

# Příklady Integrály

1) Vypočítejte neurčitý integrál:

A

$$\begin{aligned} \int x^3 \, dx & \quad \left[ \frac{x^4}{4} + c \right] \\ \int e^x \, dx & \quad [e^x + c] \\ \int \frac{x+1}{x^2+2x+9} \, dx & \quad \left[ \frac{1}{2} \ln|x^2 + 2x + 9| + c \right] \\ \int \frac{1}{x^4} \, dx & \quad \left[ -\frac{1}{3x^3} + c \right] \\ \int x^4 - x^2 \sqrt[5]{x^3} \, dx & \quad \left[ \frac{x^5}{5} - \frac{5x^{\frac{18}{5}}}{18} + c \right] \end{aligned}$$

B

$$\begin{aligned} \int \frac{1}{x} \, dx & \quad [\ln|x| + c] \\ \int \frac{x+1}{x^2+2x+9} \, dx & \quad \left[ \frac{1}{2} \ln|x^2 + 2x + 9| + c \right] \\ \int \frac{1}{x^2} \, dx & \quad \left[ -\frac{1}{x} + c \right] \\ \int 3x^5 \, dx & \quad \left[ \frac{x^6}{2} + c \right] \\ \int a + 3 \cos x \, dx & \quad [ax + 3 \sin x + c] \end{aligned}$$

C

$$\begin{aligned} \int 1 \, dx & \quad [x + c] \\ \int \sqrt{x} + \frac{1}{x-1} + 2 \, dx & \quad \left[ \frac{2x^{\frac{3}{2}}}{3} + \ln|x-1| + 2x + c \right] \\ \int \tan^2 x \, dx & \quad [\tan x - x + c] \\ \int 7x^6 - 5x^4 + 2x - 1 \, dx & \quad [x^7 - x^5 + x^2 - x + c] \\ \int \cot^2 x \, dx & \quad [-x - \cot x + c] \end{aligned}$$

D

$$\begin{aligned} \int x^n \, dx & \quad \left[ \frac{x^{n+1}}{n+1} + c, n \neq -1 \right] \\ \int \frac{1}{2x-5} \, dx & \quad \left[ \frac{\ln|2x-5|}{2} + c \right] \\ \int \tan x \, dx & \quad [-\ln|\cos x| + c] \\ \int 7e^x - \frac{5}{x} \, dx & \quad [7e^x - 5 \ln|x| + c] \\ \int \frac{x^2 \sqrt{x}}{x^5} \, dx & \quad \left[ -\frac{2}{3x^{\frac{3}{2}}} + c \right] \end{aligned}$$

2) Vypočítejte neurčitý integrál metodou substituce:

A

$$\begin{aligned} \int \frac{\ln^2 x}{x} \, dx & \quad \left[ \frac{\ln^3 x}{3} + c \right] \\ \int \frac{3x}{(x^2+4)^3} \, dx & \quad \left[ \frac{-3}{4(x^2+4)^2} + c \right] \\ \int \frac{e^{2x}}{\sqrt{e^x-1}} \, dx & \quad \left[ \frac{2(e^x-1)^{\frac{3}{2}}}{3} + 2\sqrt{e^x-1} + c \right] \end{aligned}$$

B

$$\begin{aligned} \int 10x(x^2+13)^{12} \, dx & \quad \left[ \frac{5(x^2+13)^{13}}{13} + c \right] \\ \int 8x^2(x^3+2)^5 \, dx & \quad \left[ \frac{4(x^3+2)^6}{9} + c \right] \\ \int 5xe^{x^2} \, dx & \quad \left[ \frac{5e^{x^2}}{2} + c \right] \end{aligned}$$

C

$$\begin{aligned} \int \frac{x}{x^2+1} \, dx & \quad \left[ \frac{\ln|x^2+1|}{2} + c \right] \\ \int x(x^2-1)^{10} \, dx & \quad \left[ \frac{(x^2-1)^{11}}{22} + c \right] \\ \int \frac{7 \ln^4 x}{x} \, dx & \quad \left[ \frac{7 \ln^5 x}{5} + c \right] \end{aligned}$$

D

$$\int (3x-4)^7 \, dx \quad \left[ \frac{(3x+4)^8}{24} + c \right]$$

$$\int 3x \sqrt[4]{x^2 + 5} \, dx$$

$$[\frac{6(x^2+5)^{\frac{5}{4}}}{5} + c]$$

$$\int e^{\cos 2x} \sin x \cos x \, dx$$

$$[-\frac{e^{\cos 2x}}{4} + c]$$

3) Vypočítejte určitý integrál

A

$$\int_1^3 \frac{1}{1+x} \, dx$$

$$[1]$$

$$\int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \frac{\sin 2x}{\cos x} \, dx$$

$$[\sqrt{3} - 1]$$

$$\int_0^1 \frac{1}{\sqrt{x^2 - 1}} \, dx$$

$$[\text{není definován}]$$

$$\int_6^{12} \frac{x^2 - 13x + 19}{x^2} \, dx$$

$$[\frac{91}{12} - 13 \ln 2]$$

B

$$\int_2^5 2x + 3 \, dx$$

$$[30]$$

$$\int_1^4 \sqrt{x} \, dx$$

$$[\frac{14}{3}]$$

$$\int_0^{\frac{\pi}{4}} \frac{1}{2 \cos^2 x} \, dx$$

$$[\frac{1}{2}]$$

$$\int_1^e 1 - e^x + \frac{100}{x} \, dx$$

$$[99 + 2e - e^e]$$

C

$$\int_1^3 3x^2 - 2x + 1 \, dx$$

$$[20]$$

$$\int_0^5 \frac{\cos^4 x - \sin^4 x}{\cos 2x} \, dx$$

$$[5]$$

$$\int_0^4 \frac{2x^2 - 50}{x-5} \, dx$$

$$[56]$$

$$\int_{-1}^1 \frac{x^4 - 2x^2 + 1}{x-1} \, dx$$

$$[-\frac{4}{3}]$$

D

$$\int_0^{\frac{\pi}{2}} \cos x \, dx$$

$$[1]$$

$$\int_0^1 \frac{e^x}{1+e^x} \, dx$$

$$[\ln \frac{1+e}{2}]$$

$$a^2 \int_0^{\frac{\pi}{2}} \cos^2 x \, dx$$

$$[\frac{1}{4}]$$

$$\int_1^{10} \frac{1}{x^2} \, dx$$

$$[\frac{9}{10}]$$