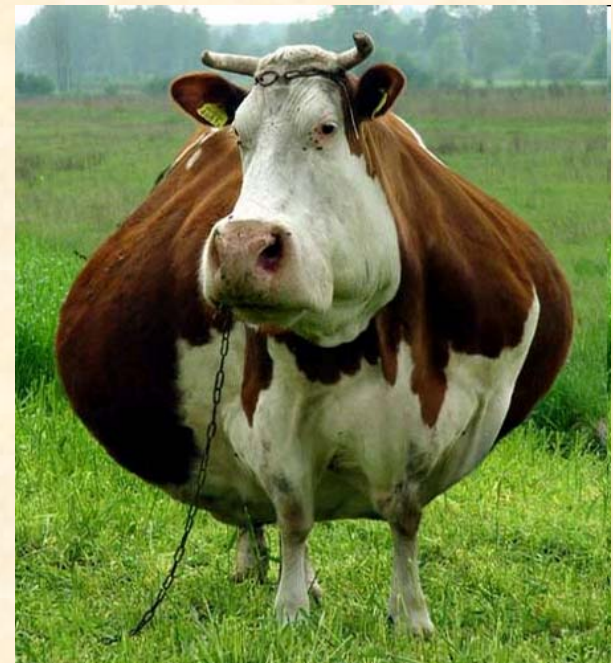


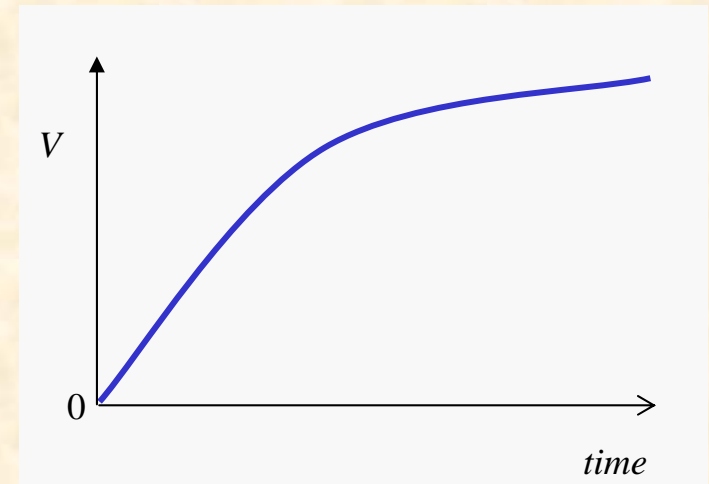
# Plant-Herbivore

- ▶ consume small amount of many different plant species
- ▶ consume a lot during life to obtain sufficient amount of N
- ▶ grazers, granivores, frugivores, herbivores
- ▶ plants are not killed only reduced in biomass
- ▶ top-down control – herbivore abundance is regulated by enemies
- ▶ bottom-up – herbivore abundance is regulated by quantity and quality of plants



# Herbivory-regrowth model

- ▶ Turchin (2003)
- ▶ assumptions
  - continuous herbivory
  - herbivore is polyphagous
  - plant biomass is homogenous
  - functional response Type II
  - herbivore density is constant
  - only small quantity of biomass is removed
- ▶ hyperbolic biomass growth



