

# Factors influencing the recession rate of Niagara Falls since the 19th century

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## ABSTRACT

The rate of recession of Niagara Falls (Horseshoe and American Falls) in northeastern North America has been documented since the 19th century; it shows a decreasing trend from ca.  $1 \text{ m y}^{-1}$  a century ago to ca.  $0.1 \text{ m y}^{-1}$  at present. Reduction of the flow volume in the Niagara River due to diversion into bypassing hydroelectric schemes has often been taken to be the factor responsible, but other factors such as changes in the waterfall shape could play a role and call for a quantitative study. Here, we examine the effect of physical factors on the historically varying recession rates of Niagara Falls, using an empirical equation which has previously been proposed based on a non-dimensional multiparametric model which incorporates flow volume, waterfall shape and bedrock strength. The changes in recession rates of Niagara Falls in the last century are successfully modeled by this empirical equation; these changes are caused by variations in flow volume and lip length. This result supports the validity of the empirical equation for waterfalls in rivers carrying little transported sediment. Our analysis also suggests that the decrease in the recession rate of Horseshoe Falls is related to both artificial reduction in river discharge and natural increase in waterfall lip length, whereas that of American Falls is solely due to the reduction in flow volume.

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## 1. Introduction

Waterfalls, a typical form of knickpoint or knickzone, are commonly observed in bedrock rivers across the world, including active orogens, volcanic areas and glacially- or tectonically-deformed areas (Gilbert, 1907; von Engeln, 1940; Derricourt, 1976; Bishop et al., 2005; Crosby and Whipple, 2005; Hayakawa and Oguchi, 2006, in press; Lamb et al., 2007). Headward erosion of waterfalls, often referred to as recession, is one of the central themes in fluvial geomorphology because the rates of waterfall recession are usually much greater than the other erosional processes involving bedrock rivers, such as incision of the entire riverbed (Begin et al., 1980; Kukul, 1990; Wohl, 1998, 2000; Hayakawa and Matsukura, 2002). Bedrock erosion at waterfalls can be significant even if rivers lack transported sediment to act as a tool of abrasion, probably due to the frequent occurrence of plucking and/or cavitation by rapid stream flows including jet flows (Barnes, 1956; Young, 1985; Bishop and Goldrick, 1992; Whipple et al., 2000; Pasternack et al., 2006). Niagara Falls is a famous waterfall in northeastern North America that has long been studied by geologists and geomorphologists (Gilbert, 1907; Spencer, 1907; Tinkler, 1987). Historical changes of the waterfall shape are well documented, especially in the last 200 years, and the actual recession rates in that period are well known. The long-term average recession rate of Niagara Falls is estimated to have been ca.  $1 \text{ m y}^{-1}$  during the Holocene (e.g., Gilbert, 1907; Ford, 1968), but it has decreased to the

order of  $0.1\text{--}0.01 \text{ m y}^{-1}$  in recent decades (Tinkler, 1993). The slowing of the waterfall recession rate is commonly attributed to the reduction in water flow over the waterfall as a result of the construction of several large power plants in the river (e.g., Tinkler, 1993, 1994). These plants divert water well above the falls and return it to the Niagara River well below the falls. The shape of the falls in plan has also changed during the recession process, and the curved shape of the waterfall crest (the 'horseshoe' shape) is supposed to be more stable in its stress distribution and thereby decreases the recession rate (Philbrick, 1970). The greater length of the curved lip may also cause the stream to be shallower with less tractive force at the lip, also reducing the recession rate, although the effects of lip length on the recession of Niagara Falls are yet to be quantified. Here we quantitatively examine the recession rate of Niagara Falls based on a previously proposed model, which estimates the waterfall recession rate from relevant physical parameters including the stream discharge (total flow) and waterfall shape.

## 2. Existing record of recession rates of Niagara Falls

Niagara Falls is located in the middle portion of the Niagara River, draining northward from Lake Erie to Lake Ontario (Fig. 1). The water of the Niagara River is supplied from the upstream Great Lakes, of glacial origin, and the stream discharge is controlled mainly by the water level in the lakes, not by immediate precipitation. The climate in the area is relatively cold, with active frost weathering of bare rocks exposed along the river from winter to spring.

