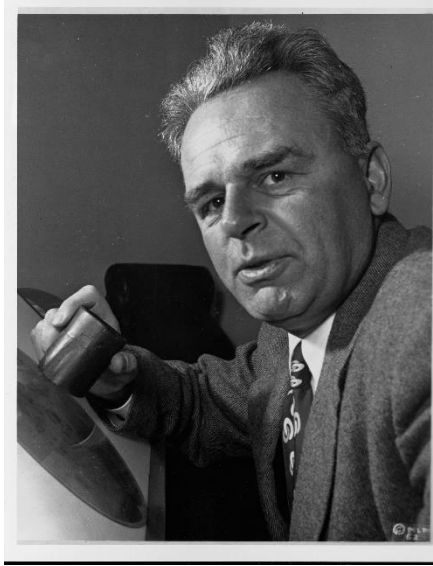


# Astronomers



**Walter Baade (1893 – 1960)**



**Bart Bok (1906 – 1983)**



**James Jeans (1877 – 1946)**

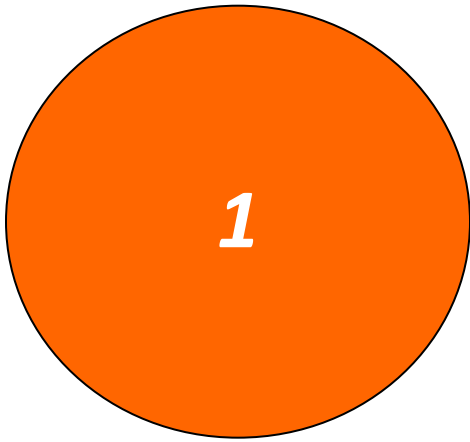


**Ejnar Hertzsprung (1873 – 1967)**



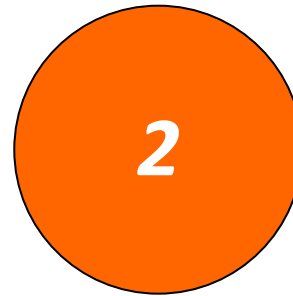
**Henry Russell (1877 – 1957)**

# Luminosity versus radius and temperature



$$R = 2 R_{\odot}$$

$$T = T_{\odot}$$

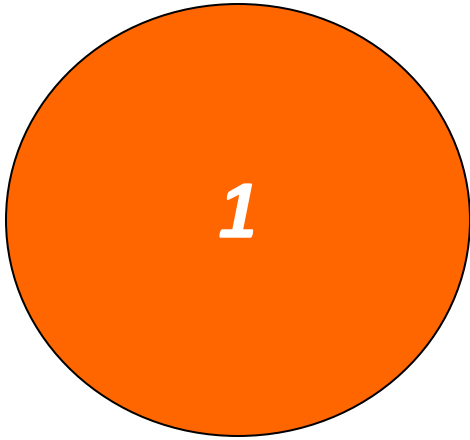


$$R = R_{\odot}$$

$$T = T_{\odot}$$

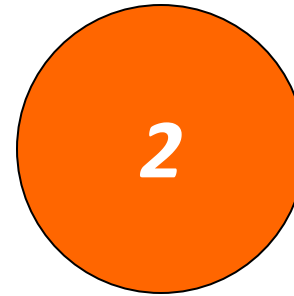
Which star is more luminous?

# Luminosity versus radius and temperature



$$R = 2 R_{\odot}$$

$$T = T_{\odot}$$

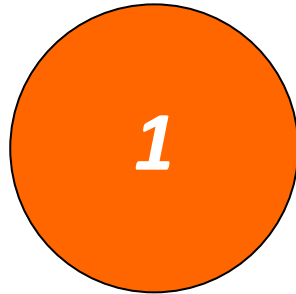


$$R = R_{\odot}$$

$$T = T_{\odot}$$

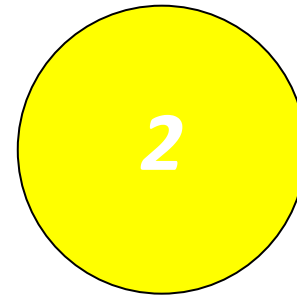
- Each  $\text{cm}^2$  of each surface emits the same amount of radiation.
- The larger star emits more radiation because it has a larger surface. It emits 4 times as much radiation.