$V$  .. plant biomass

$N$ .. herbivore density

$r$ .. intrinsic rate of increase

$K$ .. carrying capacity

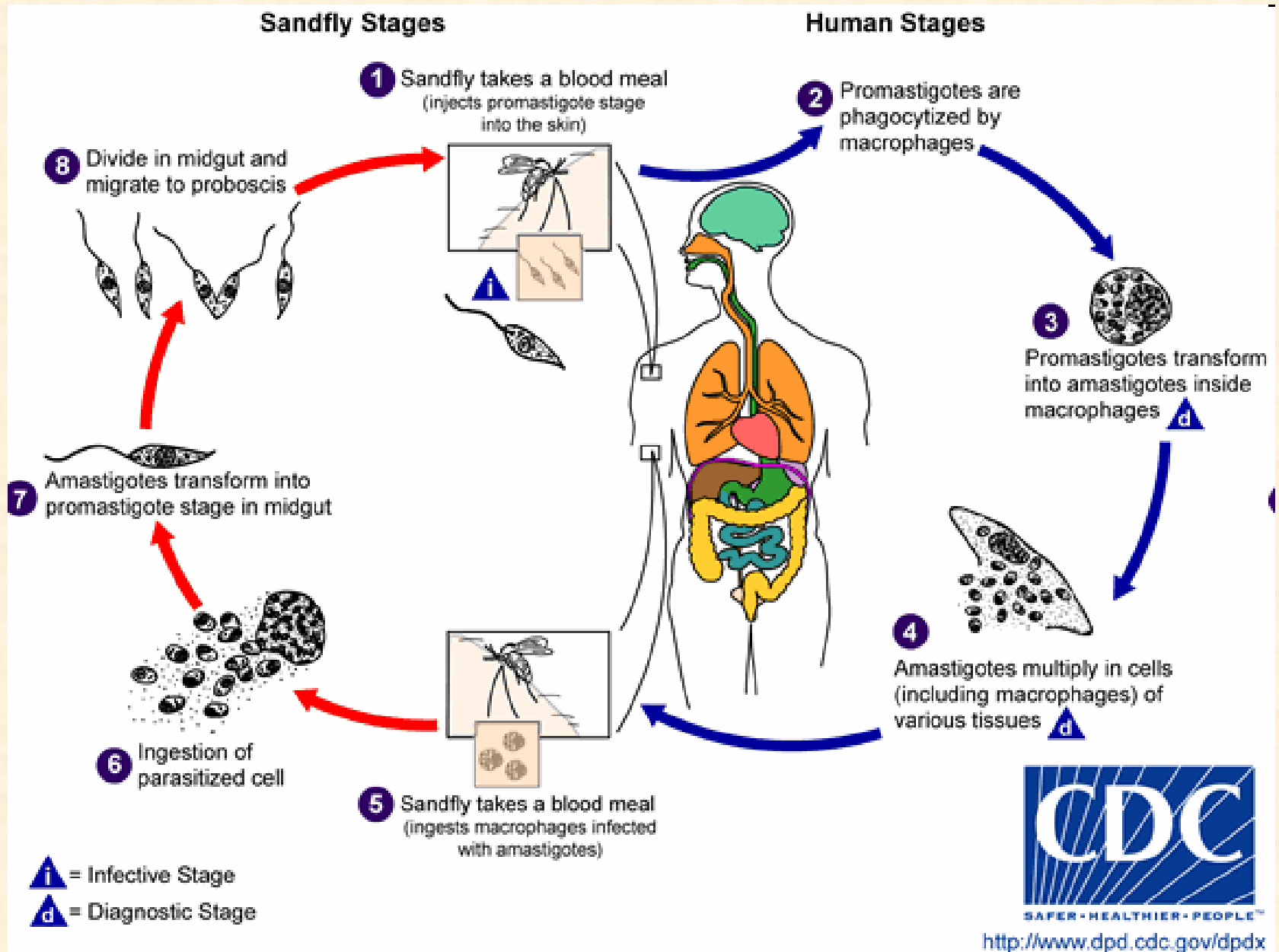
$f$ .. efficiency of removal

$T_h$ .. handling time

$$\frac{dV}{dt} = r \left( 1 - \frac{V}{K} \right) - \frac{fNV}{1 + fNT_h}$$

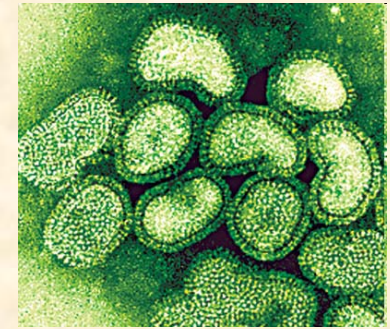
# Host-Pathogen

# Leishmania



# Agents

- ▶ microparasites: viruses, bacteria, protozoans
  - reproduce rapidly in host
  - level of infection depends not on the number of agents but on the host response
