

Inderside Interactions

"Populační ekologie živočichů"

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Types of interactions

-
- **+ + .. mutualism** (plants and pollinators)
- 0 **+ .. commensalism** (saprophytism, parasitism, phoresis)
- **+ .. predation** (herbivory, parasitism)**, mimicry**
- 0 **.. amensalism** (allelopathy)
- **- .. competition**

Model of competition

hased on the logistic model of Lotka (1925) and Volterra (1926)

$$
\frac{dN}{dt} = Nr\left(1 - \frac{N}{K}\right)
$$

-assumptions:

- all parameters are constant
- individuals of the same species are identical
- environment is homogenous, differentiation of niches is not possible
- only exact compensation is present

species 1: N_1 , K_1 , r_1 **species 2**: *N*₂, *K*₂, *r*₂

$$
\frac{dN_1}{dt} = N_1 r_1 \left(1 - \frac{N_1 + N_2}{K_1} \right)
$$

$$
\frac{dN_2}{dt} = N_2 r_2 \left(1 - \frac{N_1 + N_2}{K_2} \right)
$$

■ total competitive effect (intra + inter-specific)

 $(N_1 + \alpha N_2)$ where α . coefficient of competition $\alpha = 0$.. no interspecific competition

 α < 1. species 2 has lower effect on species 1 than species 1 on itself α = 0.5 .. one individual of species 1 is equivalent to 0.5 individuals of species 2)

 α = 1. both species has equal effect on the other one

 α > 1. species 2 has greater effect on species 1 than species 1 on itself

species 1:
$$
\frac{dN_1}{dt} = N_1 r_1 \left(1 - \frac{N_1 + \alpha_{12} N_2}{K_1} \right)
$$

species 2:
$$
\frac{dN_2}{dt} = N_2 r_2 \left(1 - \frac{\alpha_{21} N_1 + N_2}{K_2} \right)
$$

If competing species use the same resource then interspecific competition is equal to intraspecific

Analysis of the model

• examination of the model behaviour on a phase plane

- used to describe change in any two variables in coupled differentialequations by projecting orthogonal vectors

• identification of isoclines: a set of abundances for which the growth rate is 0

$$
\frac{dN}{dt} = 0
$$

- species 1 $r_1N_1(1 - [N_1 + \alpha_{12}N_2]/K_1) = 0$ r_1N_1 ([K_1 - N_1 - $\alpha_{12}N_2$] / K_1) = 0 if $r_1, N_1, K_1 = 0$ and if $K_1 - N_1 - \alpha_{12}N_2 = 0$ then $N_1 = K_1 - \alpha_{12}N_2$

if
$$
N_1 = 0
$$
 then $N_2 = K_1/\alpha_{12}$
if $N_2 = 0$ then $N_1 = K_1$

• species 2 r_2N_2 (1 - $[N_2 + \alpha_{21} N_1] / K_2$) = 0 $N_2 = K_2 - \alpha_{21} N_1$

if
$$
N_2 = 0
$$
 then $N_1 = K_2/\alpha_{21}$
if $N_1 = 0$ then $N_2 = K_2$

Isoclines

- ▶ above isocline *i*₁ and below *i*₂ competition is weak
- in-between *i1* and *i2* competition is strong

1. Species 2 drives species 1 to extinction

 \blacktriangleright K and α determine the model behaviour - disregarding initial densities species 2 (stronger competitor) willoutcompete species 1 (weaker competitor)

$$
K_1 = K_2 \t r_1 = r_2 \n\alpha_{12} > \alpha_{21} \t N_{01} = N_{02}
$$

2. Species 1 drives species 2 to extinction

- species 1 (stronger competitor) will outcompete species 2 (weakercompetitor)

$$
K_1 > \frac{K_2}{\alpha_{21}} \quad K_2 < \frac{K_1}{\alpha_{12}}
$$

$$
r_1 = r_2 \qquad K_1 = K_2
$$

$$
N_{01} = N_{02} \qquad \alpha_{12} < \alpha_{21}
$$

3. Stable coexistence of species

- disregarding initial densities both species will coexist at stable equilibrium (where isoclines cross)

- at at equilibrium population density of both species is reduced
- both species are weak competitors

Test of the model

- when *Rhizopertha* and *Oryzaephilus* were reared separately bothspecies increased to $420-450$ individuals $(= K)$

 \blacktriangleright when reared together *Rhizopertha* reached $K_1 = 360$, while O ryzaephilus K_2 = 150 individuals

combination resulted in more efficient conversion of grain $(K_{12} = 510)$ individuals)

- three combinations ofdensities converged to thesame stable equilibrium

- prediction ofLotka-Volterra model is correct

Model for discrete generations

• solution of the differential model:

$$
N_{1,t+1} = N_{1,t} e^{r_1 \left(\frac{K_1 - N_{1,t} - \alpha_{12} N_{2,t}}{K_1}\right)} \left| N_{2,t+1} = N_{2,t} e^{r_2 \left(\frac{K_2 - N_{2,t} - \alpha_{21} N_{1,t}}{K_2}\right)} \right|
$$

