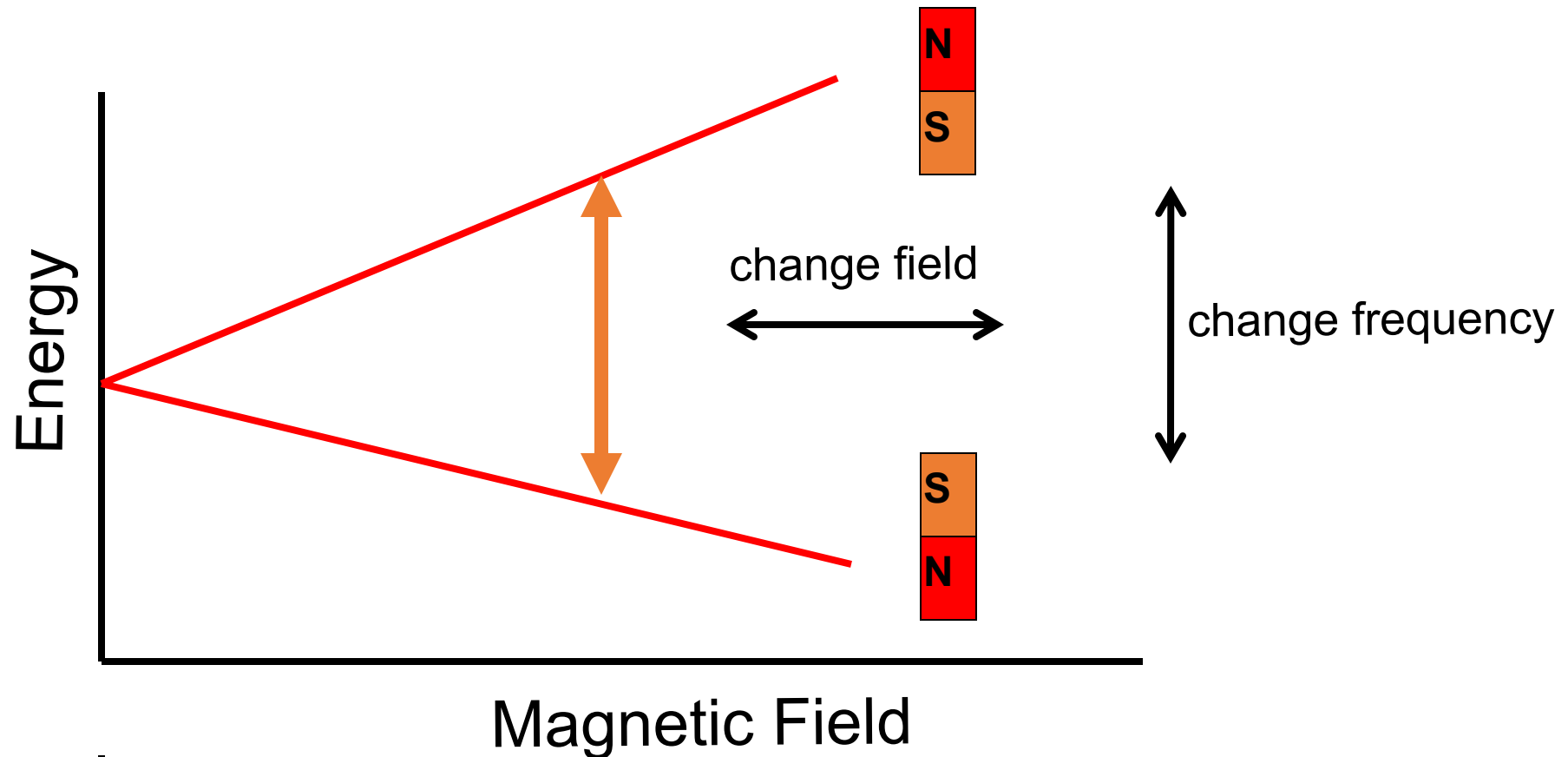


Nuclear Magnetic Resonance

Refresh

From (1) and (2): $E = h \gamma B$





CW vs. Fourier transform NMR

Problem of NMR

the magnitude of the energy changes in NMR spectroscopy small \Rightarrow **sensitivity is a major limitation**

Solution I.

increase sensitivity by recording many spectra, and then add them together; because **noise is random**, it adds as the square root of the number of spectra recorded.

For example, if **100** spectra of a compound were recorded and summed, then the **noise would increase** by a factor of **10**,

but the **signal would increase** in magnitude by a factor of **100**
 \Rightarrow large increase in sensitivity.

However, if this is done using a **CW-NMR**, the time needed to collect the spectra is very large (one scan takes **2 - 8** minutes).

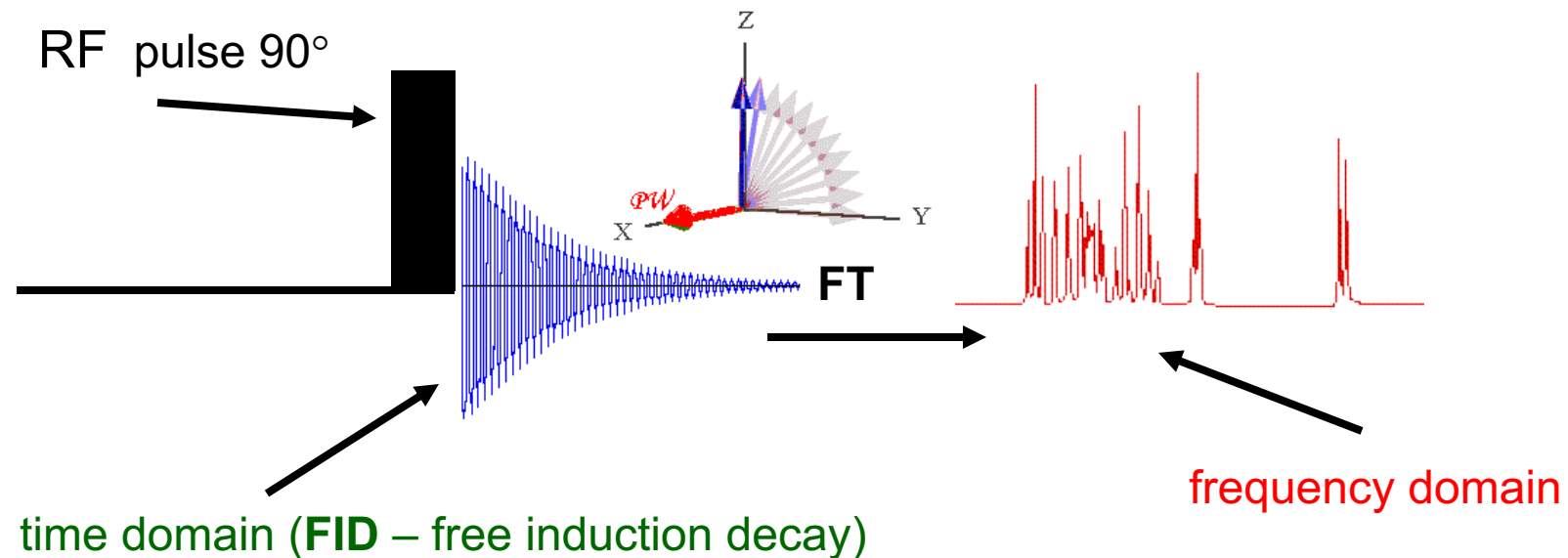
CW vs. Fourier transform NMR

Solution II.

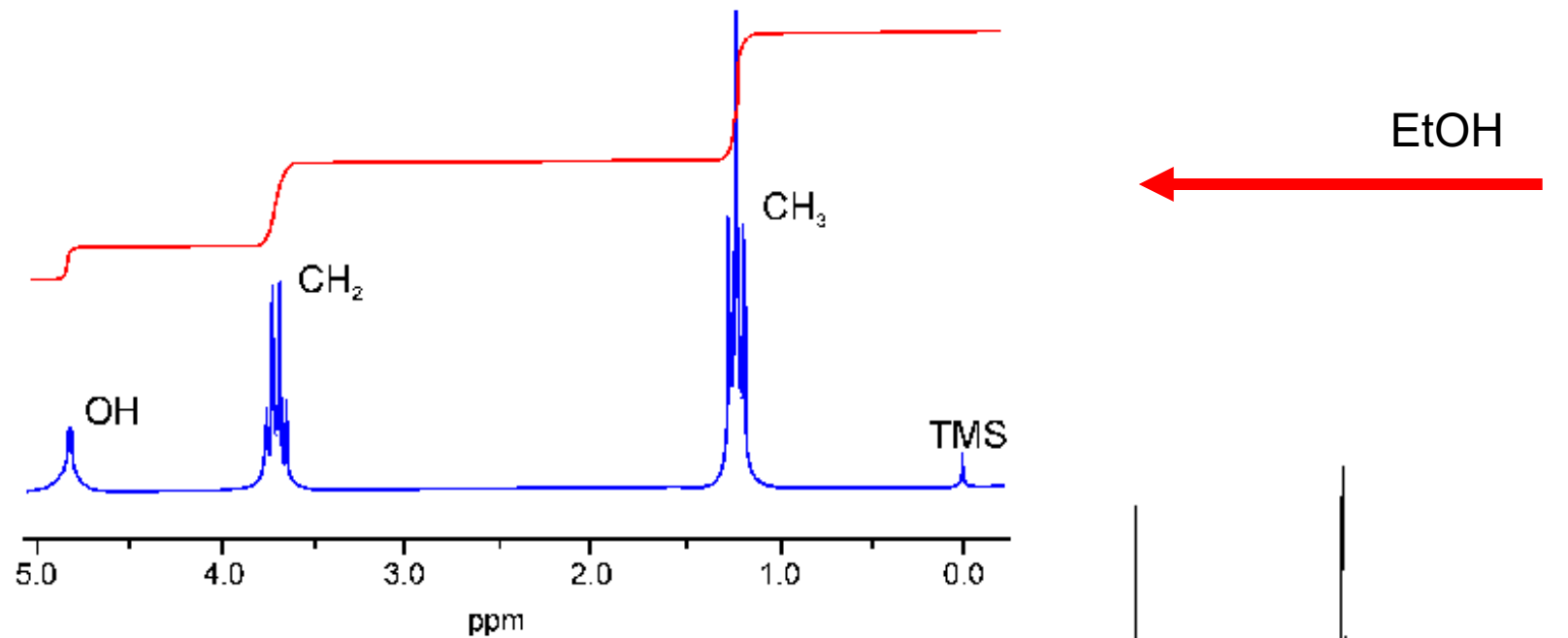
FT-NMR \Rightarrow *all frequencies* in a spectrum are *irradiated simultaneously* with a radio frequency pulse.

Following the pulse, the nuclei return to thermal equilibrium. A *time domain* emission signal is recorded by the instrument as the nuclei relax.

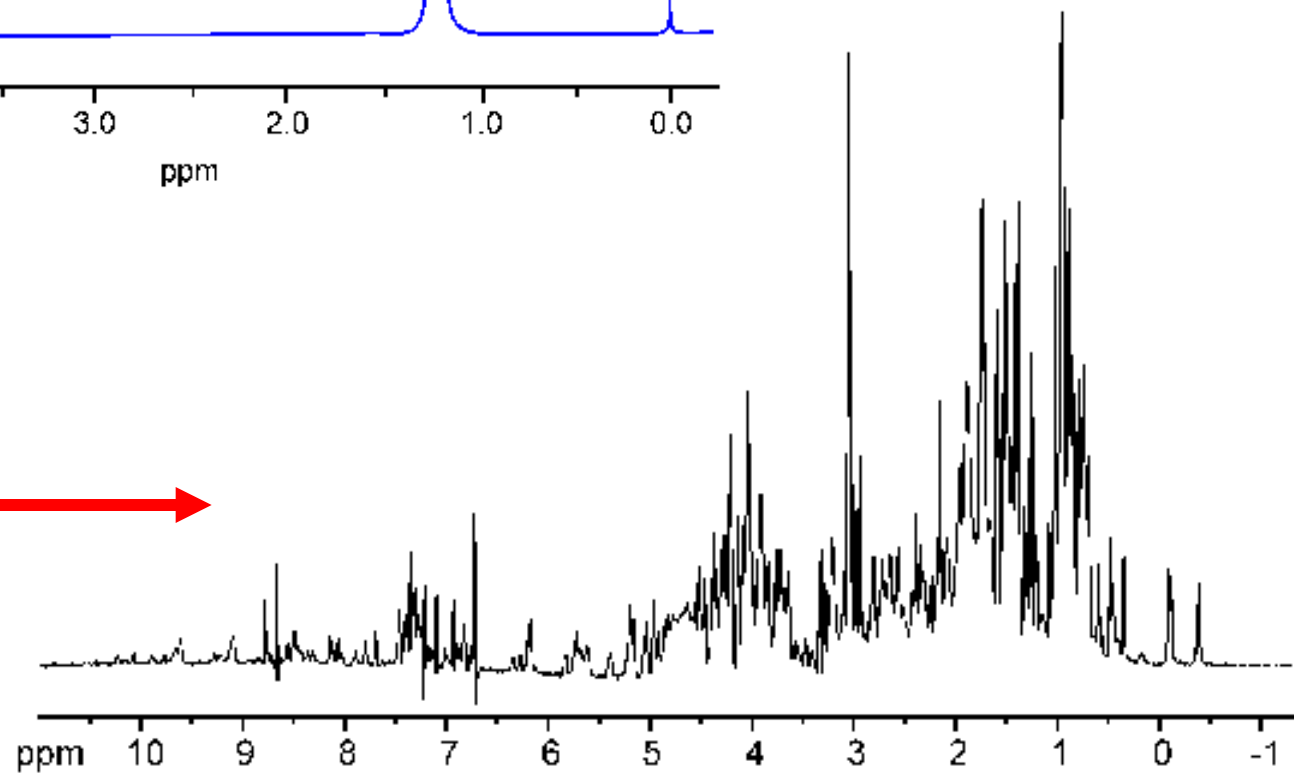
A *frequency domain* spectrum is *obtained by Fourier transformation*.