- ▶ macroparasites - helminths
  - reproduce in a vector
  - level of infection depends on the number
- ▶ incidence .. number of new infections per unit time
- ▶ prevalence .. proportion of population infected =  $1/N$



swine flu virus



*E. coli* (EHEC)



cercaria



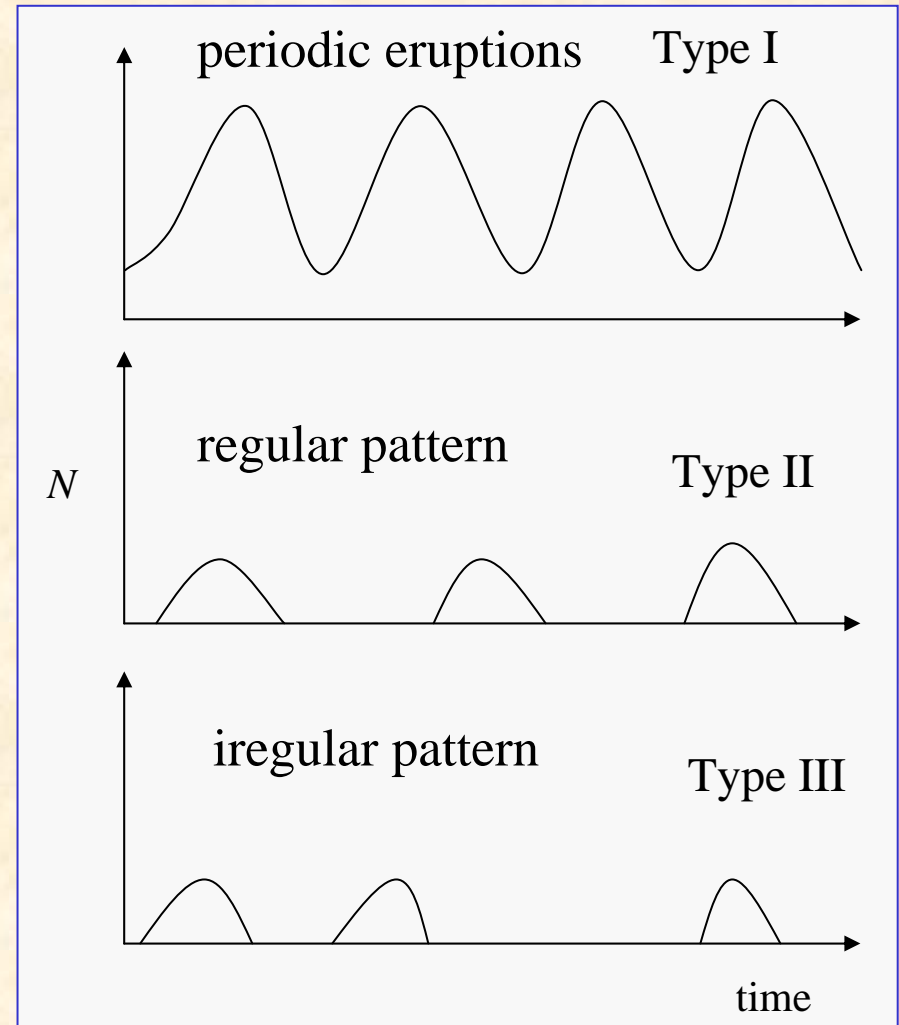
nematode

# Epidemiology

- ▶ predicts rates of disease spread
- ▶ predicts occurrence of epidemics
- ▶ predicts expected level of infection
  
