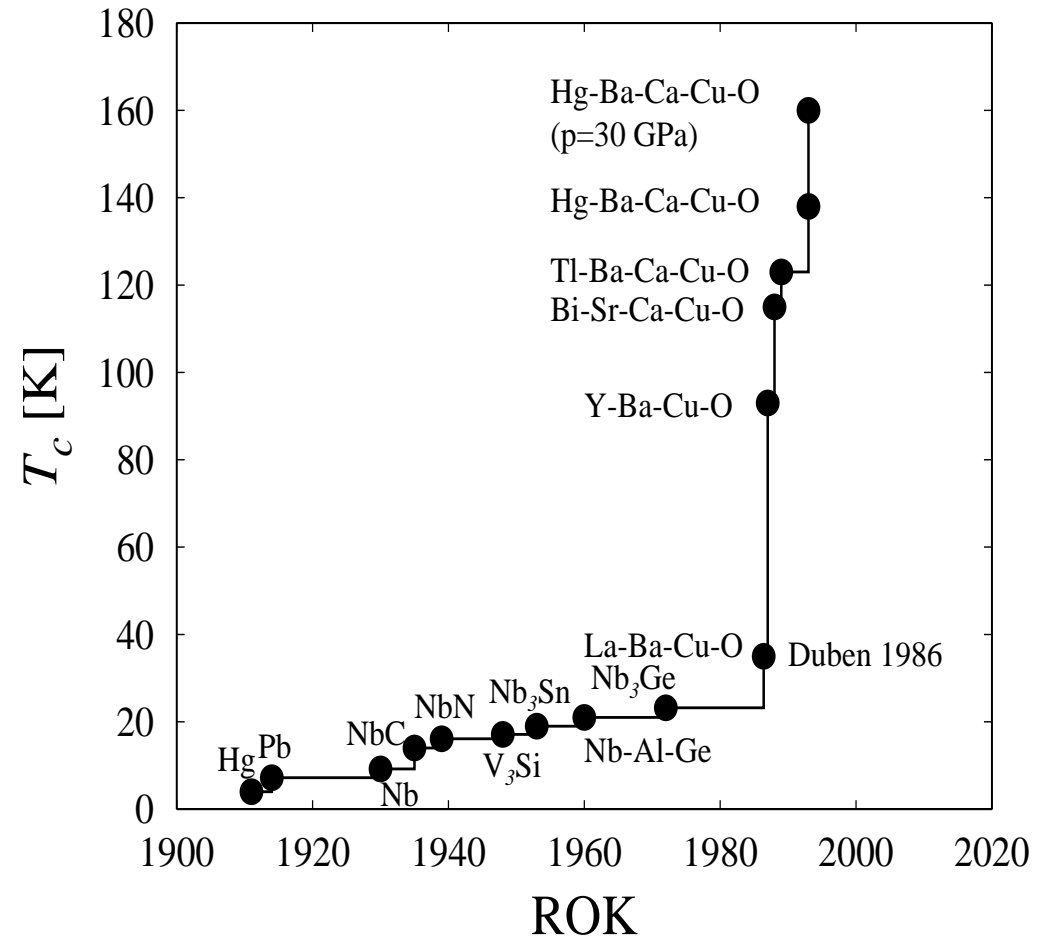
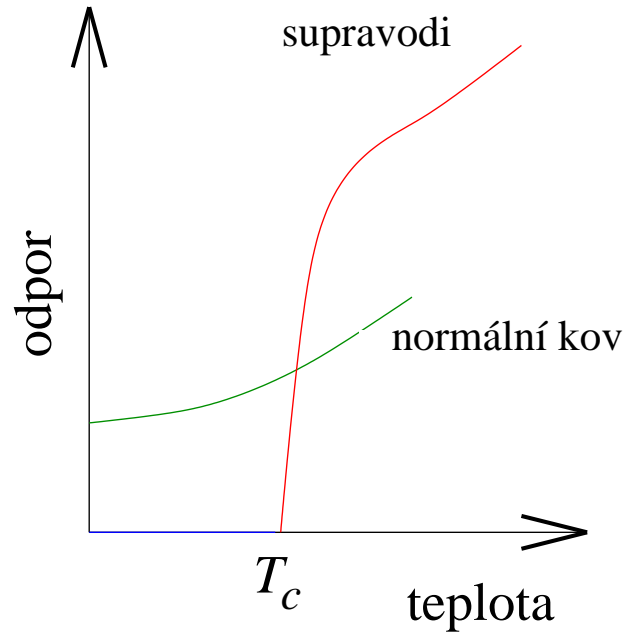


# Supravodivost a vysokoteplotní supravodiče

1. Úvod a historie
2. Nekonečná stejnosměrná vodivost a Meissnerův jev
3. Základní prvky teorie supravodivosti
4. Magnetické vlastnosti supravodičů, supravodivé víry
5. Aplikace supravodivosti: Maglev a SQUID
6. Vysokoteplotní supravodiče

# Supravodivost, $T_c$







## The Nobel Prize in Physics 1913

"for his investigations on the properties of matter at low temperatures which led, inter alia, to the production of liquid helium"



**Heike Kamerlingh Onnes**

the Netherlands

Leiden University  
Leiden, the Netherlands

b. 1853  
d. 1926

Teplotní závislost měrného odporu Pt, Hg a Au (data K. Onnese)

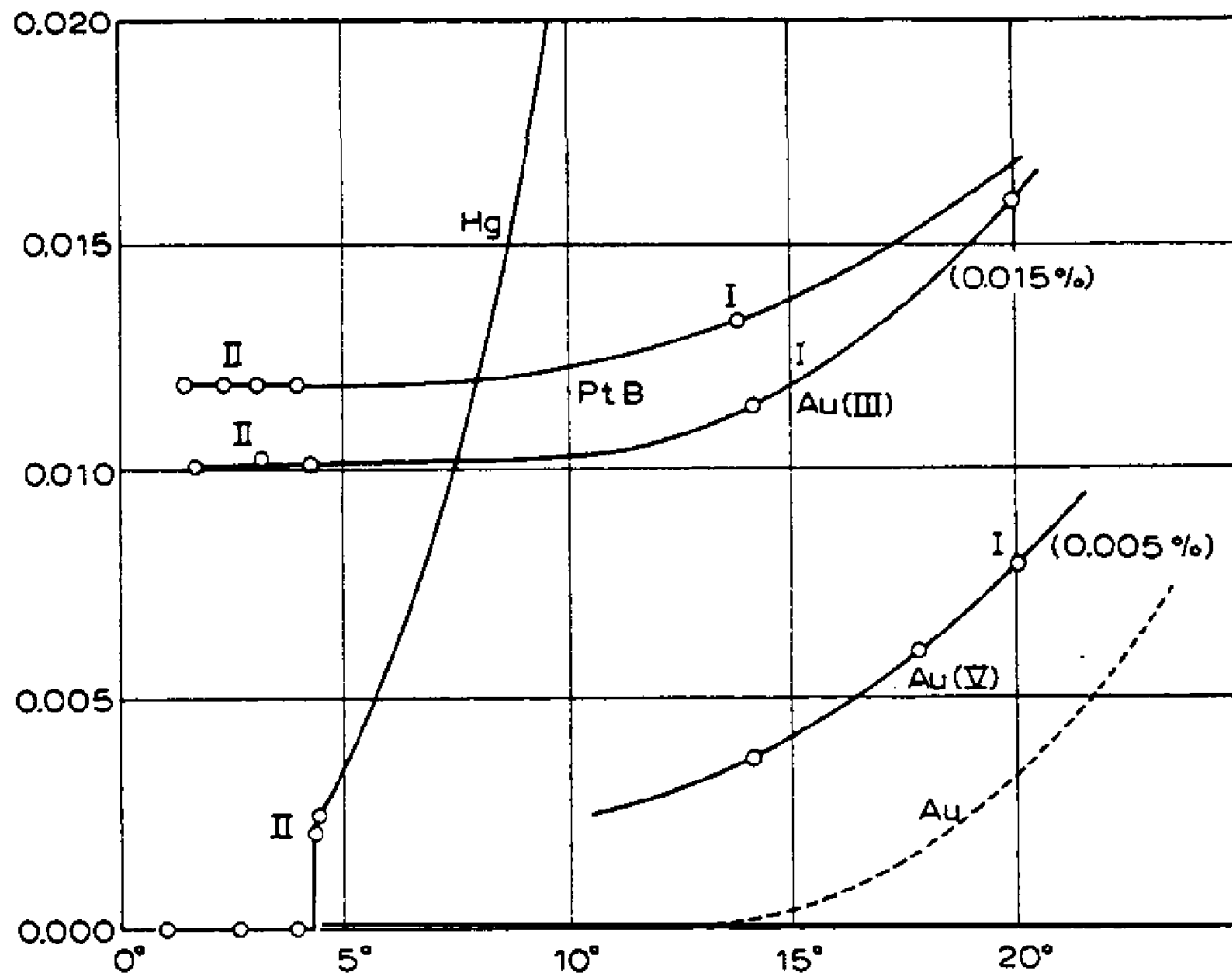
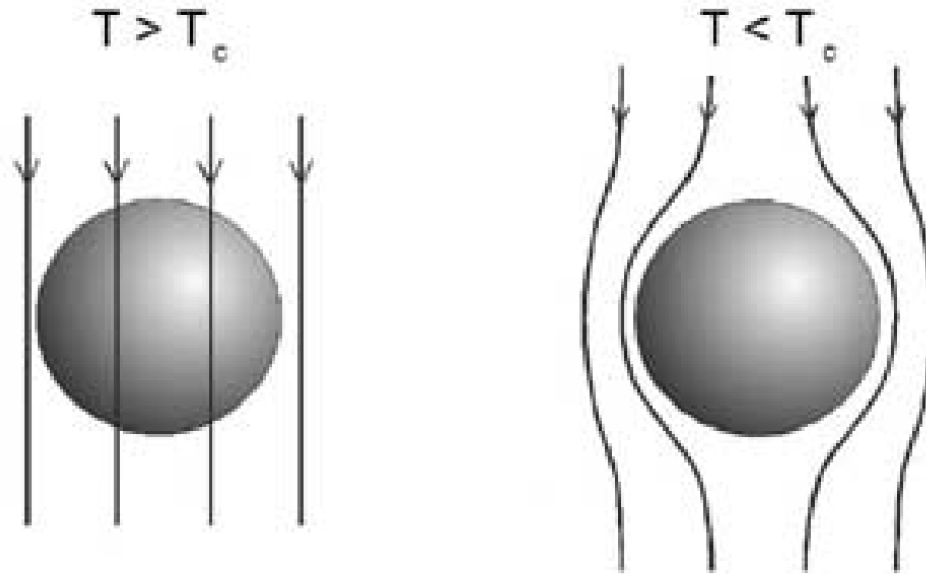