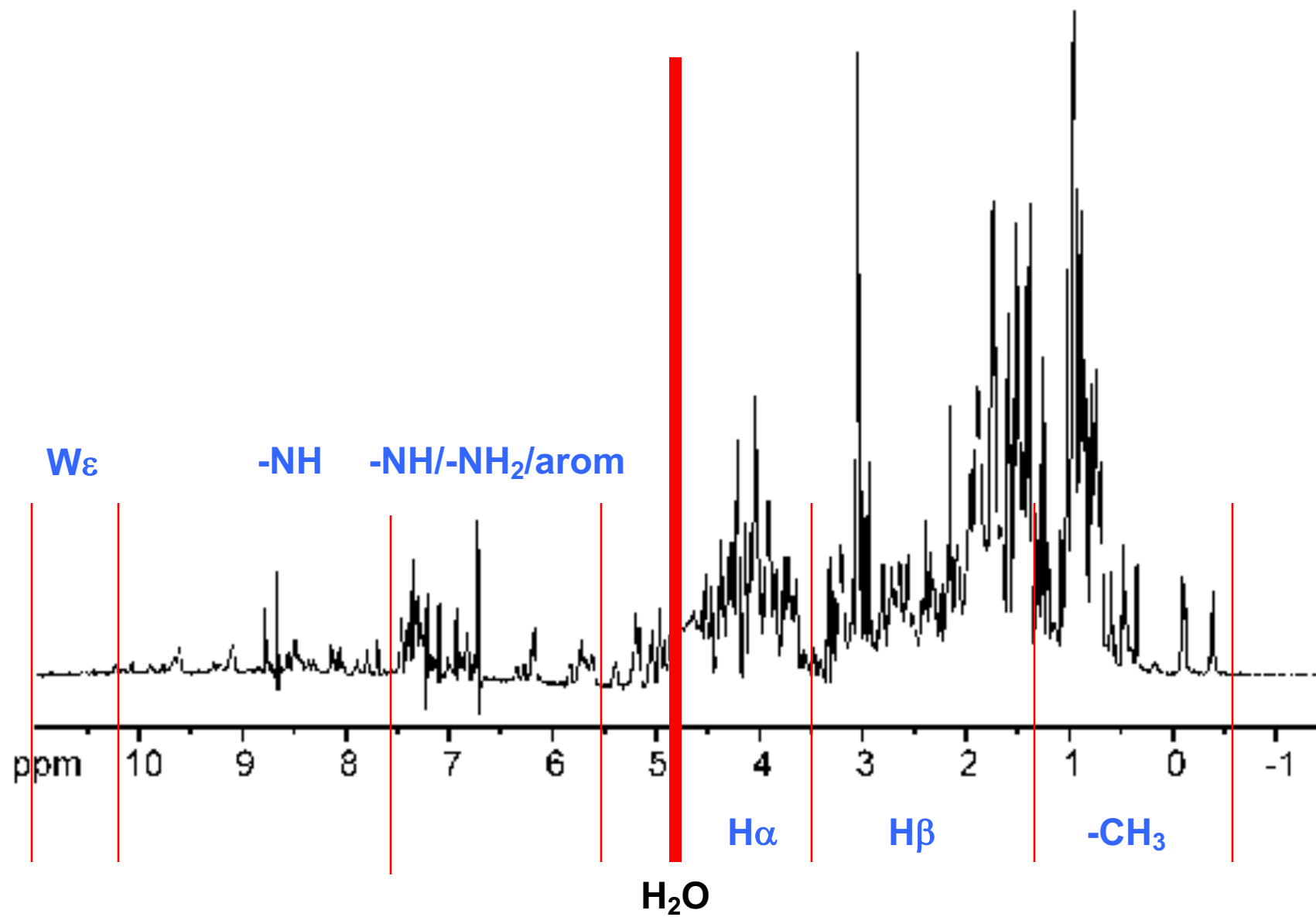
Each proton = 1 NMR signal



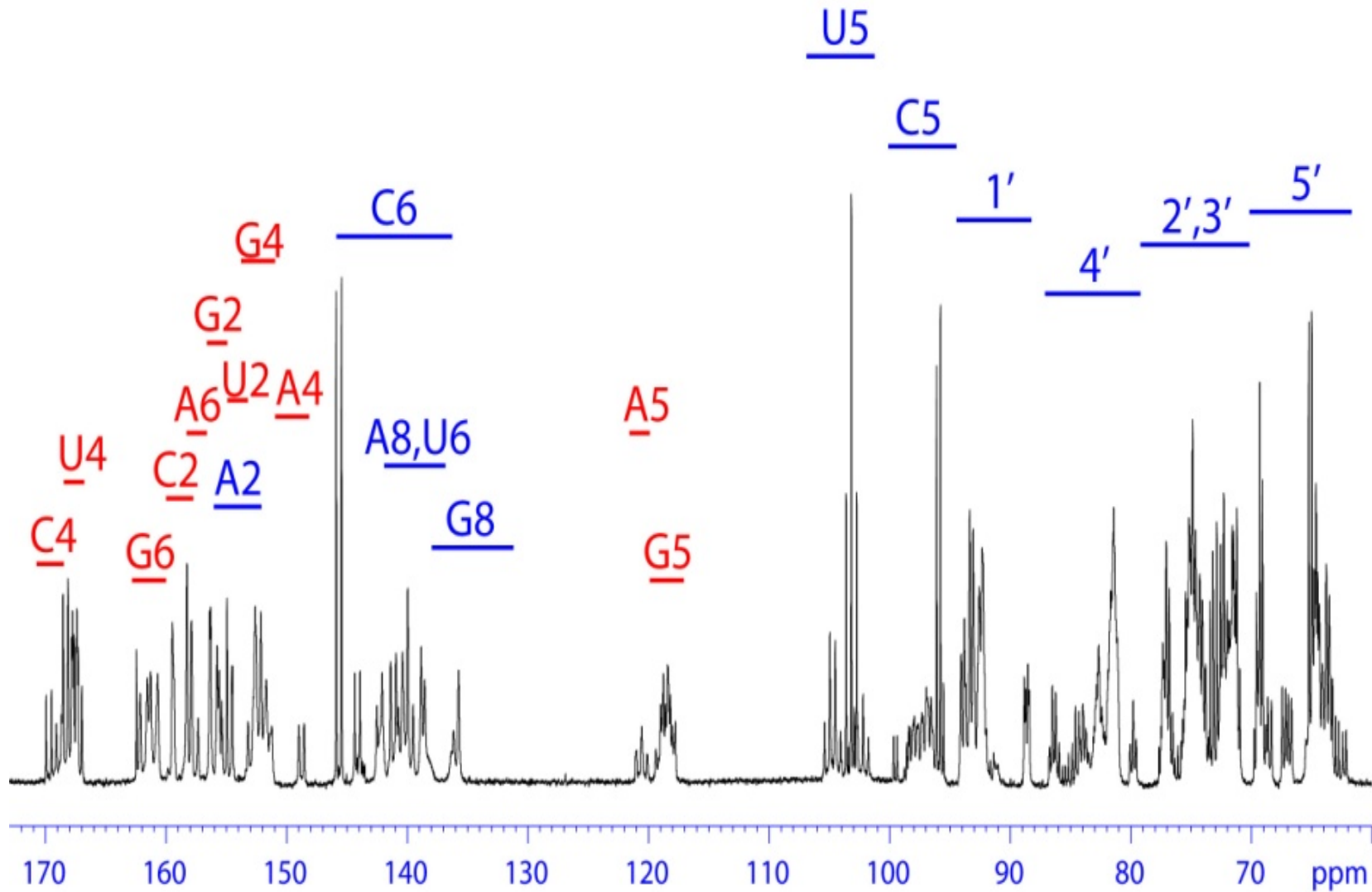
protein



Each (non-exchangeable) proton = 1 NMR signal



Each (non-exchangeable) proton = 1 NMR signal



Size



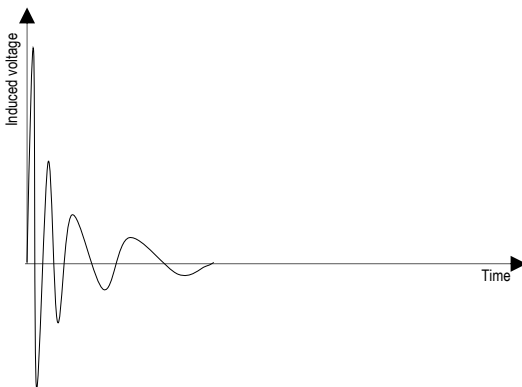
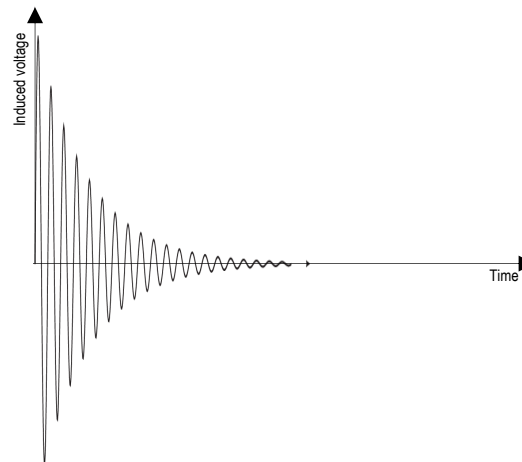
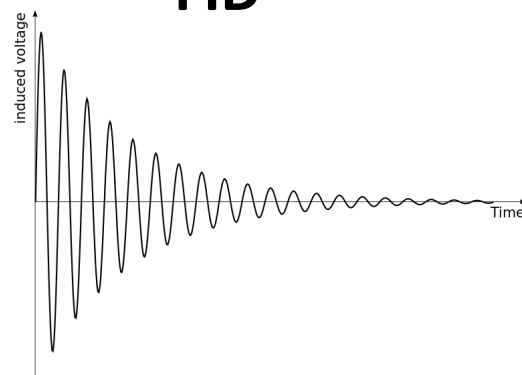
Relaxation

slow (i.e. long t_2 time)

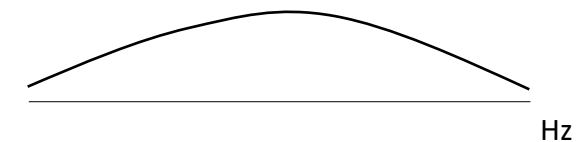
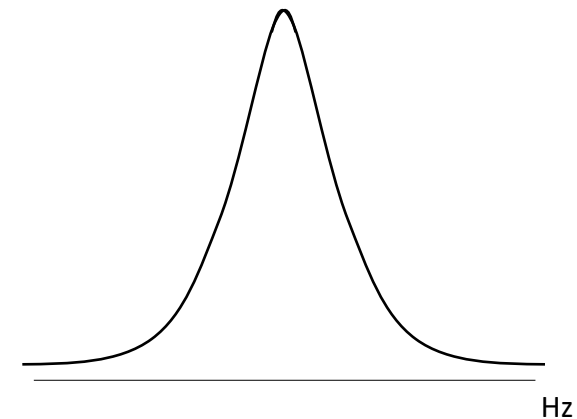
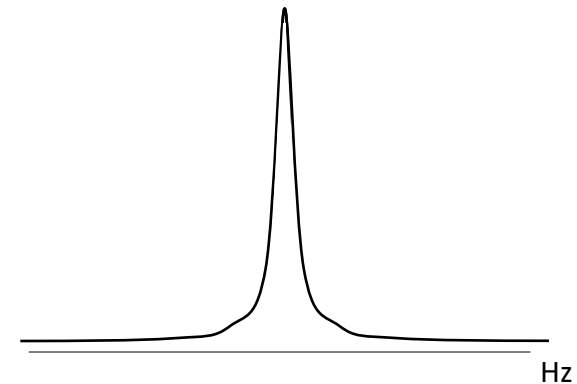
medium

fast

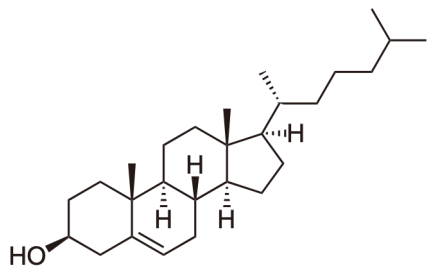
FID



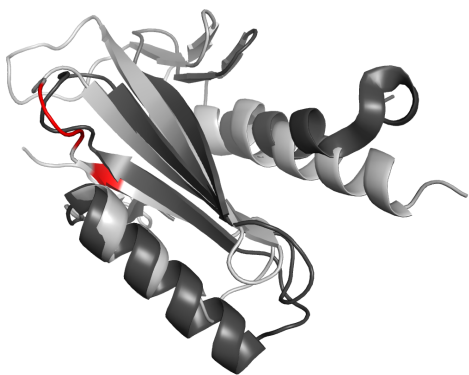
NMR line(width) after FT



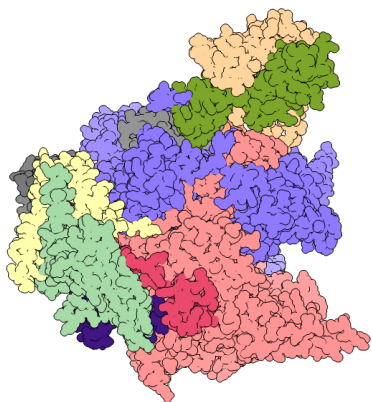
Size



e.g. Cholesterol



Biomolecules 5-30 kDa



Large molecules 50+ kDa

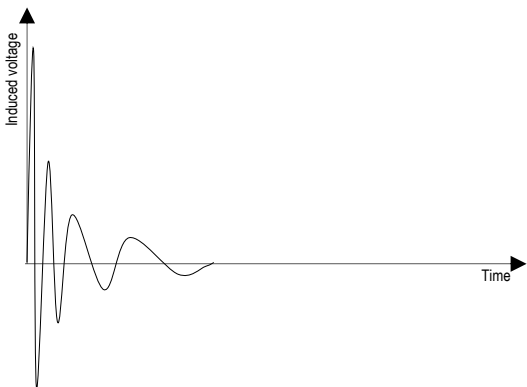
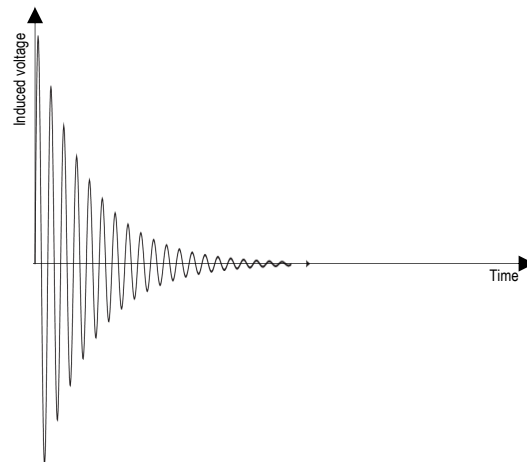
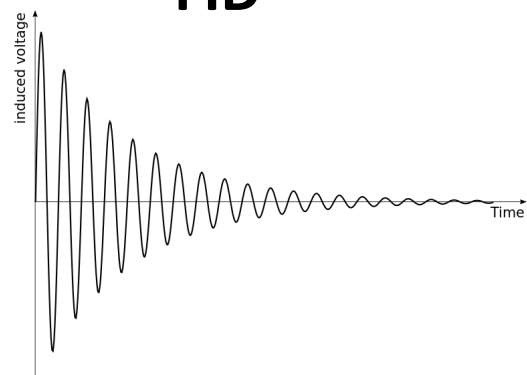
Relaxation

slow (i.e. long t_2 time)

