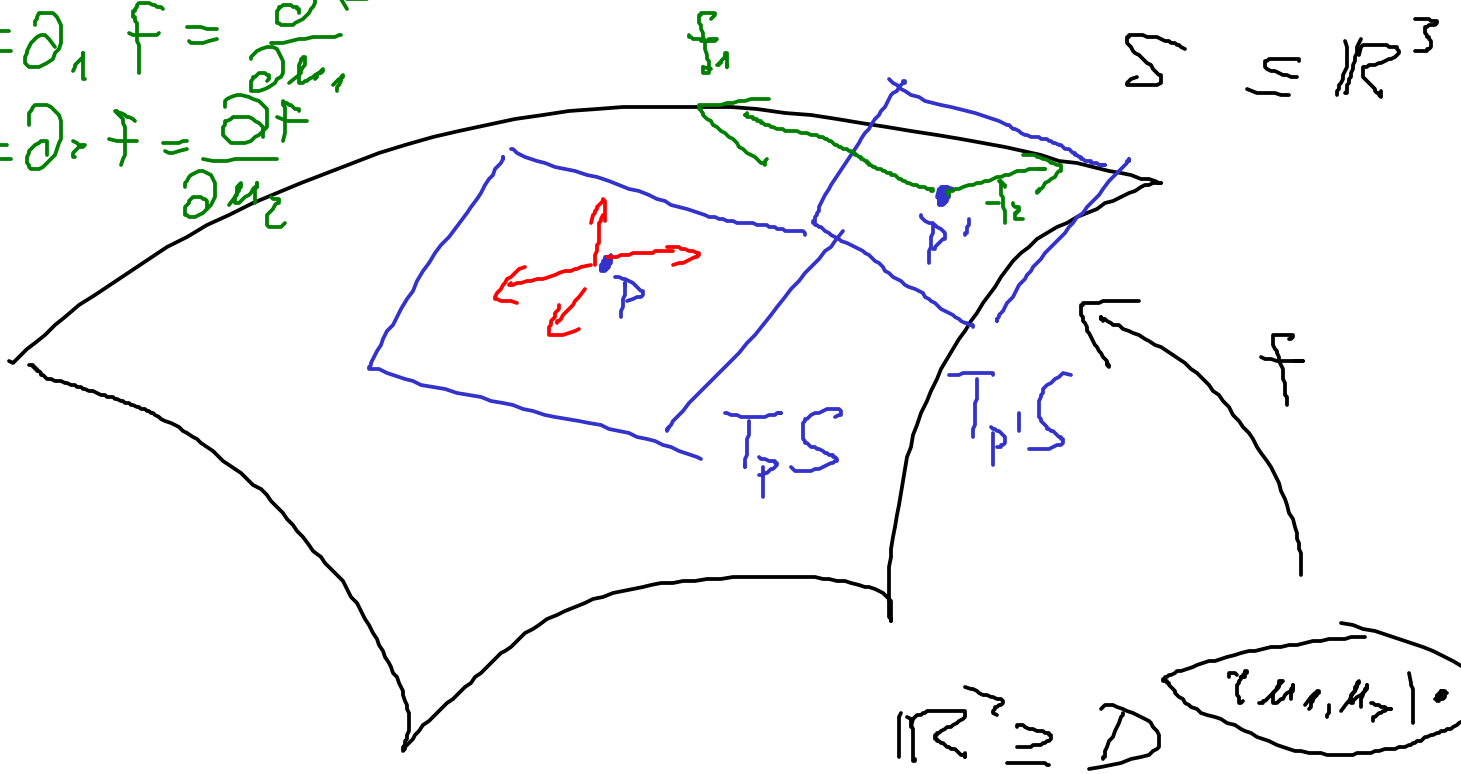


$$f_1 = \partial_1 f = \frac{\partial f}{\partial u_1}$$

$$f_2 = \partial_2 f = \frac{\partial f}{\partial u_2}$$