The waterfall originally formed at the Niagara Escarpment running west to east between the lakes, when the Laurentide ice sheet had

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Fig. 1. Study site. Niagara Falls at present comprises two major falls, Horseshoe Falls and American Falls.

receded and the river started draining over the escarpment approximately 12,500 years ago (Tinkler et al., 1994). Since then the waterfall has receded for ca. 11 km, leaving a deep narrow gorge downstream, called the Great Gorge. The long-term mean recession rate of the waterfall is therefore approximately  $1 \text{ m y}^{-1}$ , although the rate was considerably lower for about 5000 years during 10,500–5500 yBP (ca.  $0.1 \text{ m y}^{-1}$  at minimum), due to the abrupt decrease of flow caused by water level lowering and changes in stream courses in the upstream lakes (Lewis and Anderson, 1989; Tinkler et al., 1994). The mean recession rate prior to that interval was similar to that after 5500 yBP (ca.  $1.6 \text{ m y}^{-1}$ ).

Niagara Falls at present consists of several falls, due to diversion of the stream slightly upstream of the site. The largest fall in the western Canadian side, named Canadian or Horseshoe Falls and henceforth referred to as the Horseshoe, has a horizontal curved 762-m-long rim, slightly overhanging face, and a single uninterrupted fall of water with a 51-m height. Another fall at the eastern side, named American Falls, has a relatively straight rim with a length of 335 m. The face of American Falls is nearly vertical but there is no overhang and the lower portion is filled with fallen rock blocks, like talus deposit, for nearly half of its total height of 54 m.

Changes to Niagara Falls during historical times have been recorded in various documents since the 1600s. The early records were provided simply as artists' pictures, but since the 19th century detailed topographic measurements have been conducted by geologists. Philbrick (1970) gave a detailed summary of the changes in horizontal morphology of Niagara Falls based on the literature, so that we can see the dimensions of the waterfalls in the past (Fig. 2). The lip

length of the Horseshoe has increased dramatically as its horizontal shape became progressively more curved over recent centuries, whereas that of the American Falls has merely changed. The height

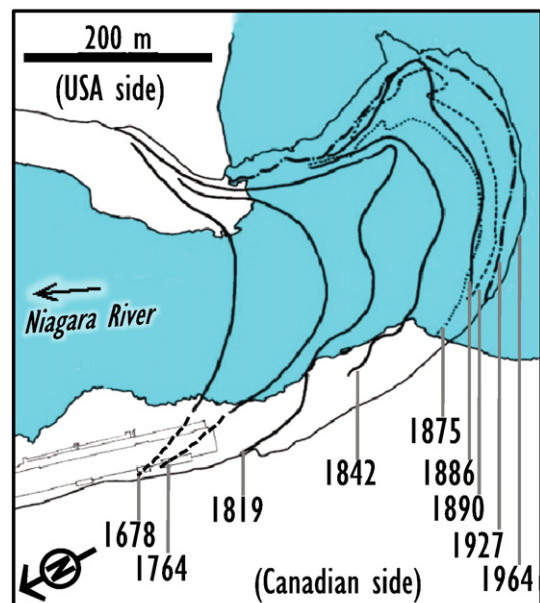


Fig. 2. Historical changes of the plan shape of Horseshoe Falls (after Philbrick, 1970).

of Niagara Falls has scarcely changed since its formation in the Holocene, as suggested by the constant height of the Great Gorge.

Since the late 19th century, diversion of water to hydroelectric power plants has caused a severe reduction in water flowing over Niagara Falls (Tiplin, 1988). The flow is now regularized to prevent shortages of flowing water for tourists. The changing flow in the river has been documented in the literature (e.g., International Joint Commission, 1953). The presence of Goat Island between Horseshoe and American Falls causes 90% of the river water to pass over the Horseshoe and 10% over American Falls.

