

Kružnice

- Napište rovnici kružnice opsané trojúhelníku ABC: A[-1,3], B[0,2], C[1,-1].
- a) Napište rovnici tečny vedené ke kružnici $k: x^2 + y^2 + 8x + 2y - 8 = 0$ jejím bodem M[0,2].
b) Určete vzájemnou polohu kružnice k a obou os souřadnic. Určete všechny průsečíky.

Řeš.:.

1.

$$\begin{array}{l} \text{k: } x^2 + y^2 + Ax + By + C = 0 \\ A \in k \quad \dots \quad 1 + 9 - A + 3B + C = 0 \\ B \in k \quad \dots \quad 0 + 4 \quad + 2B + C = 0 \\ C \in k \quad \dots \quad 1 + 1 + A - B + C = 0 \\ \hline 1) \quad \quad \quad A - B + C = -2 \\ 2) \quad \quad \quad 2B + C = -4 \\ 3) \quad \quad \quad -A + 3B + C = -10 \\ \hline 1) \quad \quad \quad A - B + C = -2 \\ 2) \quad \quad \quad 2B + C = -4 \\ 1) + 3) \quad \quad \quad 2B + 2C = -12 \\ \hline 1) \quad \quad \quad A - B + C = -2 \\ 2) \quad \quad \quad 2B + C = -4 \\ 1) + 3) - 2) \quad \quad \quad C = -8 \rightarrow B = 2 \rightarrow A = 8 \\ \hline \end{array}$$

1

2.

$$k : x^2 + y^2 + 8x + 2y - 8 = 0$$

2. a)

$$\begin{aligned} k &: x^2 + y^2 + 8x + 2y - 8 = 0 \\ k &: (x^2 + 8x + 16) + (y^2 + 2y + 1) = 8 + 16 + 1 \\ k &: (x + 4)^2 + (y + 1)^2 = 25 \end{aligned}$$

2

$$\begin{aligned} t: (x_0 + 4).(x + 4) + (y_0 + 1).(y + 1) &= 25 \\ M[0; 2] \in t \dots (0 + 4).(x + 4) + (2 + 1).(y + 1) &= 25 \\ 4.(x + 4) + 3.(y + 1) &= 25 \\ t: 4x + 3y - 6 &= 0 \end{aligned}$$

2

b)

$$\begin{aligned} P_x - ? \quad y = 0 \quad \dots \quad x^2 + 8x - 8 = 0 \\ x_{1,2} = \frac{-8 \pm \sqrt{64+32}}{2} = \frac{-8 \pm \sqrt{96}}{2} = \frac{-8 \pm 4\sqrt{6}}{2} = -4 \pm 2\sqrt{6} \\ P_{x1}[-4-2\sqrt{6}; 0], \quad P_{x2}[-4+2\sqrt{6}; 0] \end{aligned}$$

2

$$\begin{aligned} P_y - ? \quad x = 0 \quad \dots \quad y^2 + 2y - 8 = 0 \\ (y + 4).(y - 2) = 0 \\ P_{y1}[0; -4] \quad P_{y2}[0; 2] \end{aligned}$$

1

Známka:	10 – 9 bodů	1
	8 bodů	2
	7 – 5 bodů	3
	4 – 3 body	4