(1) skalární součin ve \mathbb{R}^3

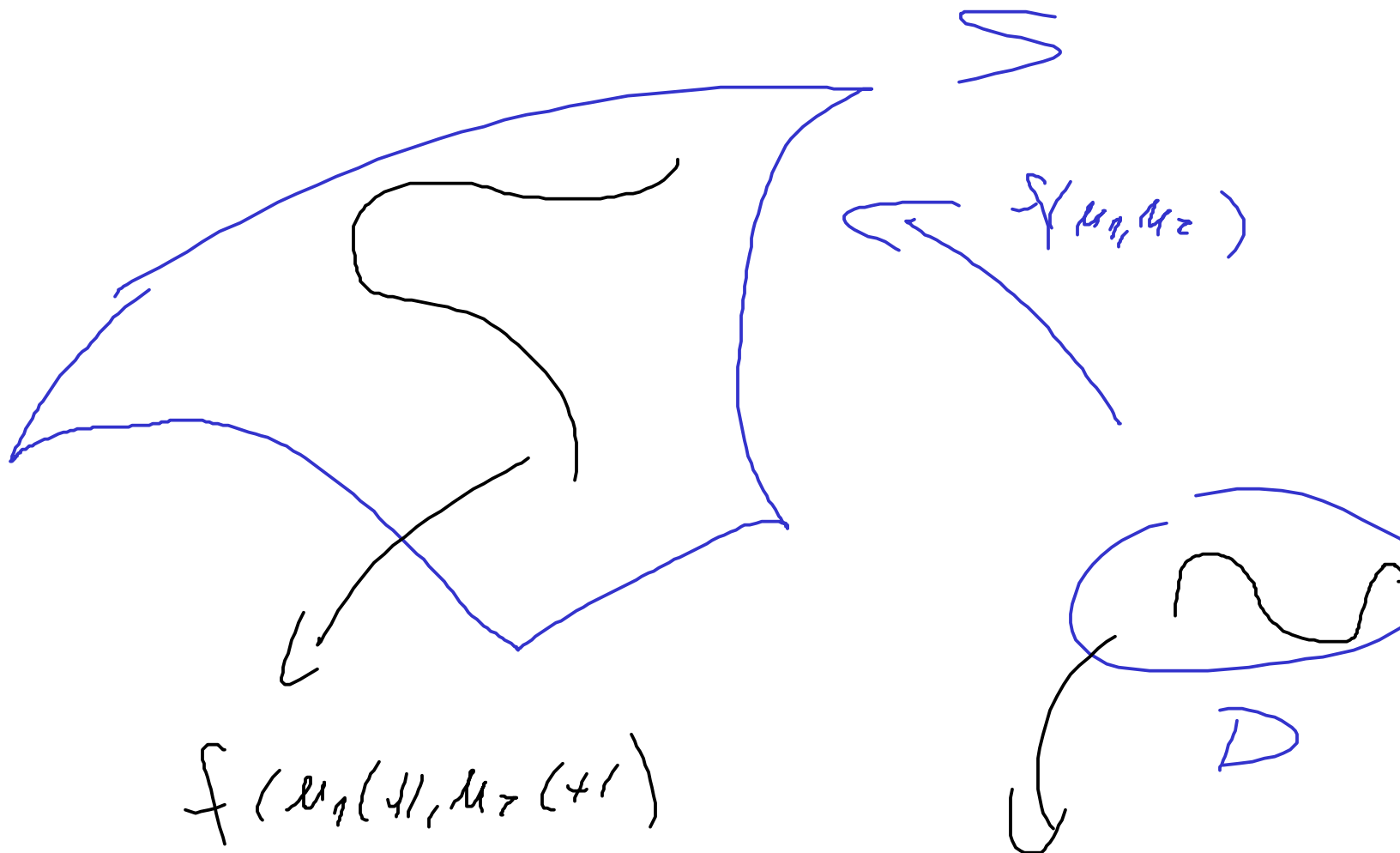
řádkem } na $T_p S$

první řádkem řada
(bi lineární forma)