The recession rate of Niagara Falls, the Horseshoe Falls in particular, has been precisely recorded in the last century (Gilbert, 1907; Philbrick, 1970; Tinkler, 1987). The largest recession rate of the Horseshoe was reported by Gilbert (1907) to be  $2.0 \text{ m y}^{-1}$  in 1875–1905, whereas the average rate in this period was about  $1.3 \text{ m y}^{-1}$  (International Joint Commission, 1953). The rate has progressively decreased due to the building of power plants during the past century (International Joint Commission, 1953; Table 1), and the current rate is supposed to be less than  $0.1 \text{ m y}^{-1}$  although no certain record is available for the recent recession (Tinkler, 1993, 1994).

The rate of recession of American Falls is much less than the Horseshoe. Gilbert (1907) inferred that the recession rate of American Falls had been about  $0.1 \text{ m y}^{-1}$  for hundreds of years. The modern rate is assumed to be of the order of  $0.01 \text{ m y}^{-1}$  (Tinkler, 1993, 1994).

### 3. Estimating waterfall recession rates from empirical equations

#### 3.1. An empirical equation for estimating waterfall recession rates

To quantify the effects of flow and lip length on the recession rate of Niagara Falls, we use a previously proposed model which estimates the relationship between the waterfall recession rate and relevant physical parameters, namely erosive force and bedrock strength (Hayakawa and Matsukura, 2003a). Supposing that the rate of waterfall recession depends on the erosional force of the stream and the strength of the resisting bedrock, dimensional analysis finds a dimensionless index, *FR*, based on these variables:

$$FR = \frac{AP}{WH} \sqrt{\frac{\rho}{S_c}} \quad (1)$$

where  $A \text{ (L}^2\text{)}$  is the upstream drainage area of a waterfall;  $P \text{ (L T}^{-1}\text{)}$  is the mean annual precipitation in the drainage basin, so that the product of  $A$  and  $P$  accounts for the annual stream flow over the waterfall;  $W \text{ (L)}$  and  $H \text{ (L)}$  are the width (lip length) and height of the waterfall,  $\rho \text{ (M L}^{-3}\text{)}$  is the water density, and  $S_c \text{ (M L}^{-1} \text{ T}^{-2}\text{)}$  is the unconfined compressive strength of bedrock. The dimensionless index *FR* represents the balance between the erosional force and bedrock resistance as a whole, where all these parameters are given in the SI unit.

**Table 1**  
Actual recession rates of Horseshoe Falls and American Falls over differing time periods.

	Duration		Recession rate $E \text{ (m y}^{-1}\text{)}$	Source
Horseshoe Falls	1842–1875	(H1)	1.2–1.3	Gilbert, 1907; International Joint Commission, 1953
	1875–1905	(H2)	1.3–2.0	Gilbert, 1907; International Joint Commission, 1953
	1905–1927	(H3)	0.98	International Joint Commission, 1953
	1927–1950	(H4)	0.67	International Joint Commission, 1953
	1950–2000	(H5)	0.1	Tinkler, 1993, 1994
	Modern	(H6)	0.1	Tinkler, 1993, 1994
American Falls	500 y (–1905)	(A1)	0.098	Gilbert, 1907
	Modern	(A2)	0.01	Tinkler, 1993, 1994

**Table 2**  
Historical changes in flow discharge over Niagara Falls.

Duration	Discharge over Niagara Falls ( $\text{m}^3 \text{ s}^{-1}$ ) (100%)	Discharge over Horseshoe Falls ( $\text{m}^3 \text{ s}^{-1}$ ) (90%)	Discharge over American Falls ( $\text{m}^3 \text{ s}^{-1}$ ) (10%)
1842–1905	5760	5184	576
1905–1927	4147	3732	415
1927–1950	3456	3110	346
1950–present	1770	1593	177

Examination of the relationship between the *FR* index and the waterfall recession rate, *E*, using data for waterfalls in the Boso Peninsula of eastern Japan gives the following equation (Hayakawa and Matsukura, 2003a):

$$E = 99.7FR^{0.73} = 99.7 \left( \frac{AP}{WH} \sqrt{\frac{\rho}{S_c}} \right)^{0.73} \quad (2)$$

This equation has been found to give good order-of-magnitude estimates of waterfall recession rates in many areas (Hayakawa and Matsukura, 2003b; Hayakawa, 2005; Hayakawa and Wohl, 2005; Hayakawa et al., 2005, 2008a), with the exception of rivers carrying abundant transported sediments (Hayakawa et al., 2008b, 2009).

