Differential Equations

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QUESTION

Sketch a direction field for the differential equation

$$y' = x^2 + y^2 - 1.$$



HELP

Question: Sketch a direction field for the differential equation

$$y' = x^2 + y^2 - 1.$$

Help: Start by computing the slope at several points. You can use following table:

x	-2	-1	0	1	2	0	1	2	0	1	2
y	0	0	0	0	0	1	1	1	2	2	2
slope											

Now draw short line segments with these slopes at these points.

The more line segments you draw in a direction field, the clearer the picture becomes.



SOLUTION

Question: Sketch a direction field for the differential equation

$$y' = x^2 + y^2 - 1.$$

Solution: After computing slopes at several points and drawing short lines segments with these slopes at these points, we get graph similar to Figure 1. More detailed direction field is shown in Figure 2.



