

# Luminescence methods

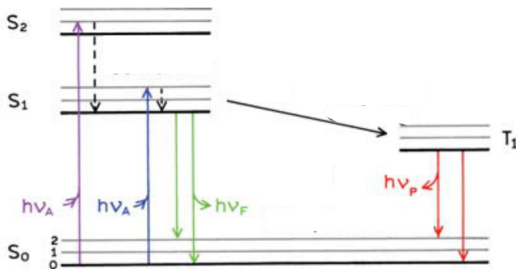
*Methods of biophysical chemistry - seminar*

Jan Novotný  
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November 13, 2019

# Energetic digram

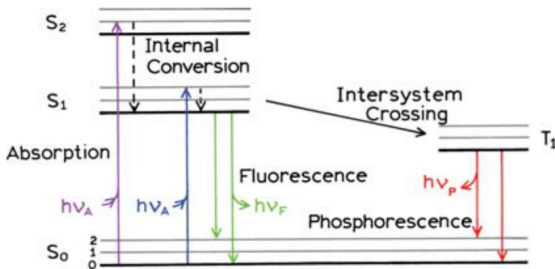
Fill in attached diagram and compare the phenomena according to parameters indicated in a table:



Phenomenon	time regime	$k$ vs. $k_{vib}$	order $\lambda_{max}$
Absorption			
Fluorescence			
Phosphorescence			

# Energetic diagram

Fill in attached diagram and compare the phenomena according to parameters indicated in a table:



Phenomenon	time regime	$k$ vs. $k_{vib}$	order $\lambda_{max}$
Absorption	$10^{-15}s$	$>$	1
Fluorescence	$10^{-9}s$	$<$	2
Phosphorescence	$10^0s$	$<$	3

## Starting problems: Are the following statements true or false. Explain your decision.

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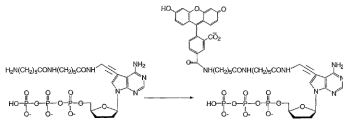
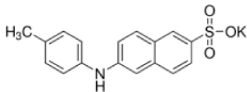
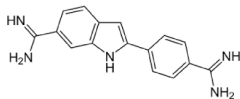
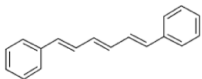
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- 8 The measurement of fluorescence anisotropy employs circularly polarized excitation radiation

# Exercise 1

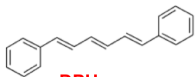
Assign displayed fluorescence probes to corresponding abbreviation and biochemical application



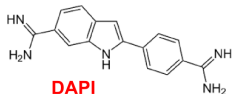
**DAPI, ddATP-Dye, DPH, TNS**

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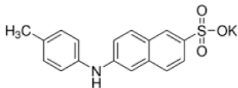
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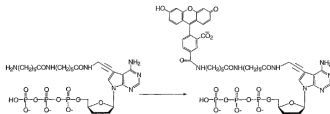
**DPH**  
biomembranes



**DAPI**  
DNA binders



**TNS**  
probing proteins



**ddATP-dye**  
nucleic acid sequencing

**DAPI, ddATP-Dye, DPH, TNS**

## Exercise 2: Fluorescence methods

*Assign the appropriate methods exploiting fluorescence techniques to following tasks:*

- A) Determination of hydrodynamic radius of a protein.
- B) DNA hybridization.
- C) Localisation of Trp residue (on surface or inside a protein).
- D) Portion of unsaturated phospholipids in biomembrane.
- E) Determination of  $K_A$  of eosin dimerisation.

Correlation time of fluorescence label, fluorescence anisotropy of DPH, Stokes shift, emission of excimer, FRET

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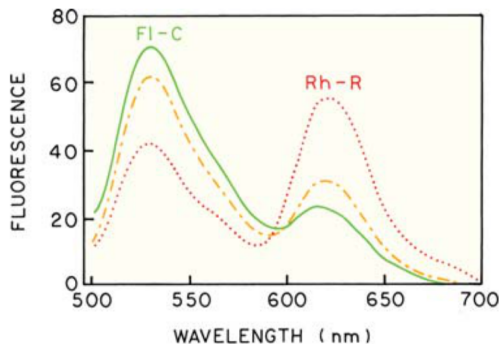
*Assign the appropriate methods exploiting fluorescence techniques to following tasks:*

- A) Determination of hydrodynamic radius of a protein. **Correlation time of fluorescence label**
- B) DNA hybridization. **FRET**
- C) Localisation of Trp residue (on surface or inside a protein). **fluorescence decay, Stokes shift**
- D) Portion of unsaturated phospholipids in biomembrane. **viscosity-anisotropy of DPH**
- E) Determination of  $K_A$  of eosin dimerisation. **emission of excimer**

Correlation time of fluorescence label, fluorescence anisotropy of DPH, Stokes shift, emission of excimer, FRET

## Exercise 3: FRET

Try to interpret following fluorescence experiment carried out on complex of protein kinase consisting of catalytic (C) and regulative (R) subunit. Both parts are labelled with probes: unit C with fluorescein (Fl) and unit R with rhodamine (Rh). In native form of  $R_2C_2$  the FRET can be detected. Identify the direction of transition and explain the effect of cAMP and PKI inhibitor added to the studied sample.



