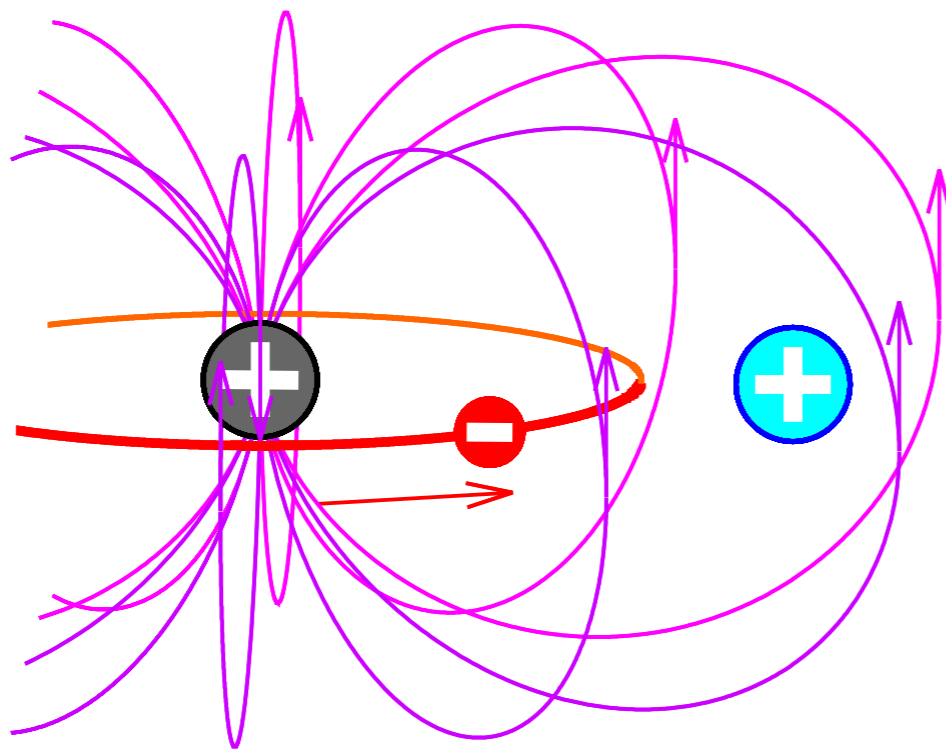
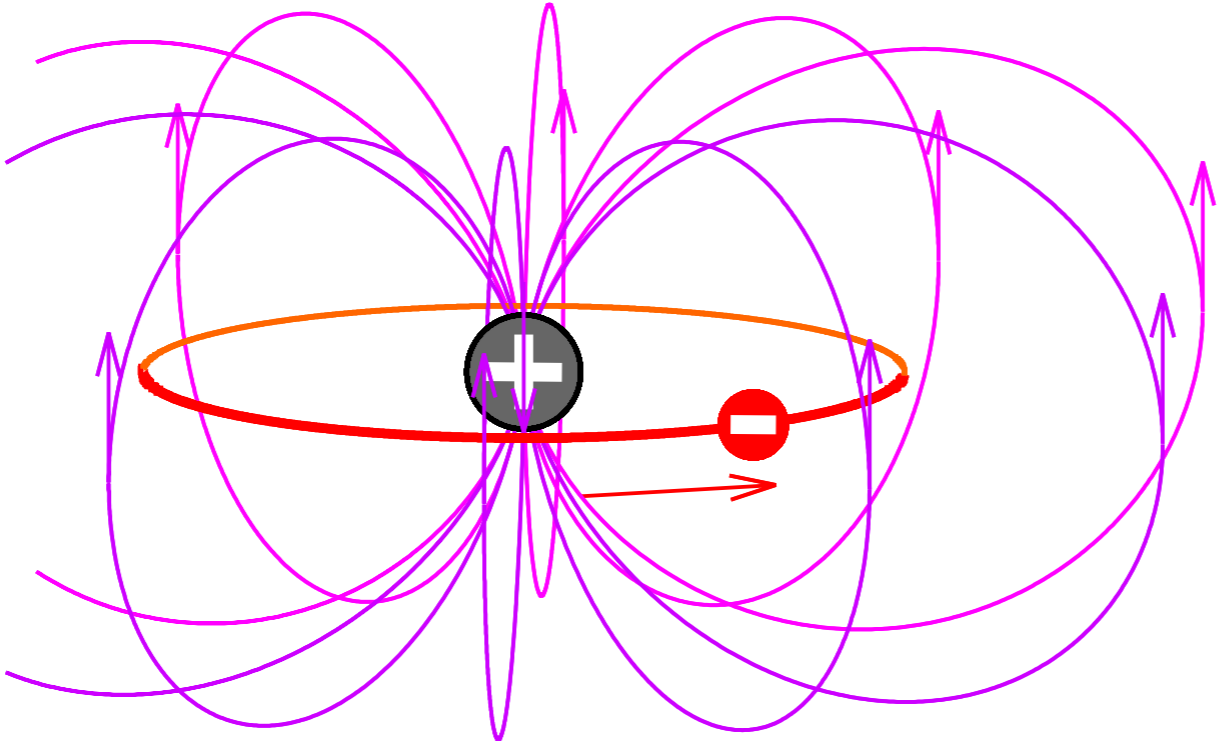