- ▶ number of deaths caused by disease exceeds that of all wars
  
- ▶ affect also animals
  - rinderpest introduced by Zebu cattle to South Africa in 1890
  - 90% buffalo population was wiped out
  
- ▶ biological control
  - *Cydia pomonella* granulosis virus



- ▶ epidemics occur in cycles
- ▶ follows 4 stages:
  - establishment - pathogen increases after invasion
  - persistence - pathogen persists within host population
  - spread - spreads to other non-infected regions, reaches peak
  - epidemics terminates

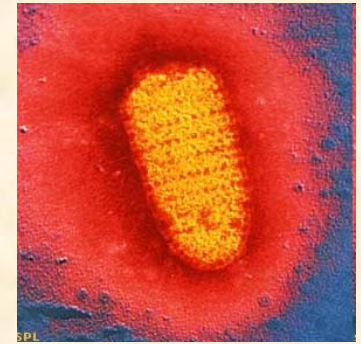




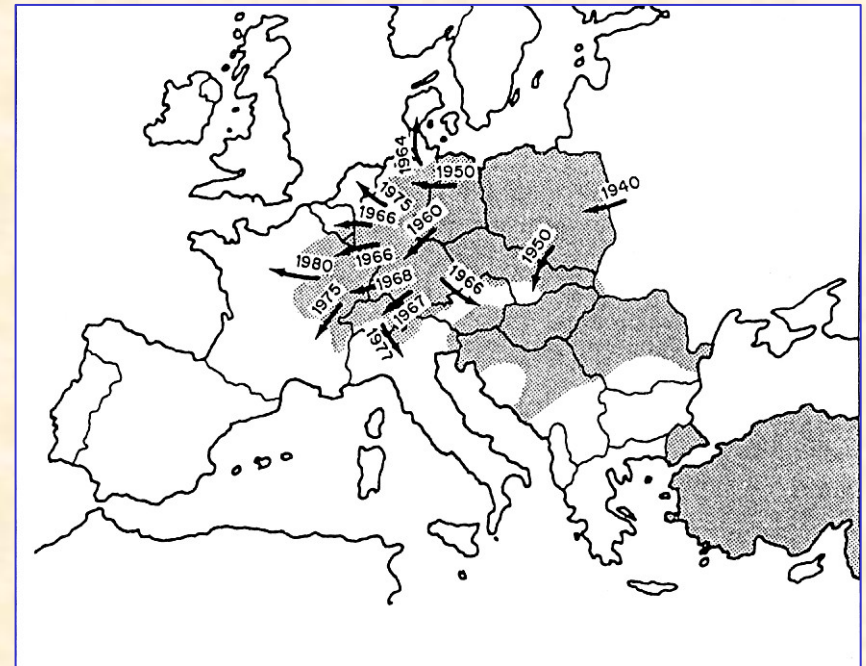
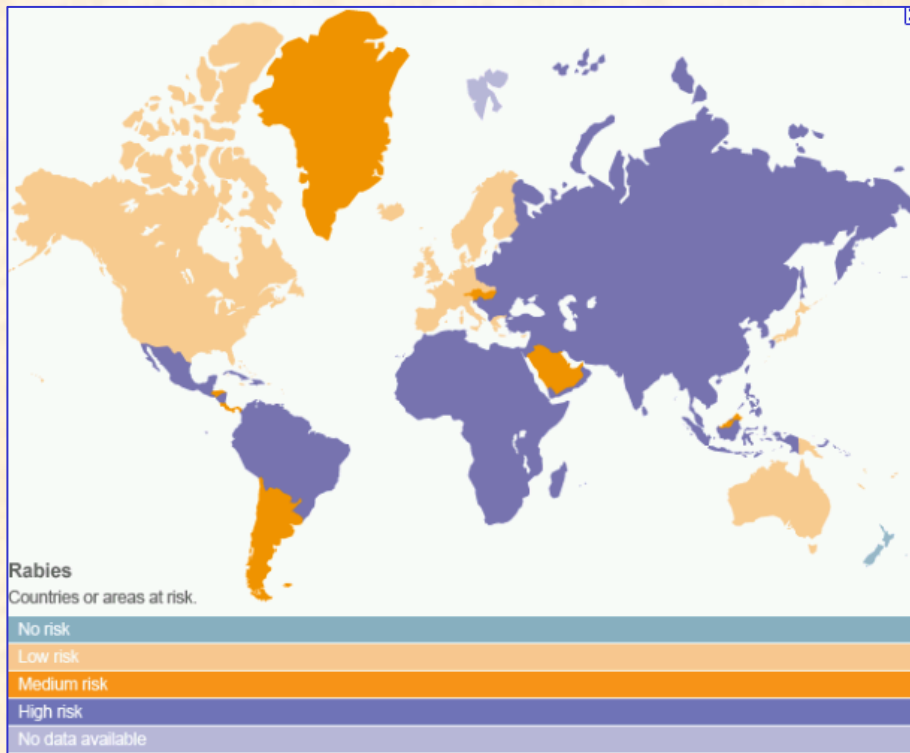
▶ rabies in Europe spread from Poland 1939