# Luminosity versus radius and temperature



$$R = R_{\odot}$$

$$T = T_{\odot}$$

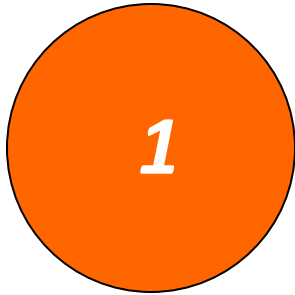


$$R = R_{\odot}$$

$$T = 2 T_{\odot}$$

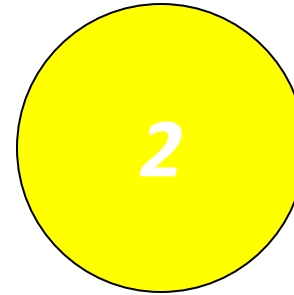
Which star is more luminous?

# Luminosity versus radius and temperature



$$R = 2 R_{\odot}$$

$$T = T_{\odot}$$



$$R = R_{\odot}$$

$$T = 2 T_{\odot}$$

Which star is more luminous?

The hotter star is more luminous.

Luminosity varies as  $T^4$  (Stefan-Boltzmann Law)

# Luminosity Law

$$L \propto R^2 T^4$$

*Luminosity*  $\propto$  *surface area*  $\propto$  (*Radius*)<sup>2</sup>

*Luminosity*  $\propto$  (*Temperature*)<sup>4</sup>

If star A is 2 times as hot as star B, and the same radius, then it will be  $2^4 = 16$  times as luminous.

# Where do stars form?

- Bok globules for low mass stars



Rosette Nebula

Characteristics of  
the Globules:

$$r < 1 \text{ pc}$$

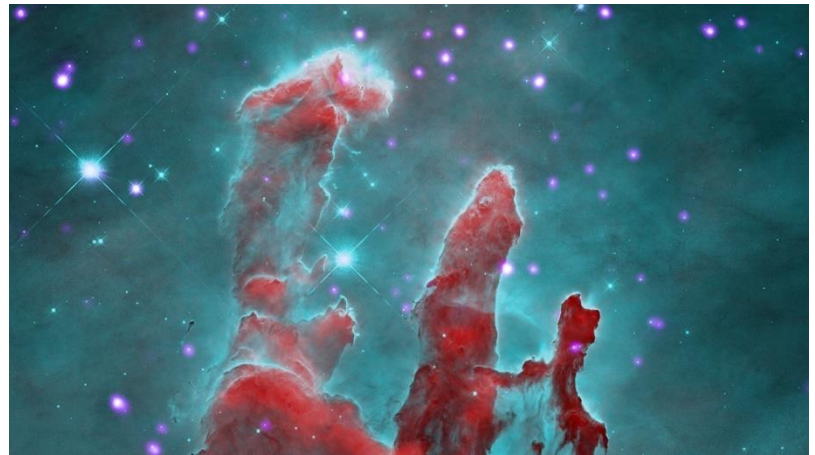
$$M < 1000 M_{\odot}$$

$$T \approx 10 \text{ K}$$



# Where do stars form?

- Giant Molecular Clouds (GMC)



Characteristics of GMCs:

$10 < r < 100$  pc

$M$  up to a few  $10^6 M_{\odot}$

$T \approx 10$  K



# Jeans Length - When does Gravity win?

- $N$  molecules of mass  $m$  in a box of size  $L$  (do not confuse with the luminosity) at temperature  $T$
- Gravitational Energy:  $E_G \sim -\frac{G M^2}{L}$
- Thermal Energy:  $E_T \sim N k T$
- Total mass:  $M = N m \sim L^3 \rho$
- Ratio:  $\frac{E_G}{E_T} \sim \frac{G M^2}{L N k T} \sim \frac{G (\rho L^3) m}{L k T} = \left(\frac{L}{L_J}\right)^2$
- Jeans Length:  $L_J \sim \sqrt{\frac{k T}{G \rho m}}$
- Gravity wins when  $L > L_J$

# Jeans Mass

- Jeans Length:  $L_J \sim \sqrt{\frac{k T}{G \rho m}}$
- Jeans Mass:  $M_J = L_J^3 \rho = \rho \left(\frac{k T}{G \rho m}\right)^{3/2} \propto T^{3/2} \rho^{-1/2}$
- Lowest Jeans Mass for cool and dense clouds