koefficienty u bází f_1, f_2

budou $(f_i, f_j) \rightarrow$ matice

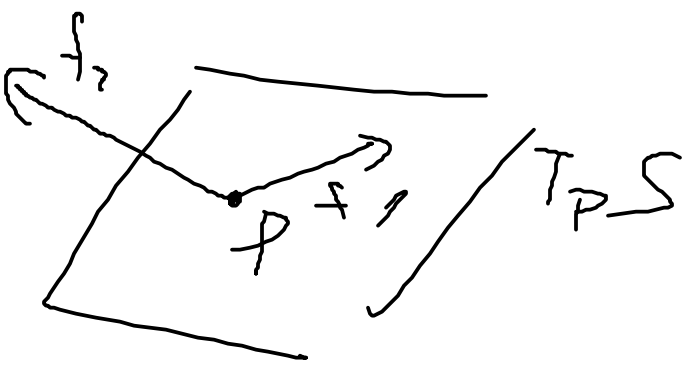
$$\begin{pmatrix} (f_1, f_1) & (f_1, f_2) \\ (f_2, f_1) & (f_2, f_2) \end{pmatrix}$$



$$f(u_1(t), u_2(t))$$

$$(u_1(t), u_2(t))$$

$$\frac{dI}{dt} = f_1 \frac{du_1}{dt} + f_2 \frac{du_2}{dt}$$



f_1, f_2 base $T_p S$

$\frac{du_1, du_2}{dt}$ base $no (T_p S)^*$

↙
linear
forma

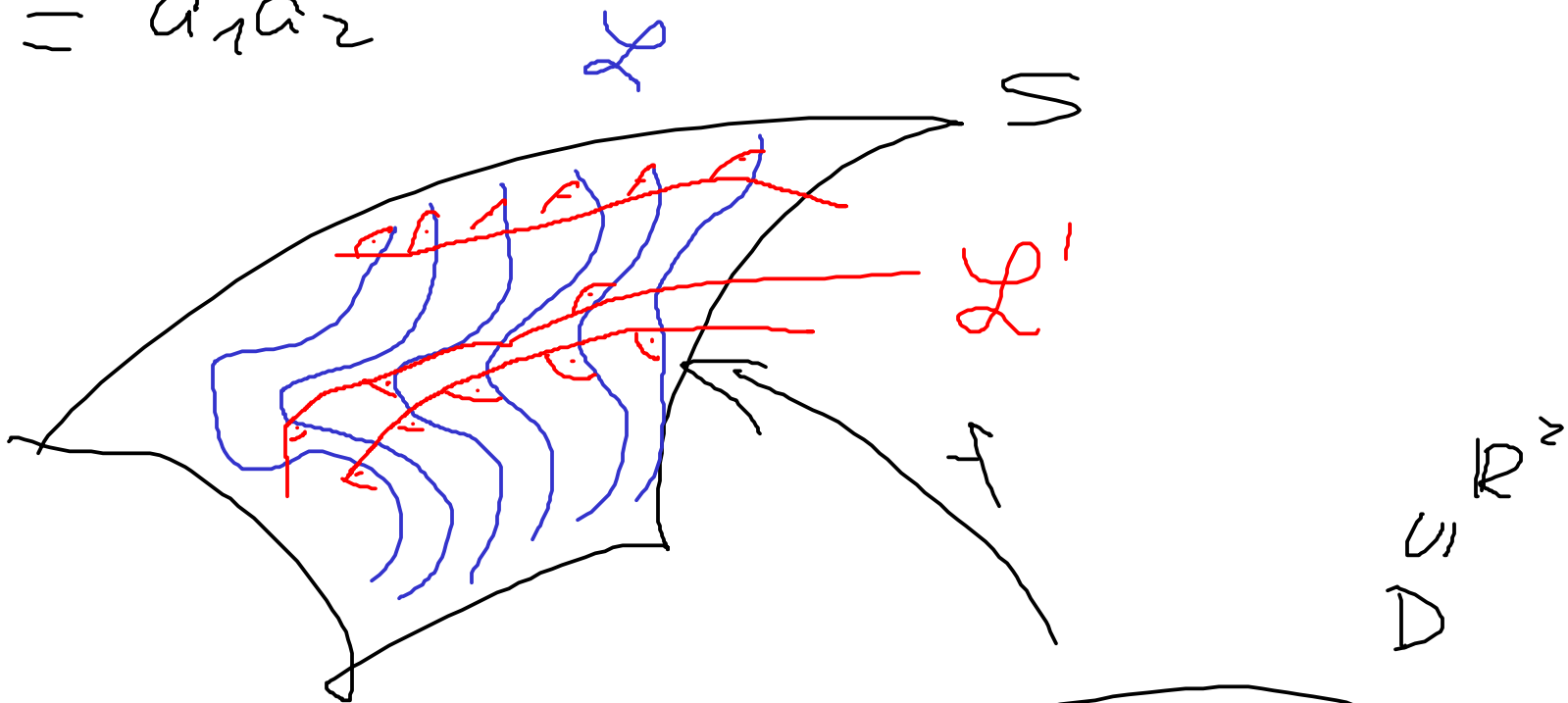
$$du_1^2 (a_1 f_1 + a_2 f_2) = \left(du_1 (a_1 f_1 + a_2 f_2) \right)^2$$