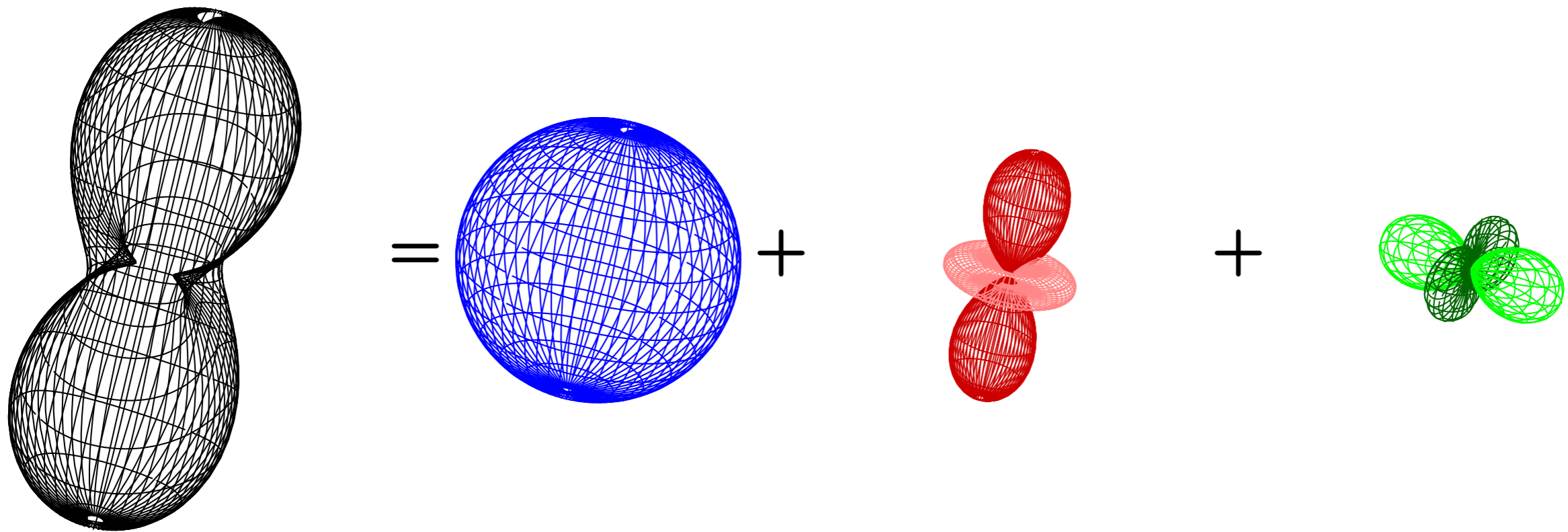