As the proxy of discharge in the *FR* index,  $A$  and  $P$  have been individually measured in previous studies, because direct measurement data of the discharge is not available for most waterfalls. Fortunately, the stream discharge has long been measured in the Niagara River. The flow volume of the Niagara is stable in normal conditions, because it depends on the water budget in the Great Lakes, which is too large to be significantly affected by individual storms and other local and short-term climatic events (Tinkler, 1993). For the same reason, estimation of the discharge of the Niagara River from drainage area and precipitation is inappropriate. We therefore use stream discharge,  $Q \text{ (L}^3 \text{ T}^{-1}\text{)}$ , for the *FR* index, instead of the product of  $A$  and  $P$ . Eqs. (1) and (2) become:

$$FR = \frac{Q}{WH} \sqrt{\frac{\rho}{S_c}} \quad (3)$$

and

$$E = 99.7FR^{0.73} = 99.7 \left( \frac{Q}{WH} \sqrt{\frac{\rho}{S_c}} \right)^{0.73} \quad (4)$$

#### 3.2. Data acquisition and model applications

The present water discharge over Niagara Falls is controlled artificially, based on an international agreement between Canada and the US made in 1953. The regulated flow discharge is  $2832 \text{ m}^3 \text{ s}^{-1}$  in summer daytime (0800 to 2200 h from April 1st to September 15th and 0800 to 2000 h from September 16th to October 31st), and half of that value ( $1416 \text{ m}^3 \text{ s}^{-1}$ ) at all other times. The annual-mean flow discharge at present is therefore  $1770 \text{ m}^3 \text{ s}^{-1}$ , which is 30% of the natural flow level of ca.  $5760 \text{ m}^3 \text{ s}^{-1}$  until a century ago (Tinkler, 1993). The present annual-mean discharge over the Horseshoe is  $1593 \text{ m}^3 \text{ s}^{-1}$  (90% of the Niagara River discharge) and that over American Falls is  $177 \text{ m}^3 \text{ s}^{-1}$  (10%).

Since water was first diverted through hydroelectric power plants in the late 19th century, the water discharge over the waterfalls was progressively reduced, until the Canada–USA treaty was agreed in 1953. The discharge was reported to be  $4147 \text{ m}^3 \text{ s}^{-1}$  (72% of natural flow) in 1905–1927, and  $3456 \text{ m}^3 \text{ s}^{-1}$  (60%) in 1927–1950 (International Joint Commission, 1953). Table 2 summarizes the historical changes of flow volume over Horseshoe and American Falls.

**Table 3**  
Historical changes in lip length of Horseshoe Falls.

Year	Lip length (m)
1819	473
1842	420
1875	501
1886	586
1890	614
1927	626
1964	723
2000	762

Lip lengths of the Horseshoe in differing years have been obtained by measuring the lengths of its past crest lines on the map by Philbrick (1970), on which the development of the shape of Niagara Falls is well documented (Fig. 2). Lines based on topographic measurement surveys have been available since 1678, but only the lines after 1819 are used because the left end of the lines in 1678 and 1764 are unclear. The lip length of the Horseshoe has increased in recent times from 420 m in 1842 to 762 m in 2000 as the profile becomes more curved (Table 3).