- hosts: foxes, badgers, roe-deer

▶ spread rate of 30-60 km/year



virus



Spread of rabies (Bacon 1985)

# Host-pathogen/parasite system



▶ used to simulate spread of a disease in the human population or in the biological control

▶ models:

- Kermack & McKendrick (1927)

- later developed by Anderson & May (1980, 1981)

▶ 3 components:

-  $S$  .. susceptible

-  $I$  .. infected

-  $R$  .. resistant/recovered and immune + dead individuals - can not transmit disease

- latent population - infected but not infectious

- vectors ( $V$ ) and pathogens ( $P$ )

- malaria is transmitted by mosquitoes, hosts become infected only when they have contact with the vector

- the number of vectors carrying the pathogens is important

- such system is further composed of uninfected and infected vectors

# Kermack-McKendrick model

▶  $\beta$  .. transmission rate - number of new infections per unit time  
 $\beta SI$  .. density-dependent transmission function (proportional to the number of contacts)

- mass action

- analogous to search efficiency in predator-prey model

$1/\beta$  .. average time for encountering infected individual

▶  $\gamma$  .. recovery rate of infected hosts  
(either die or become immune)

$\gamma = 1/\text{duration of disease}$

Assumptions:

-  $S_0 \gg I_0$

- ignores population change (increase of  $S$ )