Lecture 2: Relaxation





$$\begin{pmatrix} \delta_{XX} & 0 & 0 \\ 0 & \delta_{YY} & 0 \\ 0 & 0 & \delta_{ZZ} \end{pmatrix} = \delta_i \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} + \delta_a \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 2 \end{pmatrix} + \delta_r \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

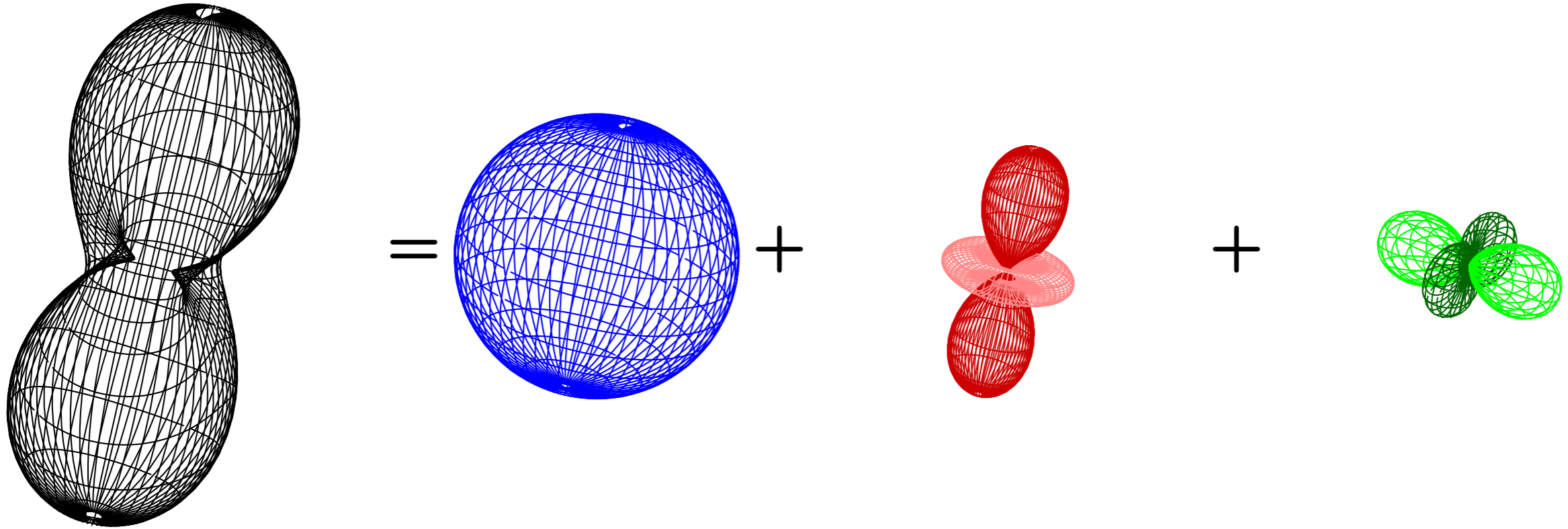


$$\delta_i = \frac{1}{3} \text{Tr}\{\underline{\delta}\} = \frac{1}{3}(\delta_{XX} + \delta_{YY} + \delta_{ZZ})$$

$$\delta_a = \frac{1}{3} \Delta_\delta = \frac{1}{6} (2\delta_{ZZ} - (\delta_{XX} + \delta_{YY}))$$