# The first stage

- Gravity tries to pull material in < = > Pressure tries to push it out
- Time to collapse = free fall time  $t_G$
- Gravitational acceleration:  $g \sim \frac{G M}{L^2} \sim \frac{L}{t_G^2}$
- Time to collapse:  $t_G \sim \sqrt{\frac{L}{g}} \sim \sqrt{\frac{L^3}{G M}} \sim \frac{1}{\sqrt{G \rho}}$
- Note:
  - Denser regions collapse faster
  - Independent of the size

# The first stage

- Pressure waves travel at the sound speed  $c_S$
- For ideal gas:  $c_S \sim \sqrt{\frac{P}{\rho}} \sim \sqrt{\frac{k T}{m}}$
- Sound crossing time:  $t_S \sim \frac{L}{c_S} \sim L \sqrt{\frac{m}{k T}}$
- Note: faster for smaller and hotter regions

# The first stage

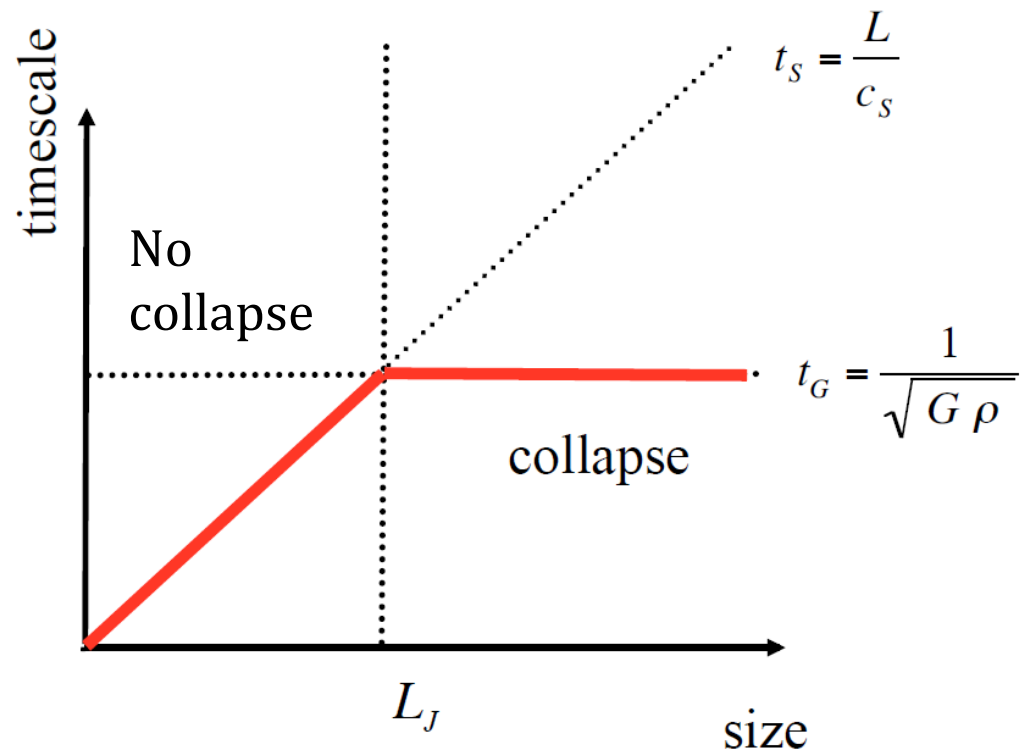
- Ratio of time scales:

$$\frac{t_S}{t_G} \sim \frac{L \sqrt{G \rho}}{c_S} \sim L \sqrt{\frac{G \rho m}{k T}} \sim \frac{L}{L_J}$$

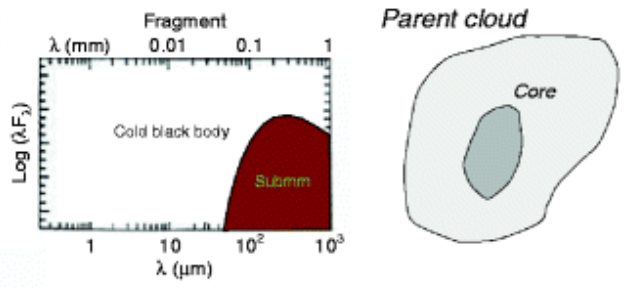
- Jeans Length:

$$L_J \sim \frac{c_S}{\sqrt{G \rho}}$$

- Larger clouds are more likely to collapse



Pre-stellar phase

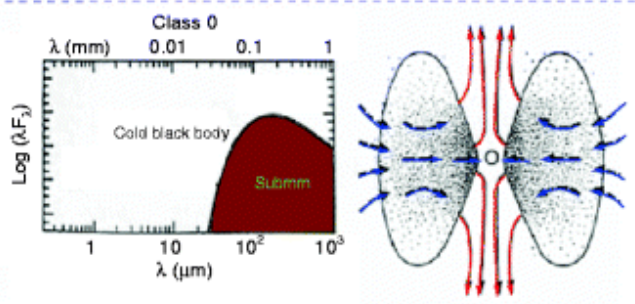


Pre-stellar dense core  
 $T_{bol} \sim 10-20$  K,  $M_{*} = 0$

-1,000,000 yr

Formation of the central protostellar object

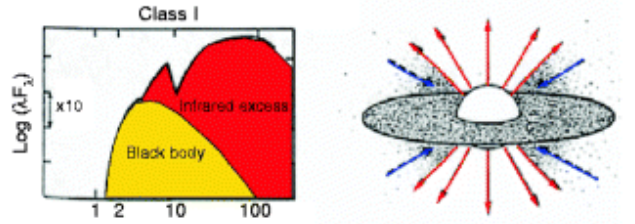
Protostellar phase



t ~ 0 yr  
 Young accreting protostar  
 $T_{bol} < 70$  K,  $M_{*} \ll M_{env}$

< 30,000 yr

Condensation of in-falling molecular gas  
 Hydrostatic low-luminosity proto-stellar object



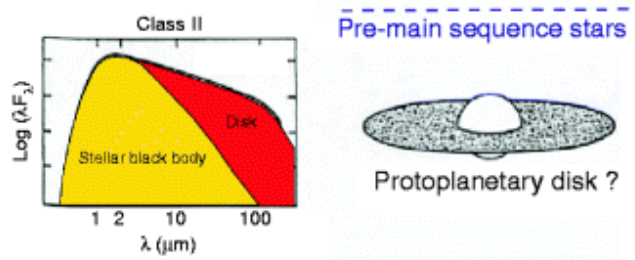
Evolved accreting protostar  
 $T_{bol} \sim 70-650$  K,  $M_{*} > M_{env}$

~ 200,000 yr

Protostar still enshrouded by optically thick material. Emission from thermal winds/jets ionized by neutral winds impacting the ambient medium

Birthline for Pre-main sequence stars

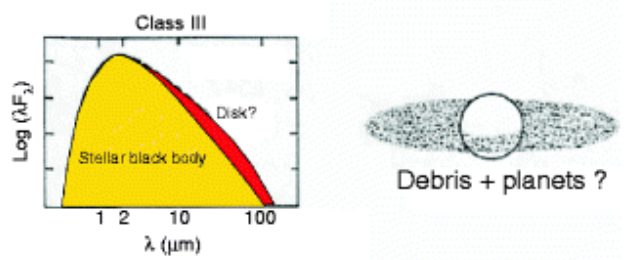
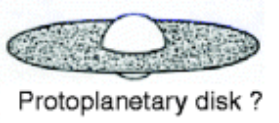
Pre-main sequence phase



Classical T Tauri star  
 $T_{bol} \sim 650-2880$  K,  $M_{Disk} \sim 0.01 M_{\odot}$

~ 1,000,000 yr

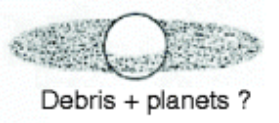
Optical emission starts to come out along with an outflow and wind



Weak T Tauri star  
 $T_{bol} > 2880$  K,  $M_{Disk} < M_{Jupiter}$

~ 10,000 000 yr

The star approaches the main sequence. Accretion substantially halted, protoplanetary disks may be present.

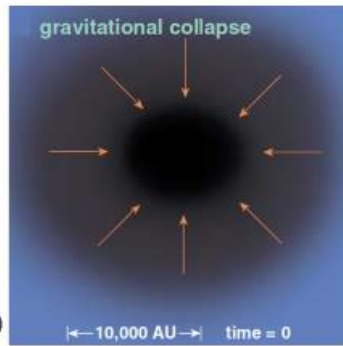
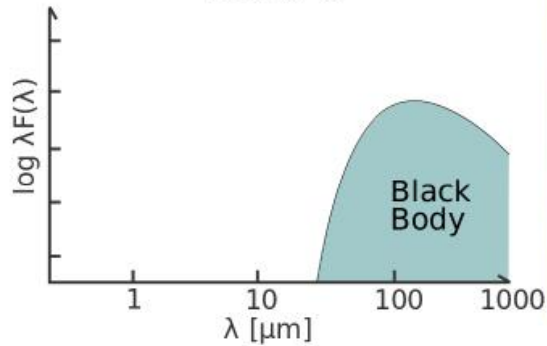