$R_2C_2$

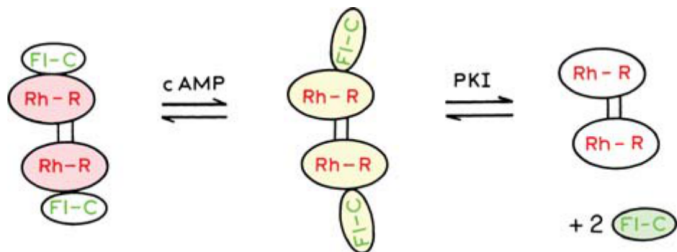
$R_2C_2$  + cAMP

$R_2C_2$  + PKI



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## Exercise 4: Kinetic parameters of fluorescence

Eosin fluorophor is characterized by quantum yield 0.65 and fluorescence life time of 3.1 ns. Calculate the life time of radiative, non-radiative transition and intrinsic life time of fluorescence.

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### Solution

$$\Phi = \frac{\Gamma}{\Gamma + k_{nr}}, \tau = \frac{1}{\Gamma + k_{nr}} \rightarrow \Gamma = \frac{\Phi}{\tau}$$

Rate constants:

$$\Gamma = \frac{0.65}{3.1} = 0.21 \text{ ns}^{-1}, k_{nr} = \frac{1}{\tau} - \Gamma = \frac{1}{3.1} - 0.21 = 0.11 \text{ ns}^{-1}$$

## Exercise 5: Perrin equation - depolarisation of emitted signal

Based on assumption of exponential decay of intensity  $I(t)$  and anisotropy  $r(t)$  of fluorescence signal derive relation between anisotropy  $r$ , life time  $\tau$  and correlation time  $\theta$ . Use the definition of time-weighted average of anisotropy  $r$  as a starting point:

$$r = \frac{\int_0^{\infty} r(t)I(t)dt}{\int_0^{\infty} I(t)dt}$$

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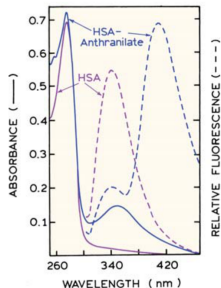
### Solution

$$I = I_0 e^{-\frac{t}{\tau}}, \quad r = r_0 e^{-\frac{t}{\theta}}$$

$$r = \frac{I_0 r_0 \int_0^{\infty} e^{-t\left(\frac{1}{\tau} + \frac{1}{\theta}\right)} dt}{I_0 \int_0^{\infty} e^{-\frac{t}{\tau}} dt} = \frac{r_0 \left(\frac{1}{\tau} + \frac{1}{\theta}\right)^{-1}}{\tau} = \frac{r_0}{1 + \frac{\tau}{\theta}}$$

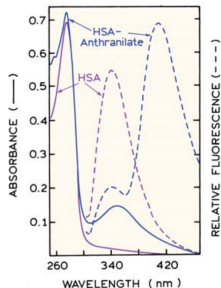
## Exercise 6: FRET

The protein human serum albumin (HSA) has a single tryptophan residue at position 214. HSA was labelled with an anthraniloyl group placed covalently on cysteine-34. Emission spectra of the labelled and unlabelled HSA are shown in attached figure. The Förster distance for Trp to anthraniloyl transfer is  $30.3\text{\AA}$ . Use the emission spectra in the attached figure to calculate the Trp to anthraniloyl distance. The rate constant of RET can be estimated using formula:  $k_{RET} = \Gamma \left( \frac{R_0}{r} \right)^6$ .



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### Řešení

$$\Phi = \frac{\Gamma}{\Gamma + k_{RET}} = \frac{\Gamma}{\Gamma + \Gamma \left(\frac{R_0}{r}\right)^6} = \frac{r^6}{R_0^6 + r^6}$$

Quantum yield  $\Phi$  at  $\lambda$  340 nm: emission of albumin with acceptor/emission of free form =  $0.2/0.55$

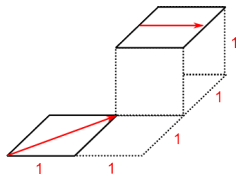
$$\Phi = 0.364 = \frac{r^6}{30.3^6 + r^6} \Rightarrow r = \frac{30.3}{1.75^{1/6}} = 27.6\text{\AA}$$

## Exercise 6: Dipolar interaction - orientation dependence

Efficiency of resonance transfer depends beside the spectral overlap and spatial distance between donor and acceptor on mutual orientation of transition moments. These moments interact as two dipoles:

$$\mu_A \cdot \mu_B - 3(\mu_A \cdot \mathbf{r})(\mu_B \cdot \mathbf{r})$$

Calculate the value of orientation factor  $\kappa^2$  for attached model.



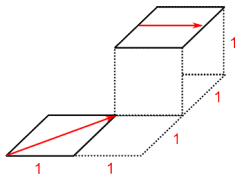


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### Solution

$$\kappa^2 = \left(-\frac{1}{\sqrt{2}}\right)^2$$

## Further reading

Joseph R. Lakowicz: **Principles of Fluorescence Spectroscopy**

Jihad Rene Albani: **Principles and Applications of Fluorescence Spectroscopy**

P. Atkins, J. de Paula: **Physical Chemistry**