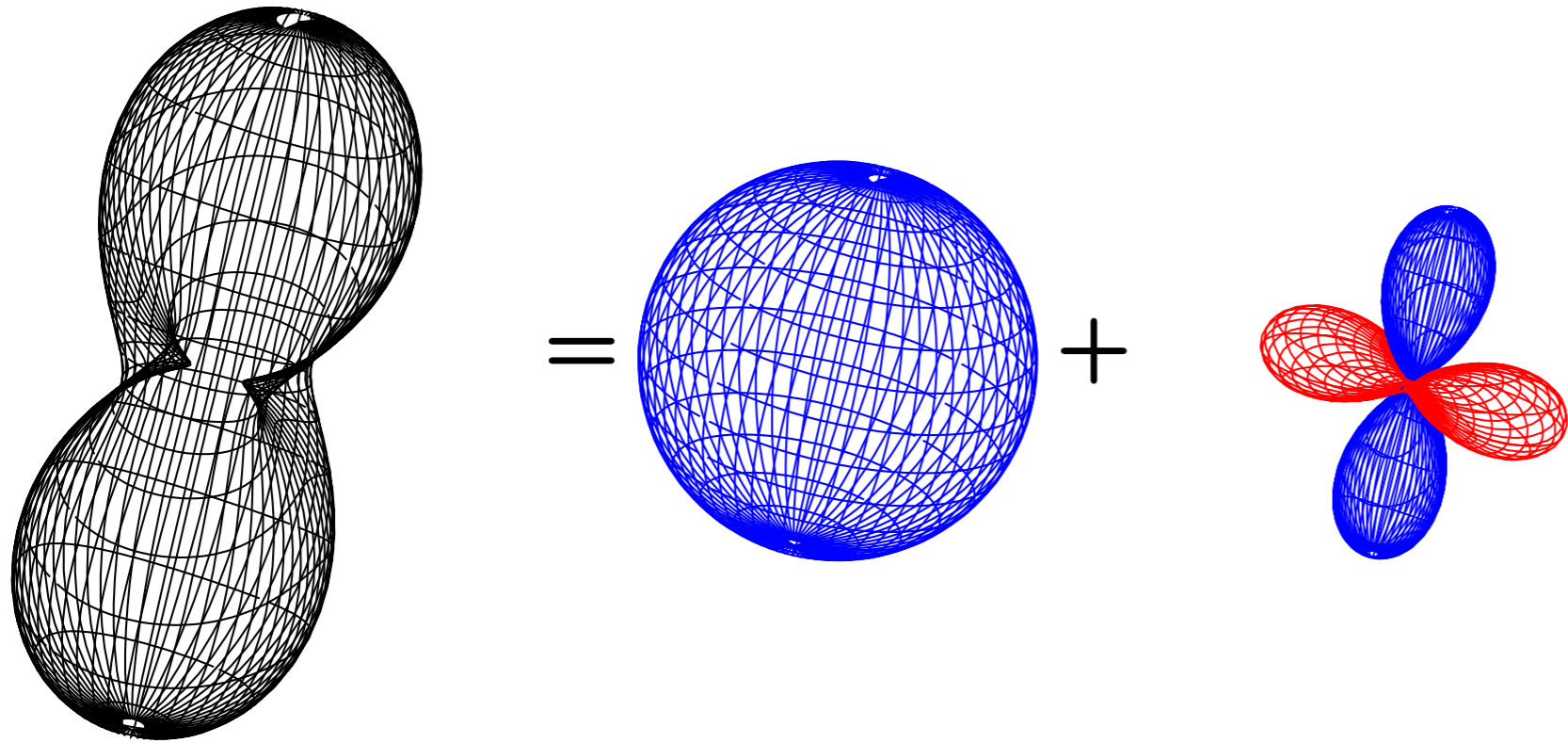
$$\delta_r = \frac{1}{3} \eta_\delta \Delta_\delta = \frac{1}{2} (\delta_{XX} - \delta_{YY})$$

$$\begin{pmatrix} \delta_{XX} & 0 & 0 \\ 0 & \delta_{YY} & 0 \\ 0 & 0 & \delta_{ZZ} \end{pmatrix} = \delta_i \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} + \delta_a \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 2 \end{pmatrix} + \delta_r \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