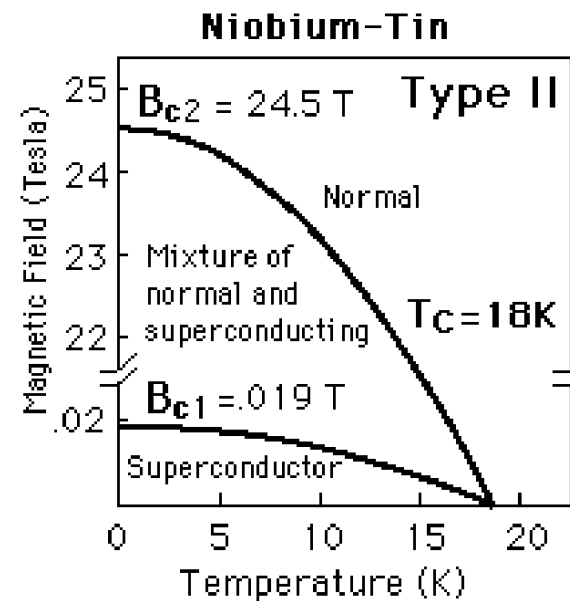
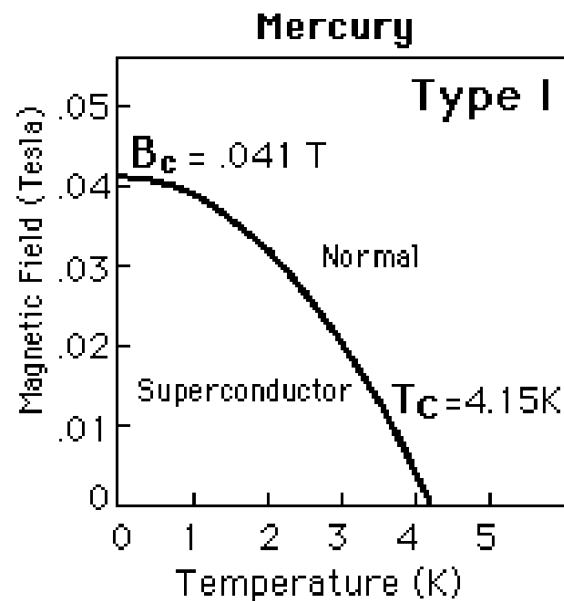
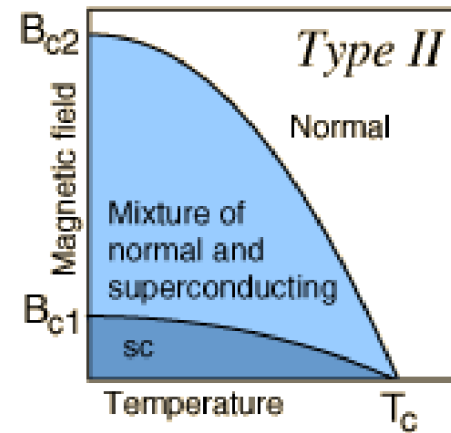
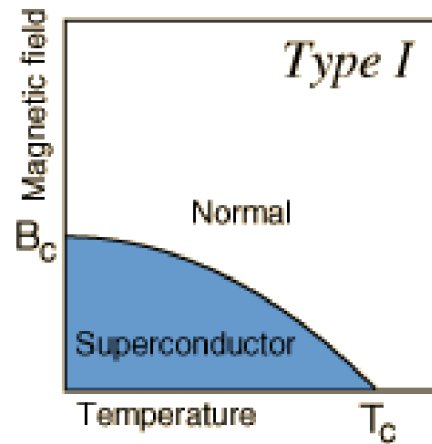
Fig. 14



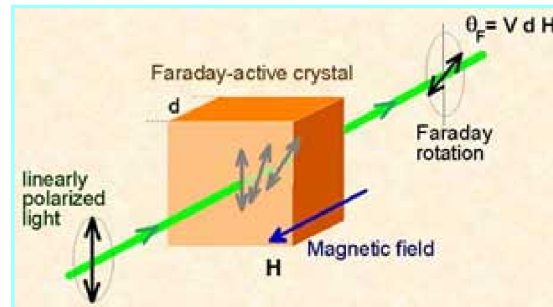
## Meissner effect

When a [superconductor](#) is cooled down below the critical temperature,  $T_c$ , its resistance to electrical current is known to disappear. The other fundamental property of superconductors is so-called [Meissner effect](#), i.e., expulsion of magnetic field. An external field is entirely compensated by shielding currents which it induces in the superconductor, and which will flow forever due to absence of resistance.

# Supravodiče 1. a 2. typu

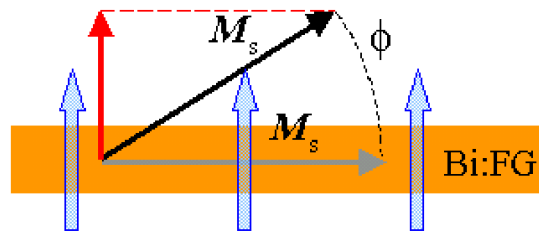


## Fundamentals of magneto-optical imaging



### Physical principles

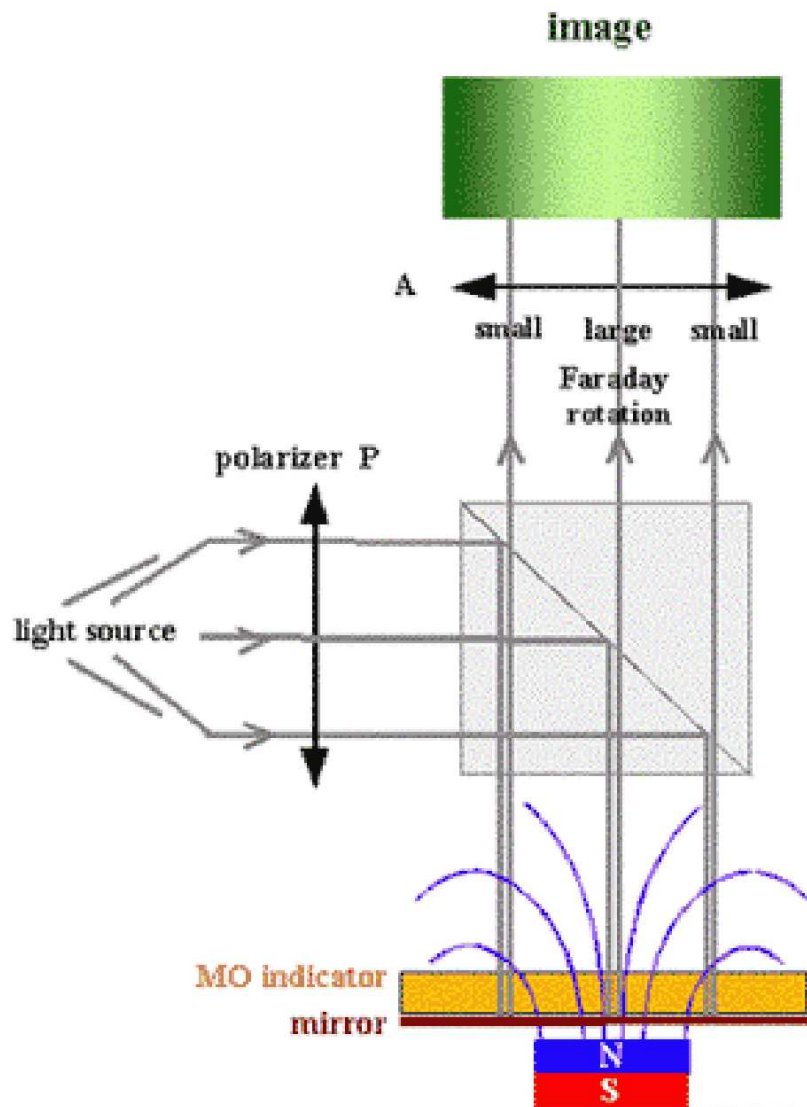
The physical idea behind the magneto-optical imaging is the [Faraday effect](#), i.e., rotation of the light polarization induced by magnetic field. On 13 September, 1845, Michael Faraday wrote in his Diary "...magnetic force and light were proved to have relation to each other. This fact will most likely prove exceedingly fertile and of great value in the investigation of both conditions of natural force" .



### Magneto-optical films

A number of different materials have been applied as indicators in MO imaging: [cerous nitrate-glycerol](#), various europium compounds (EuS, EuSe) [H. Kirchner, Phys. Lett. 26A, 651 (1968)] and bismuth-substituted iron garnets [A.A. Polyanskii et al. Sov. Tech. Phys. Lett. 15, 872 (1989)]. Today, the most popular indicator is the [ferri-magnetic Bi:YIG film](#) with in-plane spontaneous magnetization. Application of a perpendicular magnetic field creates an out-of-plane component of the magnetization responsible for the Faraday rotation. A single-crystal film with typical thickness of a few microns can be grown by liquid-phase epitaxy on a gadolinium-gallium-garnet (GGG) substrate.





## Magneto-optical setup

The MO indicator is placed in the light beam path between a polarizer and an analyzer crossed by 90 degrees. If a magnetic field is present perpendicularly to the film, the magnetization of the Bi:YIG will be tilted out of the plane. The perpendicular component of the magnetization will cause a Faraday rotation of the light. The rotation angle will be small where the magnetic field is small, and large in regions of high fields. After leaving the analyzer the light will therefore have an intensity distribution that reflects the magnitude of the field in the plane of the indicator film.



## The Nobel Prize in Physics 1972

"for their jointly developed theory of superconductivity, usually called the BCS-theory"



**John Bardeen**

🏆 1/3 of the prize

USA

University of Illinois  
Urbana, IL, USA

b. 1908  
d. 1991



**Leon Neil Cooper**

🏆 1/3 of the prize

USA

Brown University  
Providence, RI, USA

b. 1930



**John Robert  
Schrieffer**

🏆 1/3 of the prize

USA

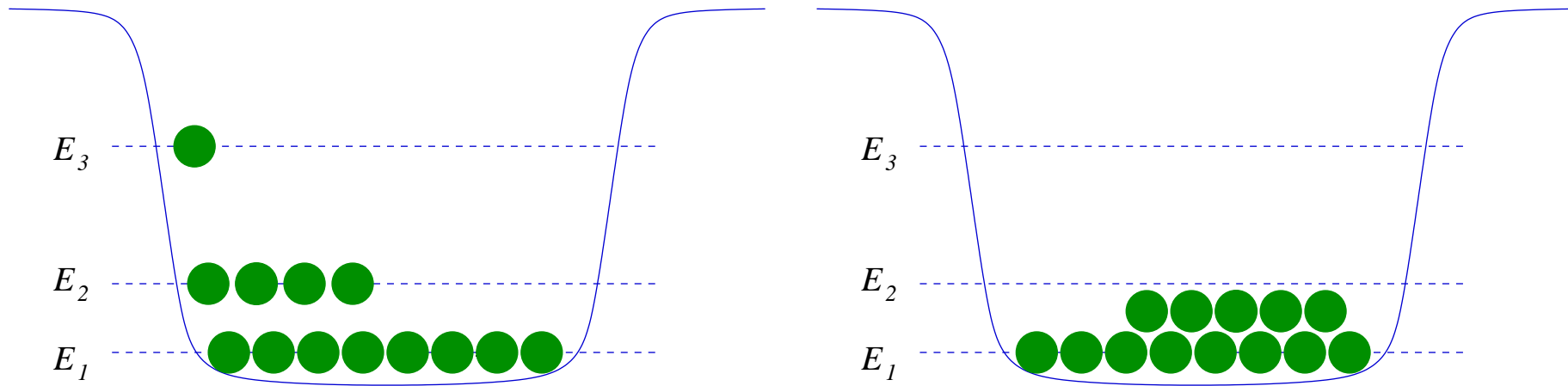
University of  
Pennsylvania  
Philadelphia, PA, USA

b. 1931

# Bose-Einsteinova kondenzace

$T > 0$

$T = 0$



$$N_i = \frac{1}{e^{\frac{E_i - \mu}{kT}} - 1}$$

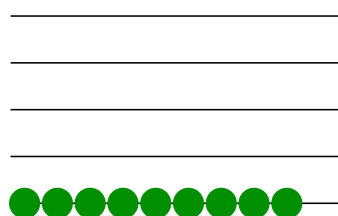
$$\lim_{N \rightarrow \infty} \frac{N_1}{N} = 0 \quad \text{pro } T > T_B$$