$$= a_1^2$$

$$(du_1 du_2) (a_1 f_1 + a_2 f_2) =$$

$$= (du_1 (a_1 f_1 + a_2 f_2)) (du_2 (a_1 f_1 + a_2 f_2))$$

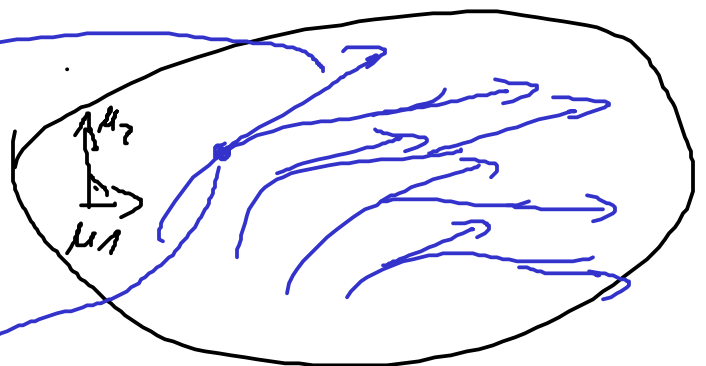
$$= a_1 a_2$$



(du_1, du_2)

symmetric

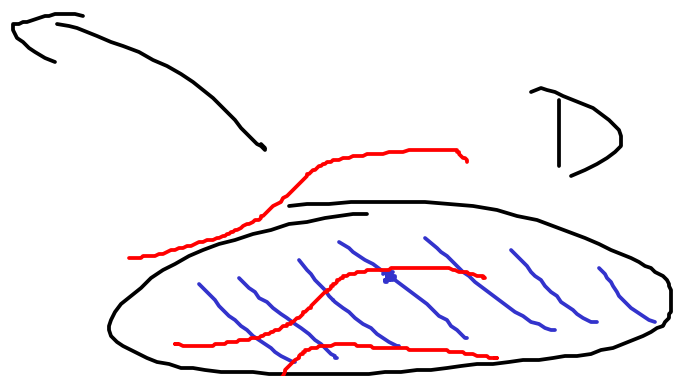
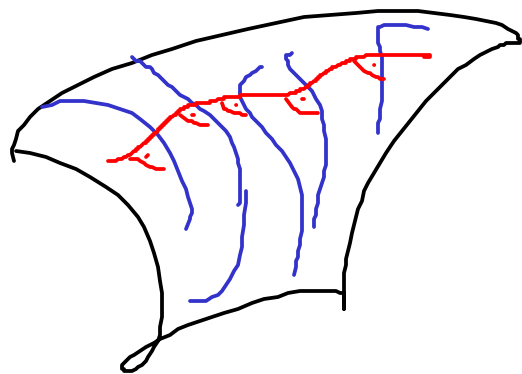
(u_1, u_2)