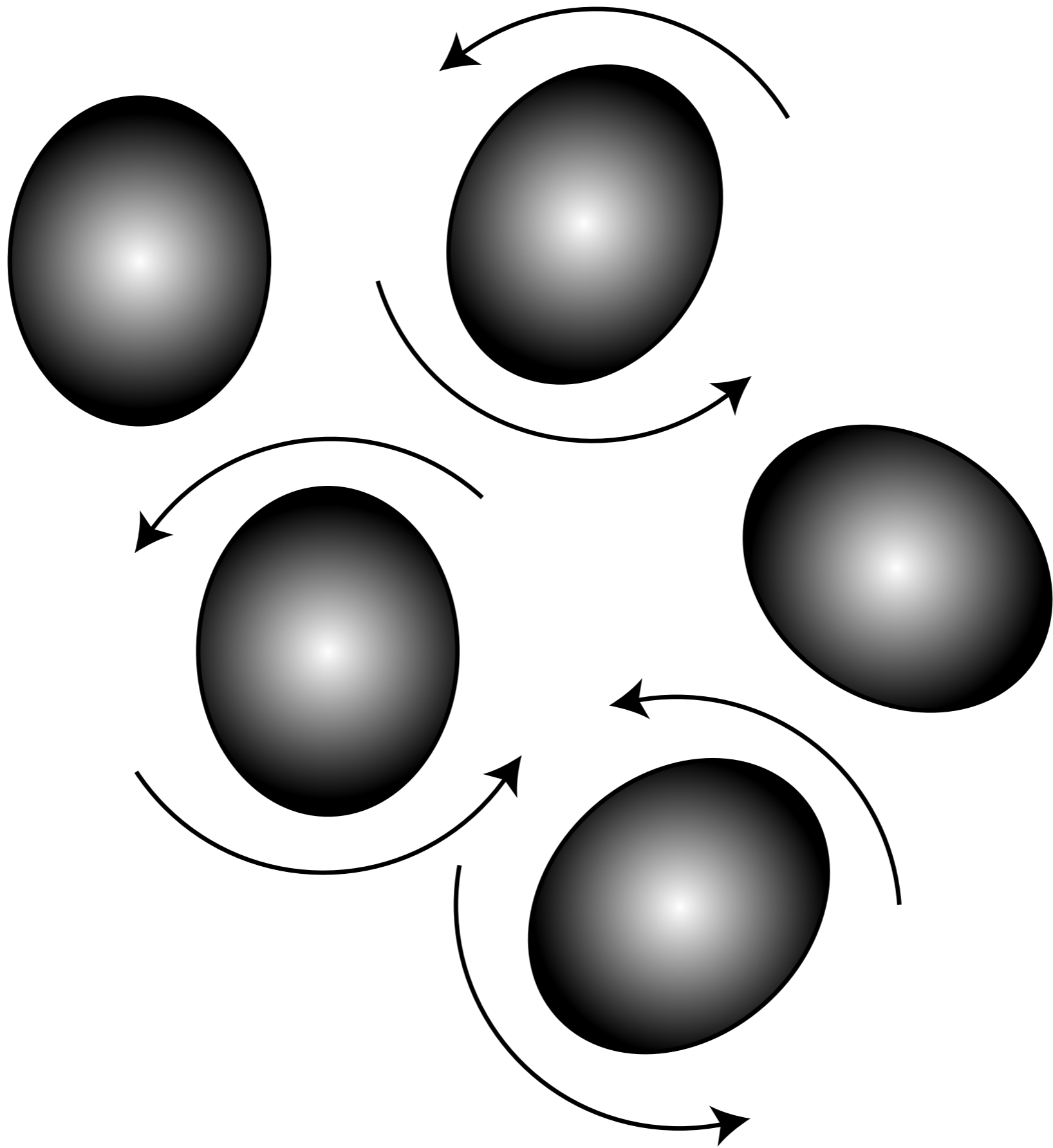


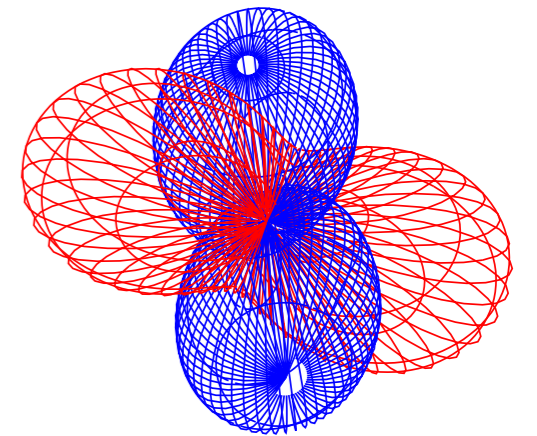
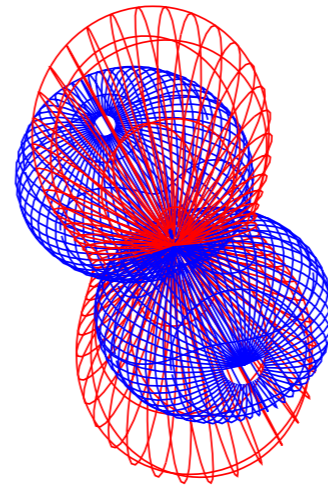
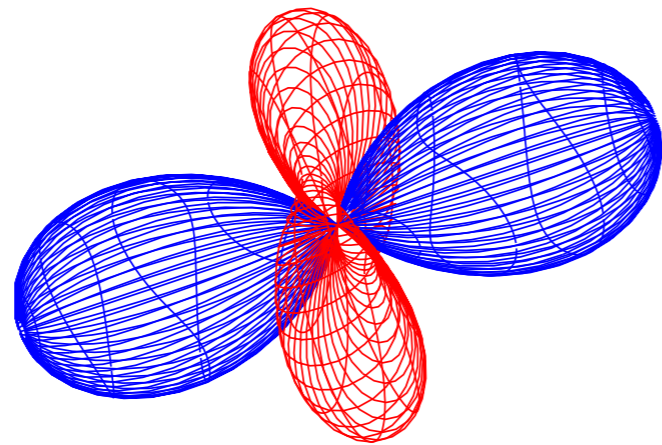
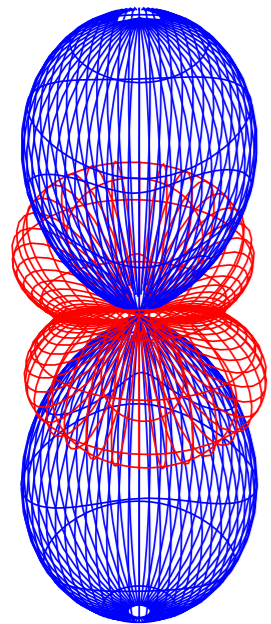
$$\vec{B}_e = \delta_i B_0 \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} + \delta_a B_0 \begin{pmatrix} 3 \sin \vartheta \cos \vartheta \cos \varphi \\ 3 \sin \vartheta \cos \vartheta \sin \varphi \\ 3 \cos^2 \vartheta - 1 \end{pmatrix} + \delta_r B_0 \begin{pmatrix} -(2 \cos^2 \chi - 1) \sin \vartheta \cos \vartheta \cos \varphi + 2 \sin \chi \cos \chi \sin \vartheta \sin \varphi \\ -(2 \cos^2 \chi - 1) \sin \vartheta \cos \vartheta \sin \varphi - 2 \sin \chi \cos \chi \sin \vartheta \cos \varphi \\ +(2 \cos^2 \chi - 1) \sin^2 \vartheta \end{pmatrix}$$