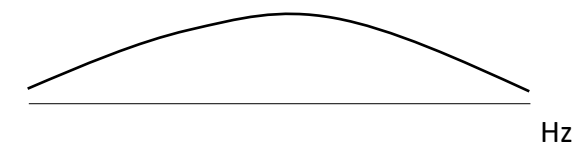
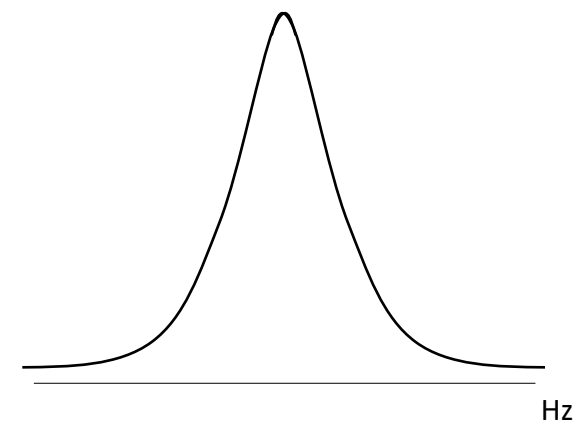
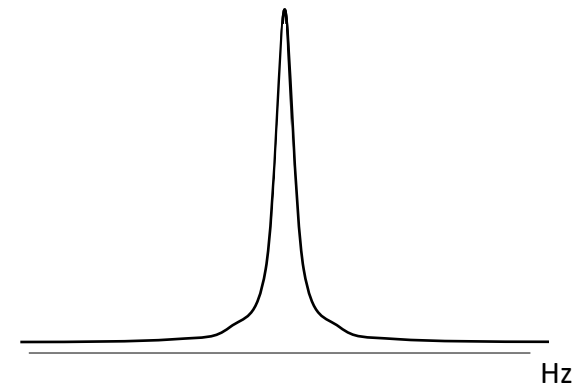
medium

fast

FID

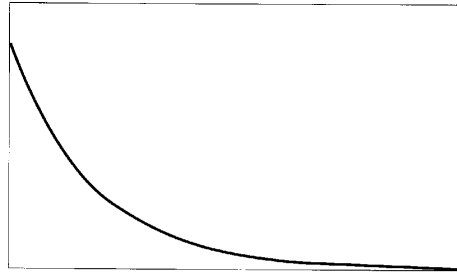


NMR line(width) after FT

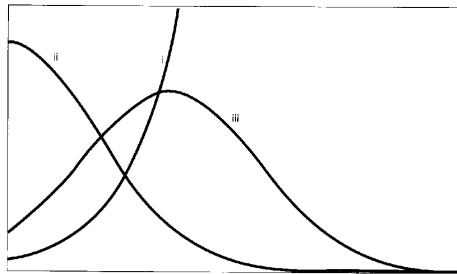


NMR data processing

NMR data processing



(a)



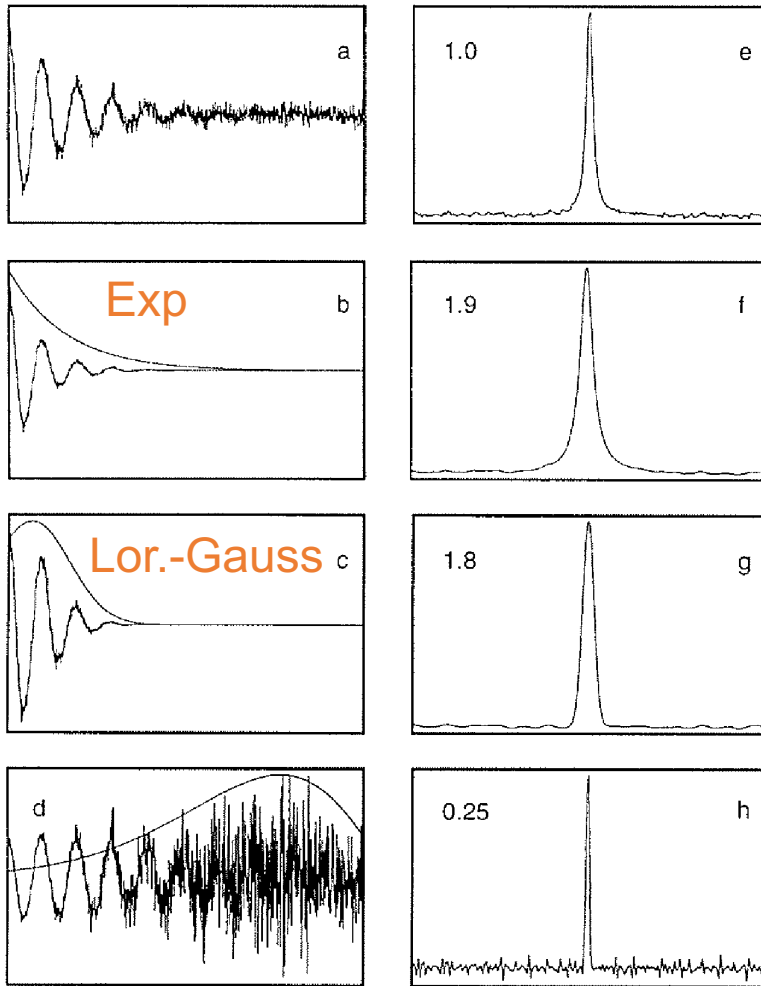
(b)

Window functions:

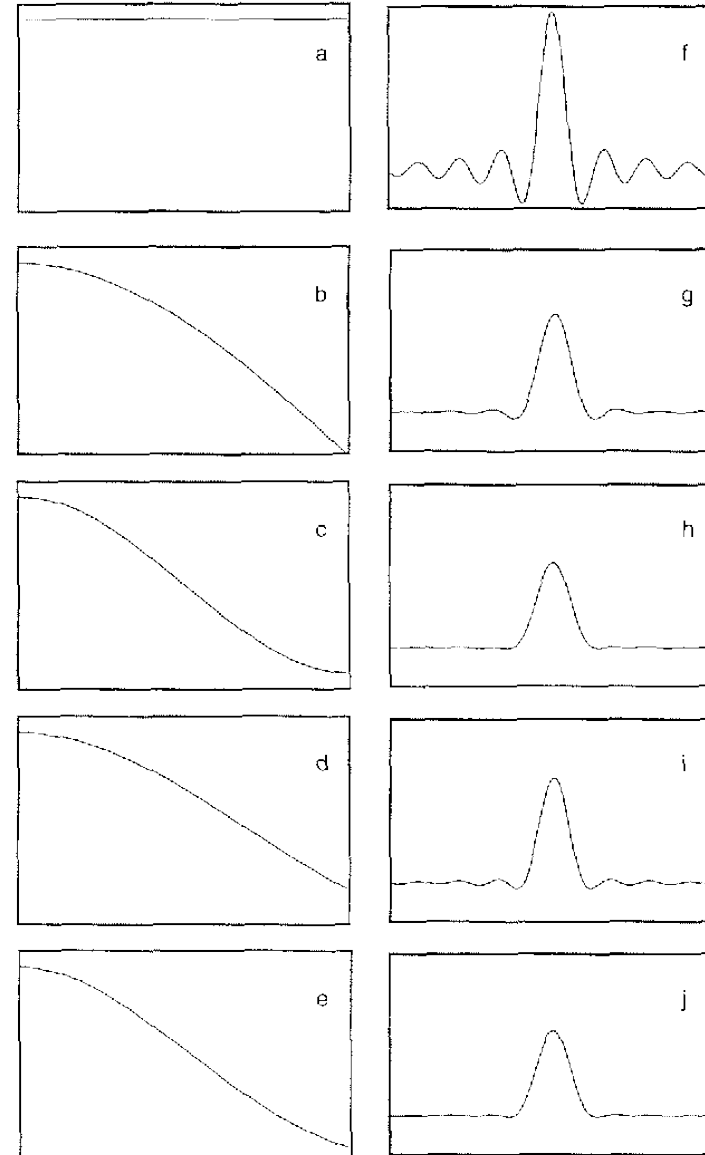
1) improvements of S/N ratio

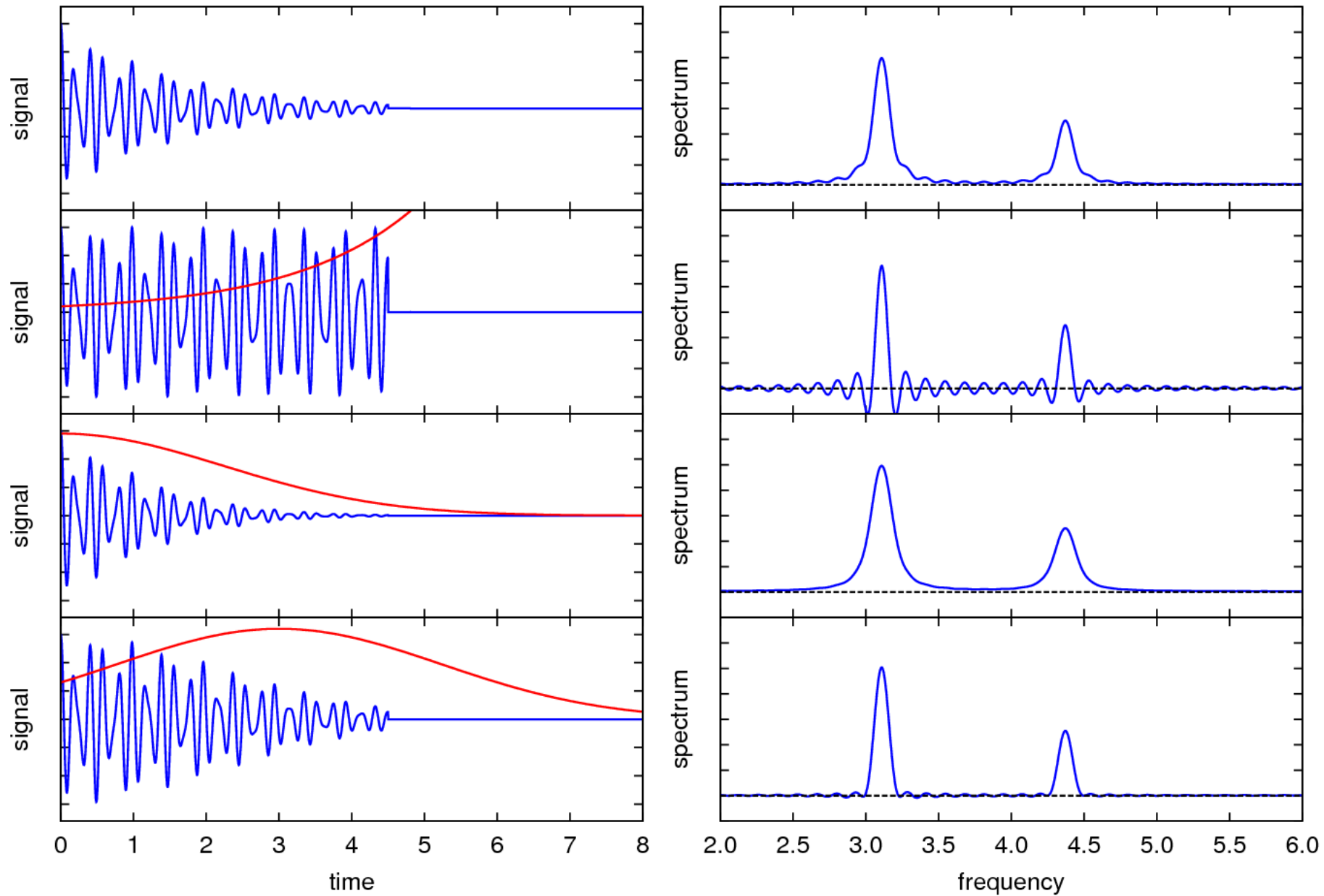
2) increasing resolution

NMR data processing – window functions – apodization



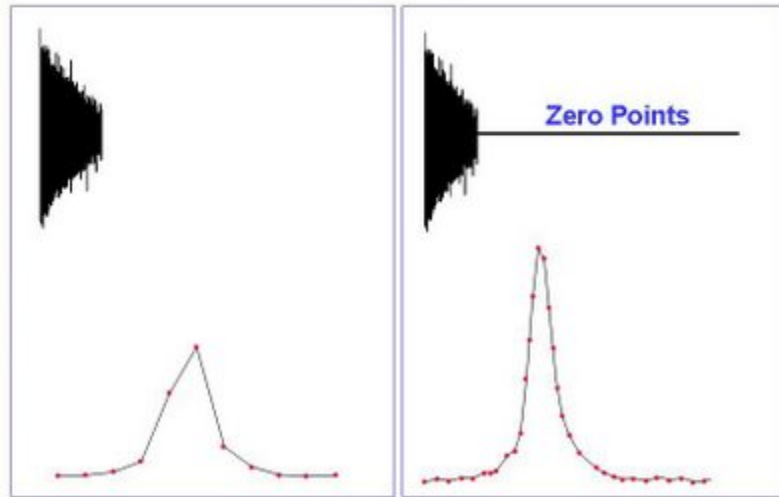
Kaiser w. function



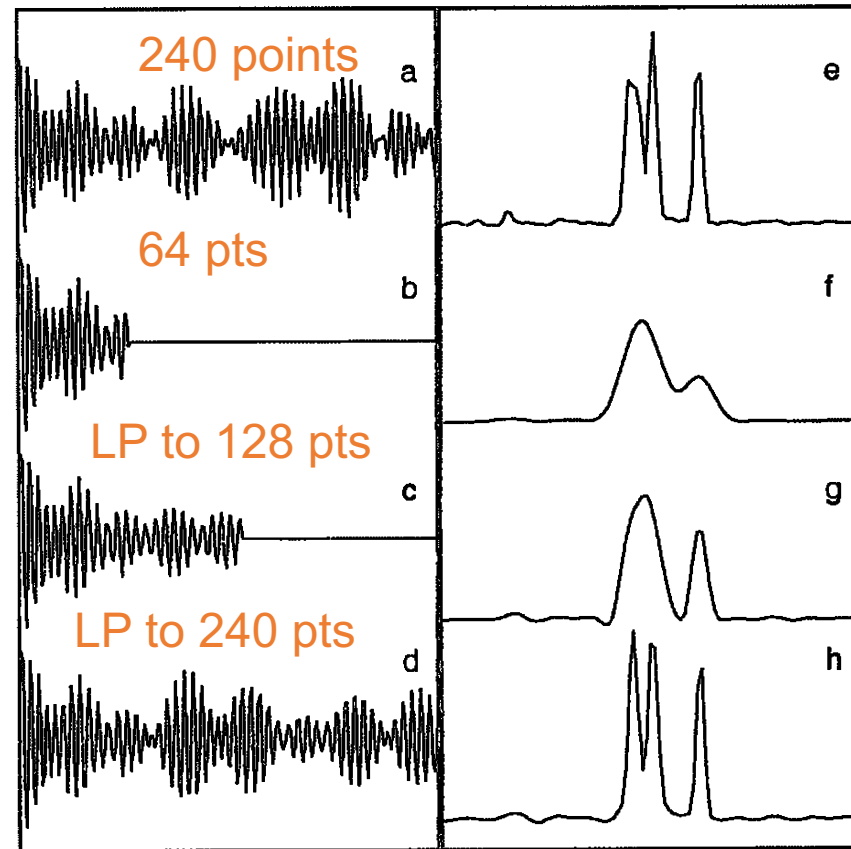


NMR data processing – Zero Filling, Linear prediction

Zero filling



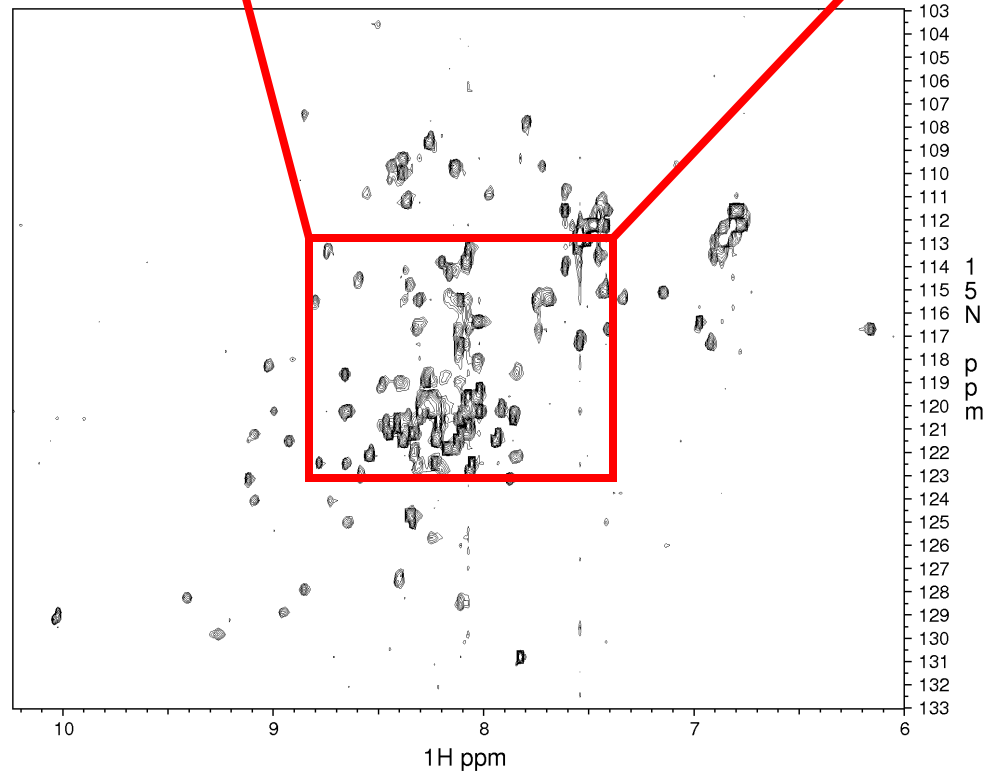
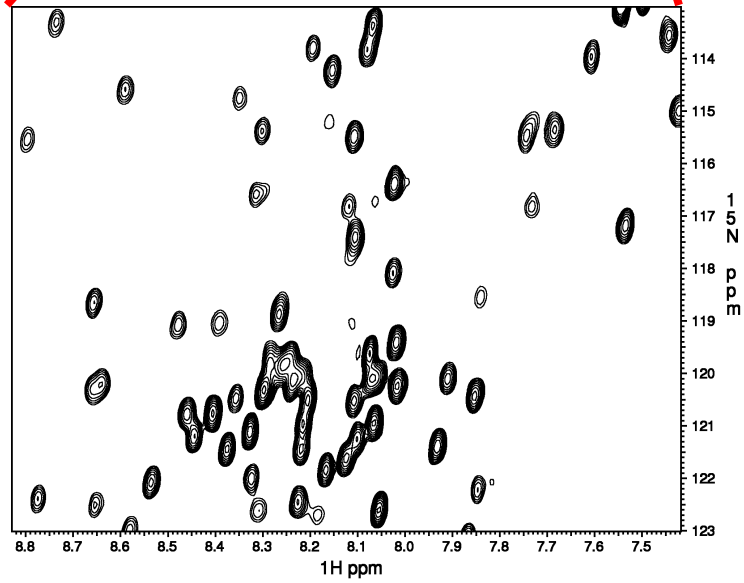
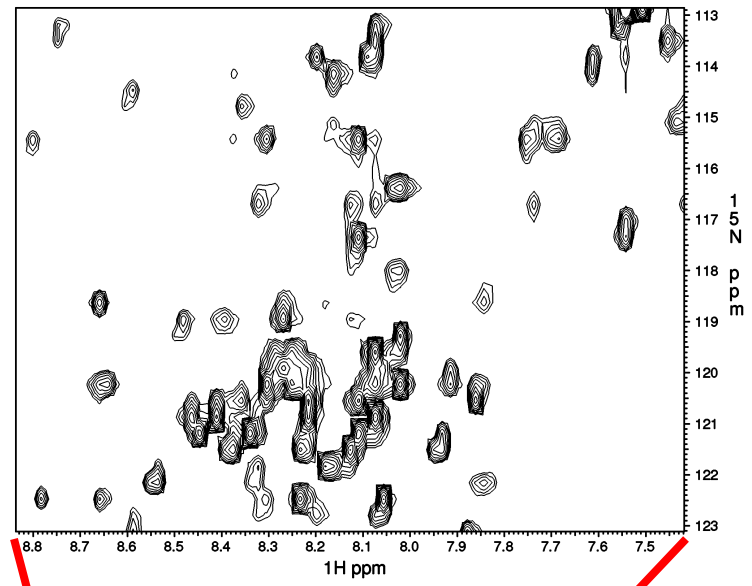
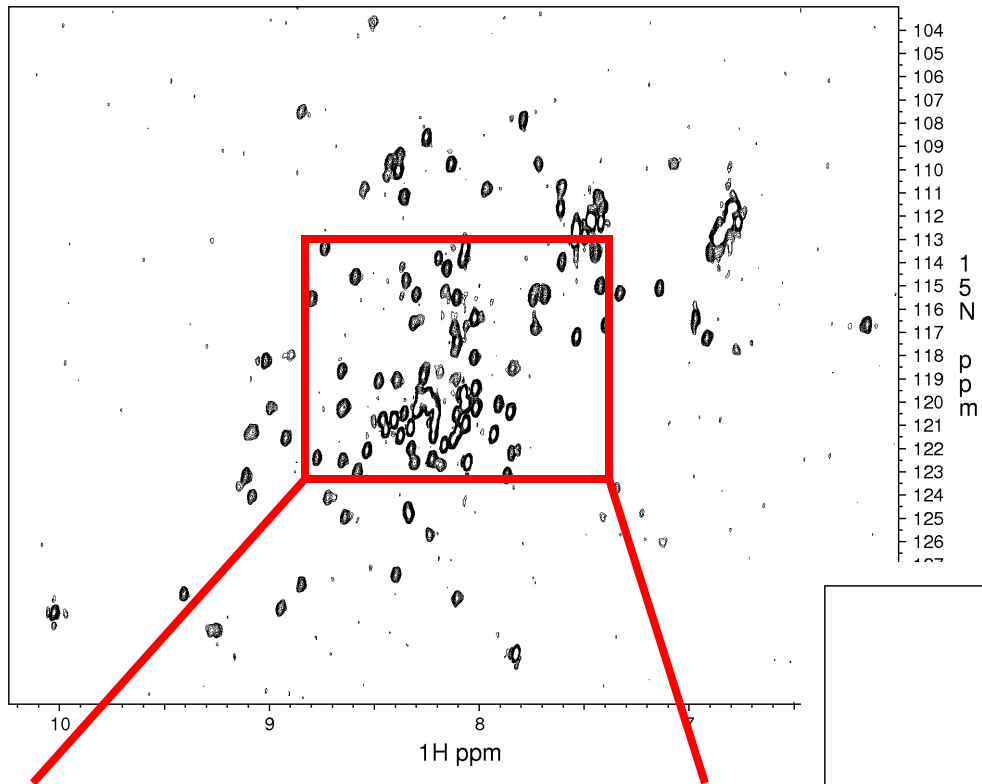
Linear prediction



NMR data processing - summary

- I) Solvent suppression
- II) Window function
- III) Zero-filling
- IV) FT
- V) Transpose (in case of multidimensional spectra)

```
|nmrPipe -fn POLY -time \  
|nmrPipe -fn SP -off 0.33 -end 0.98 -pow 2 -c 1.0 \  
|nmrPipe -fn ZF -size 2048 \  
|nmrPipe -fn FT -auto \  
|nmrPipe -fn PS -p0 -76.0 -p1 0.0 -ur \  
|nmrPipe -fn EXT -x1 11.0ppm -xn 6.0ppm -sw \  
|nmrPipe -fn POLY -ord 3 -auto \  
|nmrPipe -fn TP \  
F2
```



NMR as a tool for study **structure**, **dynamics** and **interactions** of biomolecules

- 1) Structure determination of NAs and proteins
- 2) **Protein – metal interaction**
- 3) **Protein – ligand interaction**

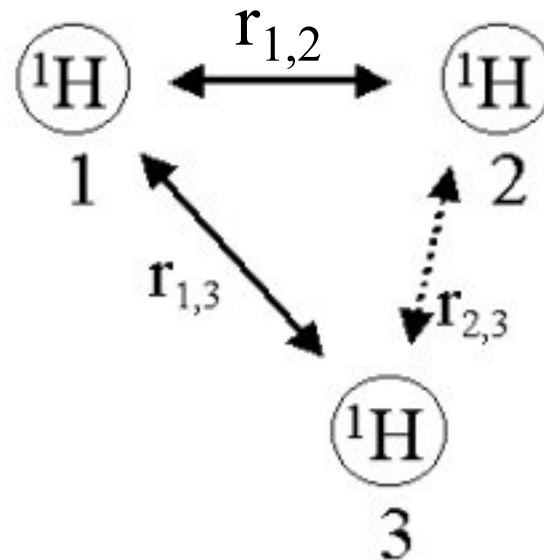
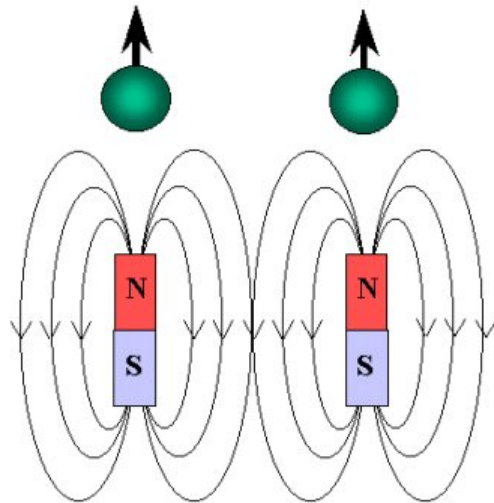
For most of the modern applications, enrichment by ^{13}C , ^{15}N and often ^2H needed!

Isotope	Ground state spin	Natural abundance [%]	Rel. Sensitivity
^1H	$\frac{1}{2}$	~100	$1.00 \times 10^{+0}$
^{13}C	$\frac{1}{2}$	1.10	1.59×10^{-2}
^{15}N	$\frac{1}{2}$	0.37	1.04×10^{-3}
^{19}F	$\frac{1}{2}$	100	8.30×10^{-1}
^{31}P	$\frac{1}{2}$	~100	6.63×10^{-2}
^{12}C	0	98.90	-
^{16}O	0	~100	-

NMR as a tool for study structure, dynamics and interactions of biomolecules

- 0) AA/NA sequence, resonance assignment, standard chemical shifts
- 1) Structure determination of proteins/NAs
- 2) NMR can provide detailed information about the structure at the atomic level resolution relying on the spatial proximity of two interacting protons – nuclear Overhauser enhancement (NOE)
- 3) Additional structural information can be obtained (residual dipolar couplings – RDCs, J -couplings, backbone chemical shifts - CSI)