- incubation period is negligible

## SI model

$$\frac{dS}{dt} = -\beta SI$$

$$\frac{dI}{dt} = \beta SI - \gamma I$$

# Outbreaks

▶ outbreak (epidemics) will occur if  $S_0 > \frac{\gamma}{\beta}$

- i.e. when density of  $S$  is high

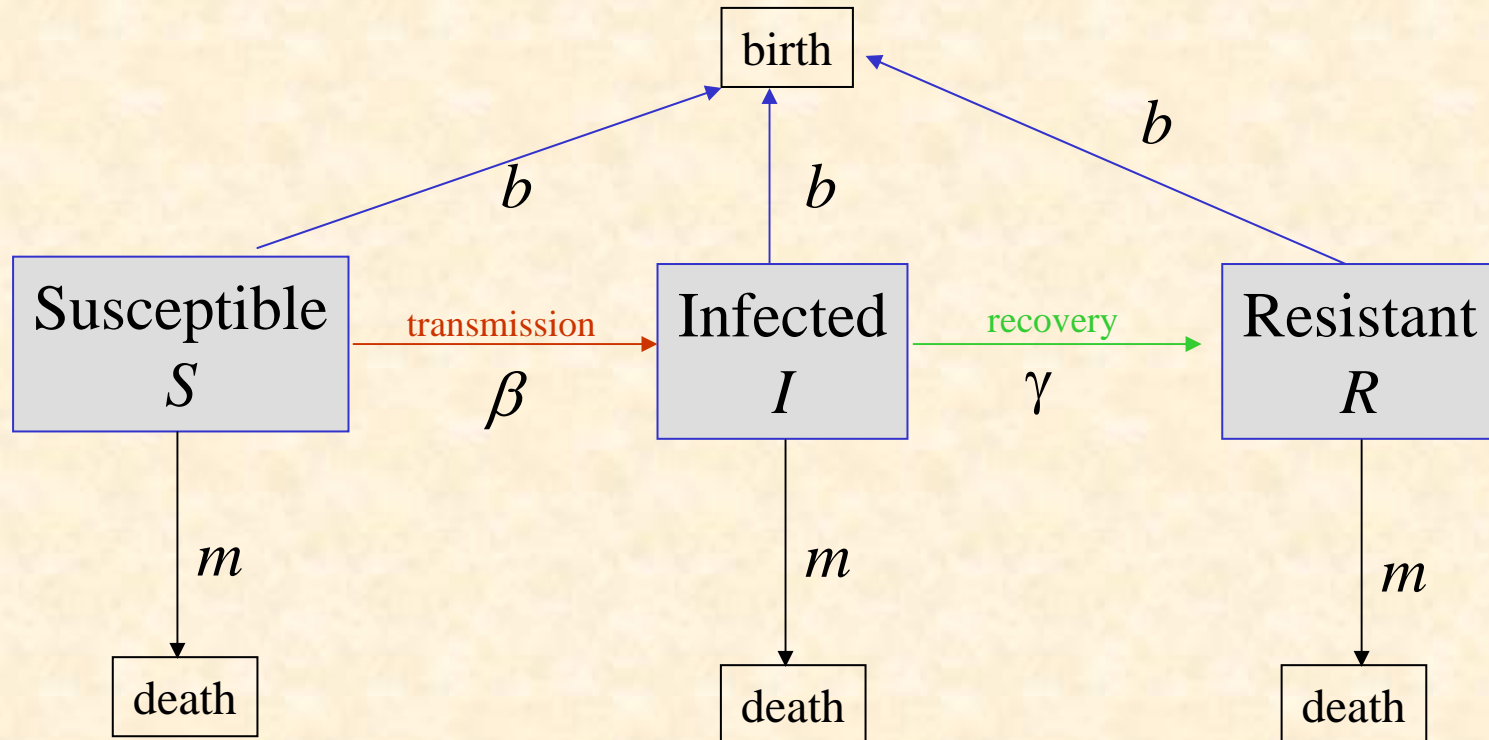
▶ making the population size small will halt the spread:  $S_0 < \frac{\gamma}{\beta}$

▶ vaccination of  $S$ , culling or isolation of  $I$  will stop disease spread

# Anderson-May model

## Assumptions:

- host population is dynamic
- newborns are susceptible
- $b$  .. host birth rate  
=  $1/\text{host life-span}$ , given exponential growth and constant population size
- $m$  .. host mortality due to other causes



# SIR model

$$\frac{dS}{dt} = b(S + I + R) - \beta SI - mS$$

$$\frac{dI}{dt} = \beta SI - \gamma I - mI$$

$$\frac{dR}{dt} = \gamma I - mR$$

$N$  .. total population of hosts per area:  $N = S + I + R$

- ▶  $R_0$  .. basic reproductive rate of the disease
- number of secondary cases that primary infection produces
- if  $R_0 > 1$  .. outbreak is plausible

$$R_0 = \frac{\beta N}{b + \gamma + m}$$

# Biological control

- ▶ fast biocontrol effect is achieved only with viruses with high  $\beta$
- ▶ low host population is achieved with pathogens with lower  $\beta$

Population dynamic of a moth and the associated granulosis virus