Time



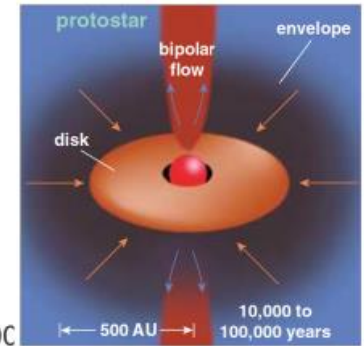
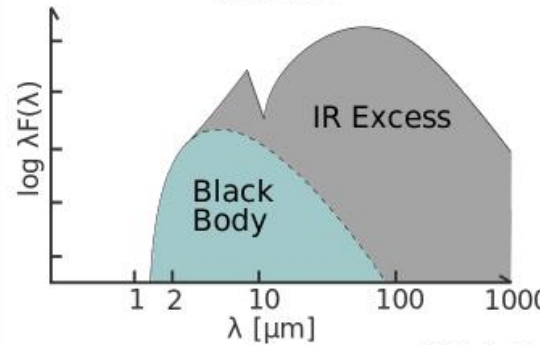
# Protostars evolve into main-sequence stars

### Class 0



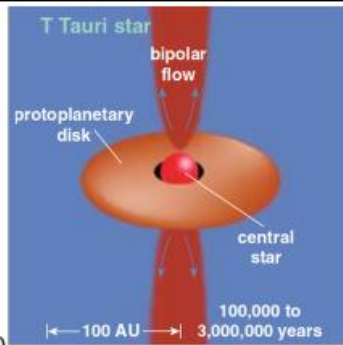
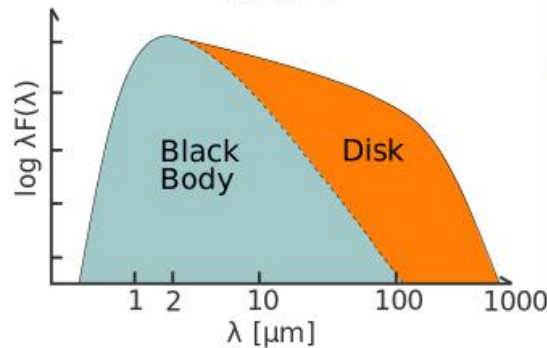
**Faint protostar deeply embedded**

### Class I



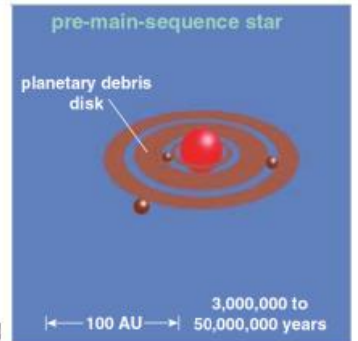
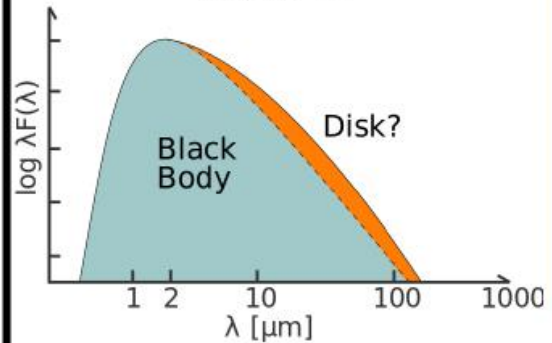
**Protostar with infalling envelop**

### Class II



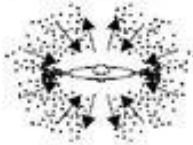
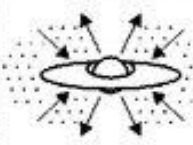
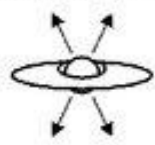
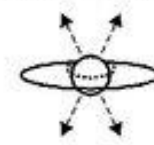