$$J^* L(x_1, x_2) := \frac{dx_2}{dx_1}$$

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STRAQ



"to" $(c, -c), c \in \mathbb{R}$

6. to Matrix Φ_1 u bazei

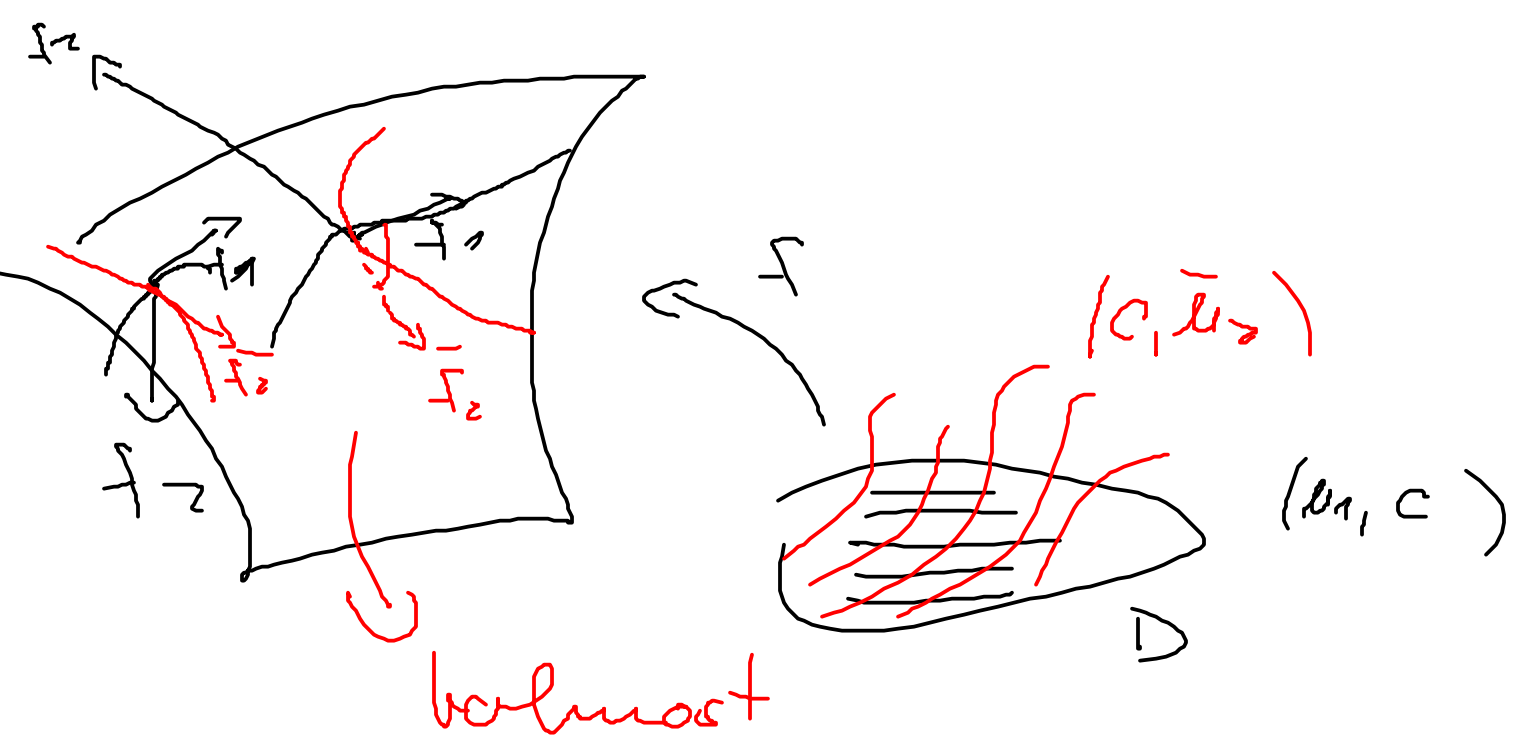
$$f_1, f_2 \quad \downarrow \quad \begin{pmatrix} g_{11} & g_{12} \\ g_{12} & g_{22} \end{pmatrix}$$

pozitivno definitna

- $g_{11} > 0$

$$g_{11} = \|f_1\|^2$$

- $\det = g_{11}g_{22} - g_{12}^2 > 0$



bolnost

na f_1 z normeno s počist
 ov togo načina tvor ob fovi
 k vektve pri nek
 ur d enije f_1

$$(u_1, \bar{u}_2) = (u_1, \psi(u_1, u_2))$$