- multiple regression analysis is used to estimate parameters fromabundances

$$
\ln\left(\frac{N_{1,t+1}}{N_{1,t}}\right) = r_1 - N_{1,t} \frac{r_1}{K_1} - N_{2,t} \frac{r_1 \alpha_{12}}{K_1} \left[\ln\left(\frac{N_{2,t+1}}{N_{2,t}}\right) \right] = r_2 - N_{1,t} \frac{r_2}{K_2} - N_{1,t} \frac{r_2 \alpha_{21}}{K_2}
$$

$$
\ln\left(\frac{N_{1,t+1}}{N_{1,t}}\right) = a + bN_{1,t} + cN_{2,t} \qquad \ln\left(\frac{N_{2,t+1}}{N_{2,t}}\right) = a + bN_{2,t} + cN_{1,t}
$$

$$
r = a \qquad \alpha = -\frac{Kc}{r} \qquad K = -\frac{r}{b}
$$

$$
r = a \qquad \alpha = -\frac{Kc}{r} \qquad K = -\frac{r}{b}
$$

Excercise 16

Two species of *Tribolium* beetles were kept together in a jar with flour. The species breed in discrete periods. Their densities wererecorded once a week. The following abundances were observed:

A: 10, 6, 5, 4, 3, 4, 6, 8, 10, 12, 15, 16B: 20, 18, 16, 11, 6, 6, 5, 3, 2, 2, 1, 1

1. Estimate r_1 , r_2 , K_1 , K_2 , α_{12} , α_{21} .

2. Simulate the dynamics using difference model system for a period of 20 years. Use estimated values of parameters and initial densities of 20individuals.

```
a<-c(10,6,5,4,3,4,6,8,10,12,15,16)b<-c(20,18,16,11,6,6,5,3,2,2,1,1)a1<-a[-1]/a[-12]
b1<-b[-1]/b[-12]
```

```
coef(lm(log(a1)~a[-12]+b[-12]))0.60443/0.02992
20.20154*0.04106/0.60443
```

```
coef(lm(log(b1)~b[-12]+a[-12]))0.399980/0.005052
79.1726*0.011438/0.399980
```

```
N12<-data.frame(N1<-numeric(1:20),N2<-numeric(1:20))N12[,1]<-20
N12[,2]<-20
for(t in 1:20) N12[t+1,]<-{
N1<-N12[t,1]*exp(0.6*(20.2-N12[t,1]-1.4*N12[t,2])/20.2)
N2<-N12[t,2]*exp(-0.4*(79.2-N12[t,2]-2.3*N12[t,1])/79.2)c(N1,N2)}
matplot(N12, type="l",lty=1:2)
legend(1,80,c("N1","N2"),lty=1:2)
```


Two species of spiders, *Pardosa* and *Pachygnatha*, occur togetherand were found to feed in the field on the following prey:

- 1. Estimate and plot niche breadth (*D*) for each species.
- 2. Estimate niche overlap (a_{12}, a_{21}) for each species.

$$
D = \frac{1}{\sum_{k=1}^{n} p_k^2}
$$
 $a_{12} = \frac{\sum_{k=1}^{n} p_{1k} p_{2k}}{\sum_{k=1}^{n} p_{1k}^2}$ $a_{21} = \frac{\sum_{k=1}^{n} p_{1k} p_{2k}}{\sum_{k=1}^{n} p_{2k}^2}$

```
Par<-c(0.61,0.15,0.12,0.07,0.05)Pach<-c(0.93,0.05,0.01,0,0.01)both<-rbind(Par,Pach)
barplot(both,beside=T,legend.text=c("Par","Pach"))1/sum(Par^2)
1/sum(Pach^2)
```
a12<-sum(Par*Pach)/sum(Par^2); a12a21<-sum(Par*Pach)/sum(Pach^2); a21

Excercise 18

An invasive ant species is spreading and may replace a native antspecies as both have similar niches. The following parameters areknow for the native (1) and invasive (2) species.

Simulate the population dynamic using differential model systemfor the period of 30 years. The initial densities are $N_{01}=200$ and $N_{02}=10$.

How to achieve stable coexistence?


```
comp<-function(t,y,param){N1<-y[1]
N2<-y[2]
with(as.list(param),{
dN1.dt<-r1*N1*(1-(N1+a12*N2)/K1)
dN2.dt<-r2*N2*(1-(N2+a21*N1)/K2)
return(list(c(dN1.dt,dN2.dt)))})}
```

```
N1<-200;N2<-10
param<-c(r1=0.2,r2=0.9,a12=1.1,a21=0.7,K1=200,K2=300)time<-seq(0,30,0.1)library(deSolve)
out<-data.frame(ode(c(N1,N2),time,comp,param))
matplot(time,out[,-1],type="l",lty=1:2,col=1)legend("right",c("N1","N2"),lty=1:2)
```

```
N1<-200;N2<-10
param<-c(r1=0.2,r2=0.9,a12=0.5,a21=0.7,K1=200,K2=300)time<-seq(0,30,0.1)library(deSolve)
out<-data.frame(ode(c(N1,N2),time,comp,param))
matplot(time,out[,-1],type="l",lty=1:2,col=1)legend("right",c("N1","N2"),lty=1:2)
```