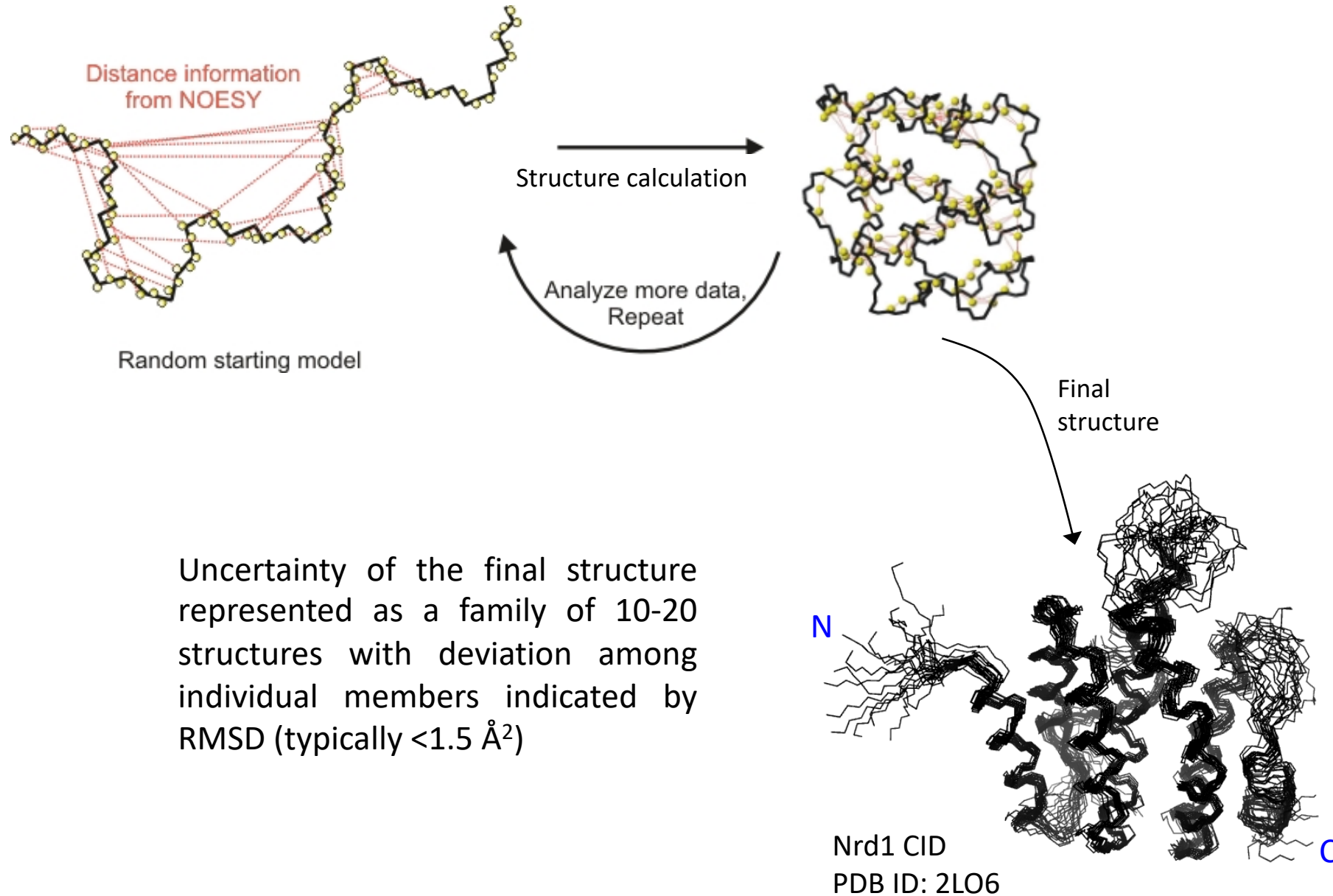
NOE:



$$r_{1,2}; r_{1,3}; r_{2,3} \leq 6 \text{ \AA}$$

$$1 \text{ \AA} = 1.10^{-10} \text{ m}$$

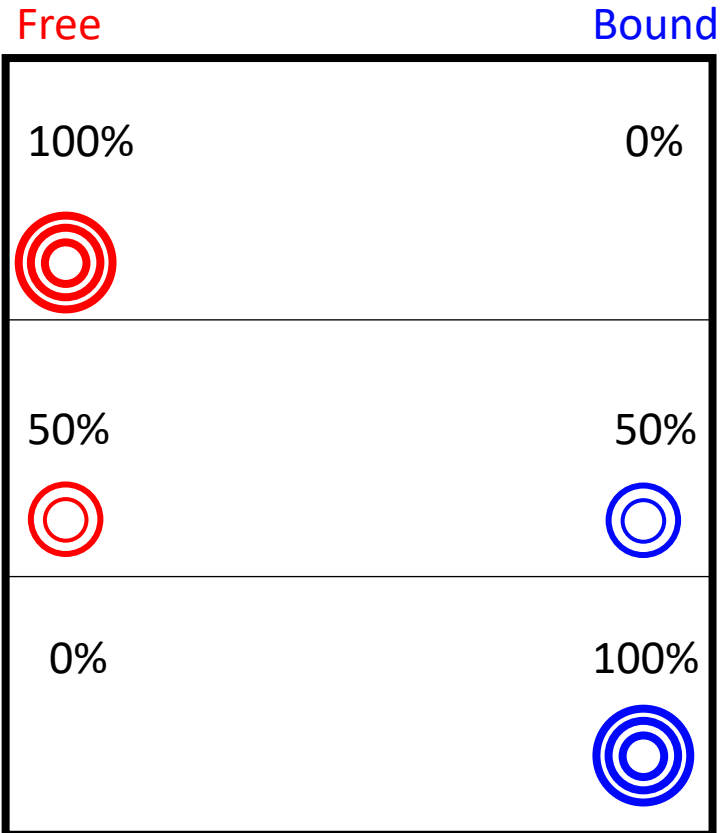
Iterative procedure of structure determination by NMR



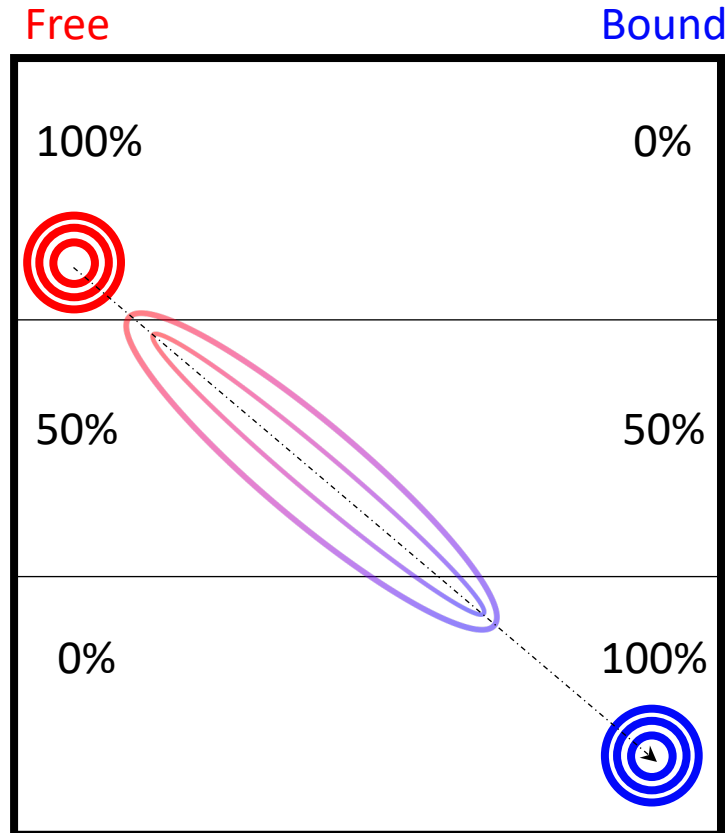
Studying interactions by NMR titration

- 1) **Slow** exch. regime (on the NMR timescale) – individual peaks for each of the studied states (e.g. free / complexed forms of a protein), peak intensity representing population of a given state
- 2) **Intermediate** exchange regime
- 3) **Fast** exchange regime – single peak whose chemical shift position is given by the molar ratio of the states present in solution

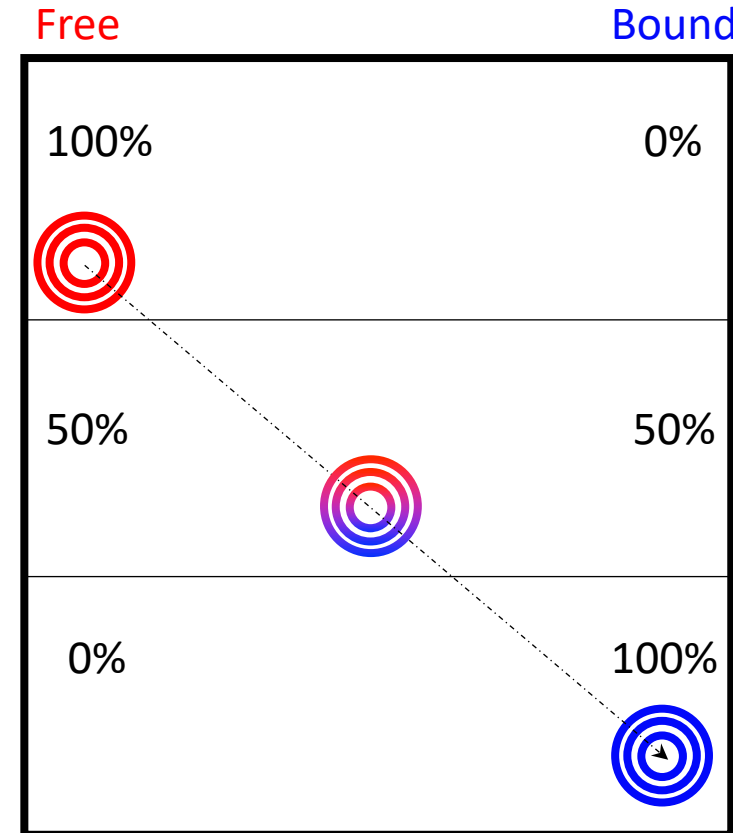
Slow ($K_D < 1 \mu\text{M}$)



Intermediate ($K_D \sim 1-10 \mu\text{M}$)

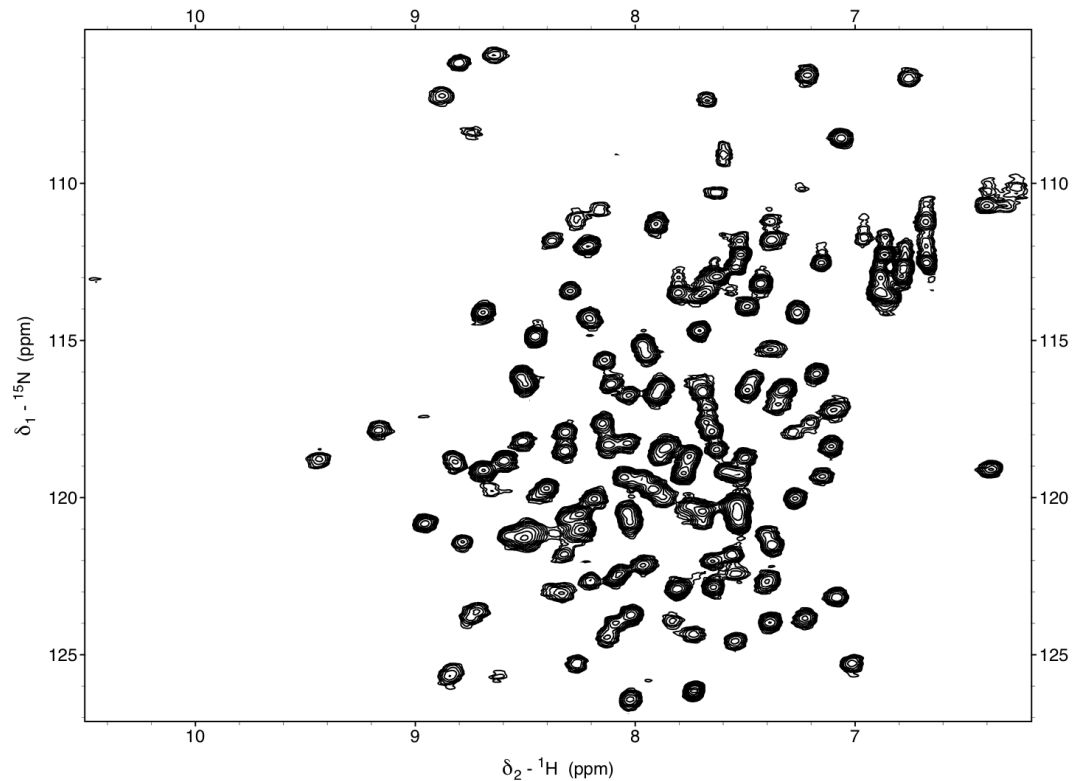
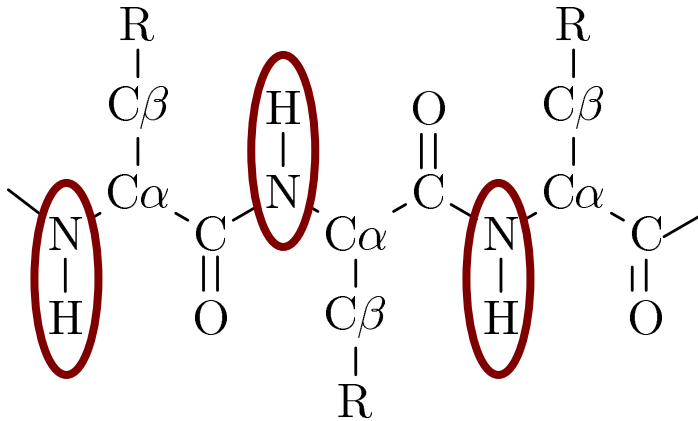


Fast exchange regime ($K_D > 10 \mu\text{M}$)