$$\begin{pmatrix} \delta_{XX} & 0 & 0 \\ 0 & \delta_{YY} & 0 \\ 0 & 0 & \delta_{ZZ} \end{pmatrix} = \delta_i \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} + \delta_a \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 2 \end{pmatrix} + \delta_r \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

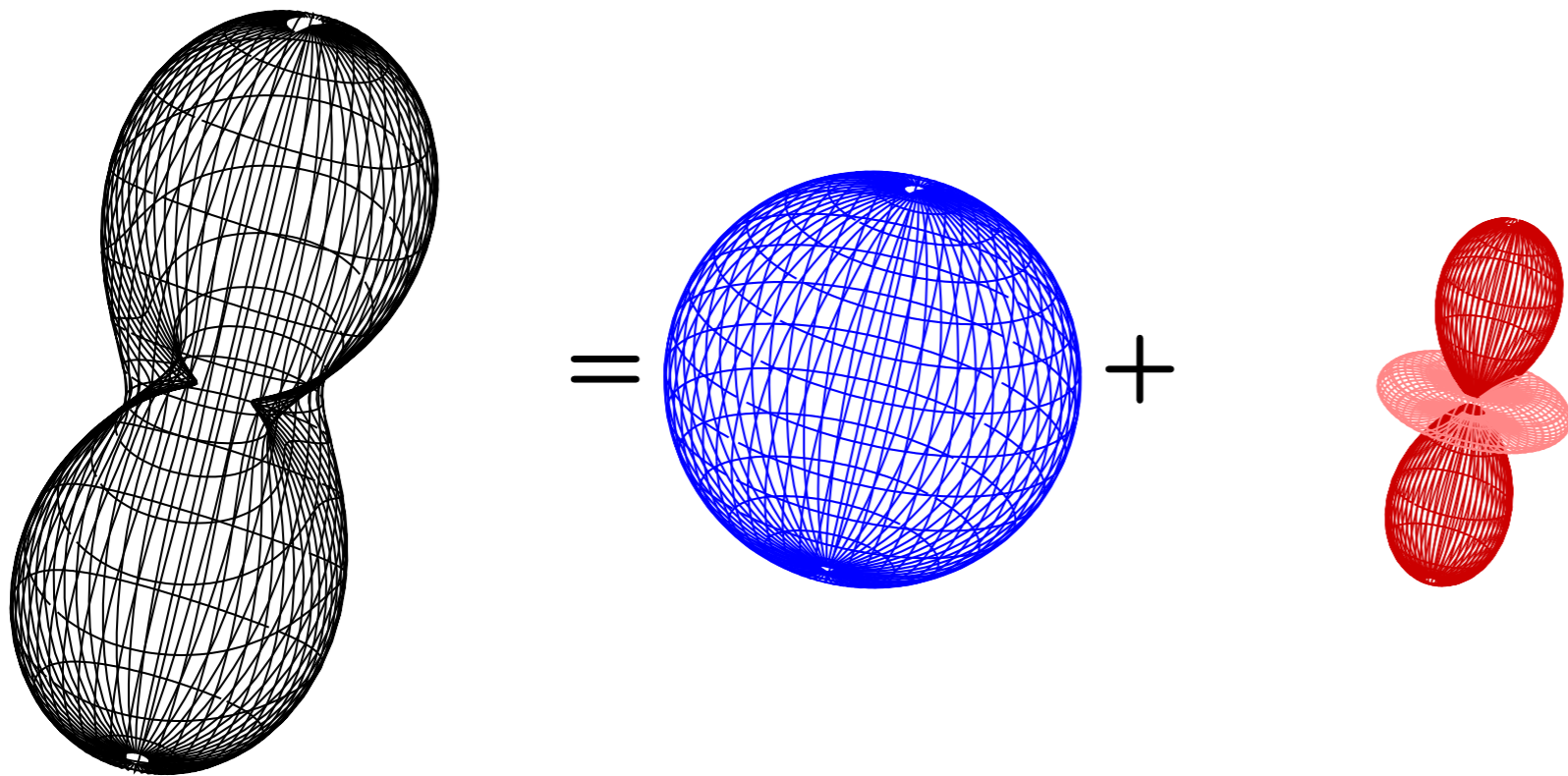


$$\vec{B}_e = \delta_i B_0 \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} + \delta_a B_0 \begin{pmatrix} 3 \sin \vartheta \cos \vartheta \cos \varphi \\ 3 \sin \vartheta \cos \vartheta \sin \varphi \\ 3 \cos^2 \vartheta - 1 \end{pmatrix} + \delta_r B_0 \begin{pmatrix} -(2 \cos^2 \chi - 1) \sin \vartheta \cos \vartheta \cos \varphi + 2 \sin \chi \cos \chi \sin \vartheta \sin \varphi \\ -(2 \cos^2 \chi - 1) \sin \vartheta \cos \vartheta \sin \varphi - 2 \sin \chi \cos \chi \sin \vartheta \cos \varphi \\ +(2 \cos^2 \chi - 1) \sin^2 \vartheta \end{pmatrix}$$