**Pre main sequence with thick disk**

### Class III

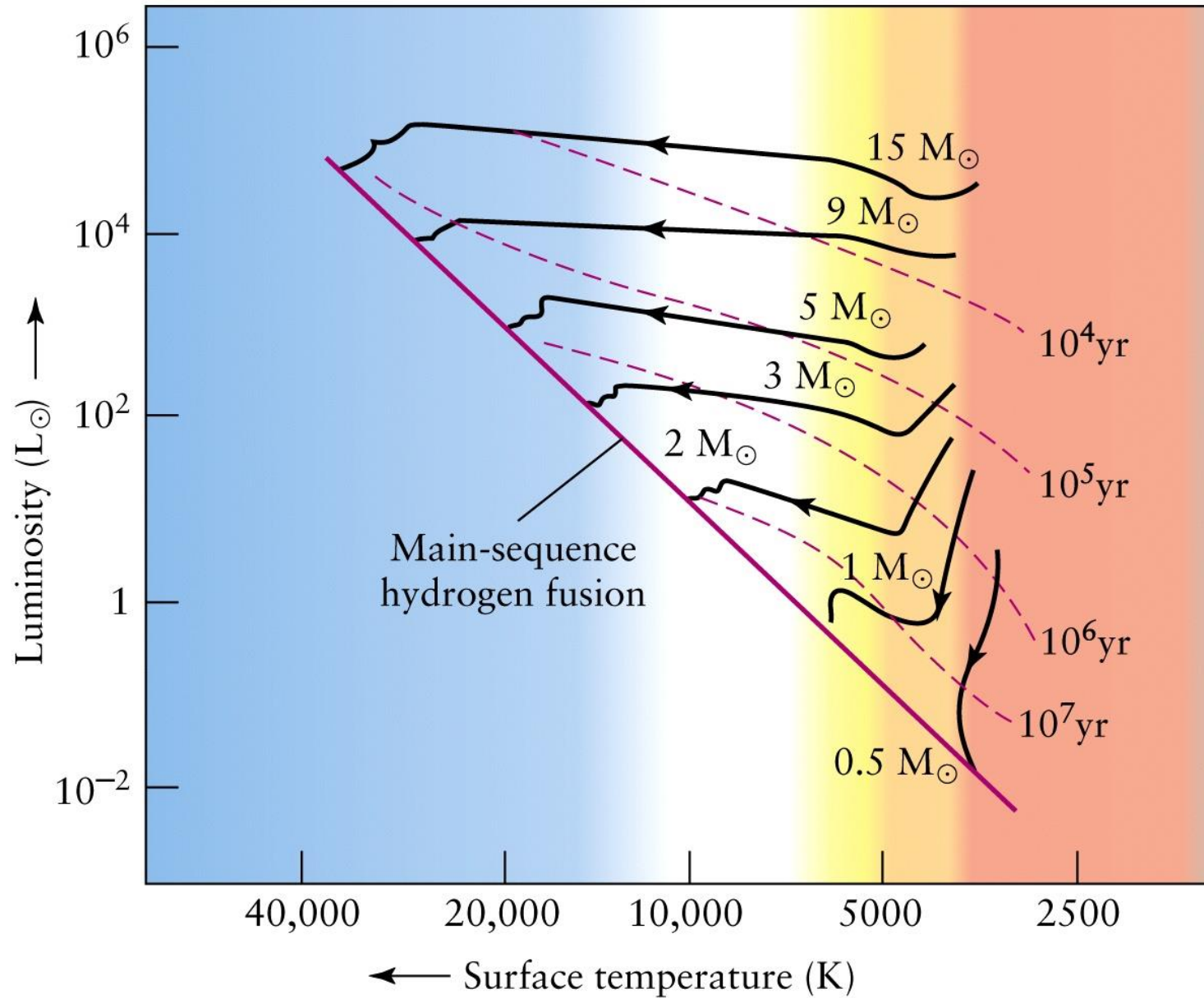


**Diskless pre main sequence**

# Protostars evolve into main-sequence stars

PROPERTIES	<i>Infalling Protostar</i>	<i>Evolved Protostar</i>	<i>Classical T Tauri Star</i>	<i>Weak-lined T Tauri Star</i>	<i>Main Sequence Star</i>
SKETCH					
AGE (YEARS)	$10^4$	$10^5$	$10^6 - 10^7$	$10^6 - 10^7$	$> 10^7$
mm/INFRARED CLASS	Class 0	Class I	Class II	Class III	(Class III)
DISK	Yes	Thick	Thick	Thin or Non-existent	Possible Planetary System
X-RAY	?	Yes	Strong	Strong	Weak
THERMAL RADIO	Yes	Yes	Yes	No	No
NON-THERMAL RADIO	No	Yes	No ?	Yes	Yes

# Protostars evolve into main-sequence stars



# Protostars evolve into main-sequence stars

