



MODULARIZACE VÝUKY EVOLUČNÍ A EKOLOGICKÉ BIOLOGIE
CZ.1.07/2.2.00/15.0204



Matrix analysis



INVESTICE DO ROZVOJE VZDĚLÁVÁNÍ

Net reproductive rate (R_0)

- average total number of offspring produced by a female in her lifetime

$$R_0 = \sum_{x=0}^n l_x m_x$$

Average generation time (T)

- average age of females when they give birth

$$T = \frac{\sum_{x=0}^n xl_x m_x}{R_0}$$

Expectation of life

- age specific expectation of life
- $o ..$ oldest age

$$e_x = \frac{T_x}{l_x}$$

where

$$T_x = \sum_x^o L_x$$

$$L_x = \frac{l_x + l_{x+1}}{2}$$

Growth rates

► Discrete time/generations

- estimate of λ (finite growth rate) from the life table:

$$\mathbf{A}\tilde{\mathbf{N}}_t = \lambda\tilde{\mathbf{N}}_t$$

where $\tilde{\mathbf{N}}_t$ is vector at stable age distribution

λ is dominant positive eigenvalue of \mathbf{A}

$$\det(\mathbf{A} - \lambda\mathbf{I}) = 0$$

- or

$$\lambda \approx \frac{R_0}{T}$$

► Continuous time

- r can be estimated from λ

$$r = \ln(\lambda)$$

- by approximation

$$r \approx \frac{\ln(R_0)}{T}$$

or by Euler's method

$$1 = \int_0^t l(x)m(x)e^{-rx}dx$$

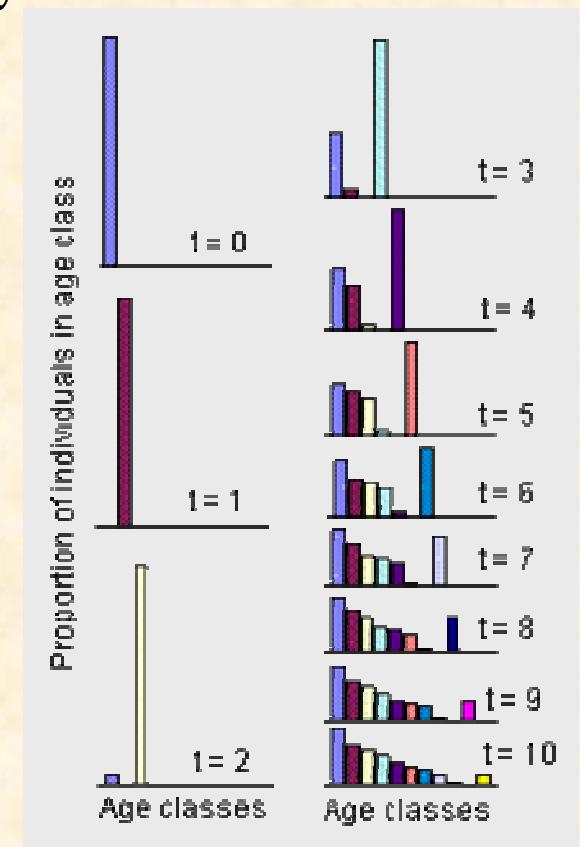
Stable Class distribution (SCD)

- relative abundance of different life history age/stage/size categories
 - population approaches stable age distribution:
 $N_0 : N_1 : N_2 : N_3 : \dots : N_s$ is stable
- once population reached SCD it grows exponentially

- \mathbf{w}_1 .. right eigenvector (vector of the dominant eigenvalue)
- provides stable age distribution
- scale \mathbf{w}_1 by sum of individuals

$$\mathbf{A}\mathbf{w}_1 = \lambda_1 \mathbf{w}_1$$

$$SCD = \frac{\mathbf{w}_1}{\sum_{i=1}^S \mathbf{w}_1}$$

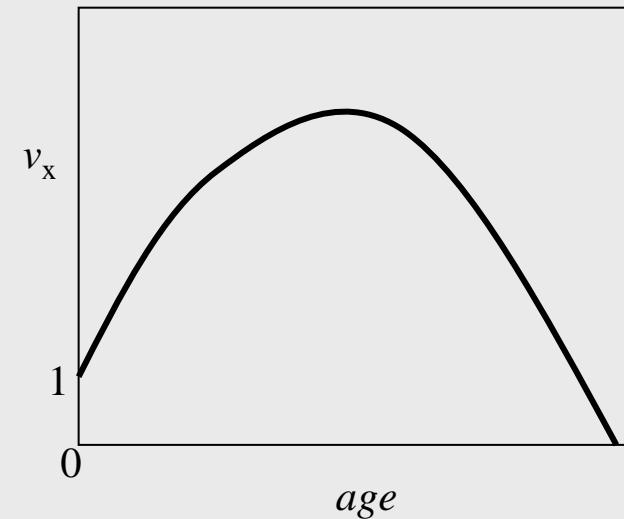


Reproductive value (v_x)

- ▶ measures relative reproductive potential and identifies age class that contributes most to the population growth
- ▶ when population increases then early offspring contribute more to v_x than older ones
- ▶ \mathbf{v}_1 .. left eigenvector (vector of the dominant eigenvalue of transposed \mathbf{A})
 - \mathbf{v}_1 is proportional to the reproductive values and scaled to the first category

$$\mathbf{v}_1' \mathbf{A} = \lambda_1 \mathbf{v}_1$$

$$v_x = \frac{\tilde{u}_x}{\tilde{u}_1}$$



Sensitivity (s)

- identifies which process (p, F, G) has largest effect on the population increase (λ_1)
- examines change in λ_1 given small change in processes (a_{ij})
- sensitivity is larger for survival of early, and for fertility of older classes
- not used for postreproductive census with class 0

$$s_{ij} = \frac{v_{ij} w'_{ij}}{\mathbf{v} \cdot \mathbf{w}}$$

← sum of pairwise products

Elasticity (e)

- weighted measure of sensitivity
- measures relative contribution to the population increase
- impossible transitions = 0

$$e_{ij} = \frac{a_{ij}}{\lambda_1} s_{ij}$$

Conservation biology

- ▶ to adopt means for population promotion or control

Conservation/control procedure

1. Construction of a life table
2. Estimation of the intrinsic rates
3. Sensitivity analysis - helps to decide where conservation/control efforts should be focused
4. Development and application of management plan
5. Prediction of future