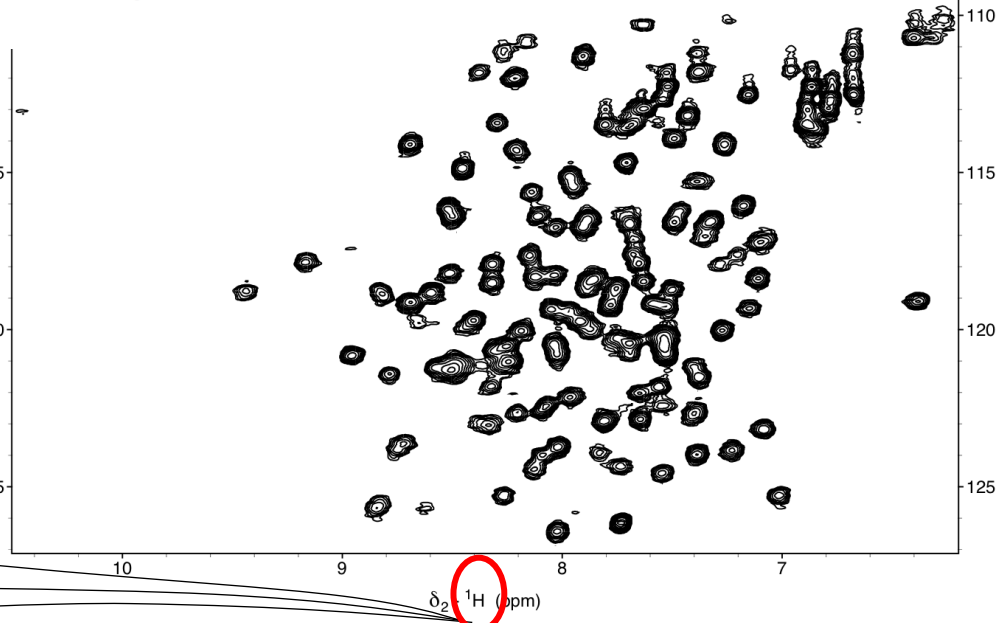
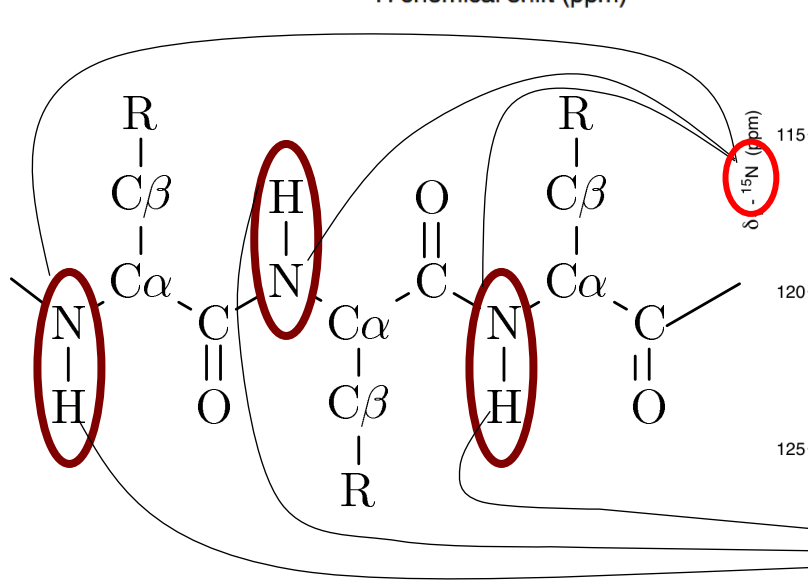
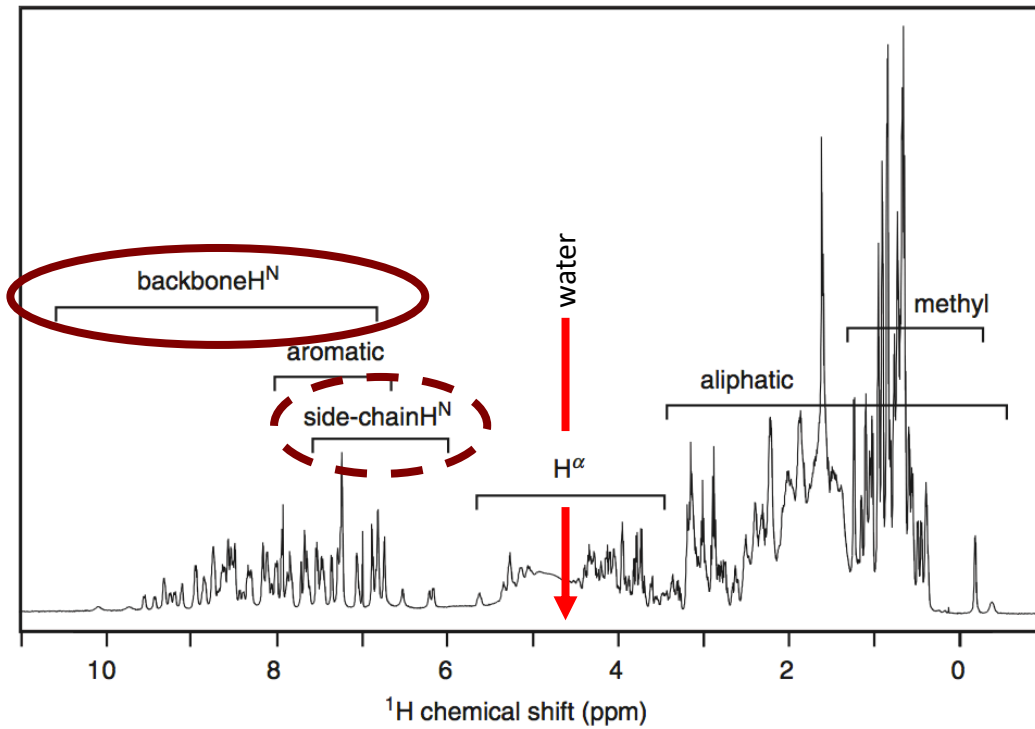
^{15}N - ^1H HSQC – Heteronuclear Single Quantum Coherence

- 1) 1 peak \cong 1 amino acid
- 2) good estimate of the protein folding status
- 3) no information about sequential assignment (which peak is which amino acid)
- 4) for sequential assignment third dimension needed (^{13}C)
- 5) once assignment of the peaks known – HSQC is optimal tool for monitoring interactions by NMR through titrations (i.e. stepwise addition of small amounts of ligand to the nearly constant volume solution with the isotopically enriched molecule)



^1H - ^{15}N HSQC, cca 155 aa, well folded, 600MHz, 293K

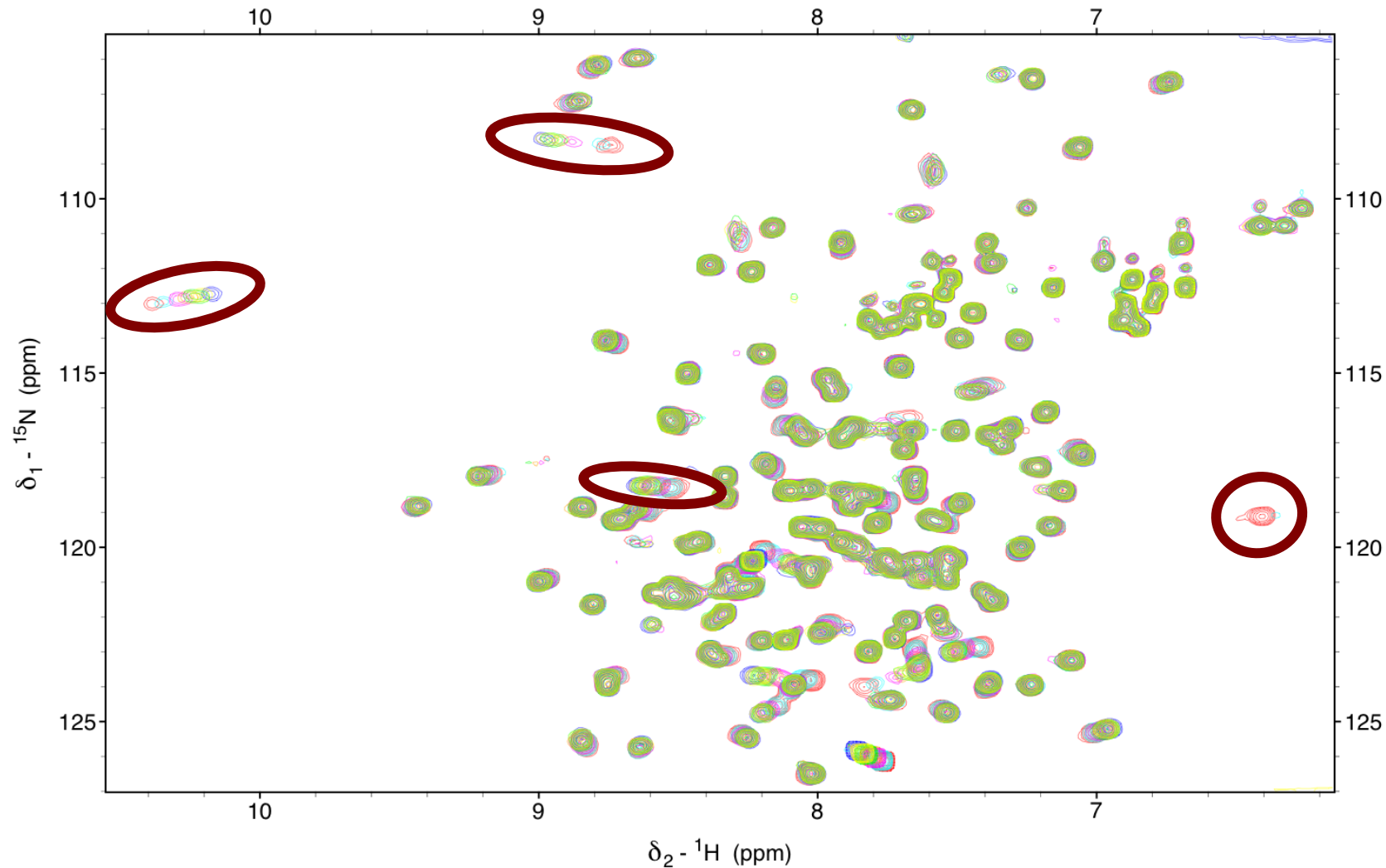
^1H 1D, Cavanagh et al., 2007



^1H - ^{15}N HSQC, cca 155 aa, well folded, 600MHz, 293K

Interaction of Nrd1-CID with C-terminal domain (CTD)

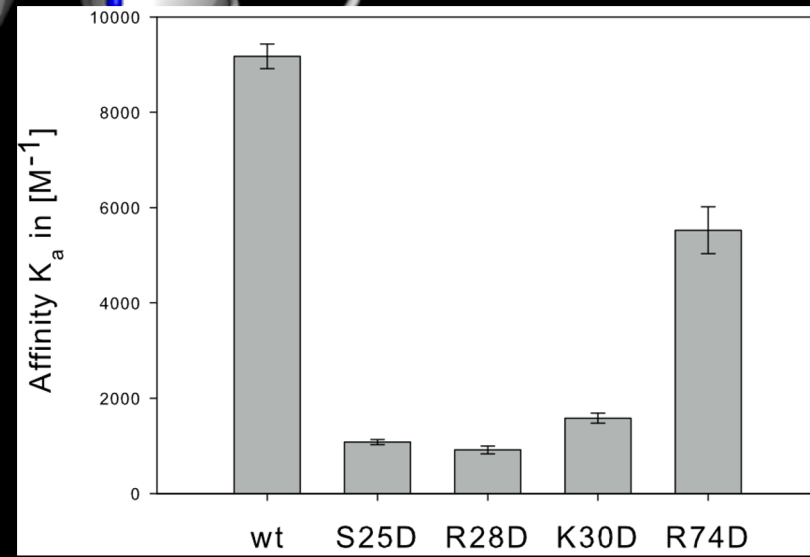
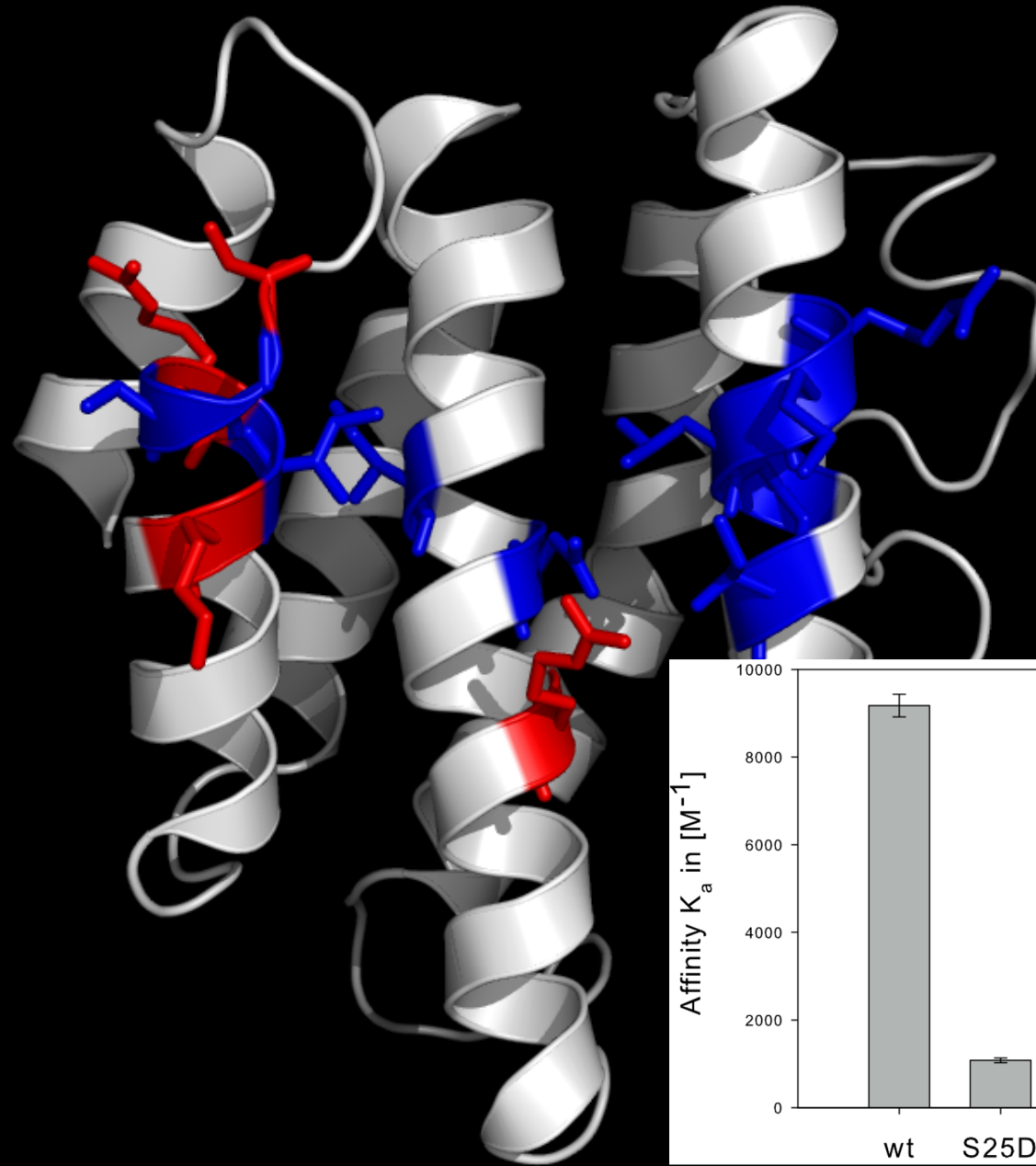
- NMR Titration
- ^{15}N enriched CID + unlabeled CTD-Ser5P in n -steps, $n=6$ in our case
 - peaks corresponding to the interacting residues of CID change their chemical shift (position in the spectrum)
 - => interaction surface, binding constant, stoichiometry