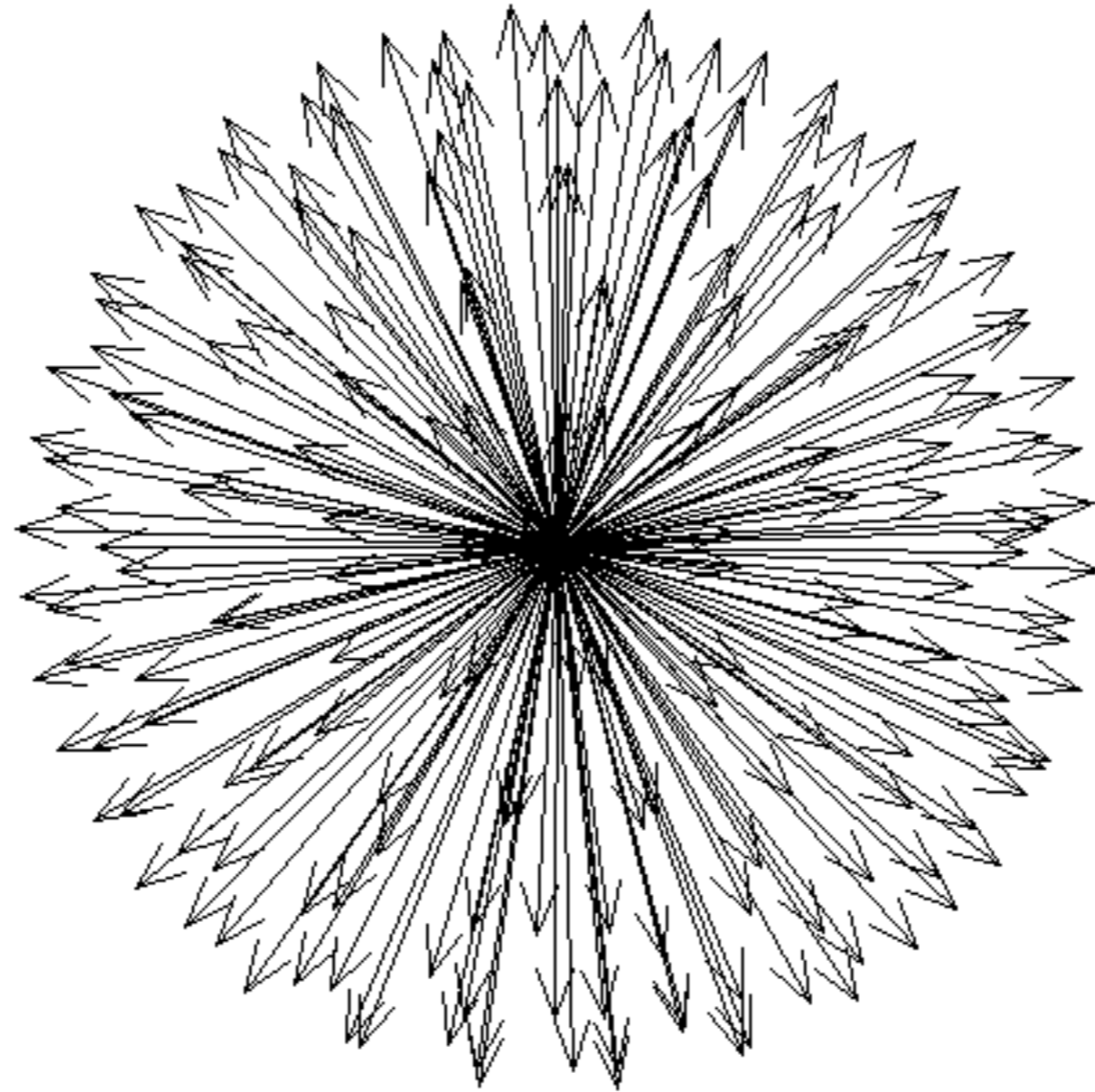




$$\begin{pmatrix} \delta_{XX} & 0 & 0 \\ 0 & \delta_{YY} & 0 \\ 0 & 0 & \delta_{ZZ} \end{pmatrix} = \delta_i \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} + \delta_a \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 2 \end{pmatrix}$$



$$\vec{B}_e = \delta_i B_0 \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} + \delta_a B_0 \begin{pmatrix} 3 \sin \vartheta \cos \vartheta \cos \varphi \\ 3 \sin \vartheta \cos \vartheta \sin \varphi \\ 3 \cos^2 \vartheta - 1 \end{pmatrix}$$



Magnetic moments in magnetic field

$$\begin{aligned}
R_0 &= (\gamma_{B_0} \delta_a)^2 \int_0^\infty (3 \cos^2 \vartheta(0) - 1)(3 \cos^2 \vartheta(t) - 1) dt \\
&= b^2 \int_0^\infty C^{\parallel}(t) dt
\end{aligned}$$

$$\left(\frac{3}{2} \cos^2 \vartheta(0) - \frac{1}{2}\right) \left(\frac{3}{2} \cos^2 \vartheta(t) - \frac{1}{2}\right) = \frac{1}{5} e^{-t/\tau_c} dt = \frac{1}{5} e^{-6D^{\text{rot}}t}$$

$$D^{\text{rot}} = \frac{k_B T}{8\pi\eta(T)r^3}$$

$$R_0 = \frac{1}{5} b^2 \int_0^\infty e^{-t/\tau_c} dt = \frac{1}{5} b^2 \tau_c = \frac{1}{5} b^2 \frac{1}{6D^{\text{rot}}}$$

$$R_1 = 3 (\gamma_{B_0} \delta_a)^2 \left(\frac{1}{2} J(\omega_0) + \frac{1}{2} J(-\omega_0) \right) \approx 3 (\gamma_{B_0} \delta_a)^2 J(\omega_0)$$

$$J(\omega_0) = \int_{-\infty}^{\infty} \overline{\left(\frac{3}{2} \cos^2(\theta(0)) - \frac{1}{2} \right) \left(\frac{3}{2} \cos^2(\theta(t)) - \frac{1}{2} \right) \cos(\omega_0 t)}$$

$$R_2 = 2 (\gamma_{B_0} \delta_a)^2 J(0) + \frac{3}{2} (\gamma_{B_0} \delta_a)^2 J(\omega_0)$$

$$R_1 = \frac{3}{4} b^2 J(\omega_0)$$

$$R_2 = \frac{1}{2} b^2 J(0) + \frac{3}{8} b^2 J(\omega_0)$$

BLOCH EQUATIONS:

$$\frac{dM_x}{dt} = -R_2 M_x - \Omega M_y + \omega_1 \sin \varphi M_z$$

$$\frac{dM_y}{dt} = +\Omega M_x - R_2 M_y - \omega_1 \cos \varphi M_z$$

$$\frac{dM_z}{dt} = -\omega_1 \sin \varphi M_x + \omega_1 \cos \varphi M_y - R_1 (M_z - M_z^{\text{eq}})$$