To estimate the intact rock strength of the waterfalls, Schmidt hammer (N-type) measurements were made using the repeated impact method, which involves averaging over 20 impacts at each point after eliminating outliers (Hucka, 1965; Matsukura and Tanaka, 2000; Matsukura and Aoki, 2004). Since the waterfall consists of two major different rock layers, dolomite and shale, the Schmidt hammer rebound values,  $R_N$  (%), of both rocks are measured at several locations around the waterfall. The rocks close to the waterfall are generally fresh, but those exposed along the walls of the Great Gorge are commonly weathered, probably by freeze-thaw processes. The measured Schmidt hammer rebound values are summarized for each rock type and weathering conditions in Table 4. Although the dolomite layer along the Gorge, forming the caprock structure of the waterfall, has been considered to be much harder than the shale layer, no significant differences were found between dolomite and shale, whereas differences were much clearer between fresh and weathered conditions (Table 4). The Schmidt hammer rebound values may include the effects of joints or anisotropy of the bedding planes in the shale at least to some extent, because the bedding spacing is small enough (several centimeters) to be reflected in the rebound values. We then use average values for the fresh rocks in calculating the unconfined compressive strength for the  $FR$  index, because rocks under flowing water should be fresh and their strength is directly related to the erosion of the waterfall. The Schmidt hammer rebound values are then converted to the unconfined compressive strength  $S_c$  (MPa) using the Schmidt hammer equipment conversion equation ( $\log(S_c/0.098) = 0.0307 R_N + 1.4016$ ).

By substituting the parameter values for the Horseshoe into Eq. (4), the present recession rate is estimated to be  $0.15 \text{ m y}^{-1}$ . The past recession rates of the Horseshoe were also computed for the following six intervals: 1842–1875 (H1), 1875–1905 (H2), 1905–1927 (H3), 1927–1950 (H4), 1950–2000 (H5) and 2000– (H6). These have differing discharge and lip length values, and the recession rates varied from 0.15 to  $0.55 \text{ m y}^{-1}$  (Table 5).

**Table 4**  
Schmidt hammer rebound values ( $R_N$ ) averaged for each rock type and weathering condition.

	Condition	
	Fresh	Weathered
Dolomite	53.4 (4.7)	31.7 (4.0)
Shale/mudstone	51.3 (3.4)	29.7 (1.4)
Average	52.3	30.7
		(%)

Numbers in parentheses show the standard deviation.

**Table 5**  
Summary of data for parameters giving the  $FR$  index and  $FR$ -based waterfall recession rates, where  $Q$  is discharge,  $W$  is lip length of waterfall,  $H$  is height of waterfall,  $R_N$  is Schmidt hammer rebound value of bedrock, and  $S_c$  is unconfined compressive strength of bedrock converted from  $R_N$ .

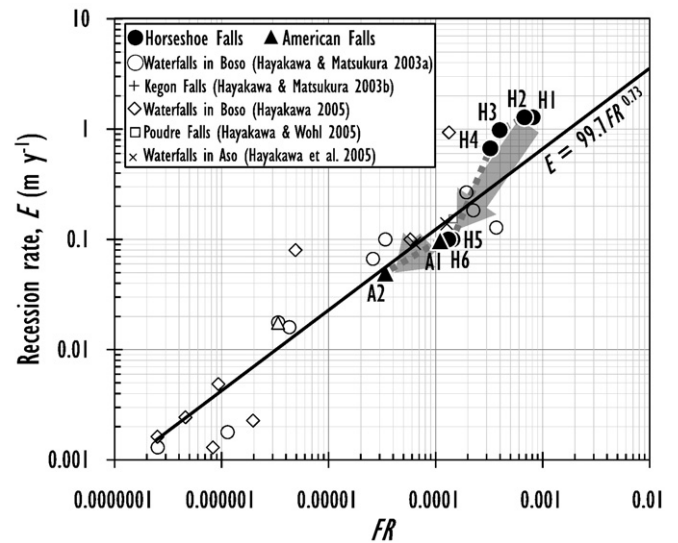
Waterfall	Duration	$Q$ ( $\text{m}^3 \text{ s}^{-1}$ )	$W$ (m)	$H$ (m)	$R_N$ (%)	$S_c$ (MPa)	$FR \times 10^3$ (–)	Computed rate ( $\text{m y}^{-1}$ )
Horseshoe Falls	1842–1875 (H1)	5184	420	51	52.3	99.7	0.766	0.53
	1875–1905 (H2)	5184	501	51	52.3	99.7	0.643	0.47
	1905–1927 (H3)	3732	614	51	52.3	99.7	0.377	0.32
	1927–1950 (H4)	3110	626	51	52.3	99.7	0.309	0.27
	1950–2000 (H5)	1593	723	51	52.3	99.7	0.137	0.15
	2000– (H6)	1593	762	51	52.3	99.7	0.130	0.15
American Falls	–1905 (A1)	576	335	54	52.3	99.7	0.101	0.12
	Modern (A2)	177	335	54	52.3	99.7	0.031	0.05

The modern lip length and height of the waterfalls are given by Niagara Falls State Park, NY.