$$\lim_{N \rightarrow \infty} \frac{N_1}{N} > 0 \quad \text{pro } T < T_B$$

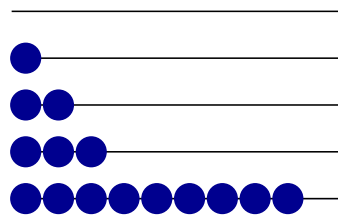
$$T_B \sim h^2$$

# Schematické znázornění základních stavů kondenzátů

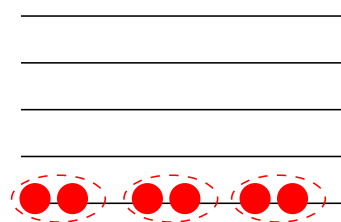
BEC



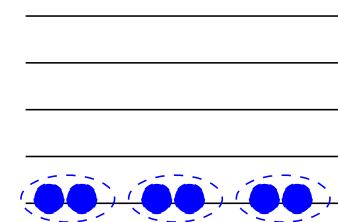
$^4\text{He}$



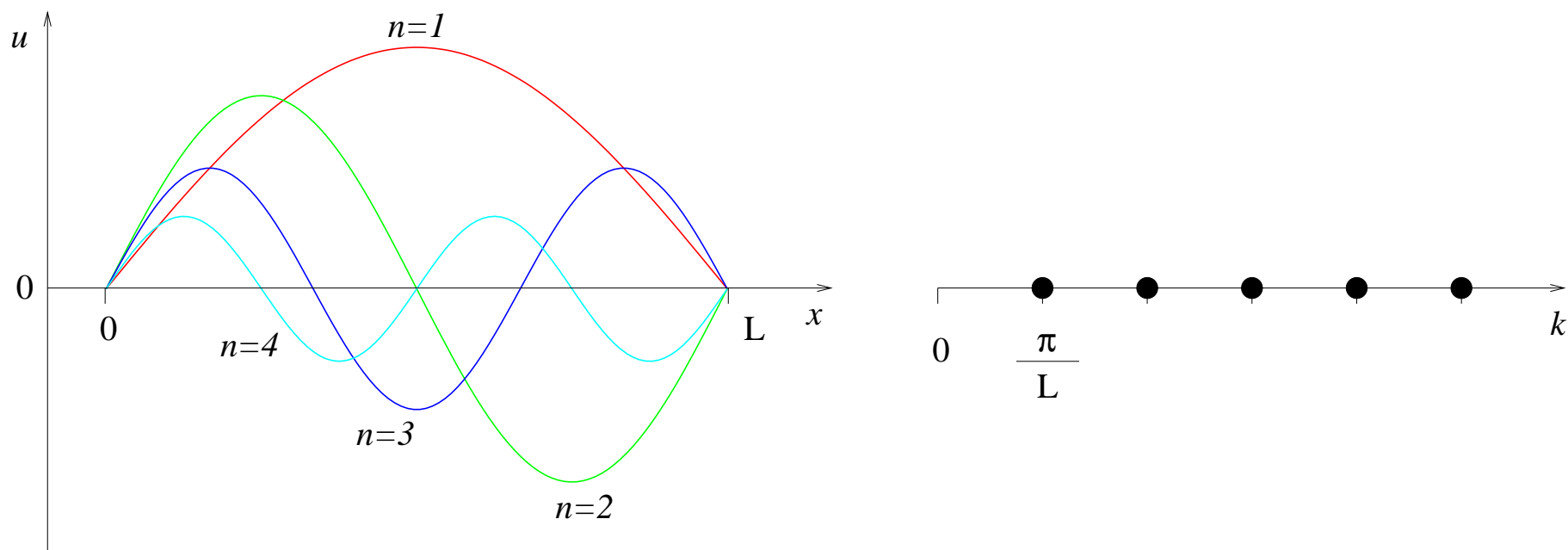
SC



$^3\text{He}$



## Kmity struny upevněné na koncích



$$\lambda_1 = 2L, \lambda_2 = 2L/2, \lambda_3 = 2L/3, \dots, \lambda_n = 2L/n$$

$$\omega = \frac{2\pi c}{\lambda} \quad \omega_n = \frac{2\pi c}{\lambda_n} = \frac{\pi c n}{L}$$

$$u_n(x, t) = \cos(\omega_n t + \varphi) \sin\left(\frac{2\pi}{\lambda_n} x\right) = \cos(\omega_n t + \varphi) \sin(k_n x)$$

$$k = \frac{2\pi}{\lambda} \quad k_n = \frac{2\pi}{\lambda_n} = \frac{\pi n}{L}$$

## Elektrony v jednorozměrném krystalu

Vlnové délky vln spojených s elektrony:

$$\lambda_1 = 2L, \lambda_2 = 2L/2, \lambda_3 = 2L/3, \dots, \lambda_n = 2L/n; k_n = \frac{2\pi}{\lambda_n} = \frac{\pi n}{L}$$

$$E_n \dots ?$$

Vztah mezi kinetickou energií a hybností:

$$E = \frac{p^2}{2m} \quad E_n = \frac{p_n^2}{2m}$$

De-Broglieho relace:

$$p = \frac{h}{\lambda} \quad p_n = \frac{h}{\lambda_n}$$

Výsledný vzorec pro energie elektronů:

$$E_n = \frac{h^2}{2m\lambda_n^2} = \frac{\hbar^2 k_n^2}{2m}$$

## Elektrony v trojrozměrném krystalu

Vlnové chování ve všech třech směrech.

Vlnové délky:

$$\lambda_{x1} = 2L_x, \lambda_{x2} = 2L_x/2, \lambda_{x3} = 2L_x/3, \dots, \lambda_{xn} = 2L_x/n; k_{xn} = \frac{2\pi}{\lambda_{xn}} = \frac{\pi n}{L_x}$$

$$\lambda_{y1} = 2L_y, \lambda_{y2} = 2L_y/2, \lambda_{y3} = 2L_y/3, \dots, \lambda_{yn} = 2L_y/n; k_{yn} = \frac{2\pi}{\lambda_{yn}} = \frac{\pi n}{L_y}$$

$$\lambda_{z1} = 2L_z, \lambda_{z2} = 2L_z/2, \lambda_{z3} = 2L_z/3, \dots, \lambda_{zn} = 2L_z/n; k_{zn} = \frac{2\pi}{\lambda_{zn}} = \frac{\pi n}{L_z}$$

$$E_{n_x, n_y, n_z} \dots ?$$

Vztah mezi kinetickou energií a hybností:

$$E = \frac{\mathbf{p}^2}{2m} = \frac{p_x^2 + p_y^2 + p_z^2}{2m} \quad E_{n_x, n_y, n_z} = \frac{p_{xn_x}^2 + p_{yn_y}^2 + p_{zn_z}^2}{2m} = \frac{\mathbf{p}_{n_x, n_y, n_z}^2}{2m}$$

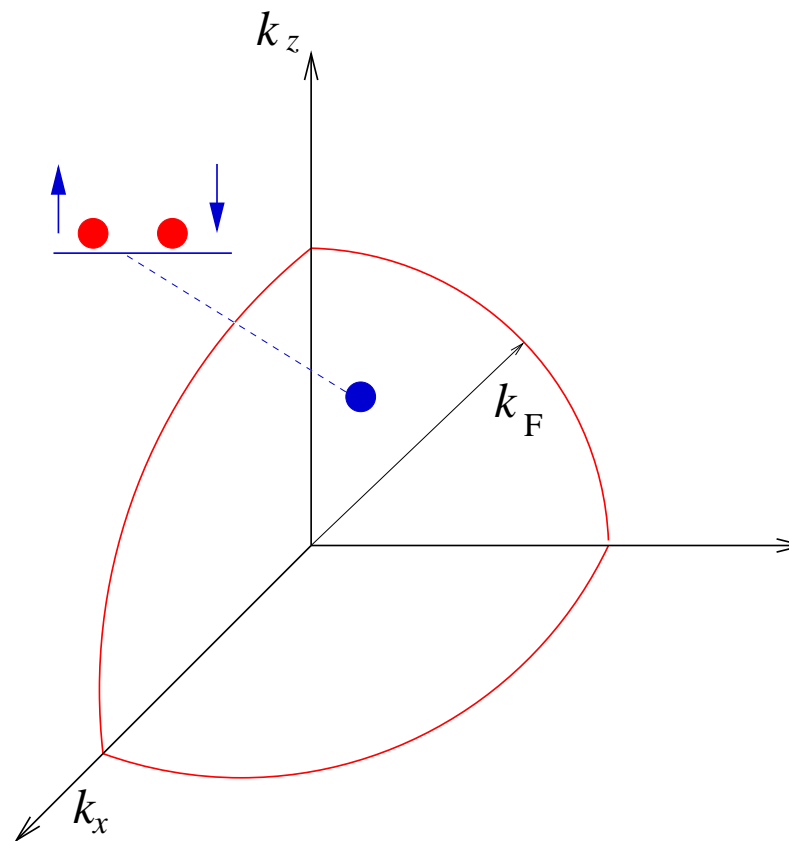
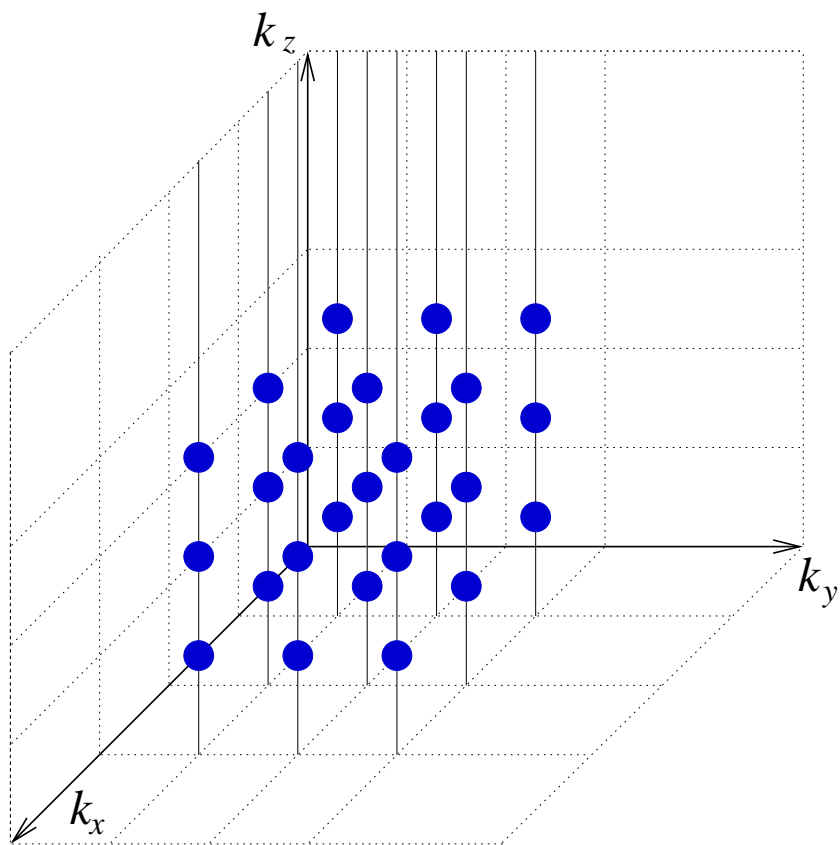
De-Broglieho relace:

$$p_x = \frac{h}{\lambda_x}, \dots \quad p_{xn} = \frac{h}{\lambda_{xn}}, \dots$$

Výsledný vzorec pro energie elektronů:

$$E_{n_x, n_y, n_z} = \frac{h^2}{2m} \left( \frac{1}{\lambda_{xn_x}^2} + \frac{1}{\lambda_{yn_y}^2} + \frac{1}{\lambda_{zn_z}^2} \right) = \frac{\hbar^2}{2m} (k_{xn_x}^2 + k_{yn_y}^2 + k_{zn_z}^2) = \frac{\hbar^2 \mathbf{k}_{n_x, n_y, n_z}^2}{2m}$$