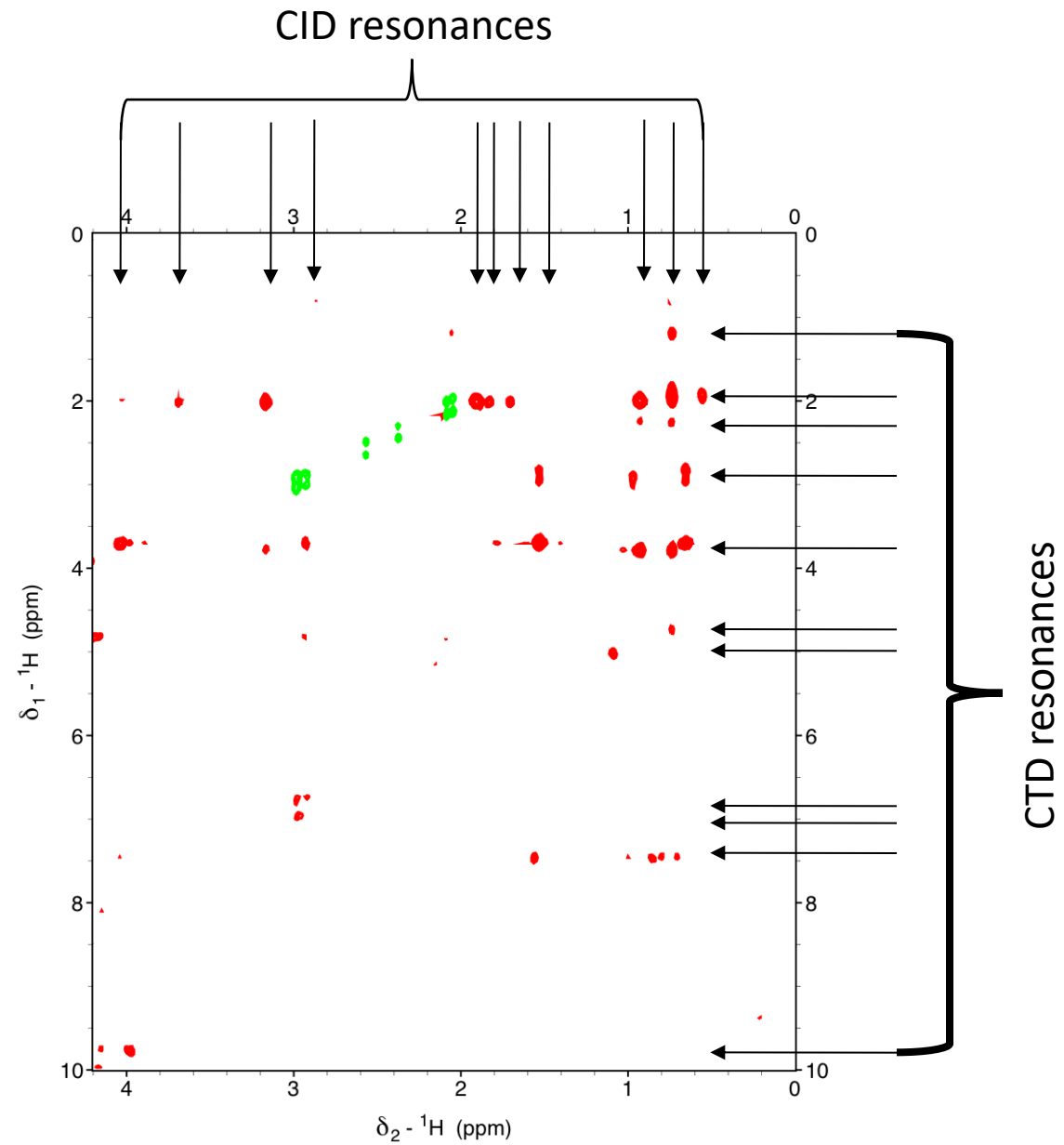
Nrd1 CID interaction surface — CID residues experiencing the largest chemical shift variations upon the interaction with 5-phospho-Ser CTD shown in blue with side-chains in stick representation



CTD-CID interaction with **mutants** studied by fluorescence anisotropy



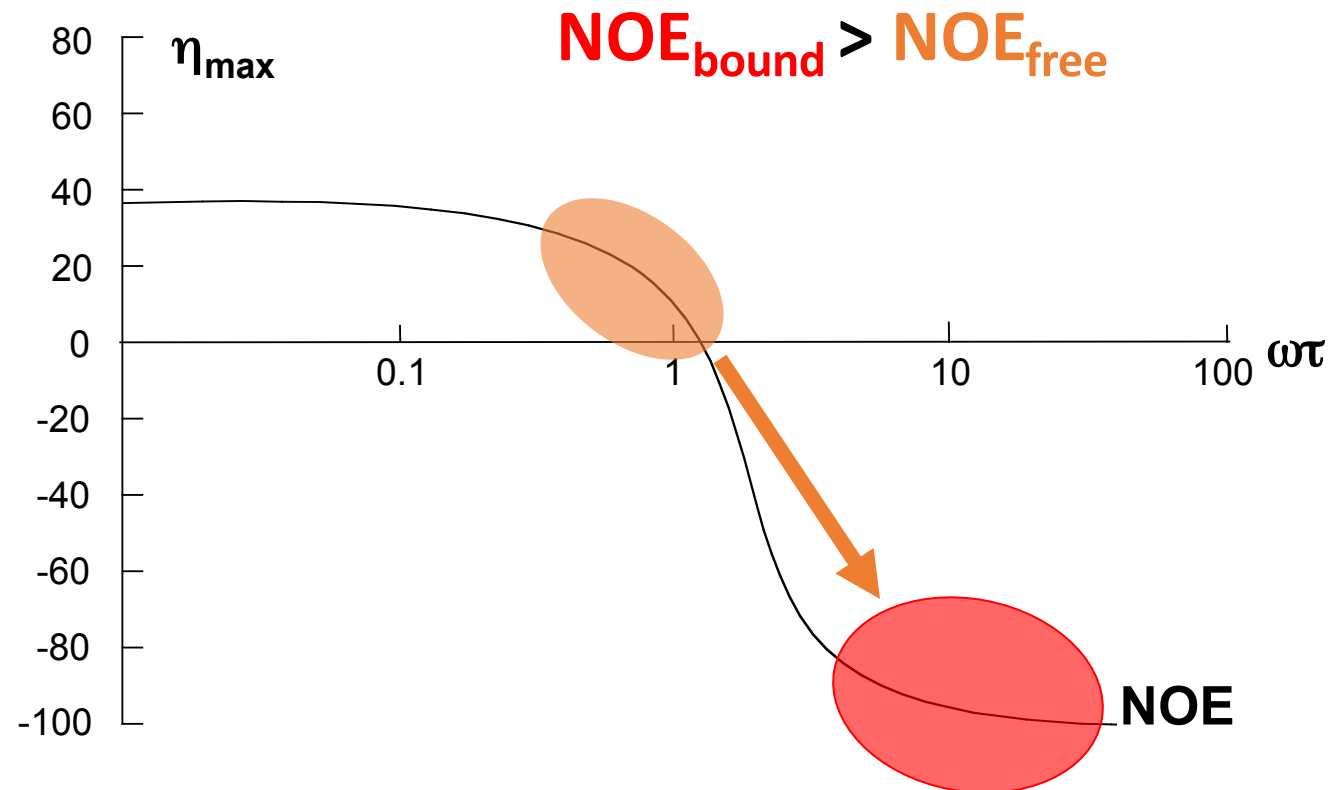
Interligand NOEs between CID and CTD – 900MHz, 150ms, 293K



Transferred-NOE

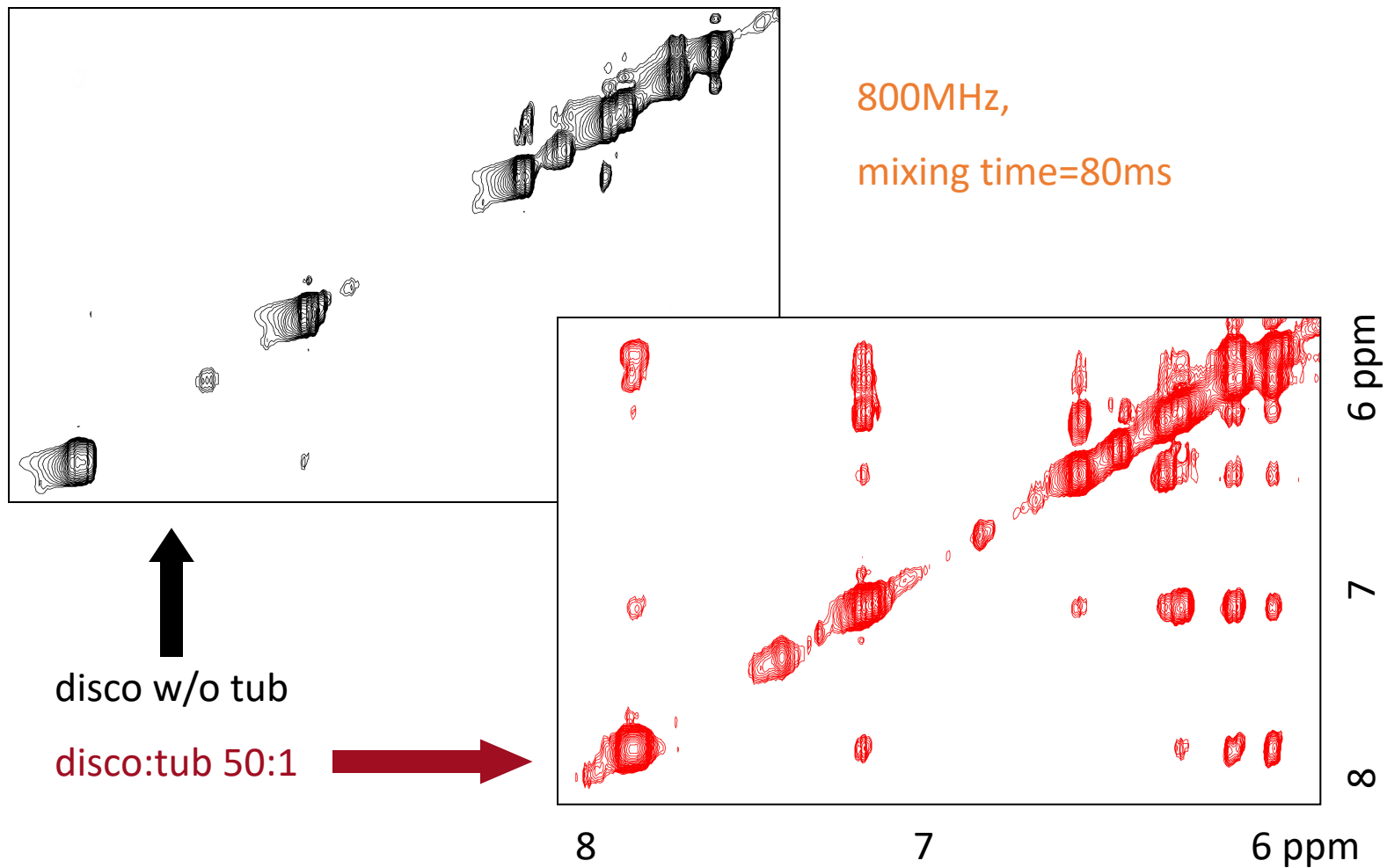
$$\text{NOE} = p_{\text{bound}} \cdot \text{NOE}_{\text{bound}} + p_{\text{free}} \cdot \text{NOE}_{\text{free}}$$

$$\tau_{c,\text{bound}} \gg \tau_{c,\text{free}} \quad (\text{and } p_{L,\text{free}} \gg p_{L,\text{bound}})$$

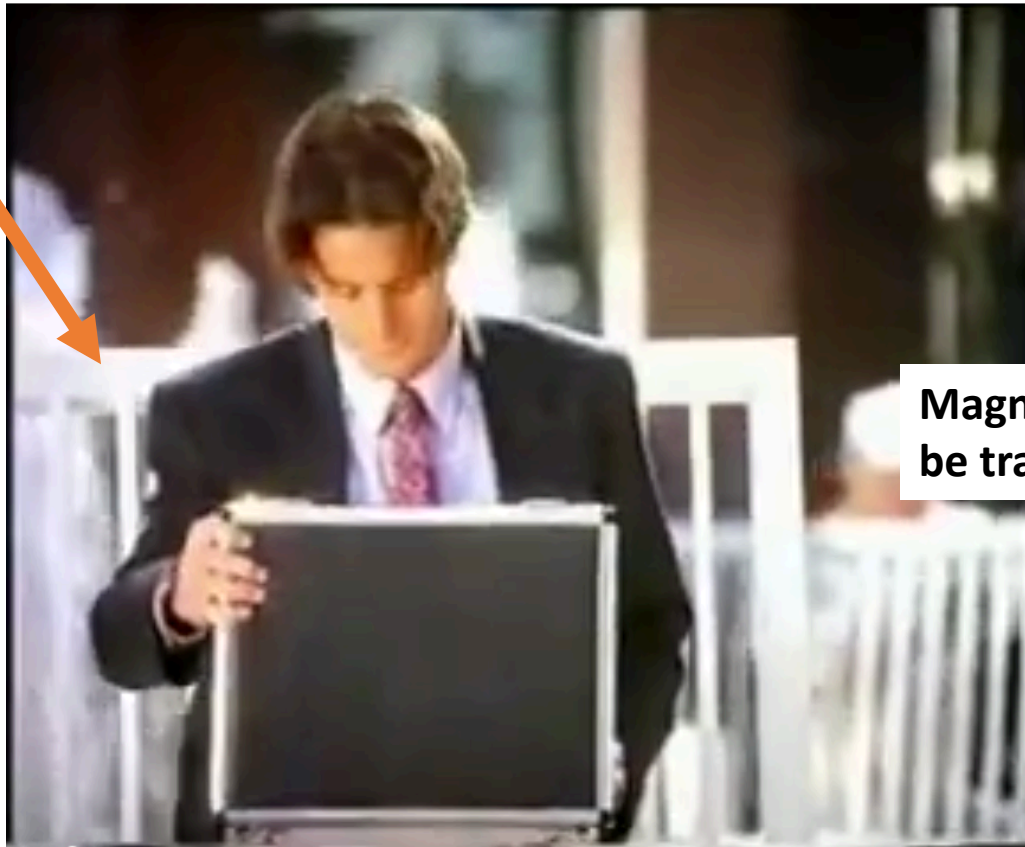


Transferred NOE Experiments

tr-NOESY ~600 μ M Discodermolide **without** and **with** ~12 μ M tubulin



protein



Magnetization to be transferred



ligand1



ligand2

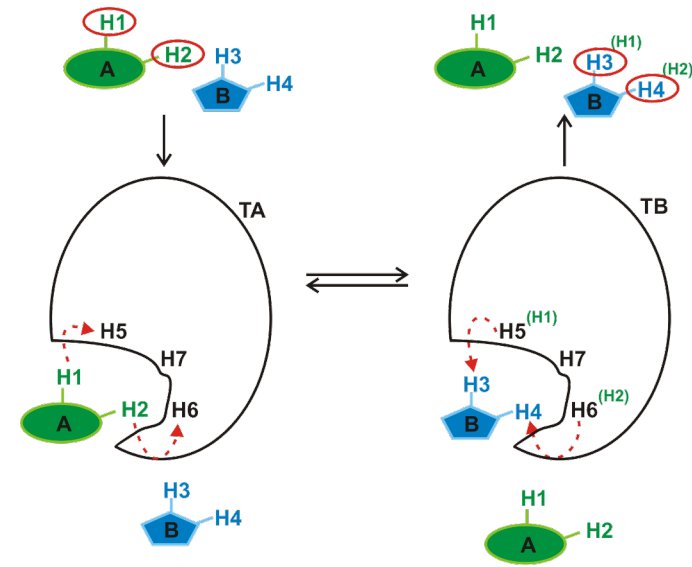


Transferred magnetization
Note the weak "signal"