The present recession rate of American Falls is estimated to be  $0.05 \text{ m y}^{-1}$  with the regulated flow (A2, Table 5). Assuming that the lip length, height and rock strength have not changed, the recession rate of American Falls in the past, i.e., under the natural conditions prevailing until a century ago (–1905), is estimated to be  $0.13 \text{ m y}^{-1}$  (A1, Table 5).

**4. Discussion and conclusions**

The estimated recession rates of the Horseshoe during the last century ( $0.15\text{--}0.53 \text{ m y}^{-1}$ ) are of the same order as the actual recession rates ( $0.1\text{--}1.2 \text{ m y}^{-1}$ ). The estimated recession rates of American Falls ( $0.05\text{--}0.12 \text{ m y}^{-1}$ ) are also in good agreement with the actual recession rates ( $0.01\text{--}0.1 \text{ m y}^{-1}$ ). Agreement is also found in the relationships between the temporally shifting  $FR$  and the actual recession rates of the Horseshoe and American Falls, in which all the data for each period are plotted around the line of Eq. (4) (Fig. 3). The Niagara River transports almost no sediment, because it is trapped upstream in the Great Lakes. Therefore, the results obtained for Niagara Falls support the validity of Eq. (4), which has been applied to



**Fig. 3.** Relationships between the calculated  $FR$  values and actual recession rates for the Horseshoe (solid circle) and American Falls (solid triangle). The suffix for each plot (H1–H6 and A1–A2) corresponds to each durations shown in Tables 1 and 5. Translucent arrows indicate time direction.

waterfalls in detachment-limited rivers with less sediment (e.g., Hayakawa and Matsukura, 2003a,b; Hayakawa et al., 2008b).

The present model gives the best results when changes in both water discharge and waterfall width are incorporated into the equation. If discharge is recovered to the past natural level, the model equation predicts the recession rate at the Horseshoe with the current shape to increase to  $0.4 \text{ m y}^{-1}$ ; whereas, if the discharge had not been reduced for the past hundred years and only the lip length changed, the present recession rate at the Horseshoe would be  $0.3 \text{ m y}^{-1}$ . These expected rates with changes in either discharge or width alone are relatively apart from the actual recession rate. This implies that the reduction of flow discharge due to water diversion through hydroelectric power plant is not the only reason for the reduced recession rate at the Horseshoe; the natural change of its shape is also important. The lip length of American Falls, in contrast, has scarcely changed, and the reduction of discharge is sufficient to explain the decreased recession rate of the waterfall. This observation supports the qualitative argument by Philbrick (1970) that the decreased Horseshoe recession rate is due to both the flow reduction and changes in its horizontal curved shape causing stress dispersion. Philbrick (1970) emphasizes that the presence of notches in the plan lip form is a major factor causing instability enhancing erosion. The effect of such plane shape is not incorporated in the *FR* index. A distinct notch along the lip of the Horseshoe existed earlier (H1 to H4) but disappeared recently (H5 and H6). This may explain the overestimation of the recession rate for H5 and H6 and underestimation for H1 to H4 (Fig. 3). In contrast, the data for American Falls are less apart from the line in Fig. 3, probably because the shape of American Falls has not changed abruptly throughout the last centuries without distinct notches nor curved lip.

Further studies on recession rates of Niagara Falls in the Holocene and the palaeoenvironments of the surrounding area are necessary in relation to the long-term changes in the parameters incorporated in the *FR* index as well as the other factors such as waterfall plan shape. The mechanisms of erosion of Niagara Falls also remain uncertain, and the classical caprock model for waterfall erosion (Gilbert, 1907) should be reassessed because the dolomite and shale layers have similar rock strengths, and undercutting of waterfall face is not common to many waterfalls (Young, 1985; Lamb et al., 2007).

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