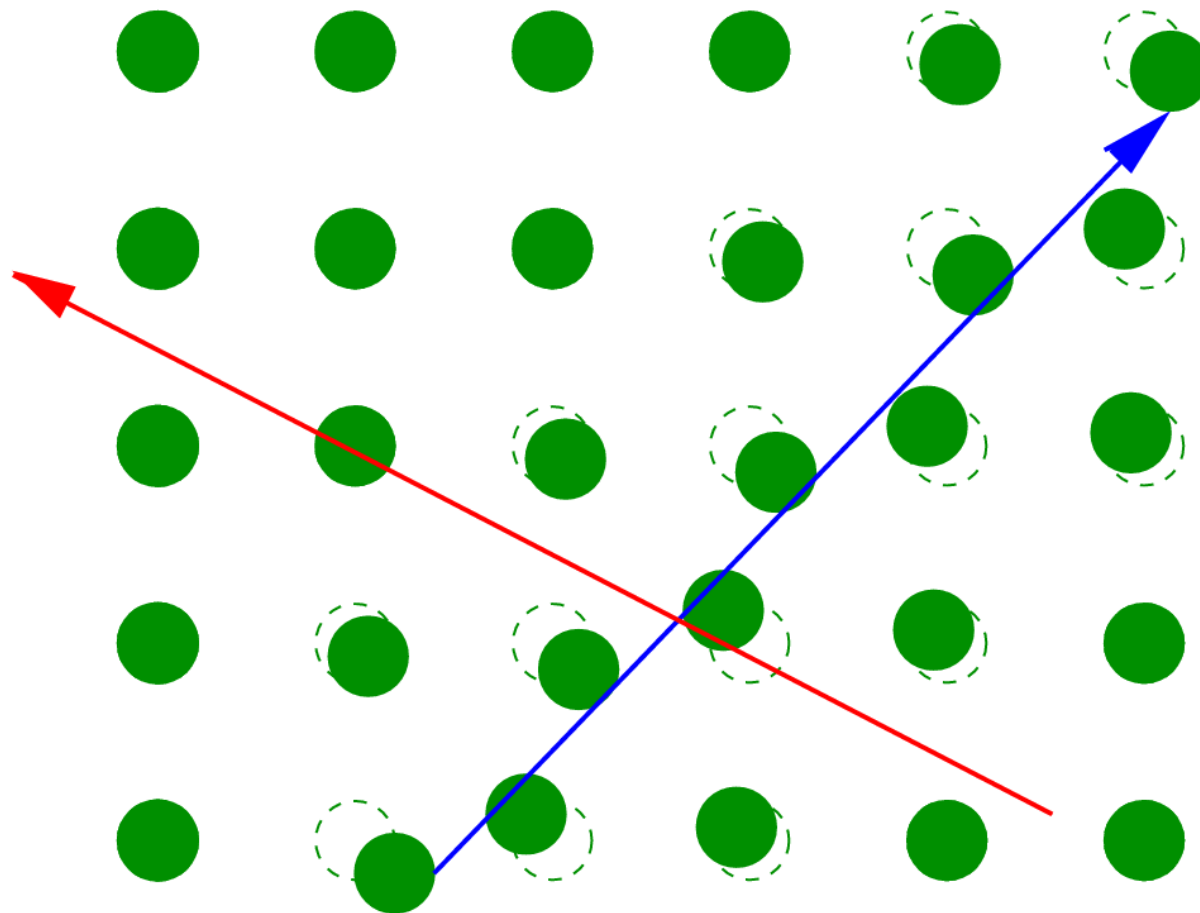
Mříž reprezentující množinu elektronových stavů, Fermiho plocha apod.



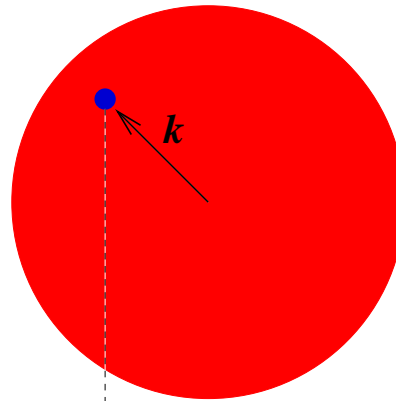
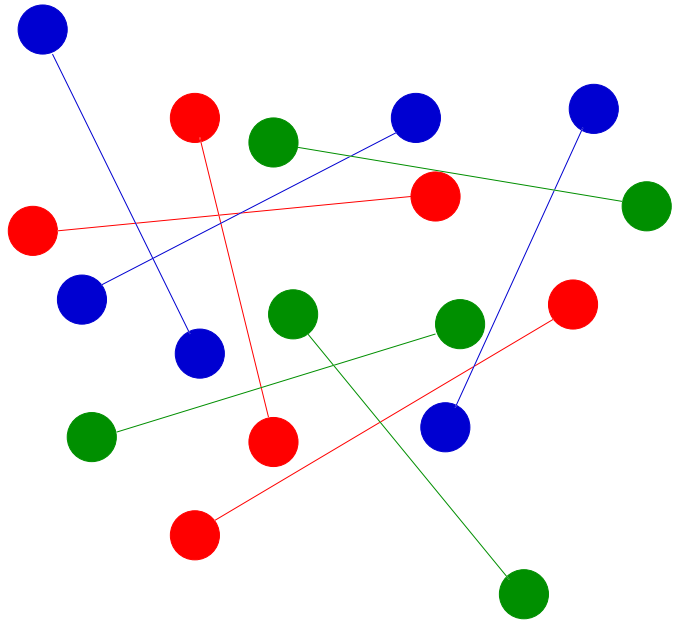


Schematické znázornění mechanismu přitažlivé elektron- elektronové interakce

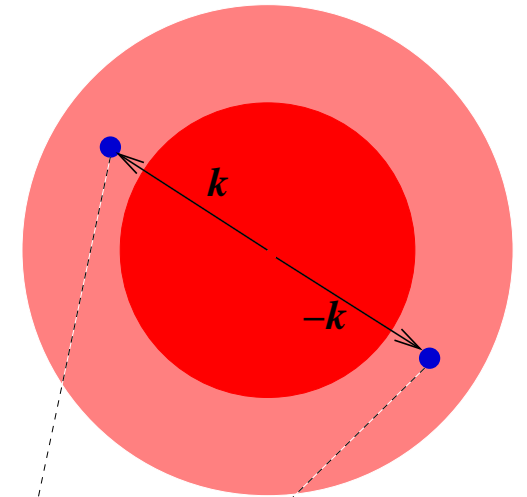
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# Schematické znázornění základního stavu teorie BCS



$$\boxed{k \uparrow \bullet \quad k \downarrow \bullet}$$



$$u_k \boxed{k \uparrow \circ \quad -k \downarrow \circ} + v_k \boxed{k \uparrow \bullet \quad -k \downarrow \bullet}$$

$$u_k \boxed{-k \uparrow \circ \quad k \downarrow \circ} + v_k \boxed{-k \uparrow \bullet \quad k \downarrow \bullet}$$

$$0 < u_k < 1$$

$$0 < v_k < 1$$

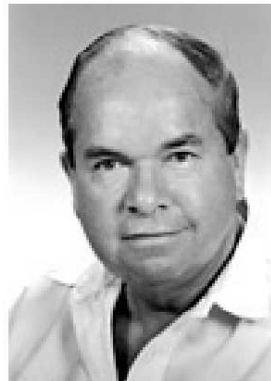
# Nobelova cena za fyziku v roce 2003

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## The Nobel Prize in Physics 2003

"for pioneering contributions to the theory of superconductors and superfluids"



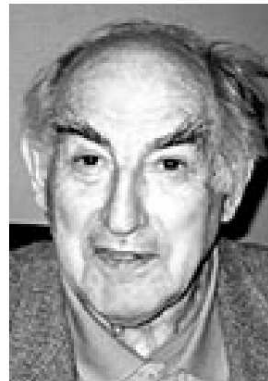
**Alexei A. Abrikosov**

🏆 1/3 of the prize

USA and Russia

Argonne National  
Laboratory  
Argonne, IL, USA

b. 1928



**Vitaly L. Ginzburg**

🏆 1/3 of the prize

Russia

P.N. Lebedev Physical  
Institute  
Moscow, Russia

b. 1916



**Anthony J. Leggett**

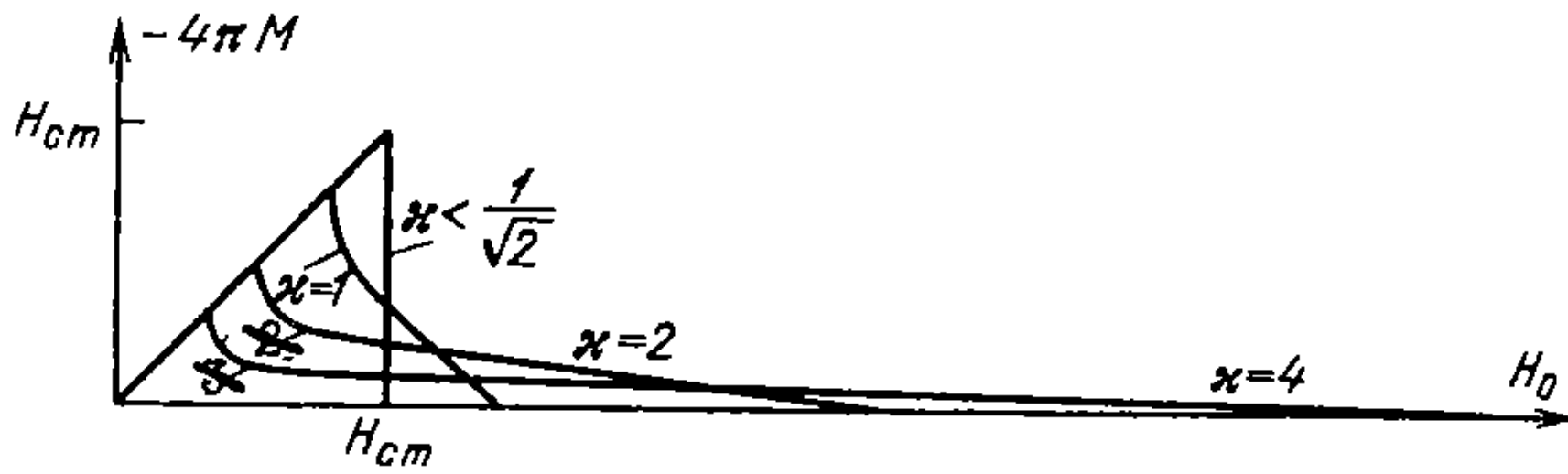
🏆 1/3 of the prize

United Kingdom and  
USA

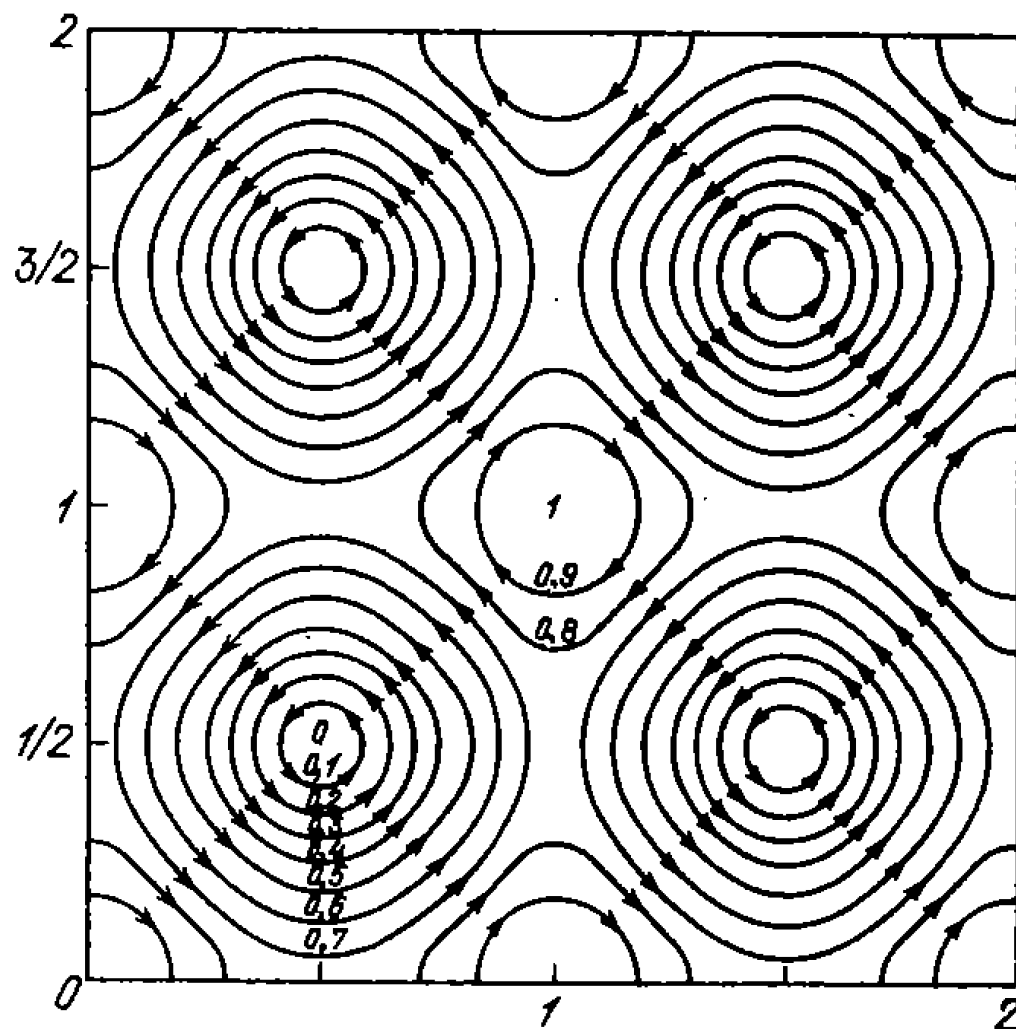
University of Illinois  
Urbana, IL, USA