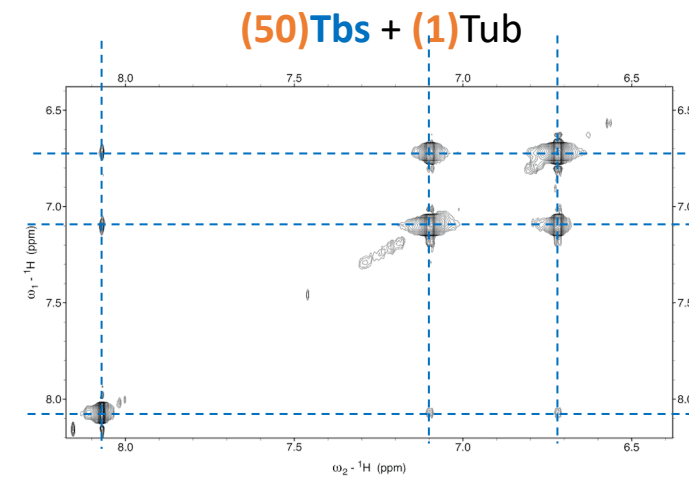
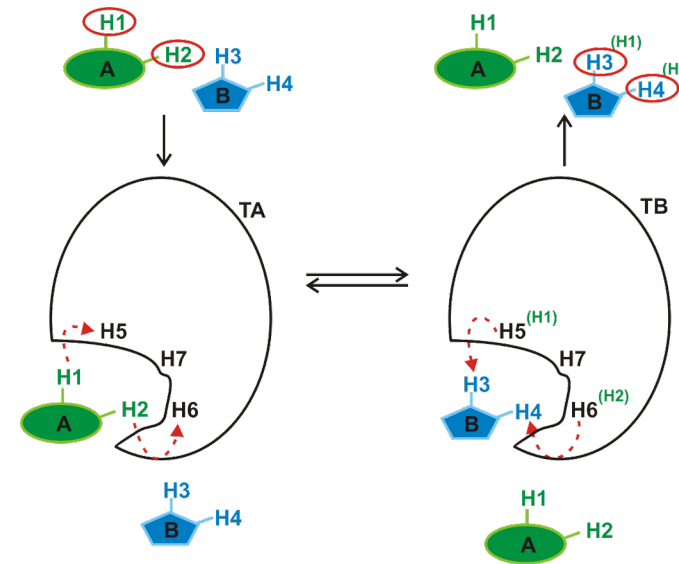
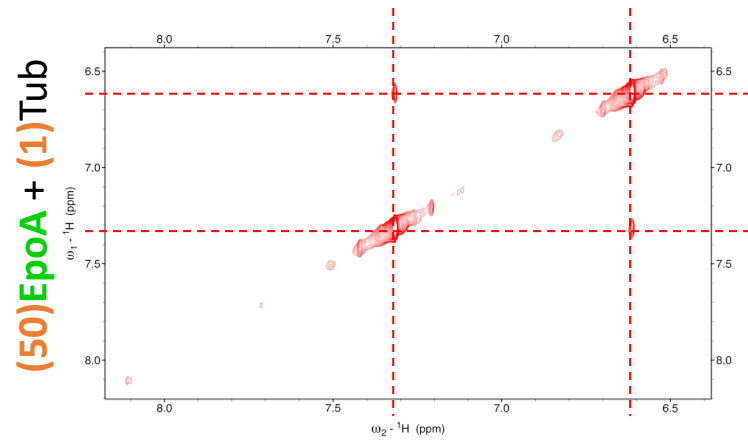


They "compete" for same place but never "meet"

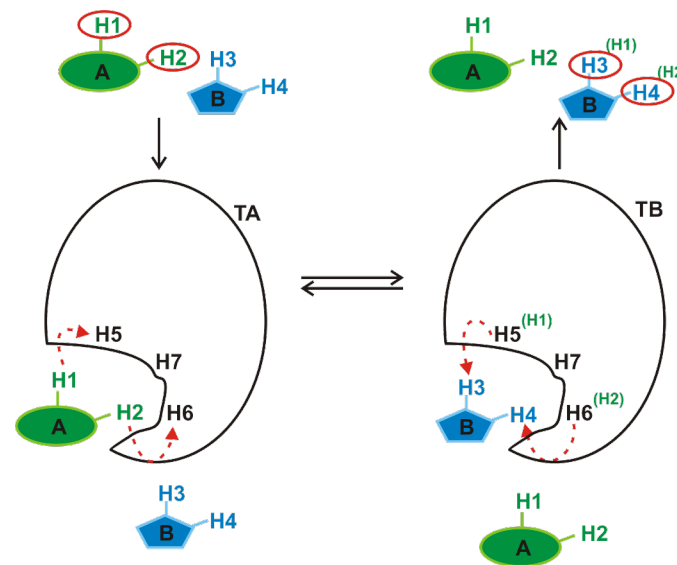
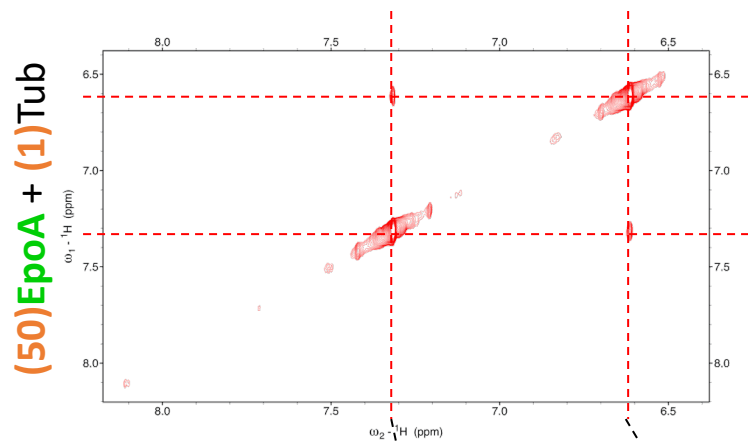
interligand NOE Experiments



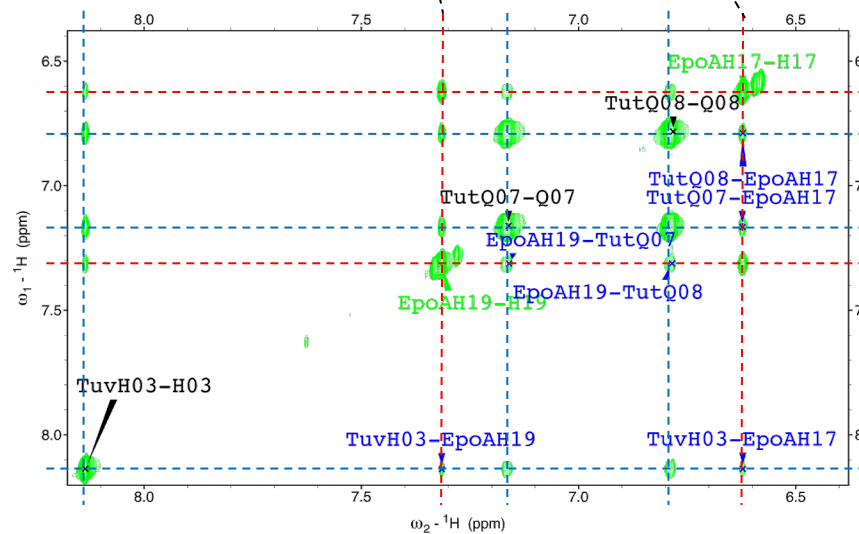
interligand NOE Experiments



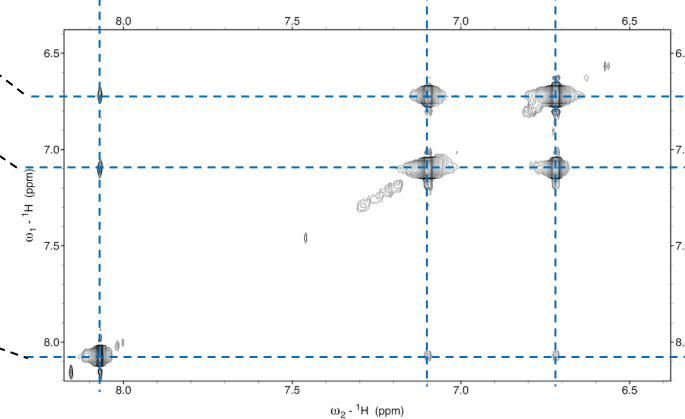
interligand NOE Experiments



(50)Tbs+(50)EpoA+(1)Tub

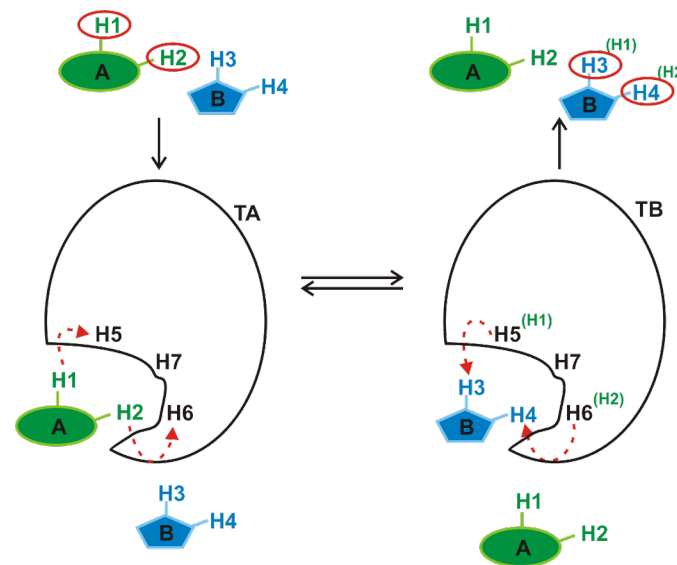
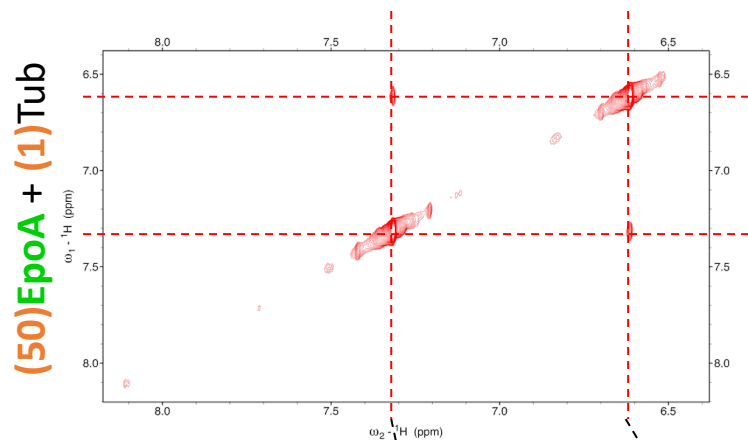


(50)Tbs + (1)Tub

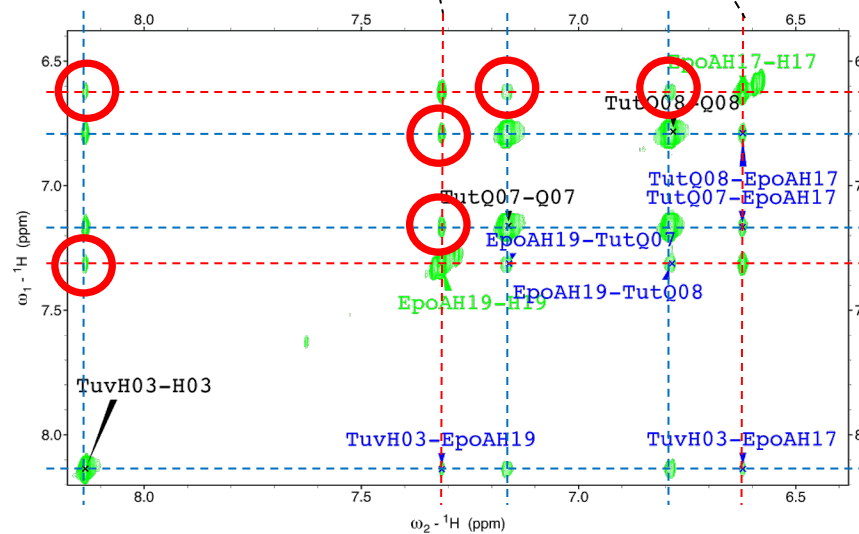


interligand x-peaks, 100-450ms, 900MHz

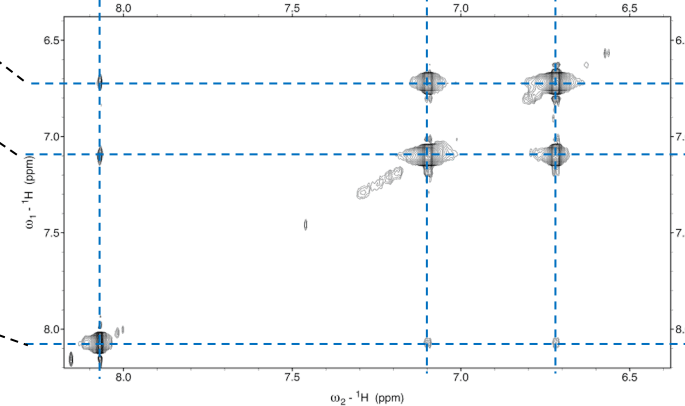
interligand NOE Experiments



(50)Tbs+(50)EpoA+(1)Tub



(50)Tbs + (1)Tub



interligand x-peaks, 100-450ms, 900MHz