b. 1938

Teoretická závislost magnetizace na přiloženém magnetickém poli

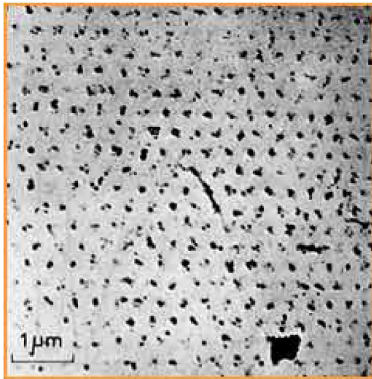


# Abrikosovova mřížka



# Vírové mřížky I

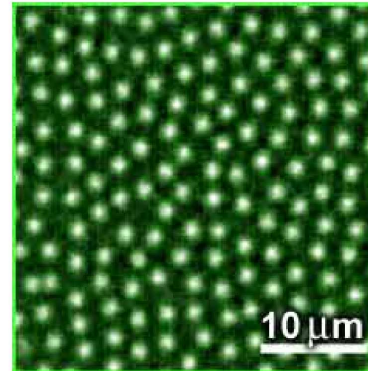
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First image of Vortex lattice, 1967

Bitter Decoration  
Pb-4at%In rod, 1.1K, 195G

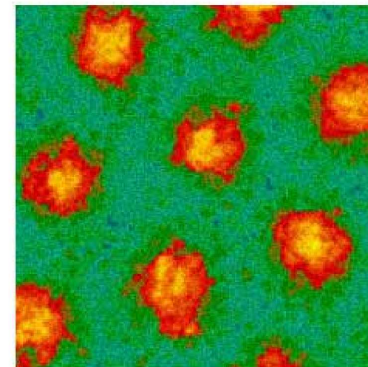
U. Essmann and H. Trauble  
Max-Planck Institute, Stuttgart  
[Physics Letters 24A, 526 \(1967\)](#)



Magneto-optical image of Vortex lattice, 2001

Magneto-Optical Imaging  
NbSe<sub>2</sub> crystal, 4.3K, 3G

P.E. Goa et al.  
University of Oslo  
[Supercond. Sci. Technol. 14, 729 \(2001\)](#)



Vortices in MgB<sub>2</sub>, 2002

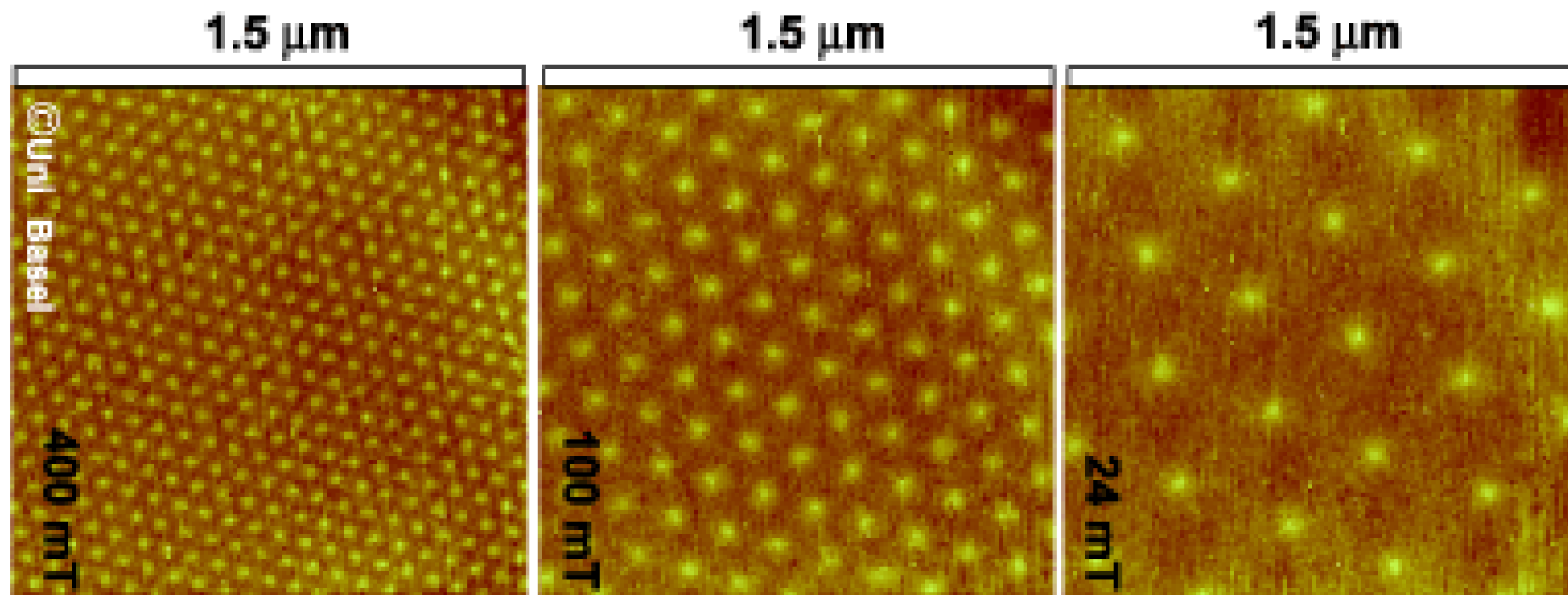
Scanning Tunnel Spectroscopy  
MgB<sub>2</sub> crystal, 2K, 2000G

M. R. Eskildsen et al.  
University of Geneva  
[Phys. Rev. Lett. 89, 187003 \(2002\)](#)



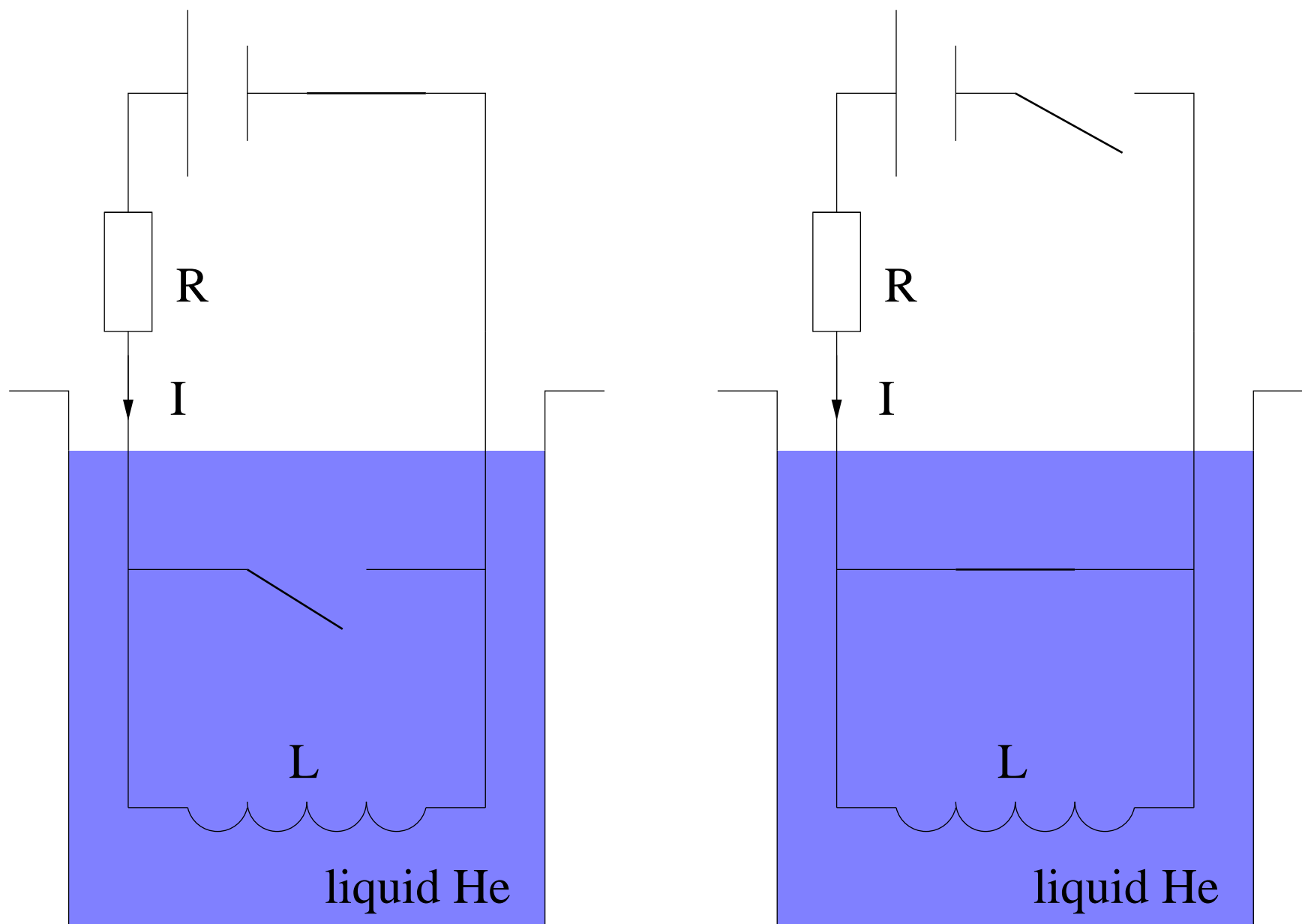
## Vírové mřížky II

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# Nabuzení supravodivého magnetu

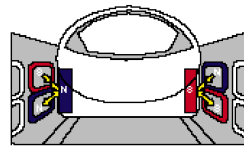


# Maglev

## Principle of Maglev

Maglev is a system in which the vehicle runs levitated from the guideway (corresponding to the rail tracks of conventional railways) by using electromagnetic forces between superconducting magnets on board the vehicle and coils on the ground. The following is a general explanation of the principle of Maglev.

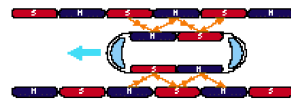
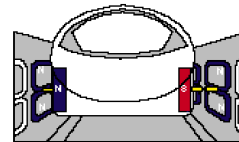
### Principle of magnetic levitation



The "8" figured levitation coils are installed on the sidewalls of the guideway. When the on-board superconducting magnets pass at a high speed about several centimeters below the center of these coils, an electric current is induced within the coils, which then act as electromagnets temporarily. As a result, there are forces which push the superconducting magnet upwards and ones which pull them upwards simultaneously, thereby levitating the Maglev vehicle.

### Principle of lateral guidance

The levitation coils facing each other are connected under the guideway, constituting a loop. When a running Maglev vehicle, that is a superconducting magnet, displaces laterally, an electric current is induced in the loop, resulting in a repulsive force acting on the levitation coils of the side near the car and an attractive force acting on the levitation coils of the side farther apart from the car. Thus, a running car is always located at the center of the guideway.



### Principle of propulsion

A repulsive force and an attractive force induced between the magnets are used to propel the vehicle (superconducting magnet). The propulsion coils located on the sidewalls on both sides of the guideway are energized by a three-phase alternating current from a substation, creating a shifting magnetic field on the guideway. The on-board superconducting magnets are attracted and pushed by the shifting field, propelling the Maglev vehicle.

## Supravodivé magnety pro studium NMR a pro LHC

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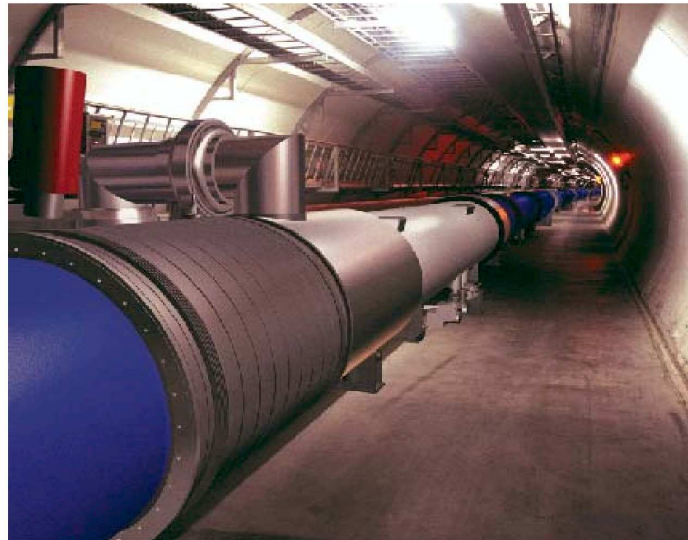


(a)



(b)

**Figure 3.** Magnets for (a) NMR 900 MHz, superfluid helium cooled and (b) full-body MRI, liquid helium bath cooled with active shield refrigeration (Bruker)



**Figure 4.** View of the Large Hadron Collider (LHC), a high-energy particle accelerator with superfluid-helium cooled superconducting magnets in construction at CERN

# Nobelova cena za fiziku v roce 1973

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## The Nobel Prize in Physics 1973

"for their experimental discoveries regarding tunneling phenomena in semiconductors and superconductors, respectively"

"for his theoretical predictions of the properties of a supercurrent through a tunnel barrier, in particular those phenomena which are generally known as the Josephson effects"



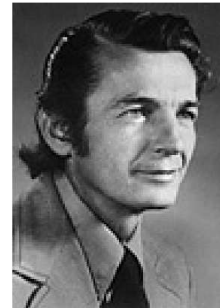
**Leo Esaki**

🏆 1/4 of the prize

Japan

IBM Thomas J. Watson  
Research Center  
Yorktown Heights, NY,  
USA

b. 1925



**Ivar Giaever**

🏆 1/4 of the prize

USA

General Electric  
Company  
Schenectady, NY, USA

b. 1929  
(in Bergen, Norway)



**Brian David  
Josephson**

🏆 1/2 of the prize

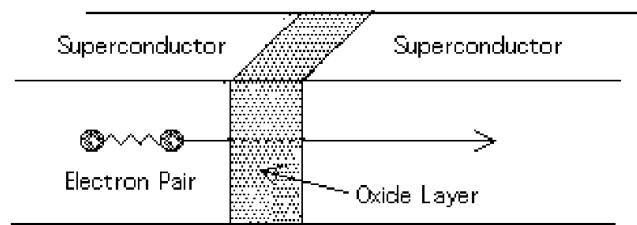
United Kingdom

University of Cambridge  
Cambridge, United  
Kingdom

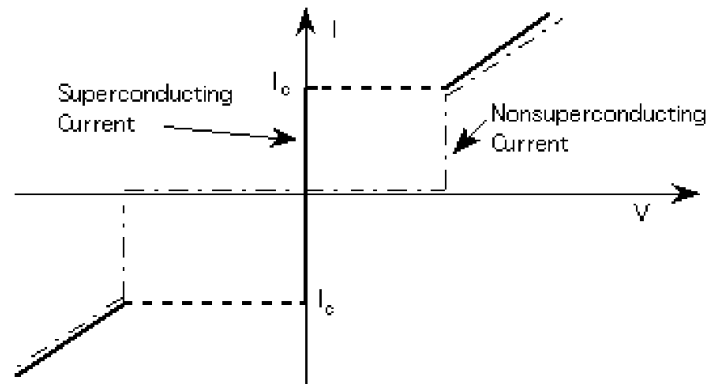
b. 1940

# Josephsonovy jevy

Josephson Effect



Josephson Junction



$$\psi_1 = |\psi_1| e^{i\phi_1}$$

$$\psi_2 = |\psi_2| e^{i\phi_2}$$

$$j = j_c \sin(\Delta\phi)$$

Na p echodu nap tí V:  $\longrightarrow$  St ídavý proud o frekvenci  
 $\Delta\phi = \text{konst} + 2eVt/\hbar$   $f = 2eV/h$

1 V = nap tí pot ebné pro vznik proudu o frekvenci 483 597.9 GHz.

# Supravodivý kvantový interferometr

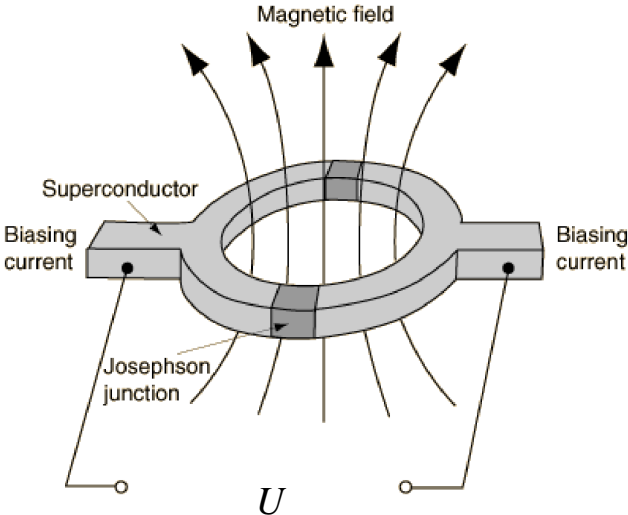


Figure 2: Neuromag Ltd. 122 MEG system

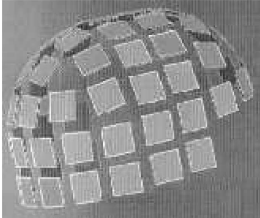


Figure 3: Neuromag Ltd. 122 sensor array

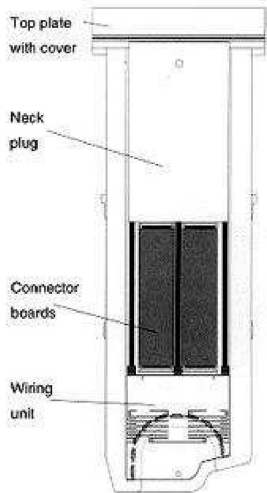


Figure 4: Neuromag Ltd. 122 probe



## The Nobel Prize in Physics 1987

"for their important break-through in the discovery of superconductivity in ceramic materials"



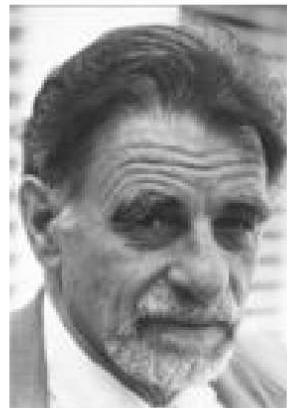
**J. Georg Bednorz**

🏆 1/2 of the prize

Federal Republic of Germany

IBM Zurich Research Laboratory  
Rüschlikon, Switzerland

b. 1950



**K. Alexander Müller**

🏆 1/2 of the prize

Switzerland

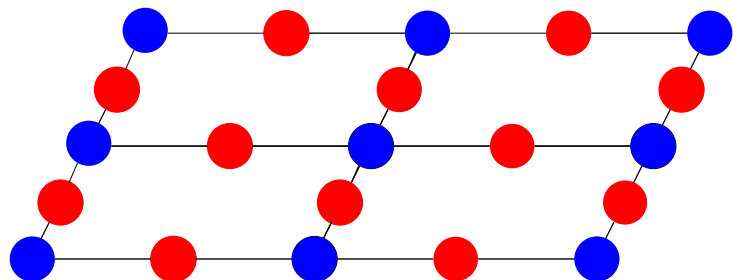
IBM Zurich Research Laboratory  
Rüschlikon, Switzerland

b. 1927

# Krystalová struktura HTCS



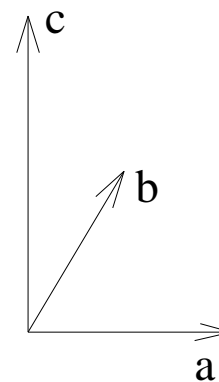
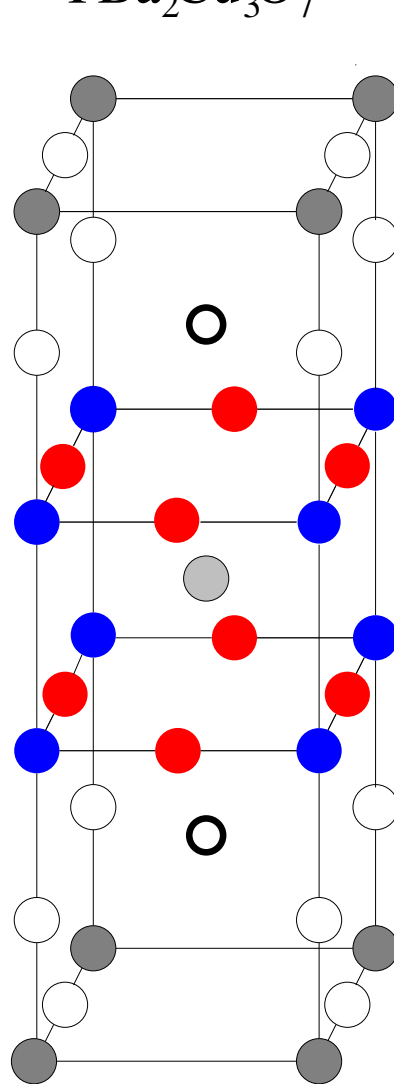
$\text{CuO}_2$  plane



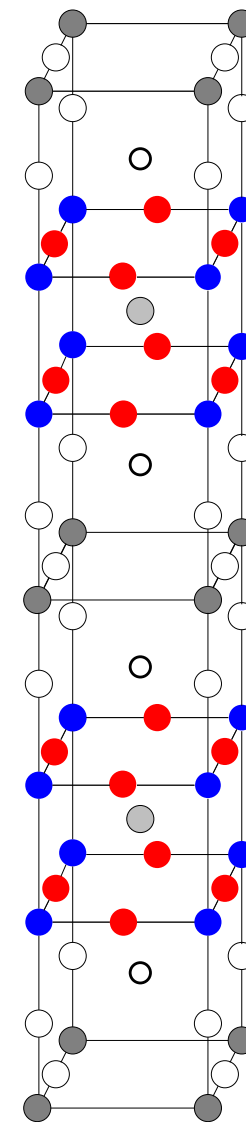
O, Cu in the  $\text{Cu}_2\text{O}$  planes

$3d^9 - 3d^8$

$2p^6$

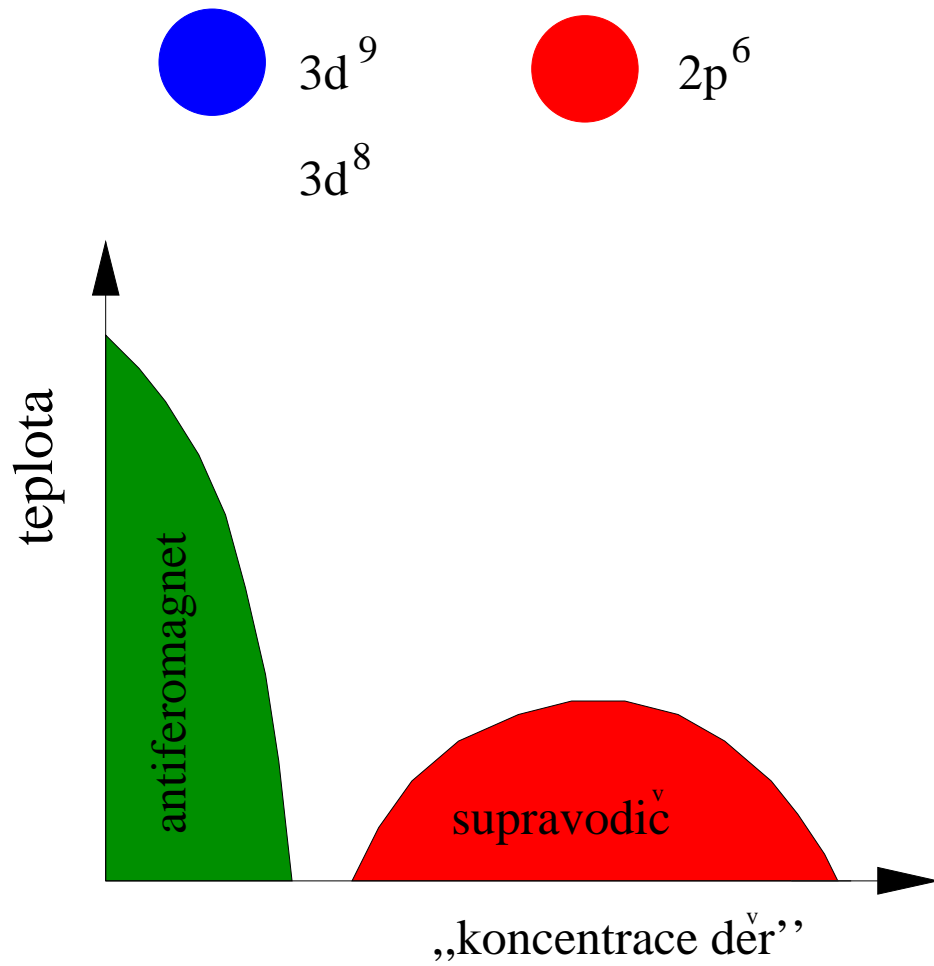


- O
- Cu
- Y
- Ba

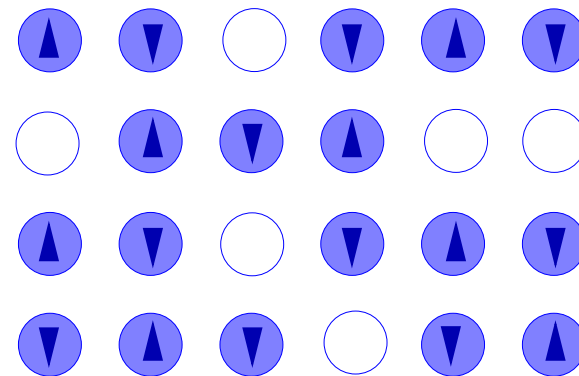
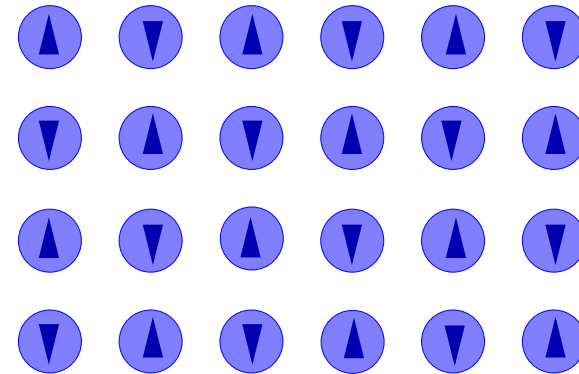




# Fázový diagram



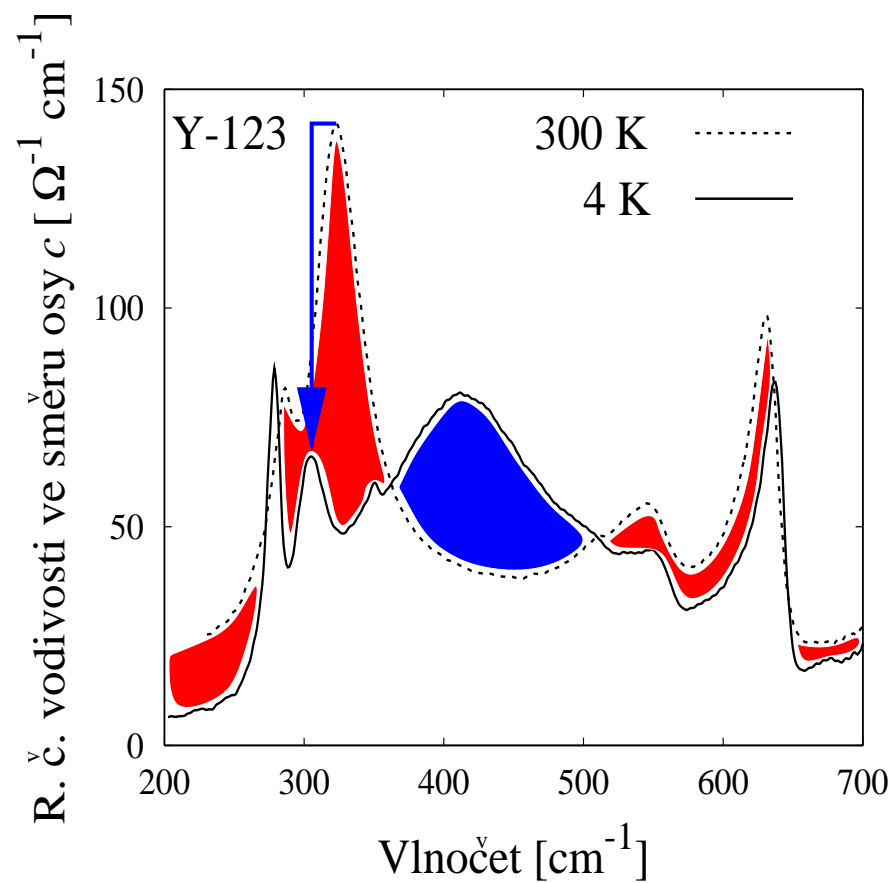
Antiferomagnet



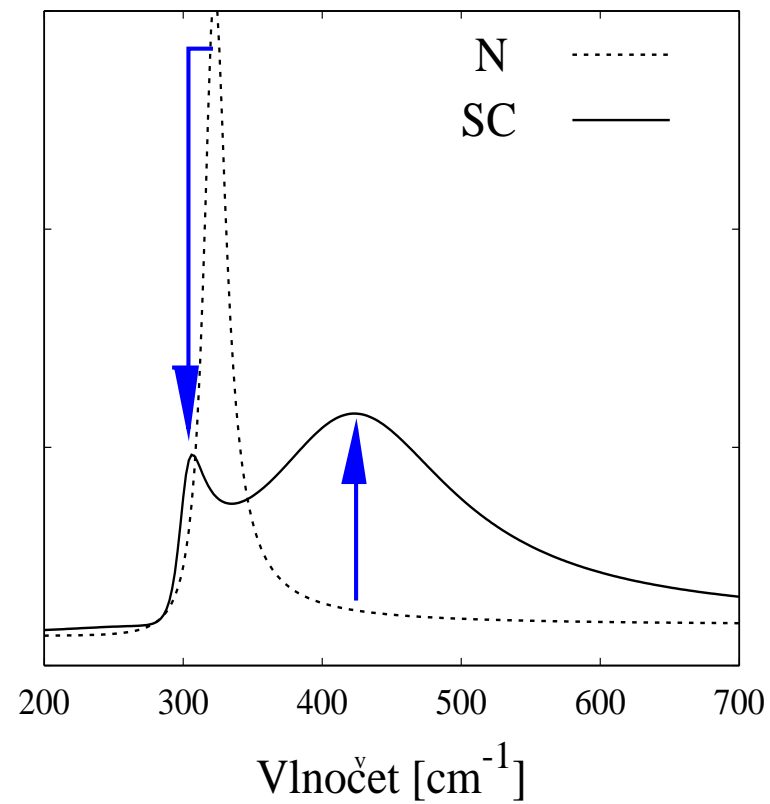
Supravodič<sup>v</sup>

?

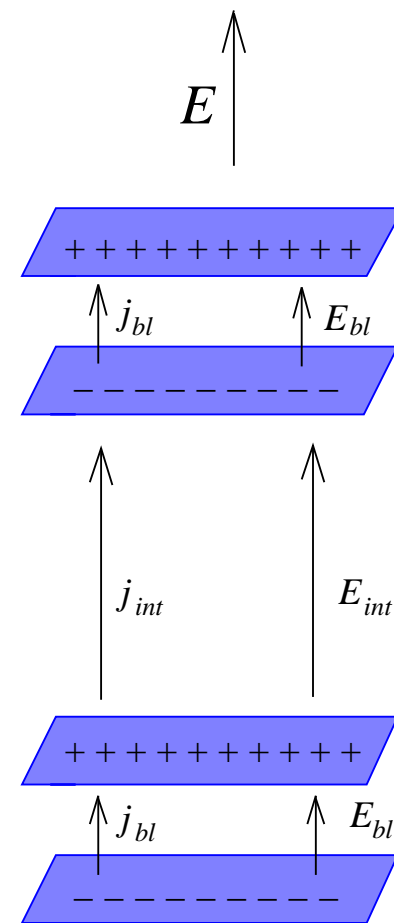
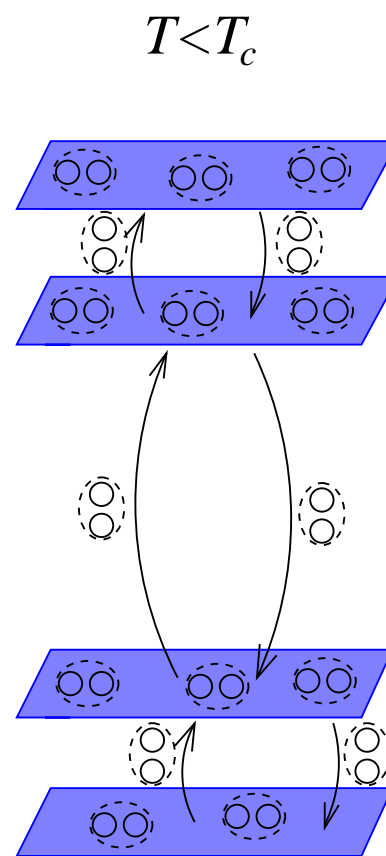
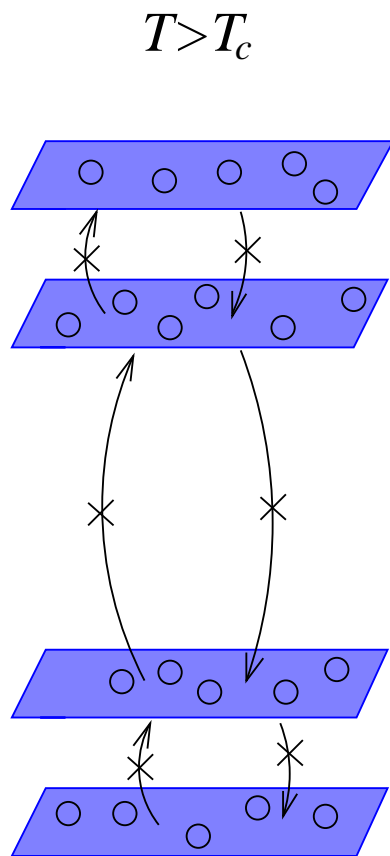
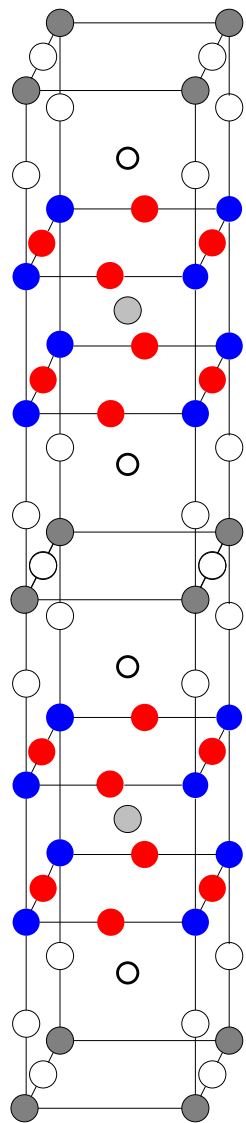
### Experiment

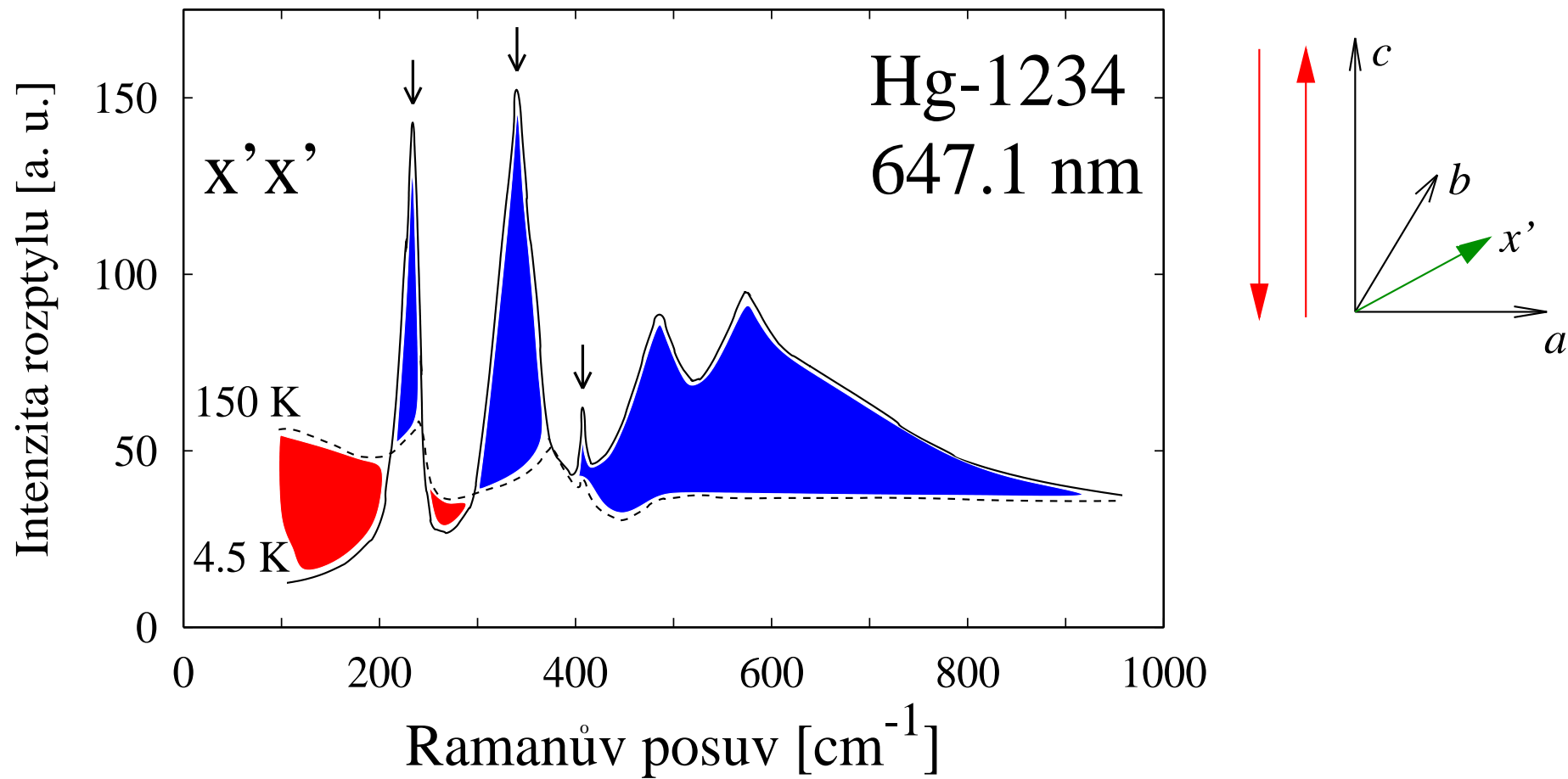


### Teorie

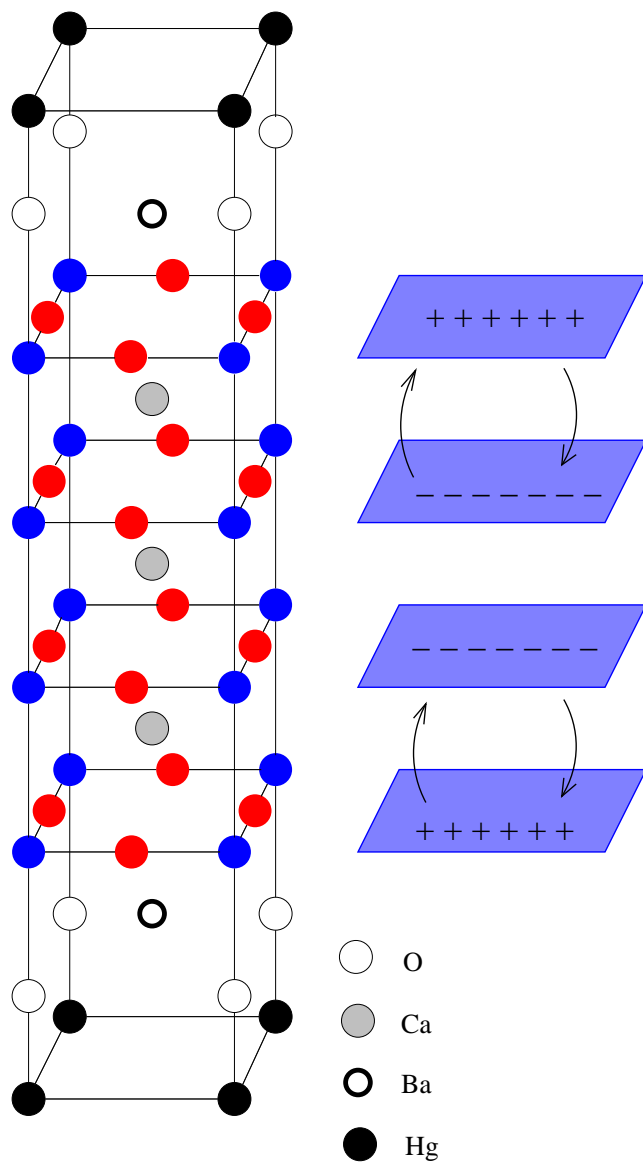


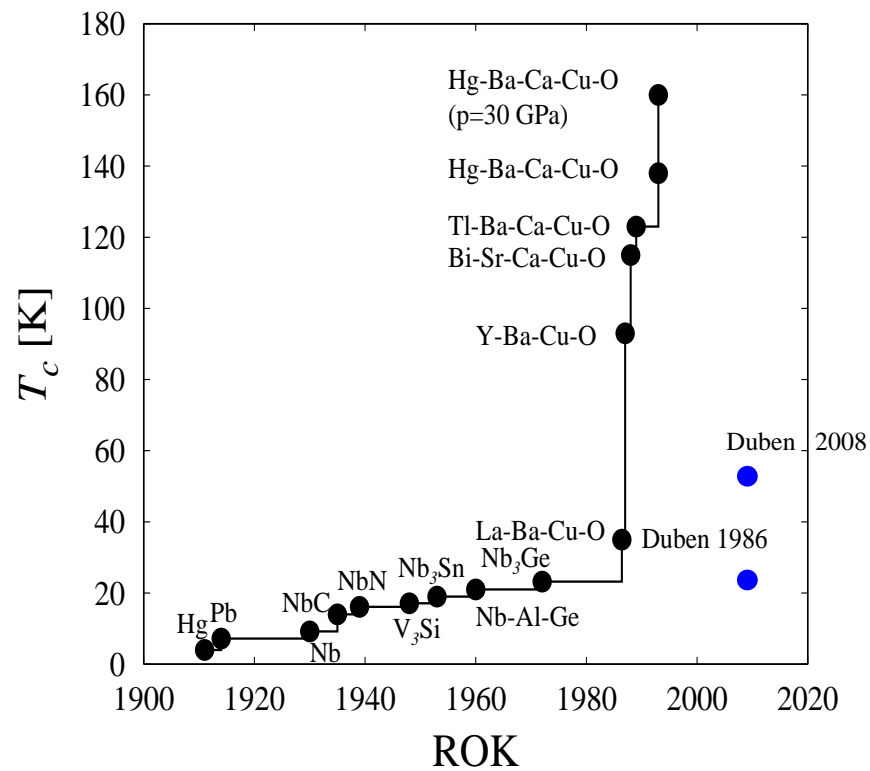
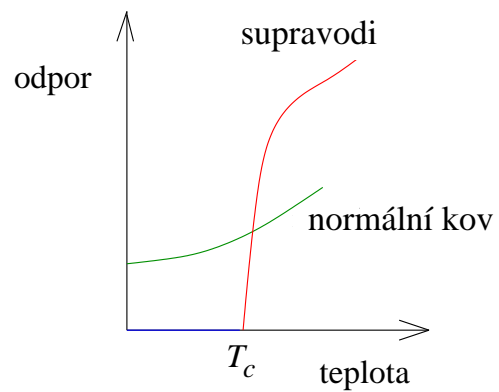
# Anomálie v optické odezvě - schematické vysvětlení





# Anomálie ve spektrech intenzity Ramanova rozptylu - schematické vysvětlení





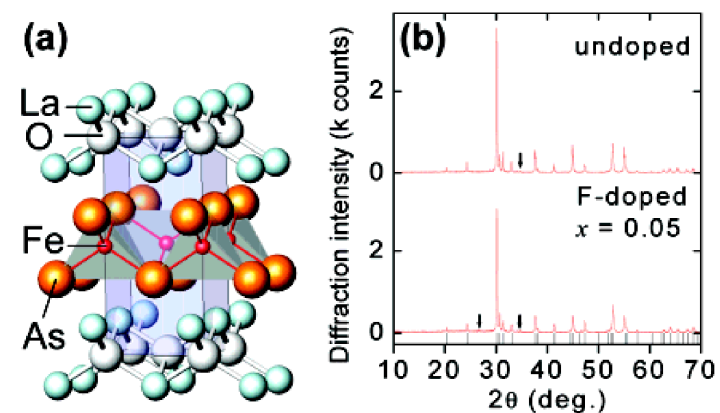
## Iron-Based Layered Superconductor $\text{La}[\text{O}_{1-x}\text{F}_x]\text{FeAs}$ ( $x = 0.05\text{--}0.12$ ) with $T_c = 26$ K

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Discovery of the copper-based superconductor  $\text{La}_{2-x}\text{Ba}_x\text{CuO}_4$ <sup>1</sup> with a high transition temperature ( $T_c$ ) triggered extensive research with the intention of developing new transition-metal-based superconductors.<sup>2,3</sup> Currently, high  $T_c$  superconductors are limited to layered perovskites that contain  $\text{CuO}_2$  structural units as the conduction layers. However, the  $T_c$  of the non-Cu-based superconductors in this category has remained low, although spin triplet superconductivity has been found in  $\text{UPt}_3$  ( $T_c \sim 0.54$  K)<sup>4</sup> and  $\text{Sr}_2\text{RuO}_4$  ( $T_c \sim 1.4$  K).<sup>5,6</sup> Here, we report a layered iron-based compound,  $\text{LaOFeAs}$ , which undergoes superconducting transition under doping with  $\text{F}^-$  ions at the  $\text{O}^{2-}$  site. Its  $T_c$  exhibits a trapezoidal shape dependence on  $\text{F}^-$  content, with the highest  $T_c$  of  $\sim 26$  K at 5–11 atom %. Further, its magnetic susceptibility indicates that F-doped  $\text{LaOFeAs}$  exhibits Curie–Weiss-like behavior in the normal conducting state.



**Figure 1.** (a) Crystal structure of  $\text{LaOFeAs}$ . (b) Powder XRD patterns of undoped  $\text{LaOFeAs}$  and  $\text{La}[\text{O}_{1-x}\text{F}_x]\text{FeAs}$ :  $x = 0.05$ . Black bars at bottom show calculated Bragg diffraction positions of  $\text{LaOFeAs}$ . Arrows denote peaks due to impurity phases, FeAs (helimagnetic),<sup>13</sup> and LaOF.

# FeAs

